

Methods and Simulation Tools for Cavity Design

SRF 2019 Tutorials

29.6.2019

Hans-Walter Glock

Helmholtz-Zentrum Berlin für Materialien und Energie

hans.glock@helmholtz-berlin.de

A **good** and a **bad** news

You almost **made** it:

Tutorial Lecture Schedule for SRF2019

	Jun 27 th , Th.	Jun 28 th , Fr.	Jun 29 th , Sa.
Registration and Welcome	8:30-9:00 P. Michel (HZDR)	-	-
Session 1	9:00-10:30 Basic Principles of RF Superconductivity G. Ciovati (JLab)	9:00-10:30 Superconducting Cavities of Interesting Shapes (Non-elliptical Cavities) S. De Silva (ODU)	9:00-10:30 Beam-cavity Interaction and Operational Aspects of SRF Systems With Beam S. Belomestnykh (FNAL)
Coffee Break	10:30 -11:00	10:30 -11:00	10:30 -11:00
Session 2	11:00-12:30 RF Basic and TM Cavities E. Jensen (CERN)	11:00-12:30 Cavity Processing and Cleanroom Techniques L. Popielarski (FRIB/MSU)	11:00-12:30 LLRF Controls and RF Operation J. Branlard (DESY)
Lunch	12:30-13:30	12:30-13:30	12:30-13:30
Session 3	13:30-15:00 Cavity Vertical and Horizontal Test and Operation T. Powers (JLab)	13:30-15:00 Pushing Bulk Nb Limits (High Q, High Gradient, Reliable SRF Accelerators) A. Grassellino (FNAL)	13:30-15:00 Fundamentals of Cryomodule Design and Cryogenics B. Petersen (DESY)
Coffee Break	15:00-15:30	15:00-15:30	15:00-15:30
Session 4	15:30-17:00 High Power Couplers and HOM Couplers E. Kako (KEK)	15:30-17:00 Materials Beyond Bulk Nb C. Antoine (Saclay)	15:30-17:00 Methods and Simulation Tools for Cavity Design H.-W. Glock (HZB)

*A good and a **bad** news*

*You **almost** made it.*

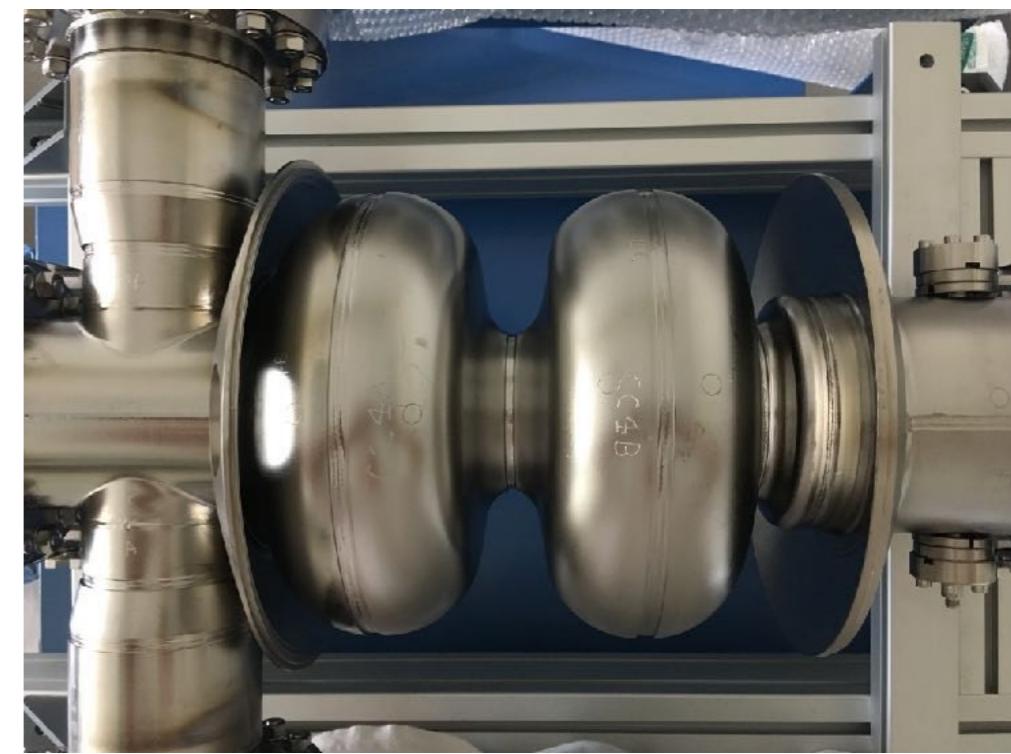
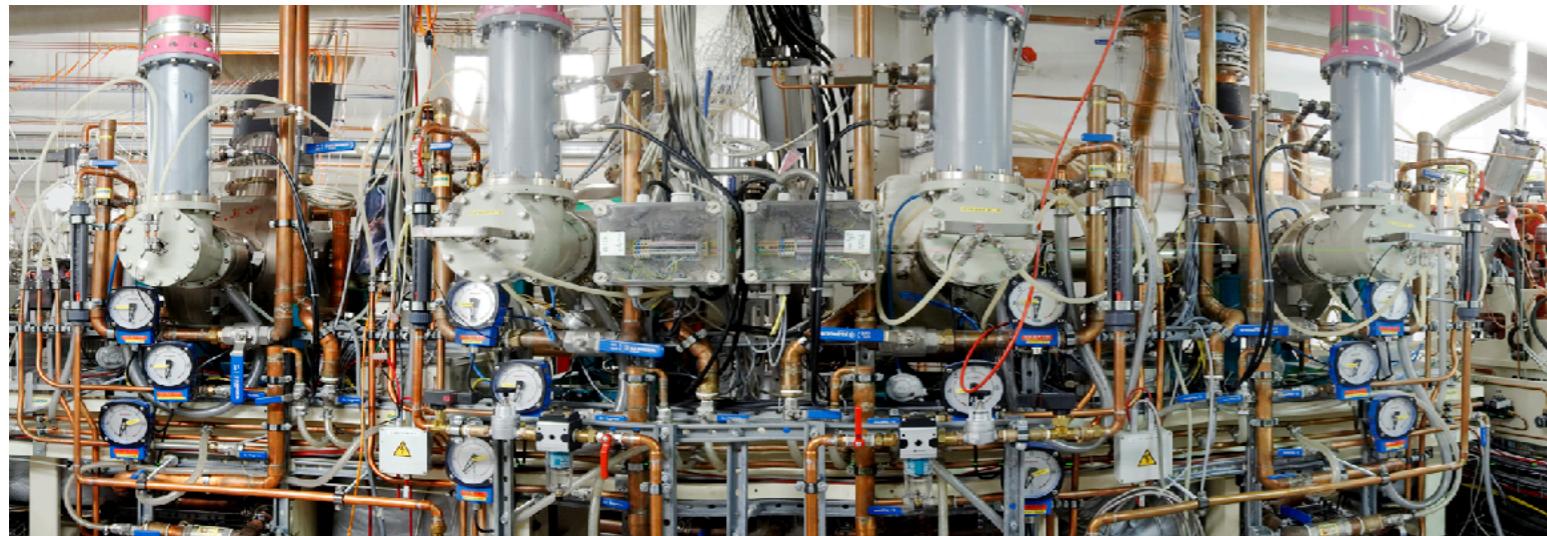
A good and a **bad** news

You **almost** made it :

The word cloud consists of various scientific and technical terms, each associated with a color and a small explanatory text. The most prominent term is 'cavity' in blue. Other significant terms include 'beam' in yellow, 'mesh' in green, 'HOMs' in orange, 'LOMs' in yellow, 'SOMs' in yellow, 'fundamental mode' in brown, 'tetrahedral' in blue, and 'TM modes' in red. Smaller terms include 'SSC' in yellow, 'eigenfrequency' in red, 'frequency domain' in blue, 'boundary conditions' in green, 'beam relevance' in yellow, 'wake simulations' in orange, 'TE modes' in red, 'multipacting' in orange, 'couplers' in green, 'bellows' in purple, 'beam pipes' in purple, 'wake fields' in blue, 'azimuthal mode types' in brown, 'tomography' in green, 'dispersive dielectrics' in blue, 'ports' in purple, 'periodic boundary conditions' in red, 'Lorentz force detuning' in green, 'tuning force' in blue, 'dielectric loss' in red, 'sensitivity analysis' in orange, 'coupler kick' in orange, 'cut-off' in purple, 'deformations' in yellow, 'non-linearities' in orange, 'leaking fundamental mode' in orange, 'single/multicell' in green, 'open Epeak' in orange, 'csc' in purple, 'polarization' in teal, 'hexahedral' in orange, 'mode trapping' in green, 'parameterized' in yellow, 'symmetry' in orange, 'Brillouin diagram' in purple, 'single/multibunch' in purple, 'Fourier-rescaling' in purple, 'partial mesh filling' in purple, 'GSM' in orange, 'Bpeak' in orange, 'thermal conductivity' in orange, 'loss power' in purple, 'thermal design' in purple, and 'tomography' in green.

What is a cavity ???

BESSY II's four main 500 MHz cavities



Cornell-style bERLinPro booster 1.3 GHz-2-cell
without tank

*by intention (found
somewhere @HZB)*

cavity



Gun I.1-cavity prepared for
vertical testing



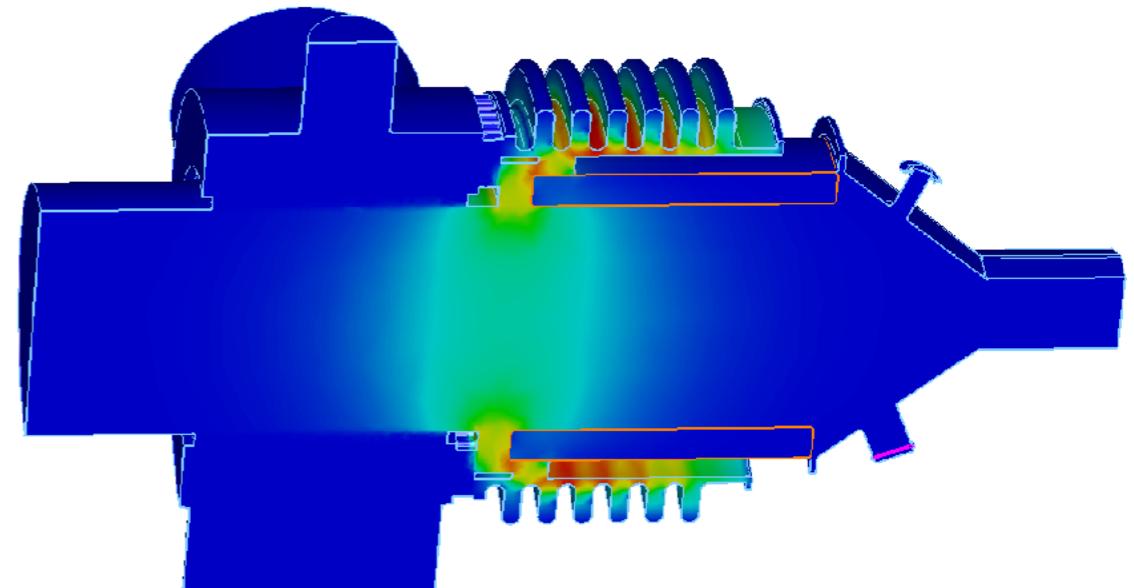
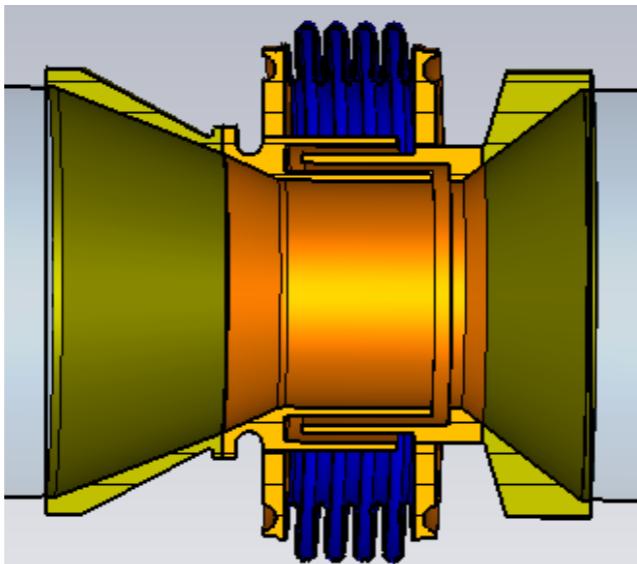
Transverse-Deflecting cavity (TCAV) in
bERLinPro's diagnostic beam line



TESLA-9-cell cavity (for display purposes)



