

# **LLRF System Analysis for the** Fermilab PIP-II LINAC

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PIP-II is a partnership of:







### **Outline**

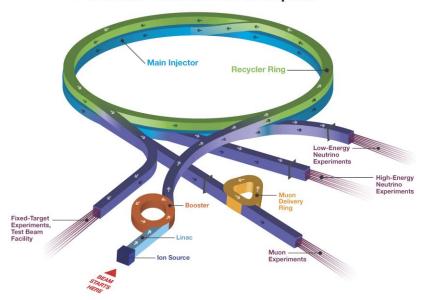
- 1. PIP2-LINAC Accelerator Components
- 2. LLRF System SEL Architecture
- 3. Calibrations and SEL Operational Modes
- 4. Physics Requirements LLRF Specifications
- 5. Analysis of Feedback Loops and Stability
- 6. Beam Loading in PIP-II cavities
- 7. Steps towards improving performance





## **Fermilab Accelerator Complex**

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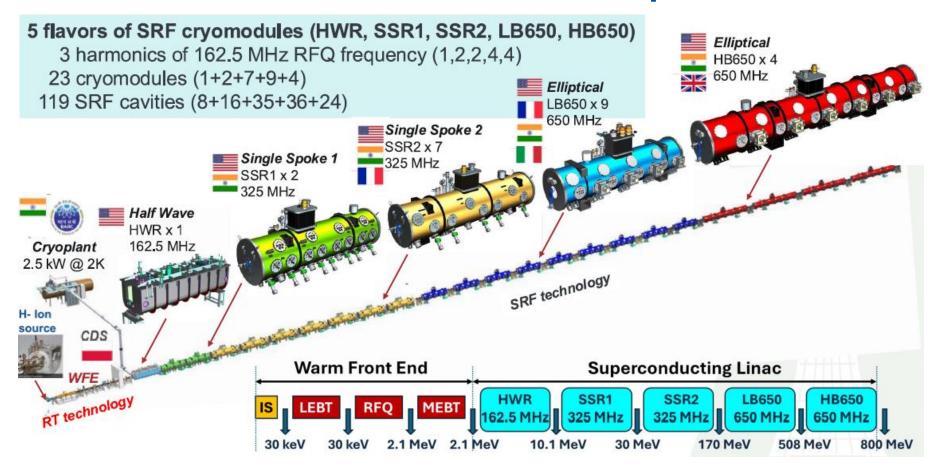








## **Fermilab Accelerator Complex**

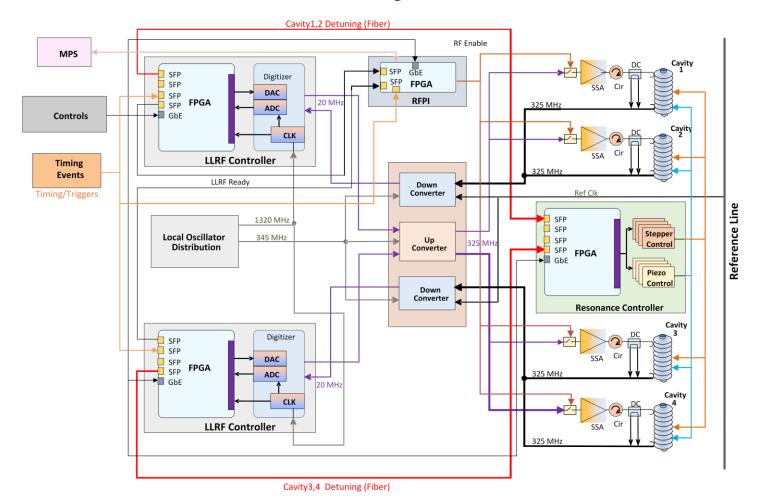








## **PIP2 4-Cavity RF Station**







## **PIP2 LLRF Systems**

CM type	Cavities per CM	Number of CMs	CM config- uration <sup>+</sup>	CM length (m)	$Q_0$ at 2K (10 <sup>10</sup> )	Surface resistance, $(n\Omega)$	Loaded Q $^{\triangle}$ (10 <sup>6</sup> )
HWR	8	1	8×(sc)	5.93	0.5	9.6 (2.75 <sup>†</sup> )	2.32
SSR1	8	2	4×(csc)	5.53	0.6	14 (10 <sup>‡</sup> )	3.02
SSR2	5	7	sccsccsc	6.3*	0.8	14.4	5.05
LB650	4	9	cccc	5.52*	2.15	9.0	10.36
HB650	6	4	ccccc	9.92*	3	8.7	9.92