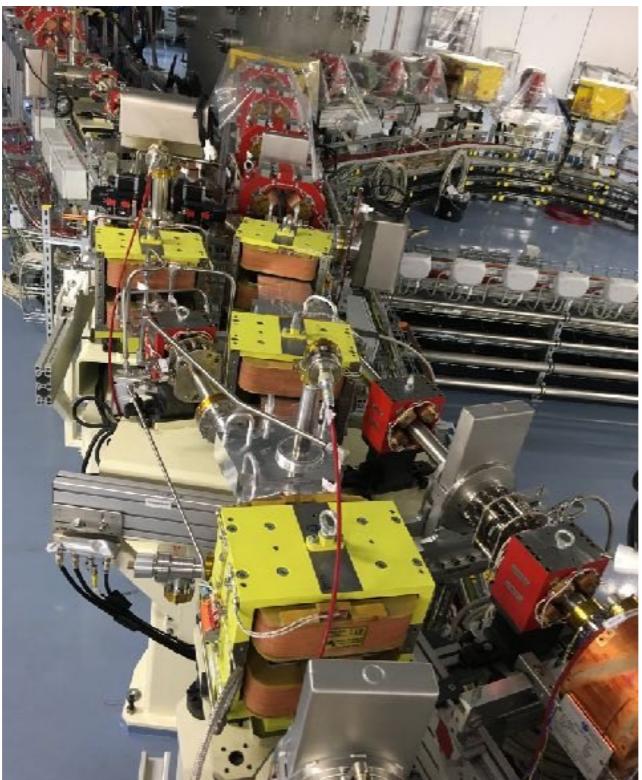
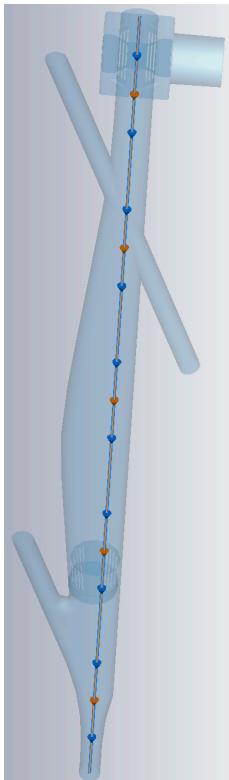
Collimating Shielded Bellow for BESSY-VSR-Upgrade



Draft of BESSY-VSR end group

unwanted cavity

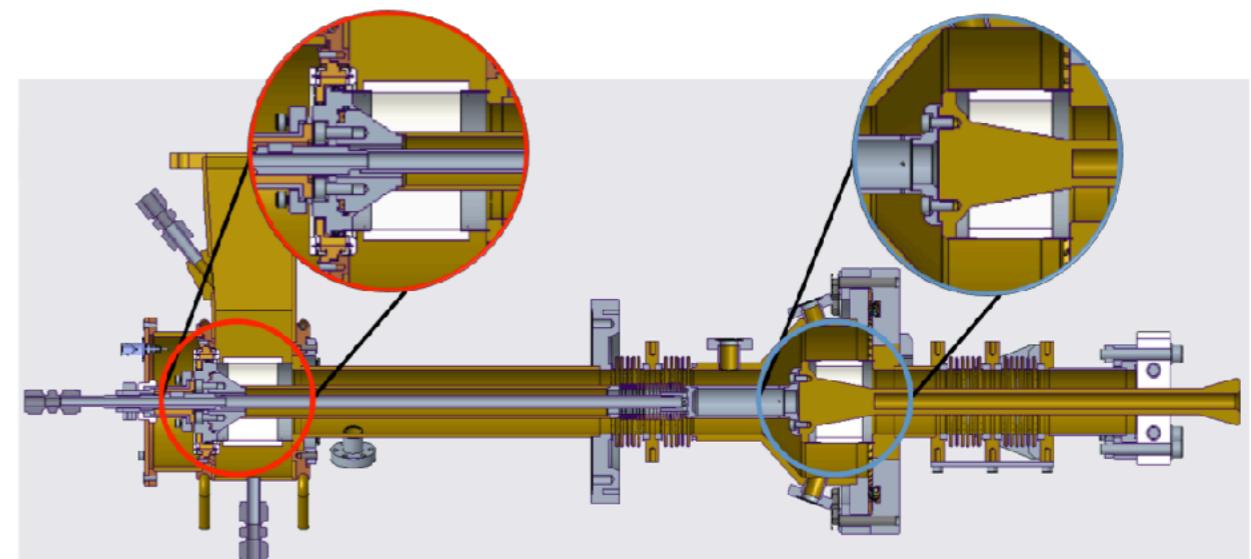
(found somewhere
@HZB)



bERLinPro merger section



below in bERLinPro's temporary
replacement beamline



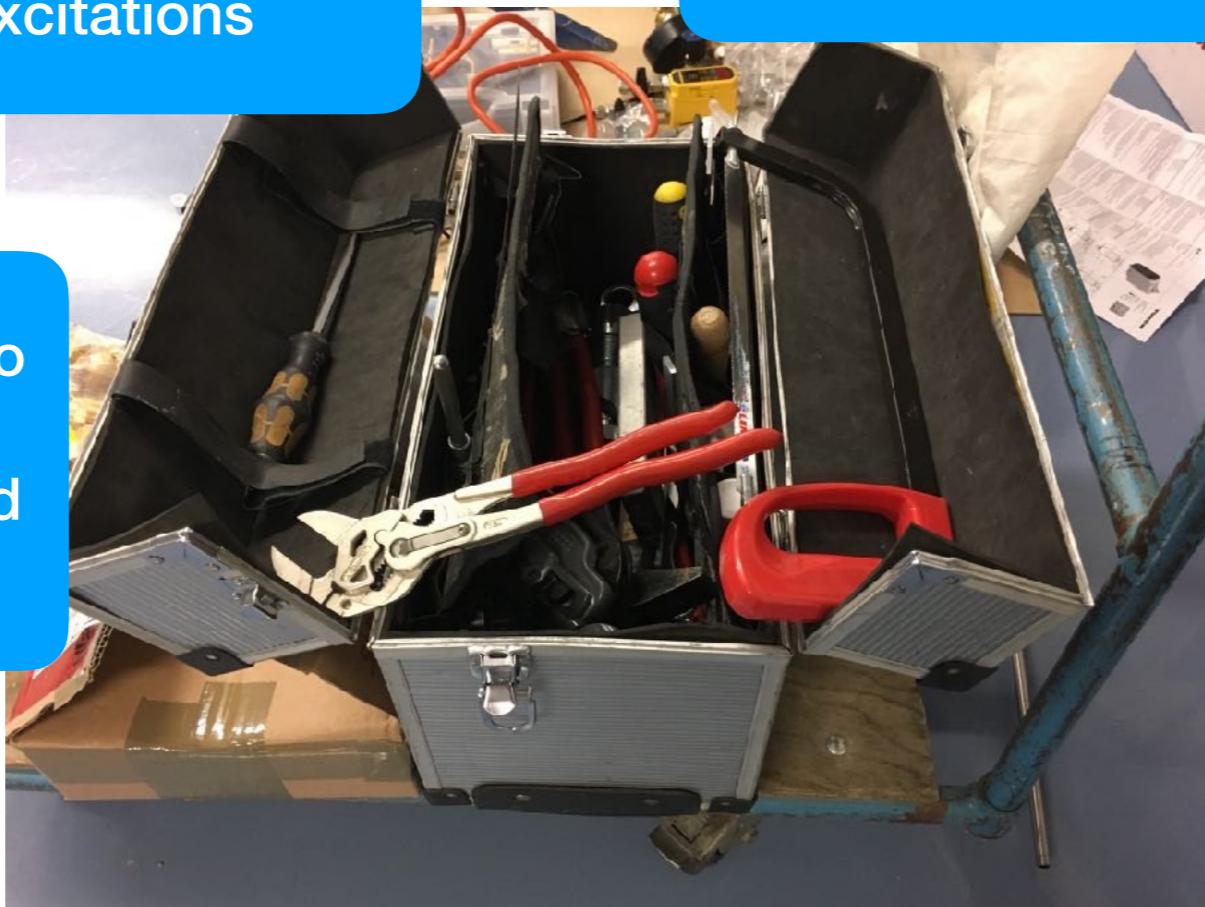
Dielectric windows in the BESSY-VSR upgrade fundamental power coupler
construction (courtesy Emmy Sharples)

The tool box: You should have ...

a frequency domain solver to compute the reaction of a cavity or an open structure on externally given driving excitations

a wakefield solver to observe the time-domain reaction of a beam line element on a driving bunch

an eigenmode solver to determine the natural resonances of a closed cavity



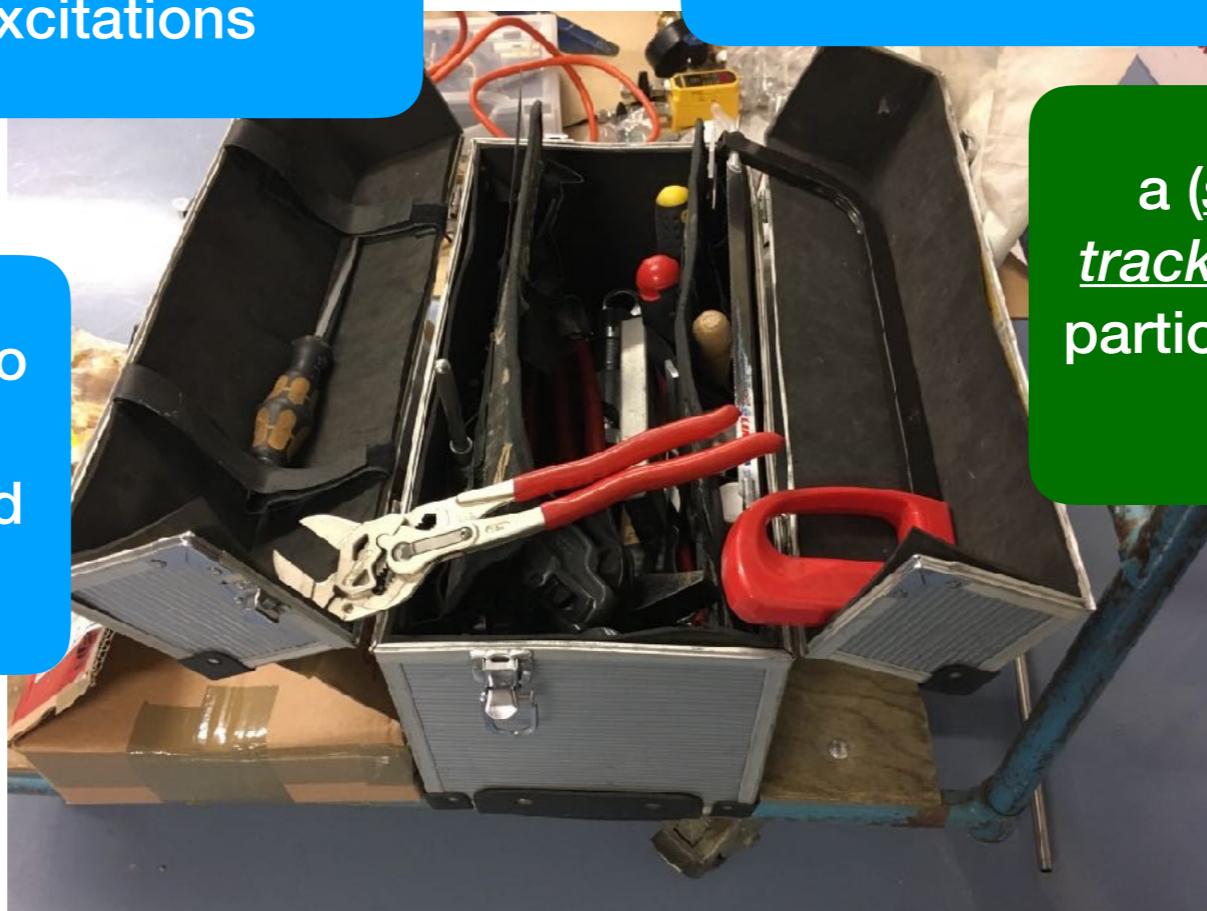
The tool box: ... and you also may find useful

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a (self-consistent) particle tracker to perform (expensive) particle(/field co-)simulations in time domain



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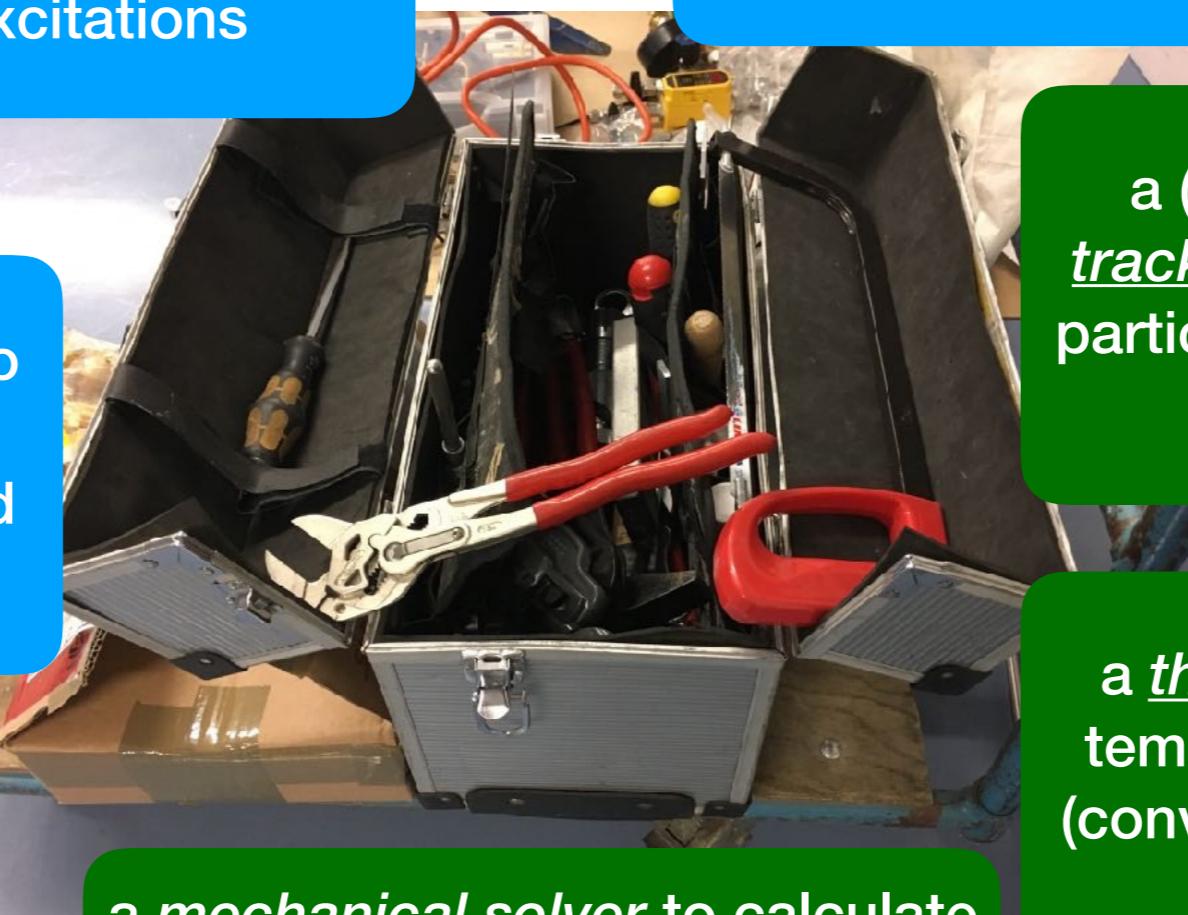
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a mechanical solver to calculate elastic/plastic) cavity deformations based on Lorentz-/ pressure/tuning forces + mechanical eigenmodes