	Station	Total										
	1	2	3	4	5	6	7	8	9	10	11	
	RFQ,	HWR	SSR1-	SSR2-	SSR2-	SSR2-	LB650-	LB650-	LB650-	HB650-	HB650-	
	B1-4		1,2	1,2,3	4,5	6,7	1,2,3	4,5,6	7,8,9	1,2	3,4	
Number of	6	8	16	15	10	10	12	12	12	12	12	125
cavities												
RF Freq	162.5	162.5	325	325	325	325	650	650	650	650	650	
(MHz)												

S3 — SSR1-1, SSR1-2

| SSR1-1 | SSR1-2 | SSR1-2

S4-S11 – SSR2 (7), LB650 (9), HB650 (4)

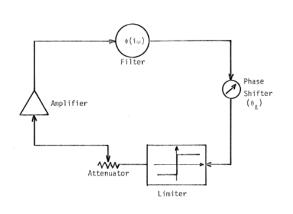


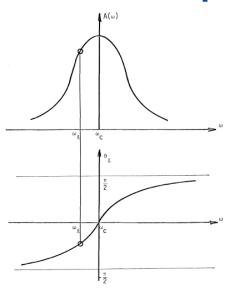


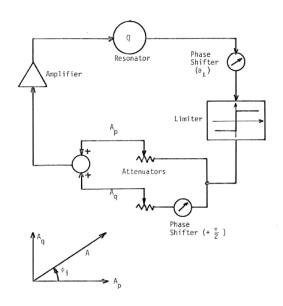




## **SEL Principle**







### **Key Features**

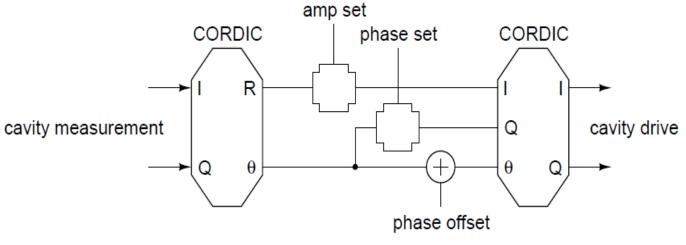
- Positive feedback configuration requires limiters
- Loop phase offset is  $2n\pi$  of oscillation frequency
- Cavity stored energy and field magnitude depends on the real or inphase(I) component of forward power
- Detuning due to microphonics and other disturbances are compensated by the quadrature(Q) component
- In GDR mode (SELAP) both positive(low gain) and negative(high gain) feedback loops are active

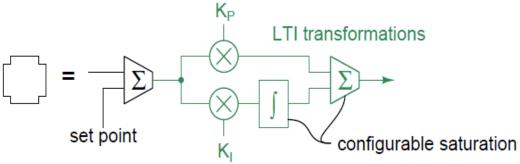






## **SEL System Architecture**

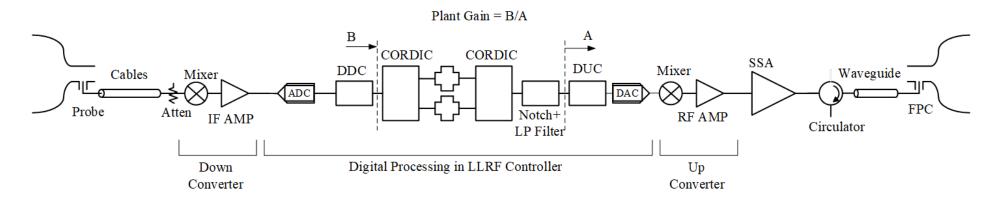


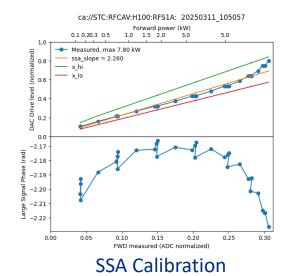






## **SEL System Calibrations**





$$V_0 = \left[ P_t \times Q_0 \times \frac{r}{\overline{Q}} \right]^{1/2}$$

**Transmitted Power** 

$$V_0 = \left[ U \times \frac{r}{Q} \times 2\pi f_0 \right]^{1/2}$$

Stored Energy from Reverse Power during cavity decay

**Gradient Calibration** 





## **Computing SEL Mode Limits**

#### **Real Power**

$$V_{Des} = E_{Des} \times l \quad MV$$

$$\sqrt{U} = \frac{V_{Des}}{\left[\frac{r}{Q} \times 2\pi f_0\right]^{1/2}} \quad \sqrt{J}$$