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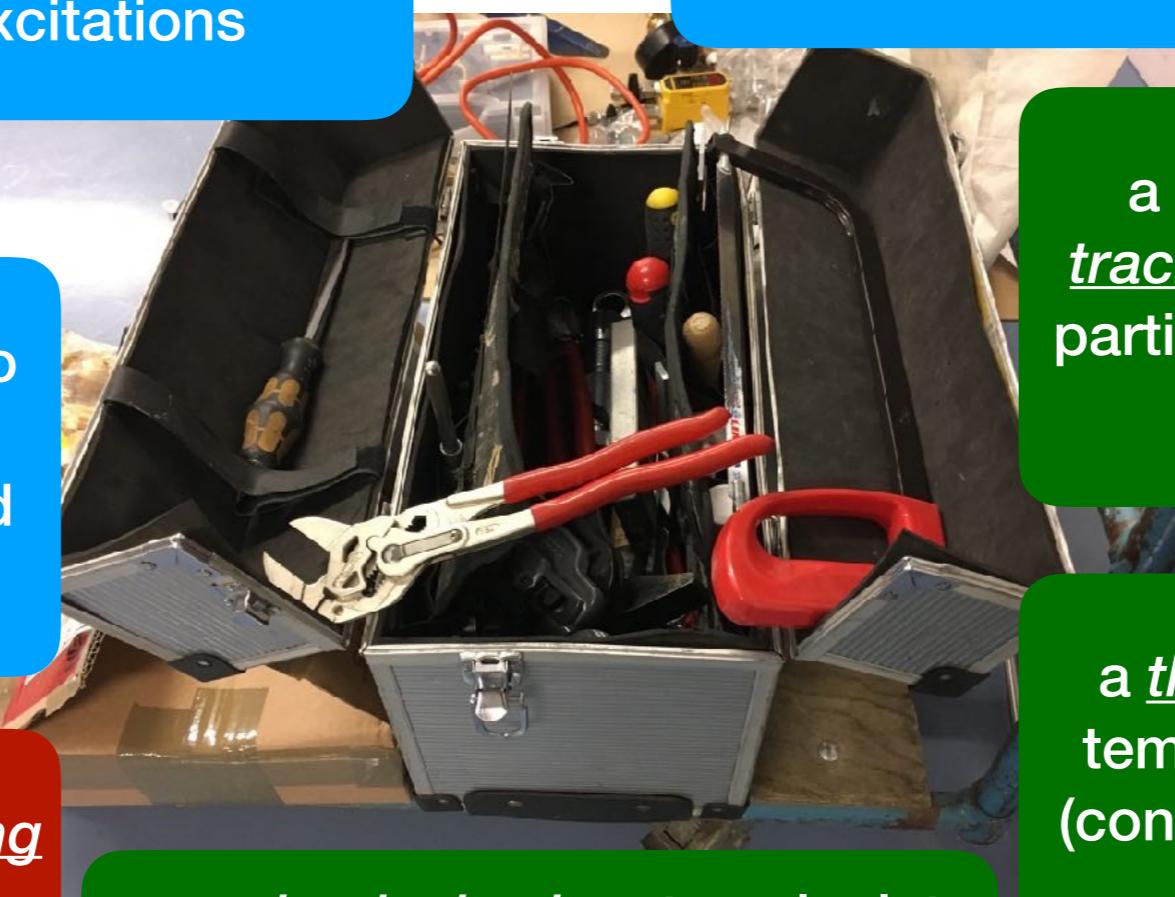
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an external programming environment for other evaluations of exported field data

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The tool box: ... and you also may find useful:

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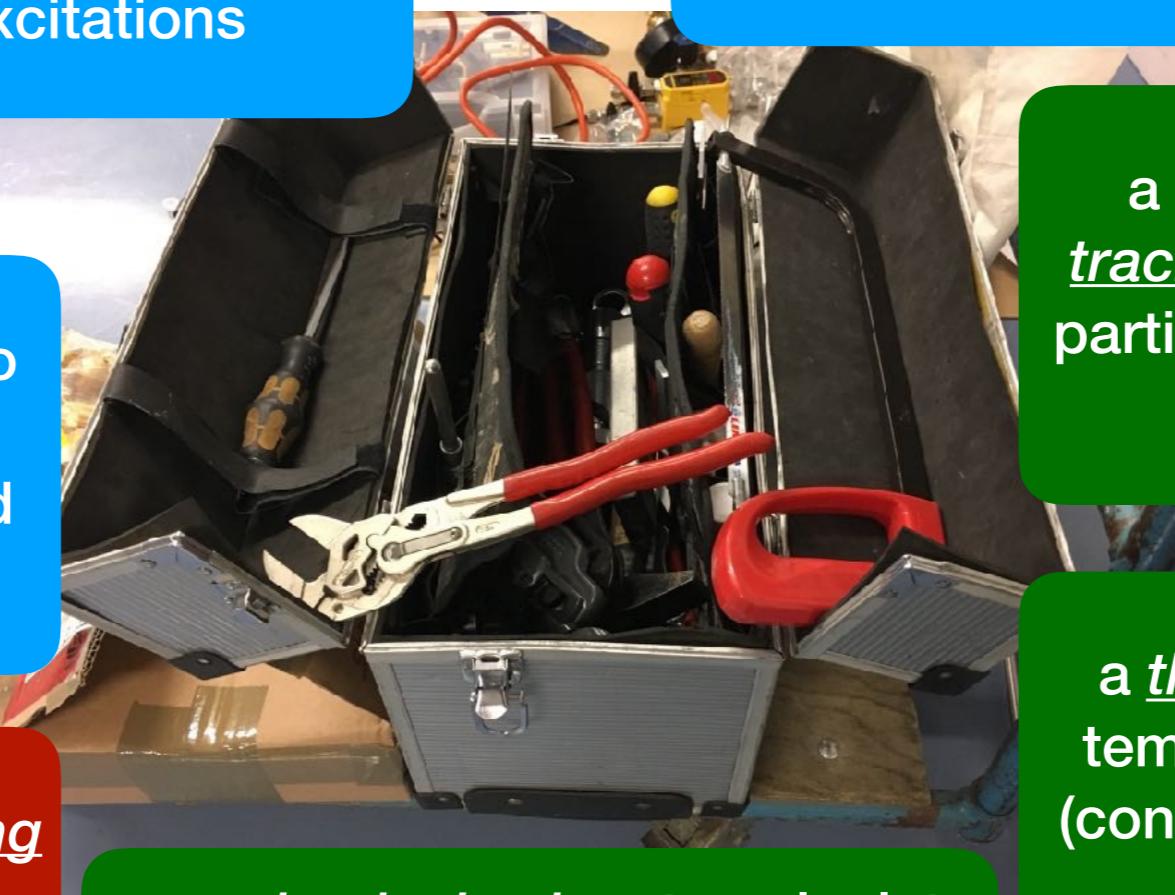
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For those purposes I recommend the following software brands:

... page intentionally left free, because ...

The tool box: You should have ...

an eigenmode solver to
determine the natural
resonances of a closed
cavity



What is an „eigenmode“ of a cavity? — rather a strange thing:

1. *It exists inside an entirely closed cavity, made of some Perfect Electric Conductor (PEC, which is a fiction).*
2. *It exists with non-vanishing amplitude without any energy source (which sounds profitable).*
3. *It oscillates infinitely long with a pure single „eigen“-frequency (which is said twice).*
4. *It has an infinite number of companions (most of them fortunately of less interest).*

What is an „eigenmode“ of a cavity? — rather a ~~strange~~
~~stranger~~ thing:

1. It exists inside an entirely closed cavity, made of some ~~Perfect~~
~~Electric Conductor~~
~~or containing lossy material~~
~~finite~~
2. It exists with non-vanishing amplitude without any energy source (which sounds profitable).
3. It oscillates infinitely long with a pure single „eigen“-frequency (which is said twice).
~~but constantly decaying~~
~~complex~~
4. It has an infinite number of companions (most of them fortunately of less interest).

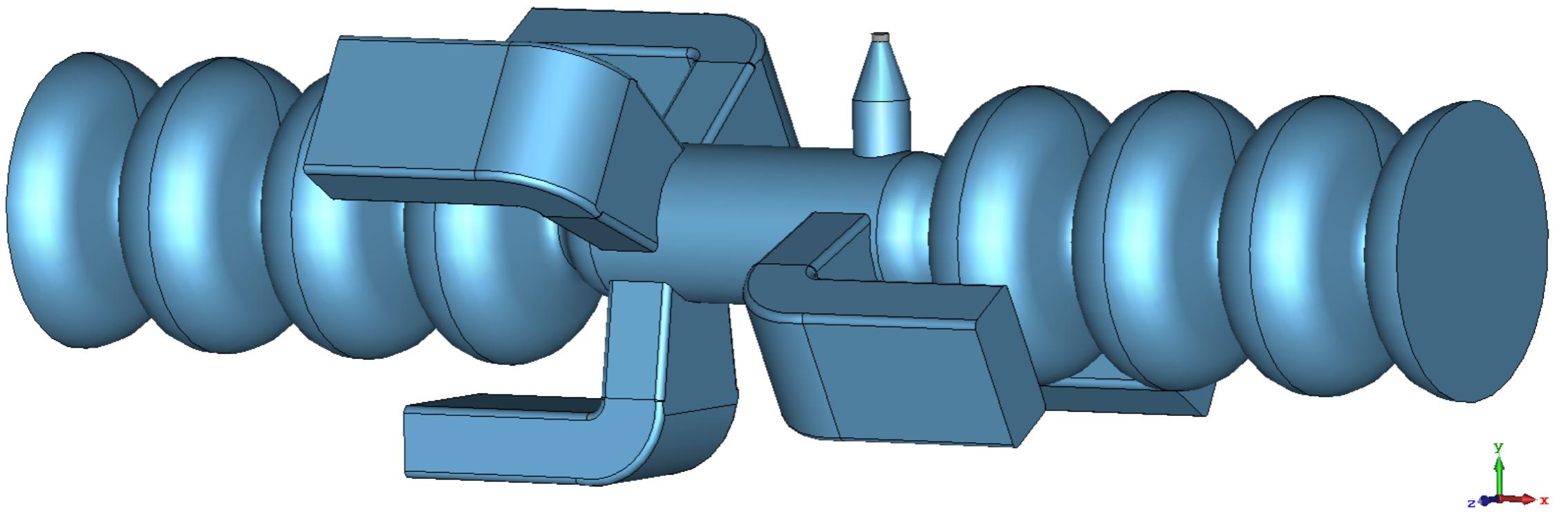
... so, let us compute some eigenmodes ...

... so, let us compute some eigenmodes of a:

- *7-cell elliptical cavity*
- *strongly HOM-damped with 5 waveguides*
- *a fundamental power coupler*
- *and a beam pipe*

... so, let us compute some eigenmodes of a:

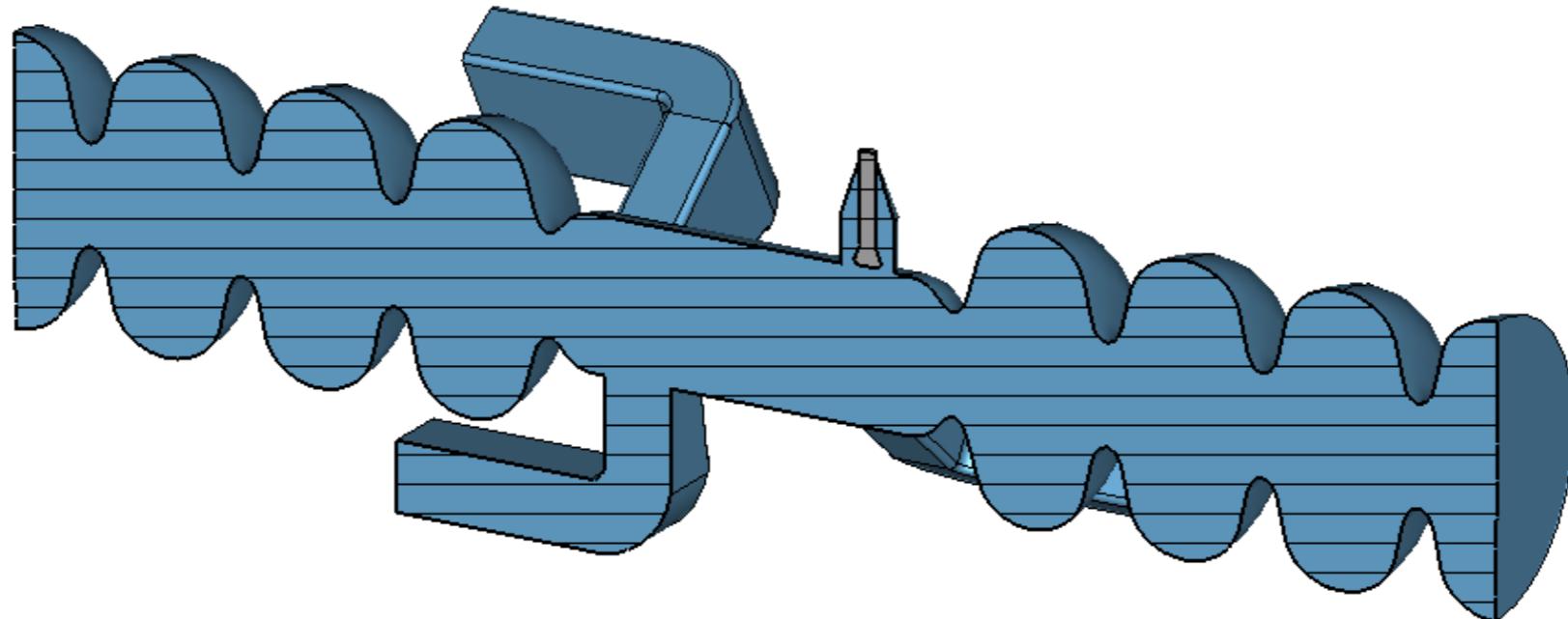
- 7-cell elliptical cavity*
- strongly HOM-damped with 5 waveguides*
- a fundamental power coupler*
- and a beam pipe*



- which is going to be placed in a chain of identical neighbors, so we would like to study the beam-pipe-coupling as well*

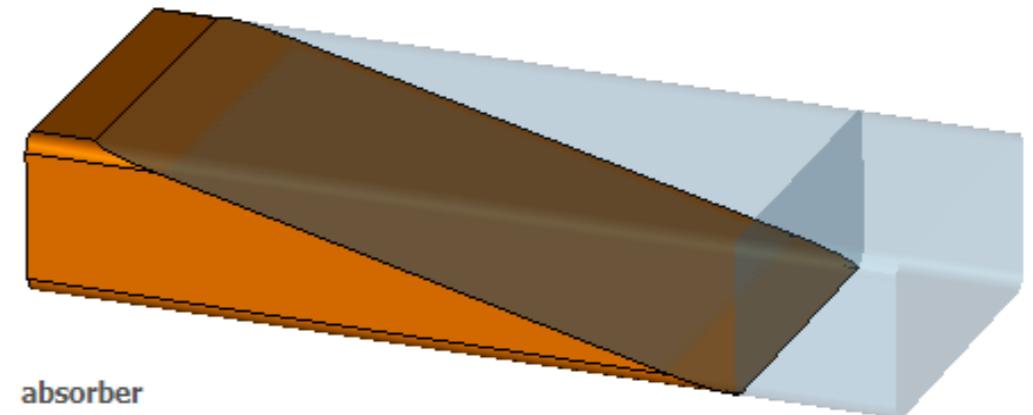
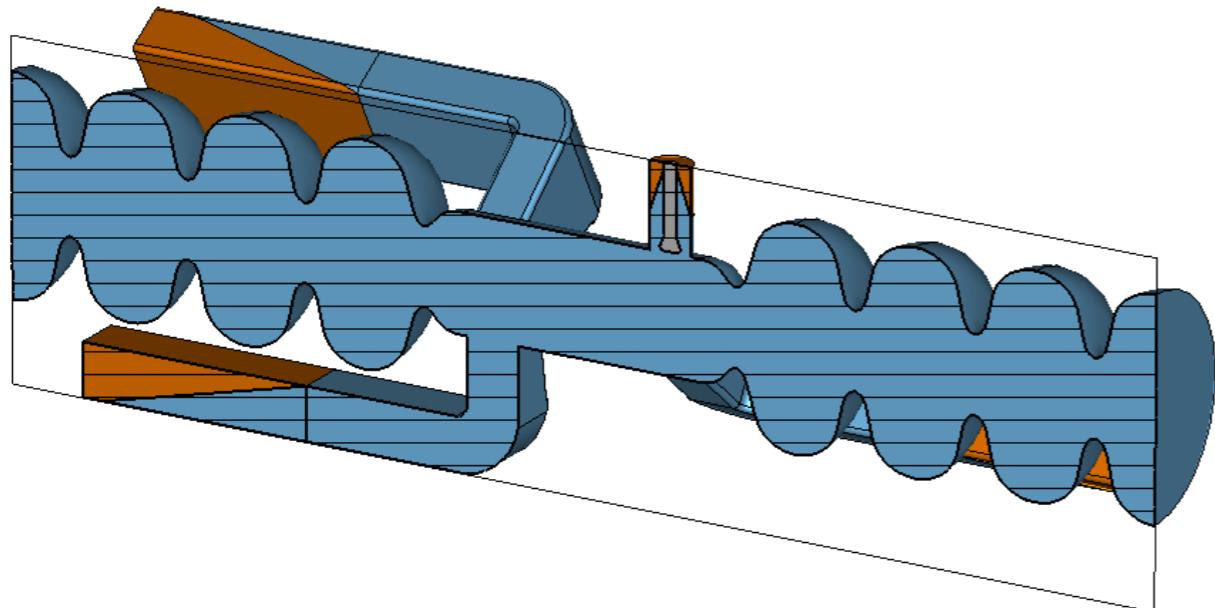
We need:

- I.) *the cavity (+ waveguides + coupler) shape, either CAD-constructed externally or composed using the geometrical primitives of the field solver*



We need:

2.) some *virtual absorber simulating well matched waveguide(/coax) terminations*



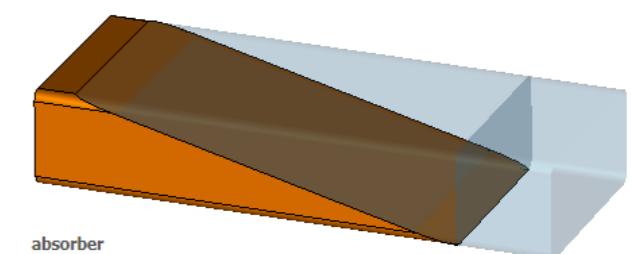
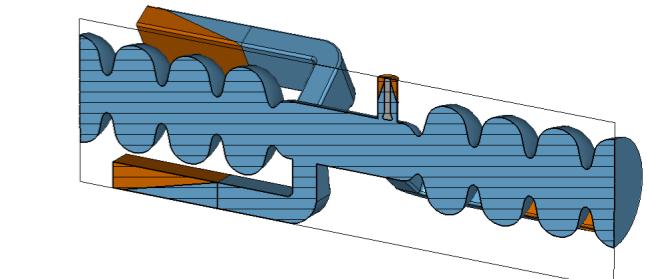
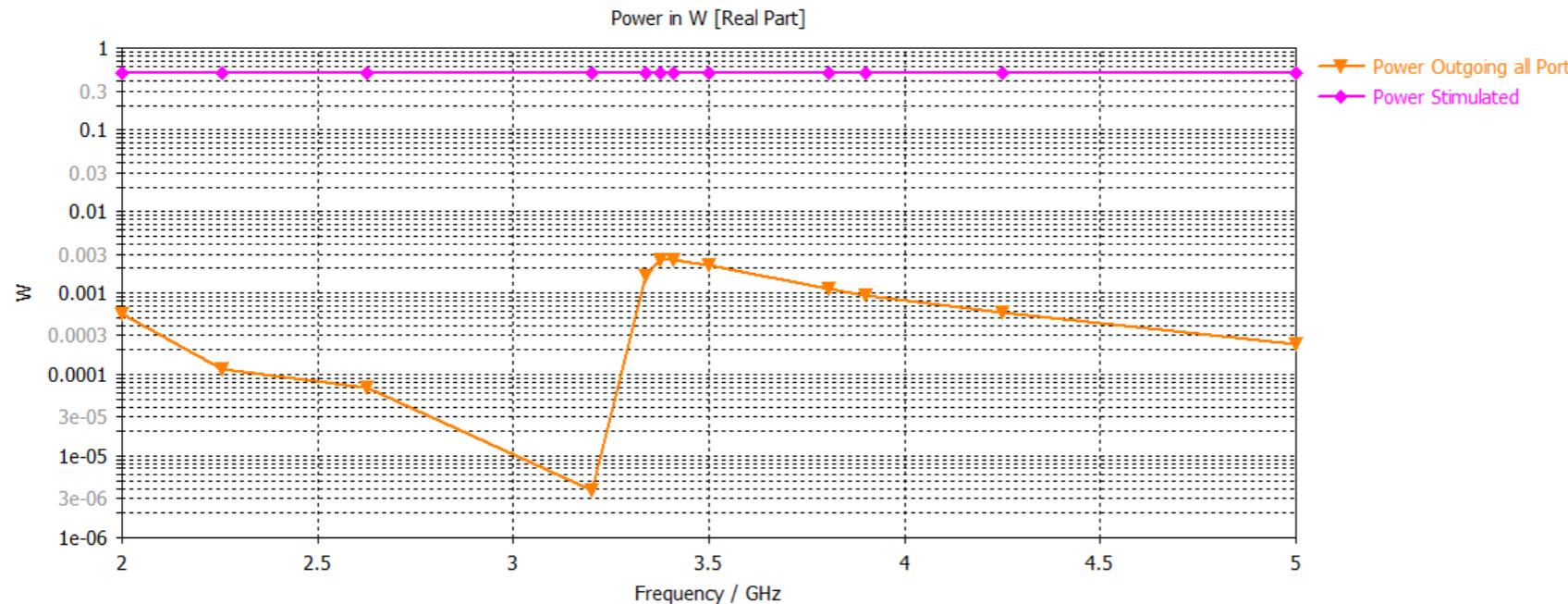
absorber

Type	Normal
Epsilon	5
Mu	5
Electric cond.	0.5 [S/m]

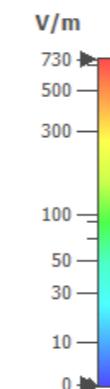
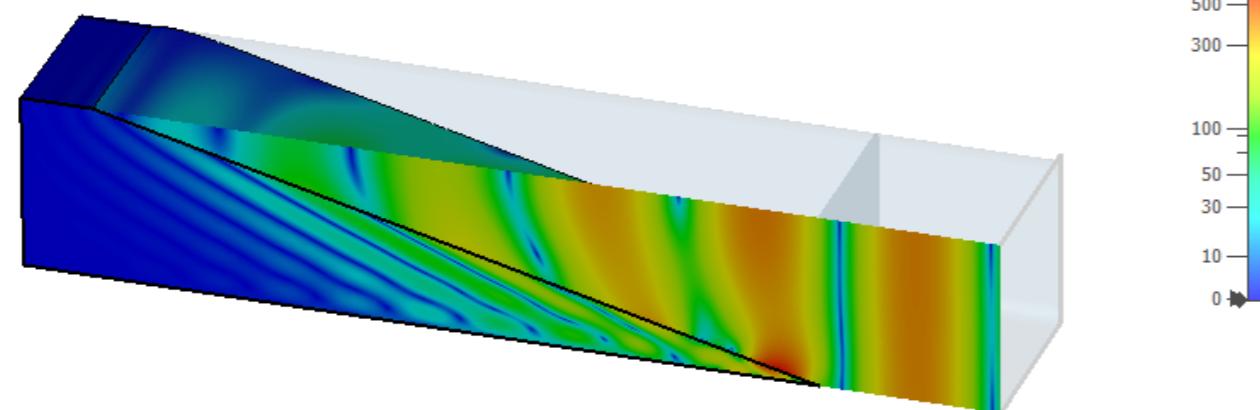
... using a virtual material of $\epsilon'_r = \mu_r = 1$, thus keeping vacuum wave impedance to avoid reflections, with a conductivity $\sigma = 0.5 \text{ } I/(\Omega \text{ m})$ to dissipate the power

We need:

2.) some *virtual absorber* simulating well (better -25 dB)
matched waveguide(/coax) terminations