$$\sqrt{P} = \sqrt{\overline{U}} \times \sqrt{\frac{\pi f_0}{2Q_L}} \quad \sqrt{\overline{W}}$$

$$ADC_{Fwd} = \frac{\sqrt{P}}{C_{FSfwd}}$$

$$X_{tgt} = SSASlope \times ADC_{Fwd}$$

#### **Imag Power**

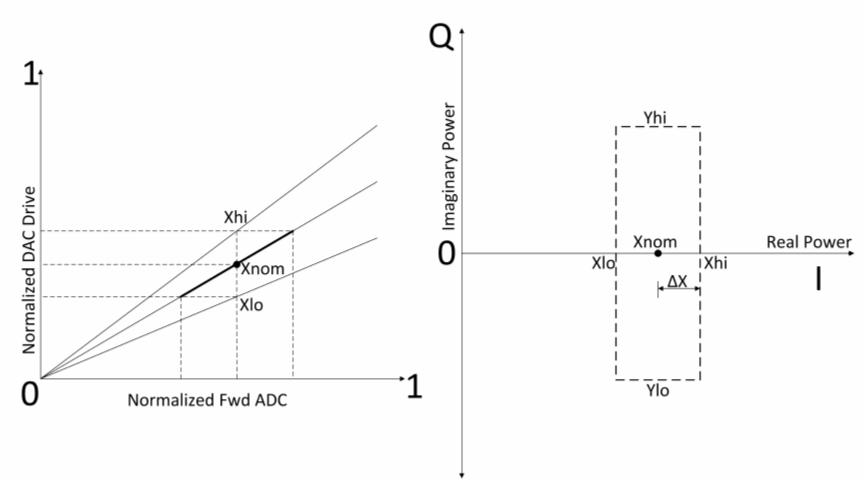
$$D_{Real} = \sqrt{1 - {D_{Imag}}^2}$$
 
$$Y_p = D_{Max} \times D_{Imag}$$
 
$$X_{Max} = D_{Max} \times D_{Real}$$

Mode	$X_{lo}$	$X_{hi}$	$Y_{lo}$	$Y_{hi}$
SEL Raw	-	-	-	-
SEL	$X_{tgt}$	$X_{tgt}$	0	0
SELA	$X_{tgt} \times 0.85$	$X_{tgt} \times 1.15$	0	0
SELAP	$X_{tgt} \times 0.85$	$X_{tgt} \times 1.15$	$-Y_p$	$Y_p$





## **Computing SEL Mode Limits**



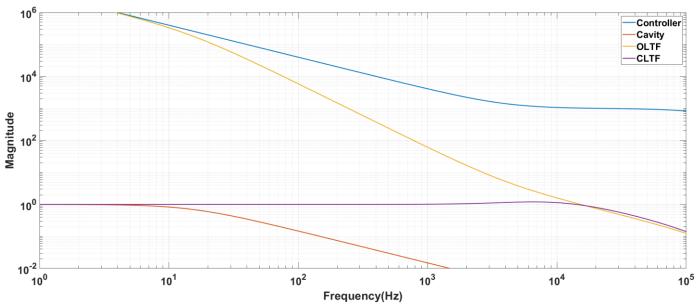
**SSA Calibration** 

**Forward Power** 





# **Gain Tuning Procedure LCLS-II**



ADC Sampling Clock	94.286	MHz
System Latency	1.2	$\mu$ S
Cavity Half BW	16	Hz
Plant Gain	0.73	
Field Set Point	14.6	MV
Field Full Scale	40.6	MV
Low Pass Filter BW	150	kHz
Controller Zero Place	0.25	
Target Close Loop BW	16000	Hz

Increase system gain and check if SEL limits are exceeded in the amplitude or phase feedback loops.