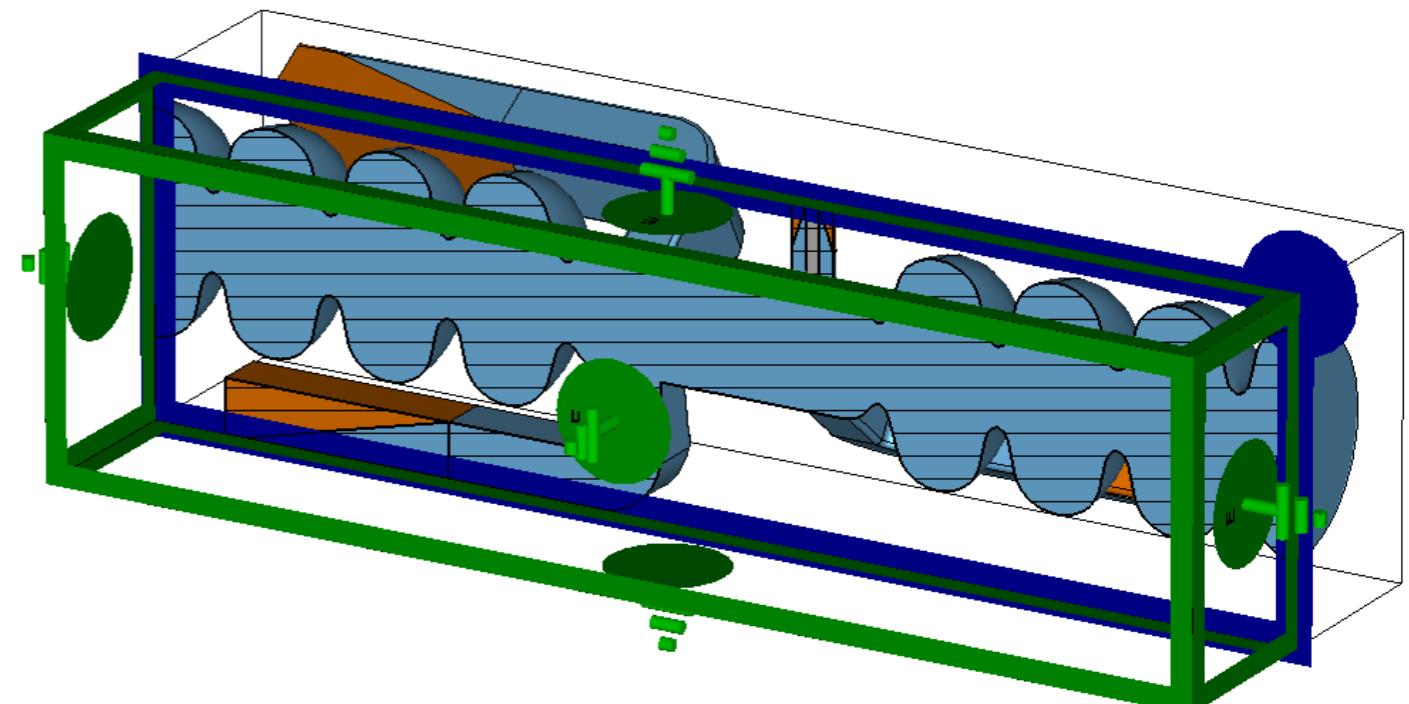
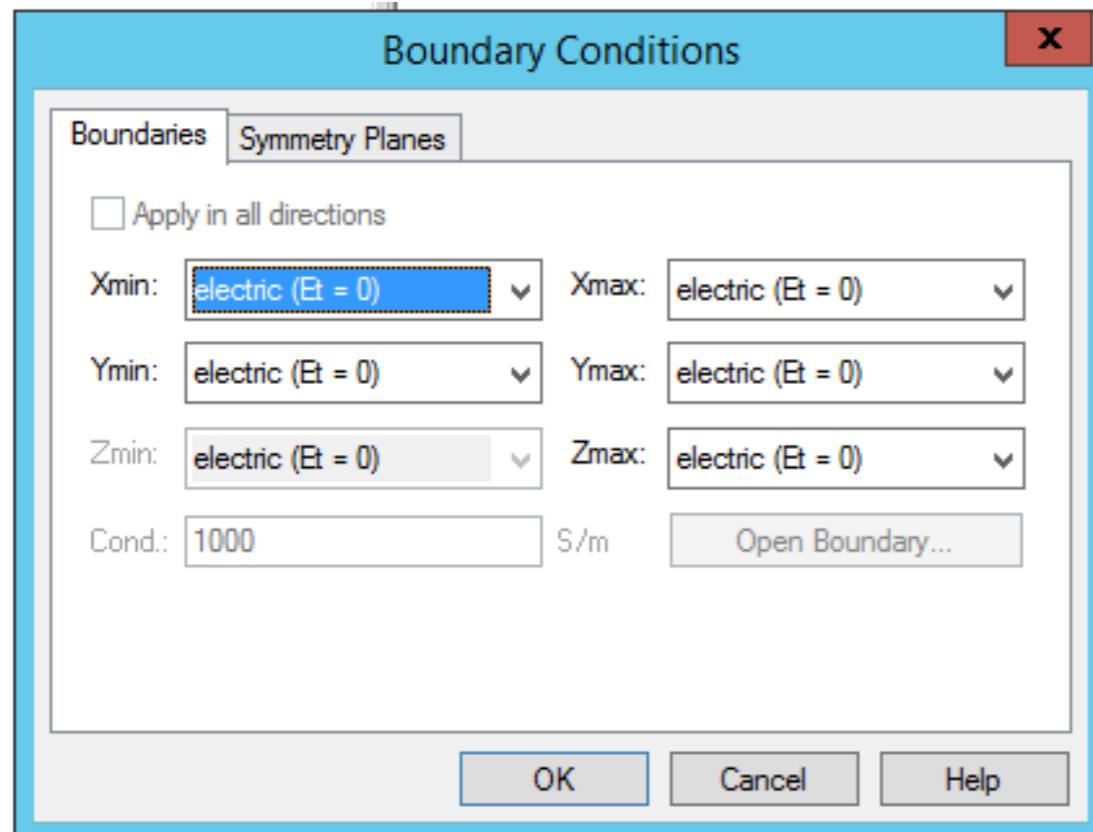
absorber	
Type	Normal
Epsilon	5
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Electric cond.	0.5 [S/m]



... by the way: Which kind of computation results in S-parameters ?

We need:

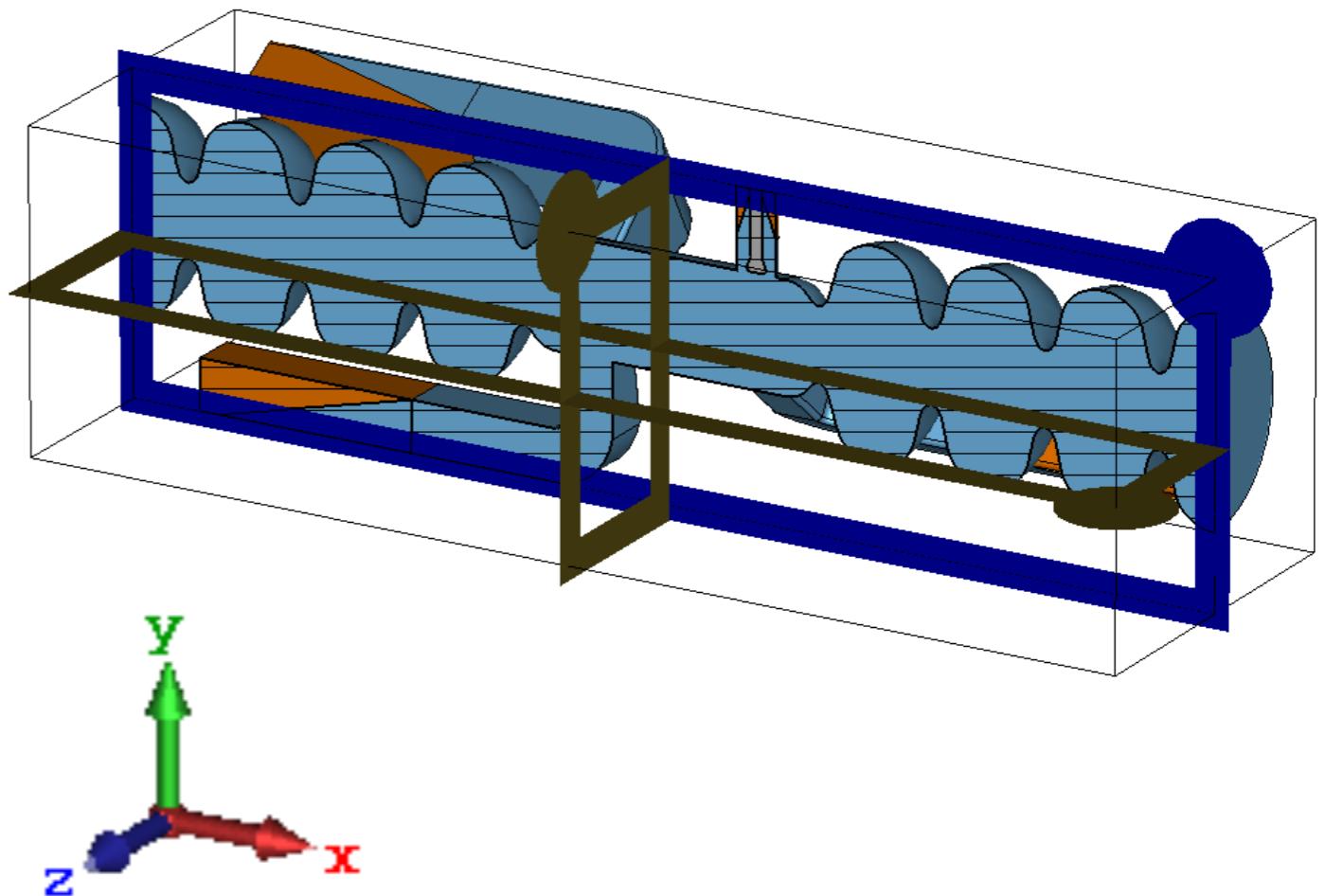
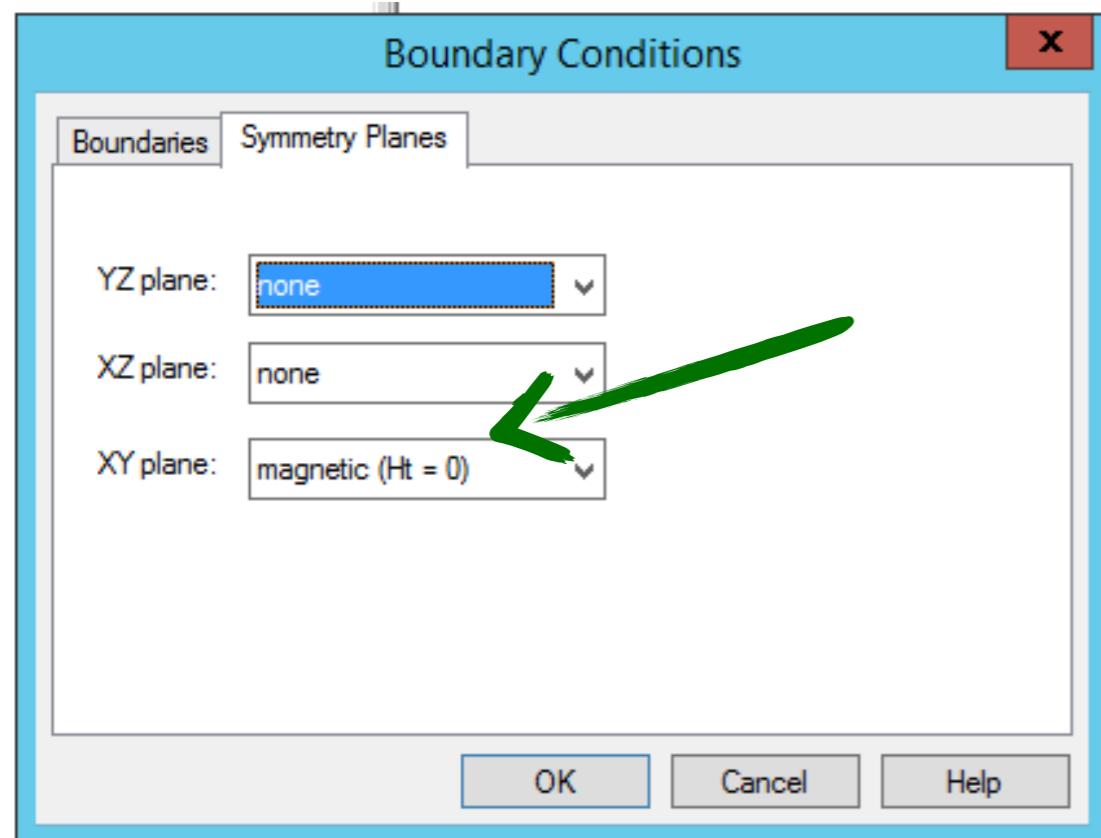
3.) boundary conditions, which define field behavior where the structure touches the borders of the computation domain, here: everywhere **Perfect Electric Conductor (PEC)** like the background material, short-cutting every tangential electric field (like a good conductor)



... by the way: What would you think is a PMC ?

We can (in this case) take profit of:

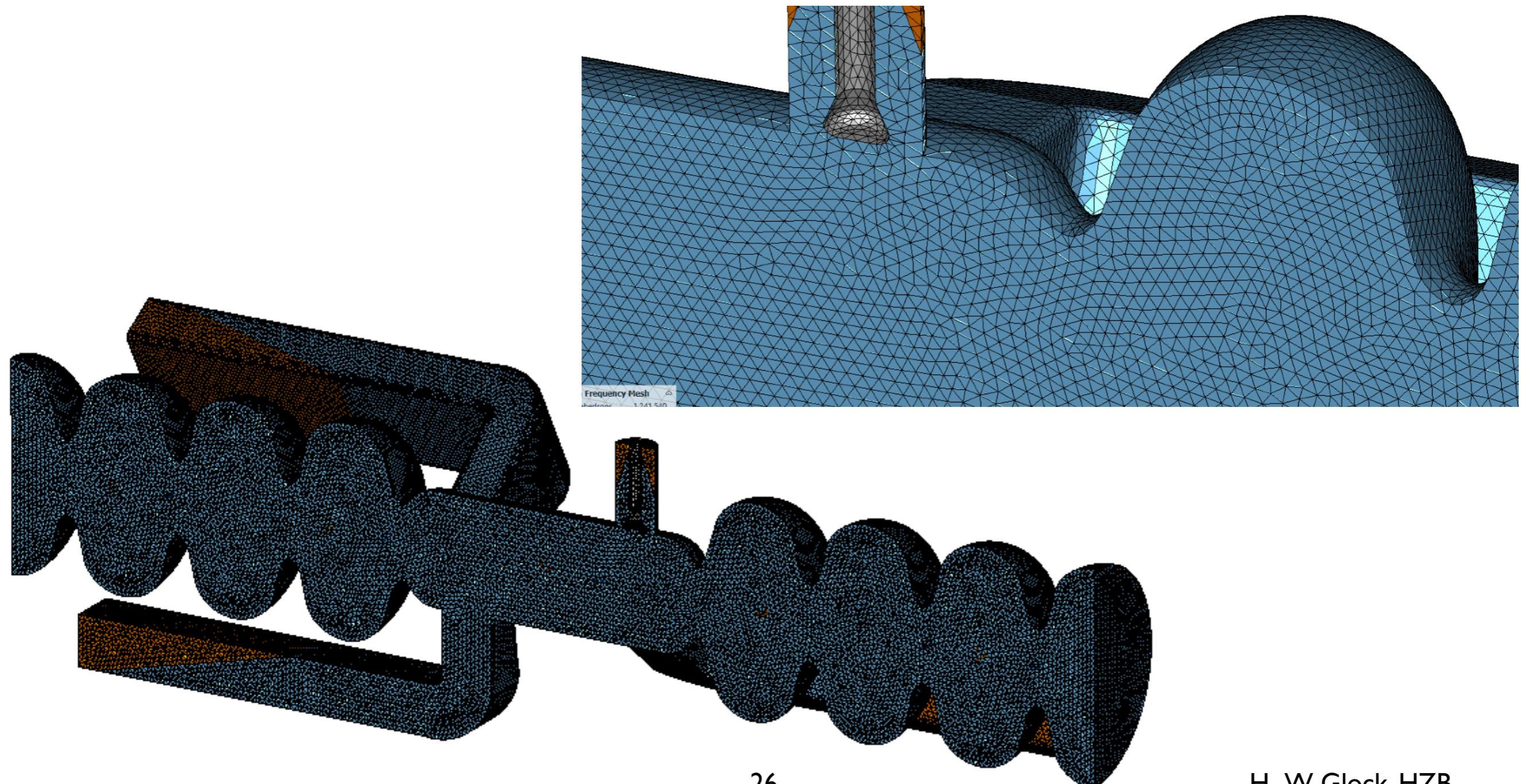
3.) a structure's symmetry plane, by defining one of the two different kind of fields only possible under those conditions.



... by the way: What kind of fields do you expect if $E_{\text{tangential}} = 0$ in the symmetry plane?

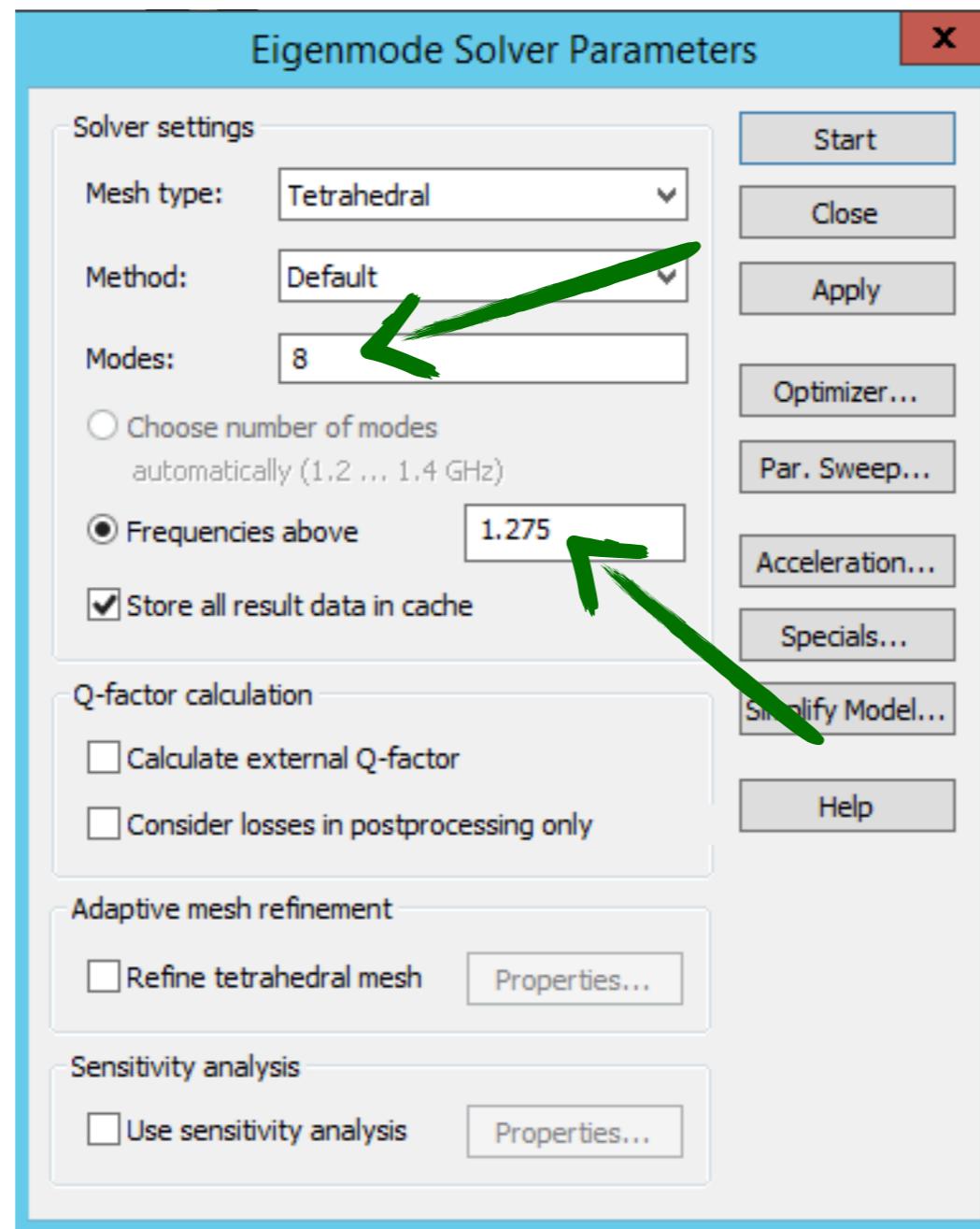
We need:

4.) a mesh to reduce the problem to a finite number of unknowns. Most common is a volume discretization in irregular tetrahedrons



We need:

5.) some parameters to control the solver, especially how many modes we are looking for starting at which frequency:



... by the way: How many modes can exist in a cavity ?

We get (after 760 s @ 12core Xeon® E5-2643v2, 3.50 GHz, allocating ~14 GB RAM) :

I.) a list of mode frequencies (here together with Q-values, cave: volume losses only)

Mode	Frequency	Accuracy	Q (volume losses)
1	1.274571 GHz	1.266e-07	infinity
2	1.274573 GHz	1.15e-07	infinity
3 ^	1.283637 GHz	5.505e-08	3.638e+07
4	1.283671 GHz	4.526e-08	infinity
5 ^	1.295234 GHz	1.678e-07	1.542e+07
6	1.29524 GHz	2.28e-07	infinity
7	1.300506 GHz	6.906e-08	infinity
8 ^	1.30052 GHz	1.166e-07	2.413e+07

^ = The material properties at the evaluation frequency differ from those at the eigenfrequency.

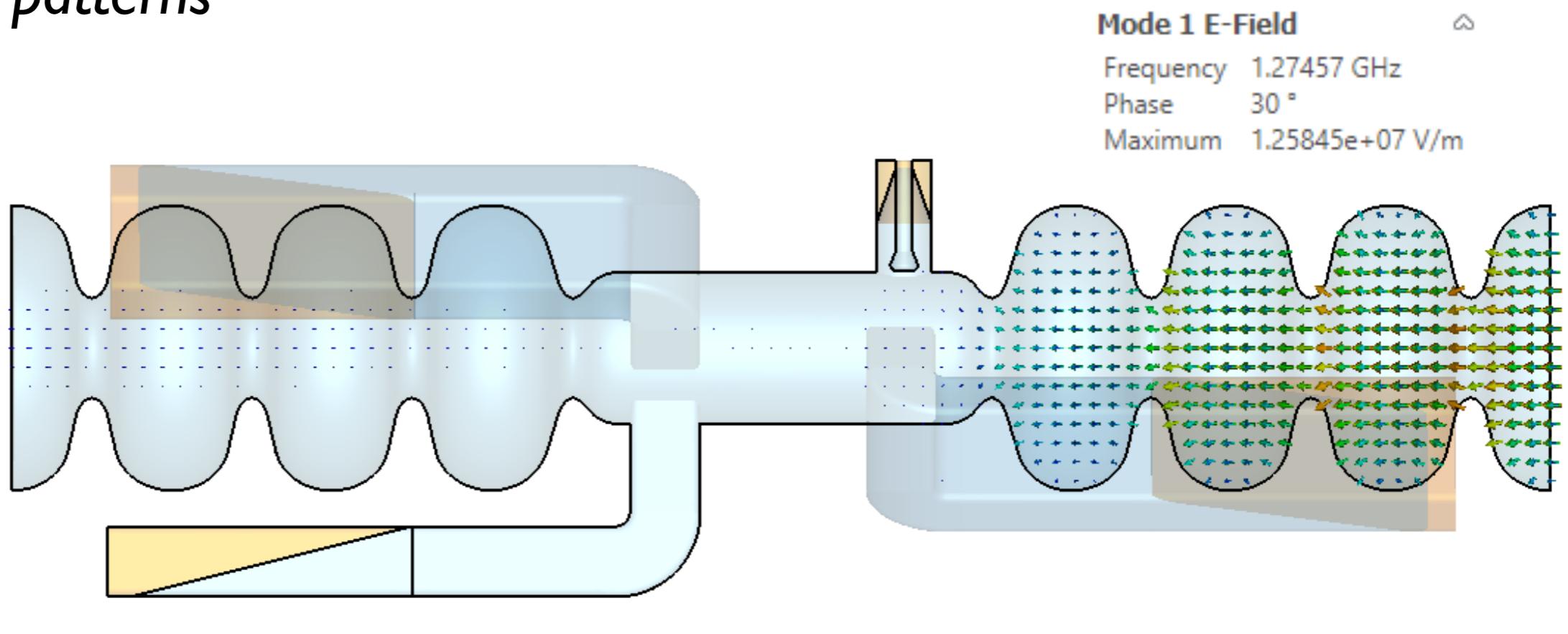
Eigenmode solver successful

Messages Progress

... by the way: Which order of Q-value do you expect for a good copper cavity ?

We get :

2.) a list of according eigenmode field (E -, H -, energy density, surface currents) patterns



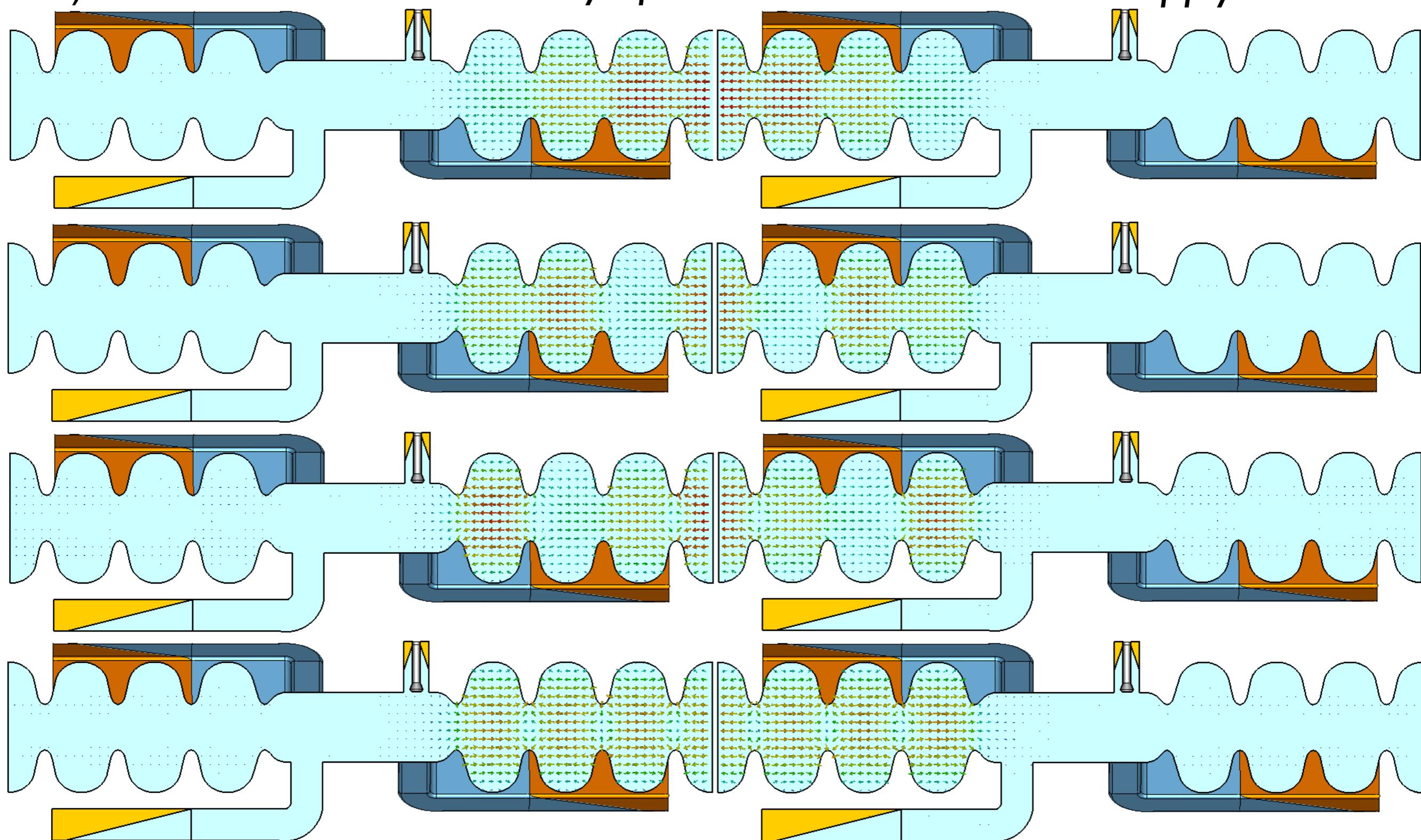
Attention: Complex-valued fields have real and imaginary part, i.e. a phase.