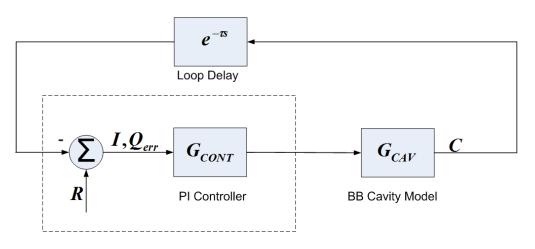
If one of the limits is crossed reduce closed loop bandwidth (system gain) Till the outputs are within the SEL limits





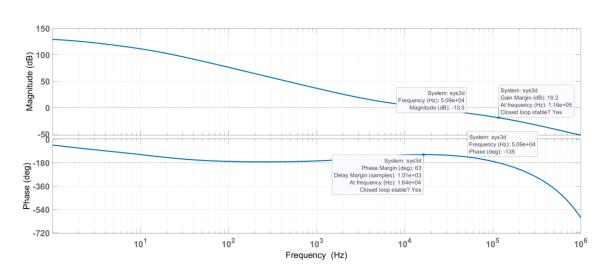


## **Stability Analysis with Bode Plot**



$$G_{CONT}(s) = \frac{K_I}{s} + K_P$$

$$G_{CAV}(s) = \frac{1}{1 + s/\omega_H}$$







# **PIP-II Loop Delay Components**

Delay	RFQ	Buncher	HWR	SSR1	SSR2	LB650	HB650
Total	985	1200	920	2720	2720	2770	2720
LLRF Controller Delay	500	500	500	2100	2100	2100	2100
LLRF-Amplifier Drive (cable)	50	150	20	70	70	70	70
Amplifier	200	100	100	200	200	200	200
HPRF Distribution	150	200	200	200	200	250	200
RF Fanback to LLRF (cable)	85	250	100	150	150	150	150
Cavity half bandwidth (Hz)	5542	8125	35	53.8	32.2	31.4	32.76
Gain (Max with 45 deg phase margin)	23	16	3846	881	1462	1479	1430

Cavity Type	$Q_L$	$f_0$	$f_H$	$K_P$
		(MHz)	(Hz)	
Warm Cavity	3000	53	$8.83 \times 10^{3}$	15
RFQ	15000	162.5	$5.542 \times 10^{3}$	23
Buncher Cavity	10000	162.5	$8.125 \times 10^{3}$	16
HWR Cavity	$2.32 \times 10^{6}$	162.5	35	3548
SSR1 Cavity	$3.02 \times 10^{6}$	325	53.8	2317
SSR2 Cavity	$5.05 \times 10^{6}$	325	32.2	3846
LB650 Cavity	$10.36 \times 10^{6}$	650	31.4	3935
HB650 Cavity	$9.92 \times 10^{6}$	650	32.76	3801
LCLSII Cavity	$4 \times 10^7$	1300	16.25	7600

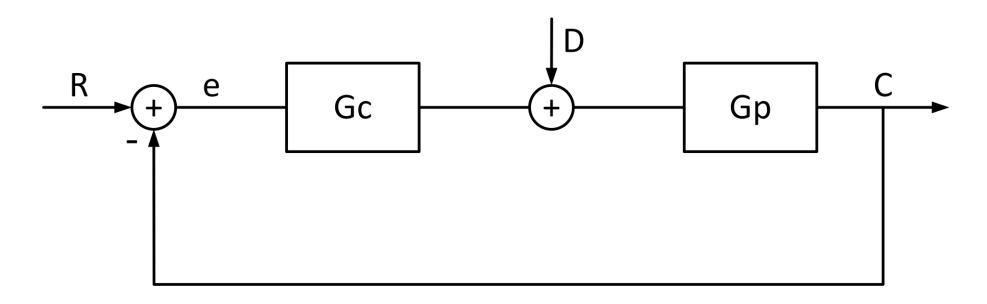
Assumed loop delay = 1 us







## Disturbance Rejection and Regulation Requirements



$$|e| = \frac{|D|}{1 + G_c}$$

#### **PIP-II Specifications**

- Energy Stability(Linac) < 0.01%</li>
- Amplitude Regulation(individual cavity) < 0.06 rms %
- Phase Regulation < 0.06 rms deg
- Maximum detuning < 20 Hz







## Disturbance Rejection and Regulation – Amplitude Loop

$$A = K_C \sqrt{P_N}, \quad A + \delta A = K_C \sqrt{P_N + \delta P}$$

$$P_N + \delta P = 1.15 \times P_N$$

$$1 + \frac{\delta A}{A} = \sqrt{1.15}, \quad \frac{\delta A}{A} = 0.0724$$

When above limits are used

$$G_{Min} = \frac{0.0724}{.0006} = 120, \quad \frac{D}{A} \le 0.0724$$

Stability analysis gives a max gain for SSR1 cavities of 880 Provided the box limits are increased

$$G_{Max} = 880, \quad \frac{D_{Max}}{A} \le 0.528 = 880 \times 0.0006$$







## **Disturbance Rejection and Regulation – Phase Loop**

$$D_{Real} = \sqrt{1 - D_{Imag}^{2}}$$

$$Y_{p} = D_{Max} \times D_{Imag}$$

$$X_{Max} = D_{Max} \times D_{Real}$$

For example, if  $D_{Imag} = 0.6$ ,  $Y_P = \pm 37$  degrees

$$G_{Min} = \frac{37}{06} \approx 615, \quad D_{\Phi} \leq 37 \quad degrees$$

Stability analysis gives a max gain for SSR1 cavities of 880 Provided the box limits are increased

$$G_{Max} = 880, \quad D_{\Phi} \le 52.8 = 880 \times 0.06 \quad degrees$$





## **PIP-II Cavity/Amplifier Parameters**

Cavity type	Aperture (diameter) (mm)	Effective length (cm)	Accelerating gradient (MV/m)	$E_{peak} \ ({\sf MV/m})$	$B_{peak}$ (mT)	$R/Q$ $(\Omega)$	<i>G</i> (Ω)
HWR	33	20.7	9.7	44.9	48.3	272	48
SSR1	30	20.5	10	38.4	58.1	242	84
SSR2	40	43.8	11.4	40	64.5	297	115
LB650	88	70.3	16.9	40.3	74.6	341	193
HB650	118	106.1	18.8	38.9	73.1	610	260

Device or Cryomodule Type	Frequency [MHz]	Number of RF Cavities	Number of RF per Cavity	Max. RF Power per Cavity [kW]	RF Amplifier Power [kW]
RFQ	162.5	1	2	65	75
MEBT bunch cavities	162.5	4	1	1.2	3
First HWR cavity	162.5	1	1	0.4	3
Other HWR cavities	162.5	7	1	6.2	7
SSR1	325	16	1	6	7
SSR2	325	35	1	17.2	20
LB650	650	36	1	38.2	40
HB650	650	24	1	58	70







## **Beam Loading in PIP-II Cavities**

- PIP-II Beam Current = 2000 μA
- LCLS-II Beam Current =  $100 \mu A / 300 \mu A$
- JLAB Beam Current = 400 μA

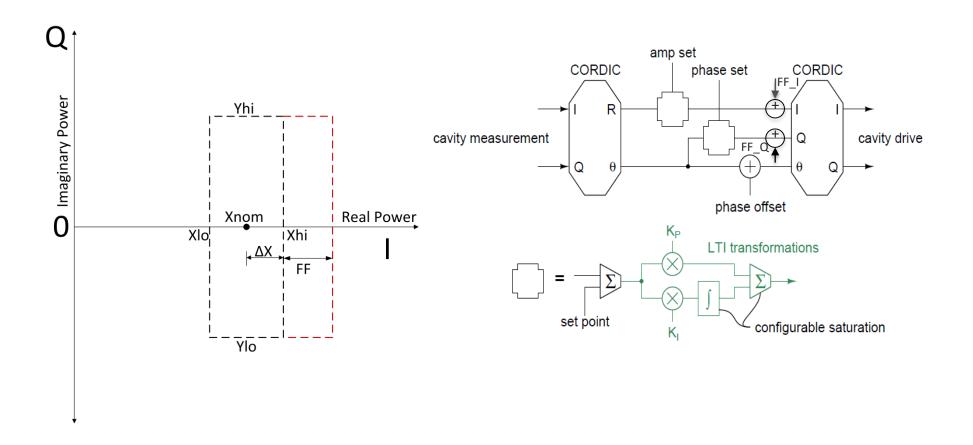
Cavity Description	Cavity Voltage (MV)	Forward Power – No beam (kW)	Forward Power – With Beam (kW)	√Power Ratio	Amplifier Max Power(kW)
HWR_6	2.008	2.64	4.45	1.3	7
SSR1_8	2.050	1.98	4.13	1.44	7
SSR2_5_4	4.993	6.40	11.92	1.36	20
LB650_5_3	11.88	15.93	28.97	1.35	40
HB650_4_2	19.953	24.28	40.71	1.29	70