Phase 0° not necessarily means highest field values.

... by the way: How are the currents in the cavity (inner) surface correlated with the H -field directly above ?

We get :

3.) an idea how well the theory of identical resonator chains apply

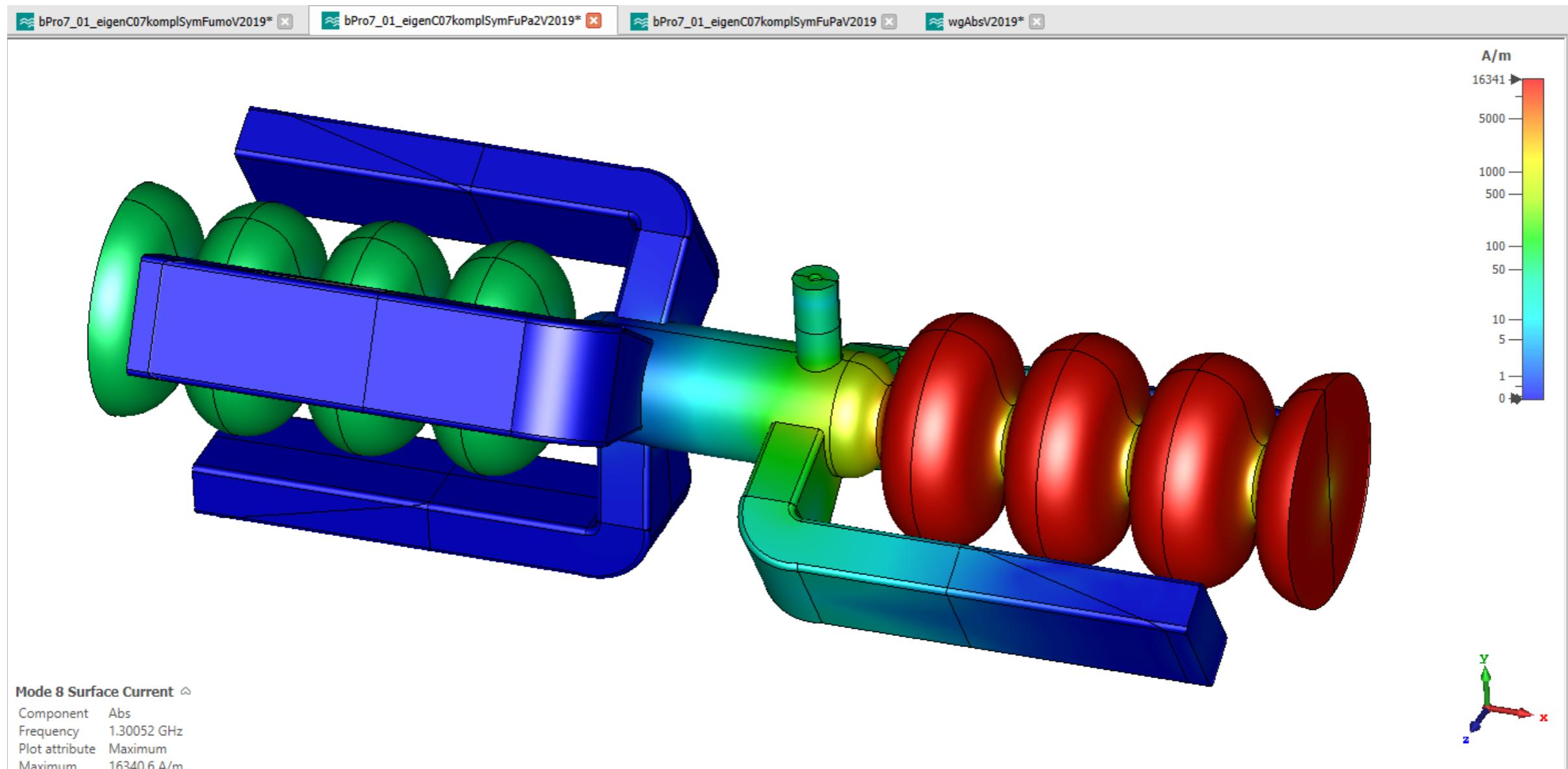


... by the way: How can we compute the missing modes of the passband ?

We get :

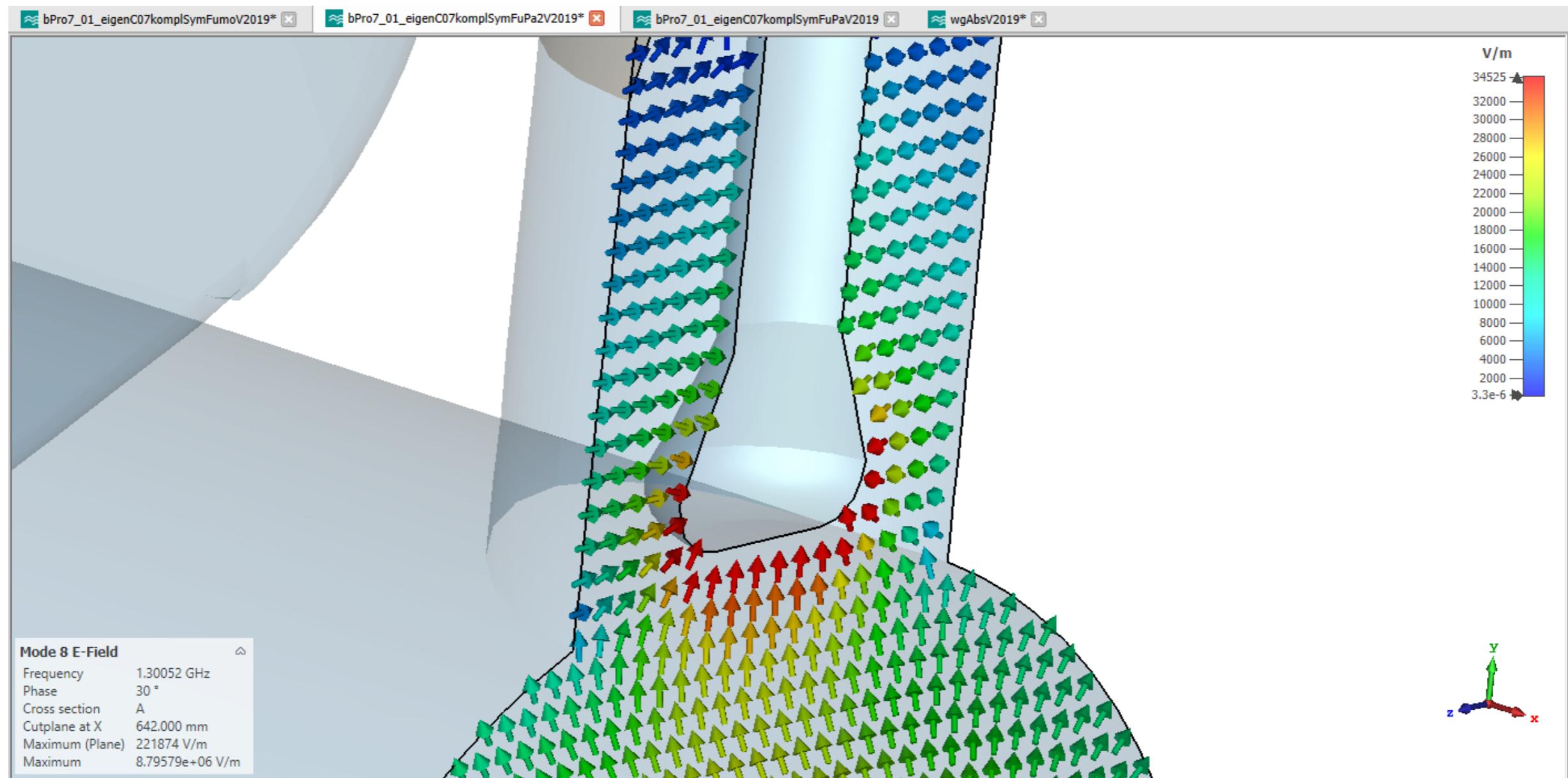
4.) a lot of further fancy post-processing information

e.g. logarithmic-scaled surface current density



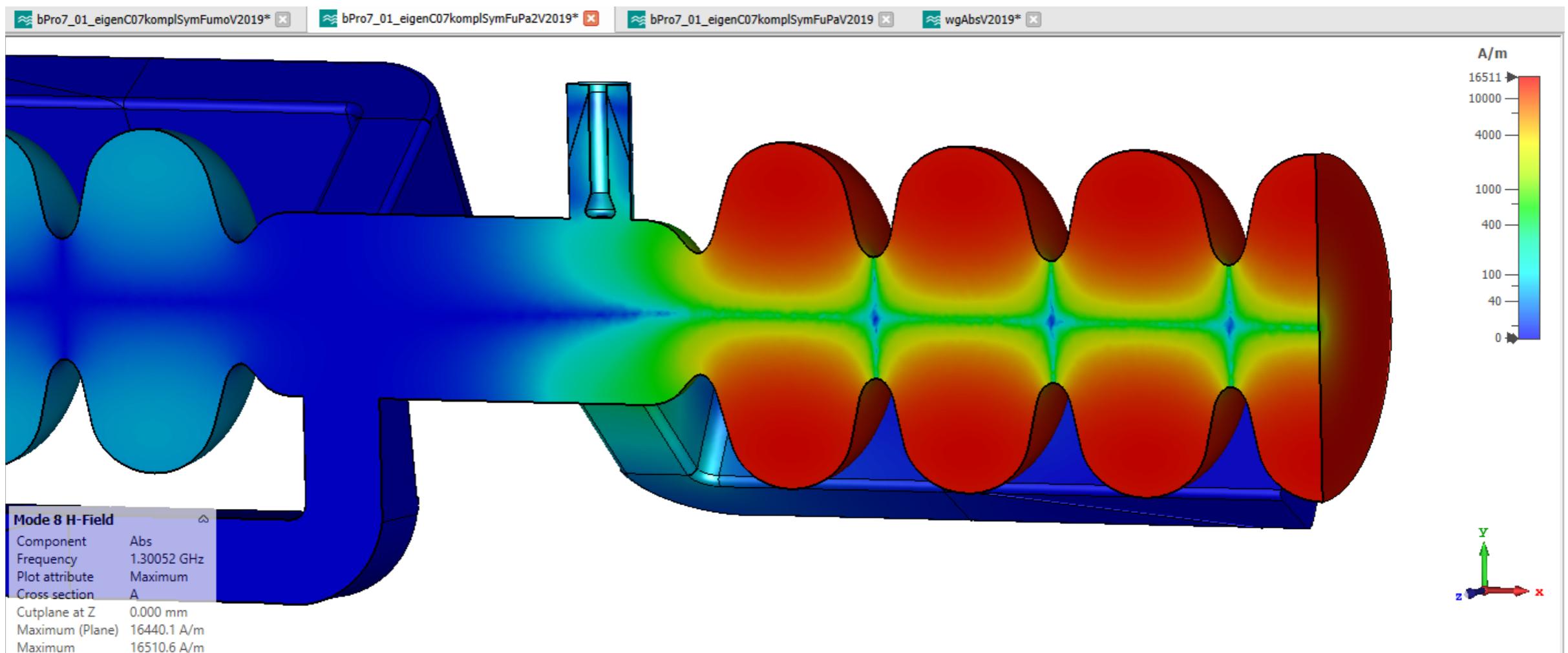
We get :

4.) a lot of further fancy post-processing information
the electric field distribution close to the coupler tip



We get :