- Feedback limits currently allow for 1.15 increase in power ratio
- Feedforward beam loading compensation is needed





## **Adding Gated Feedforward for Beam Loading**

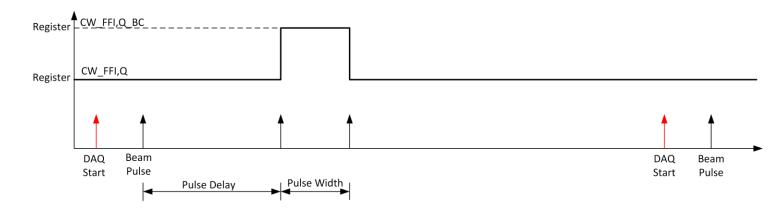




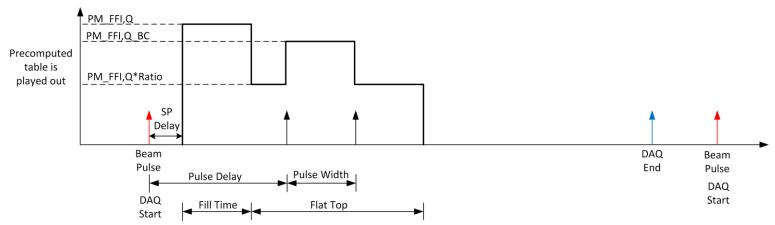


## **Adding Gated Feedforward for Beam Loading**

CW Mode DAQ is NOT Synchronised To Beam Pulse Beam Comp IS synchronised



Pulse Mode
DAQ and Beam
Comp ares
Synchronised
To Beam Pulse
by design

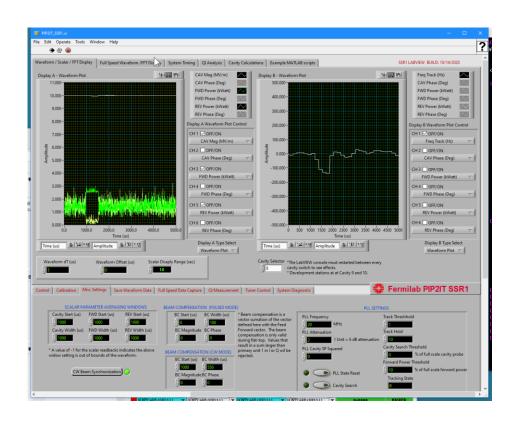


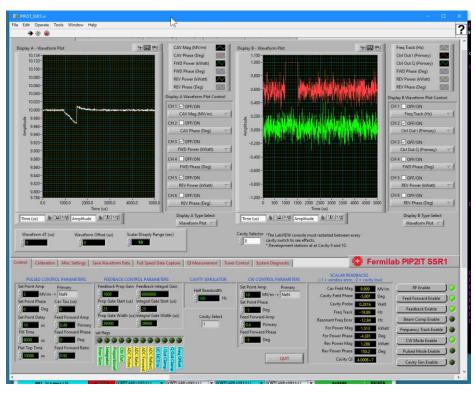






## **Beam Loading in SSR1 Cavity**



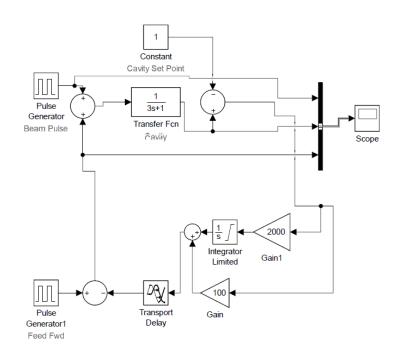


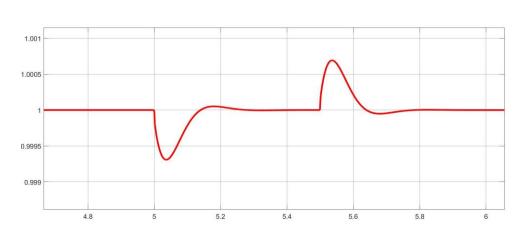






## **Beam Loading in SSR1 Cavity**









LLRF System Analysis

## **Steps Towards Performance Improvement**

- Add feedforward(FF) beam loading compensation(BLC)
- Gating of FF BLC with beam arrival trigger is required PIP-II beam
   Duty cycle is only 1%
- DAC drive limits need to be adjusted for each cavity type due to differing beam/no beam power ratios
- Loop delays of ~ 3 μs can be improved with firmware changes
- Amplifier non-linearity should be handled correctly as a variety of amplifier sizes and vendors are being used
- LCLS-II and PIP-II linacs are using the same codebase both projects will benefit from the improvements







## **Summary**

- The SEL Implementation for PIP-II was described
- Stabilty Analysis was used to determine theoretical feedback gain limits
- The beam loading for PIP-II cavities was compared with the output saturation limits currently being used
- The need for gated feed forward beam loading compensation was demonstrated
- Steps for improving performance were discussed





# Thank You!





# Backup Slides





## **Beam Loading Power Calculation**

$$P_f = \frac{V_a^2 (1+\beta)^2}{4\beta Q_0 \left(\frac{r}{Q}\right)} \left[ \left(1 + \frac{I_{Re} T\left(\frac{r}{Q}\right) Q_0}{V_a (1+\beta)}\right)^2 + \left(\frac{Q_0}{1+\beta} \frac{2\delta f}{f}\right)^2 \right]$$

$V_a$	Cavity Voltage
I	Beam Current
f	Cavity Frequency
$\delta f$	Microphonics Detuning
T	Transit Time Factor
$\beta$	Cavity Coupling Factor

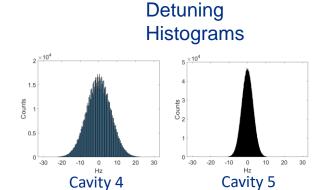


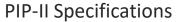




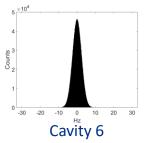
## **HWR Control Performance**

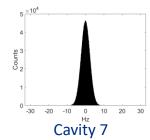
HWR Amplit	ude and	Phase R	egulatio	n						
Cavity4 Cavity5 Cavity6 Cavity7 Cavity8										
Cavity Field Setpoint (MV/m)	2.89	6.04	8.94	8.5	8					
Amplitude Regulation (rms) %	0.0135	0.0106	0.0101	0.0081	0.0103					
Phase Regulation (rms) deg	0.0228	0.0065	0.0056	0.0055	0.0062					
Feedback Proportional Gain	1000	1000	1000	1000	1000					
Feedback Integral Gain (rad/sec)	1,000,000	1,000,000	1,000,000	1,000,000	1,000,000					

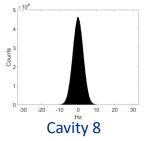




- Energy Stability(Linac)
- < 0.01%
- Amplitude Regulation(individual cavity) < 0.06 rms %
- Phase Regulation < 0.06 rms deg
- Maximum detuning < 20 Hz





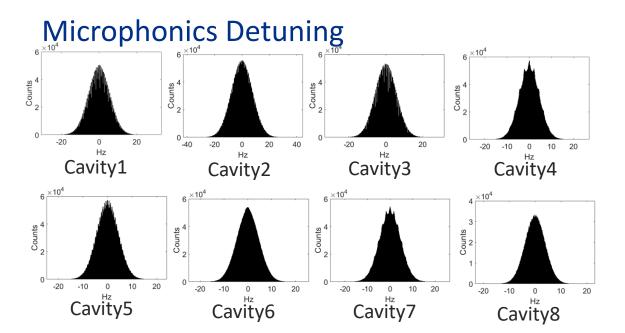






## **SSR1** Cryomodule Testing

SSR1 Amplitude and Phase Regulation										
Cavity1 Cavity2 Cavity3 Cavity4 Cavity5 Cavity6 Cavity7 Cavity8										
Cavity Field Setpoint (MV/m)	4.88	4.63	4.78	7.32	7.8	7.56	7.32	10		
Amplitude Regulation (rms) %	0.0194	0.0289	0.0219	0.0157	0.014	0.0158	0.0147	0.0124		
Phase Regulation (rms) deg	0.0116	0.0164	0.0118	0.0091	0.0088	0.0093	0.0092	0.0076		
Feedback Proportional Gain	1600	1600	1600	1600	1600	1600	1600	1600		
Feedback Integral Gain (rad/sec)	3,000,000	3,000,000	3,000,000	3,000,000	3,000,000	3,000,000	3,000,000	3,000,000		



## Piezo Transfer Function – C1