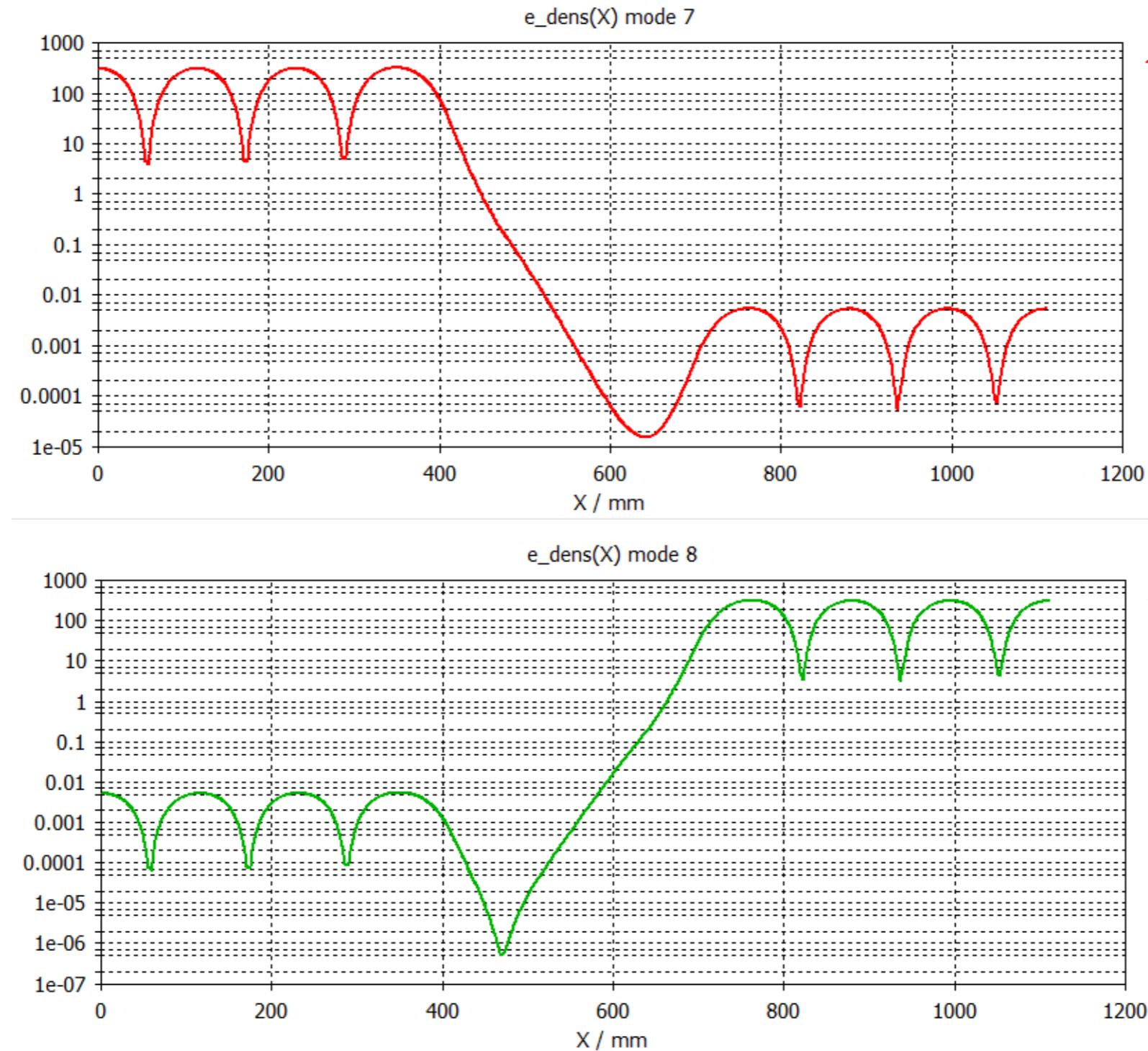
4.) a lot of further fancy post-processing information
leaking of the fundamental mode's H-field into the beam pipe



We get :

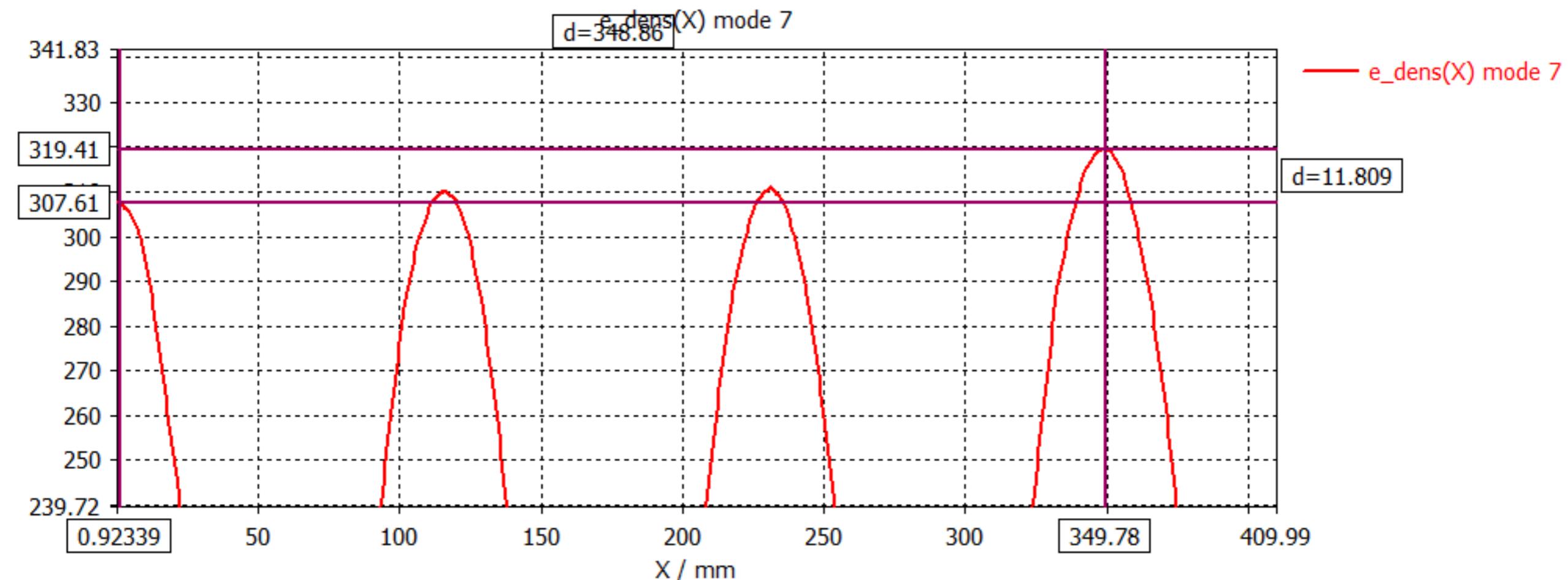
4.) a lot of further fancy post-processing information

cavity-cavity coupling of the fundamental mode



We get :

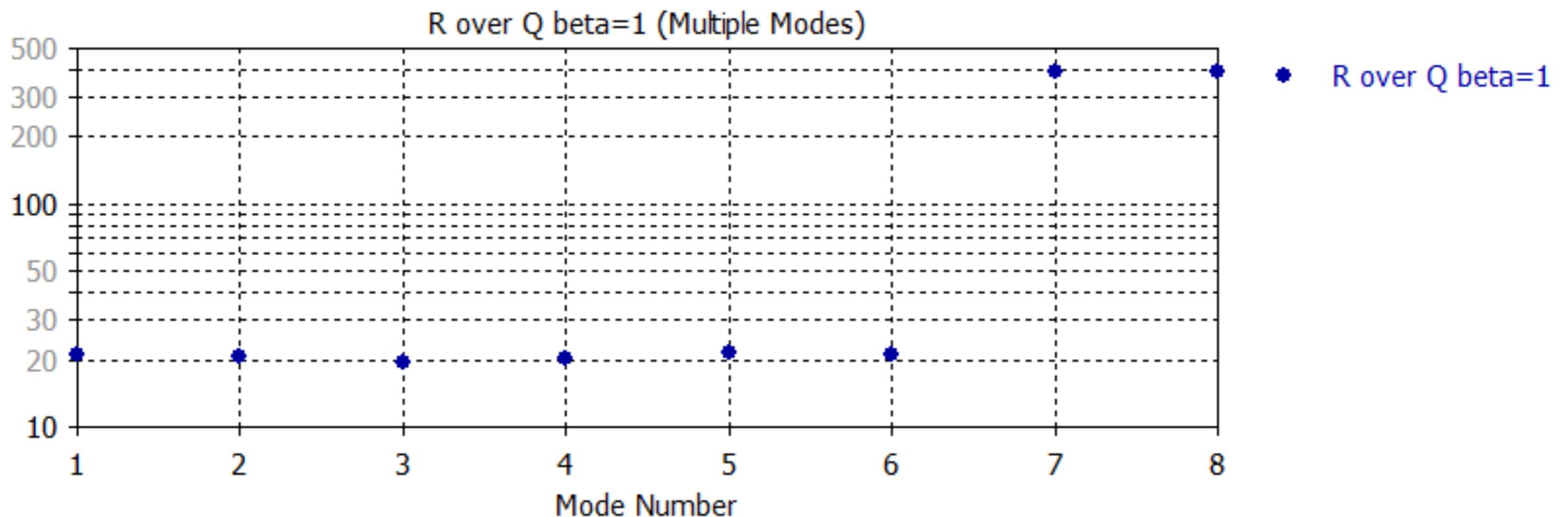
4.) a lot of further fancy post-processing information
(numerical) field flatness



... by the way: Which kind of experiment gives this information for a real-world-cavity ?

We get :

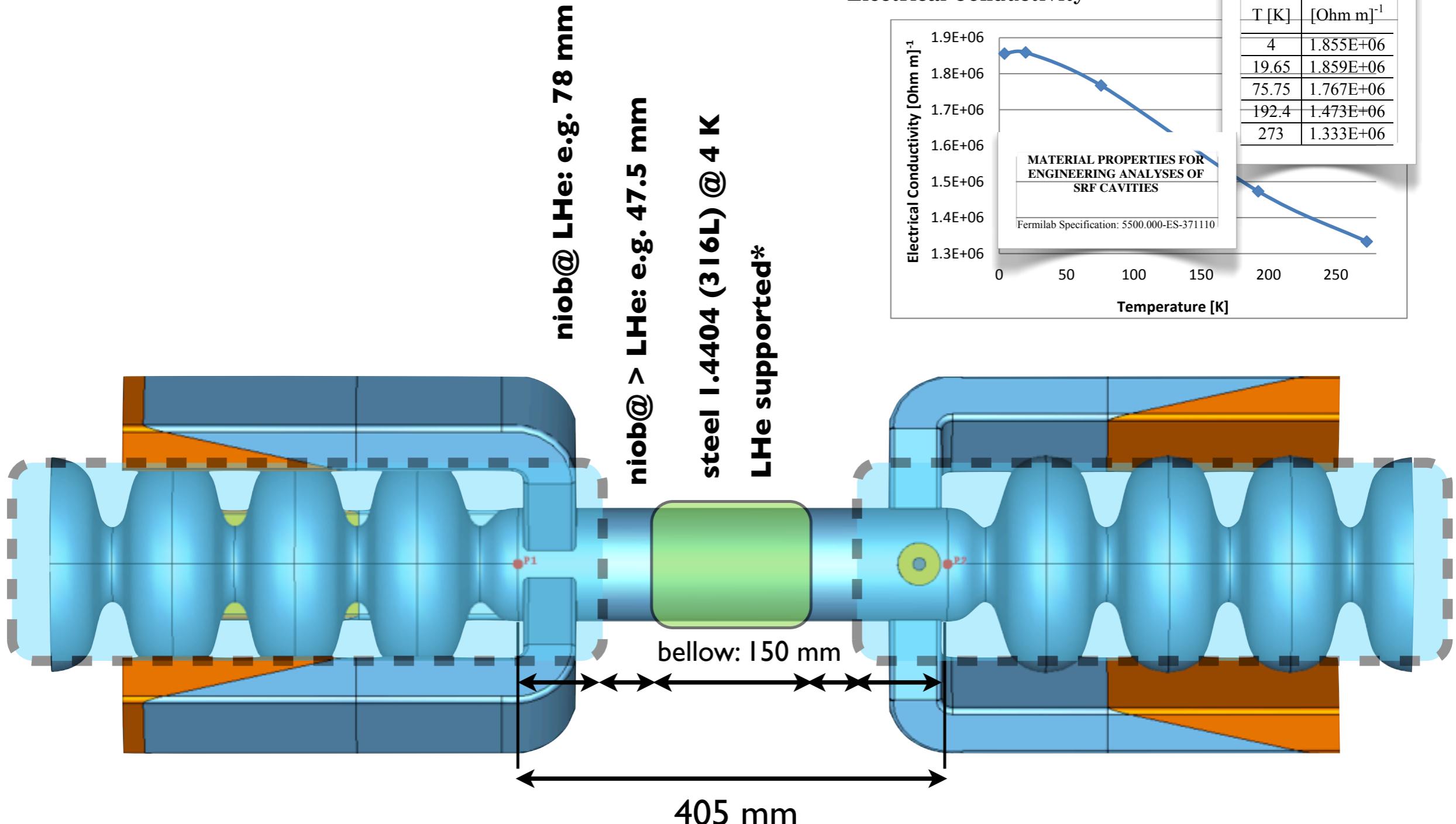
4.) a lot of further fancy post-processing information
(numerical) field flatness



... by the way: Is the R/Q-value depending on the test particle's velocity ?

An engineering question, based on eigenmodes:

Cavity-cavity-connection: Something similar to this ...

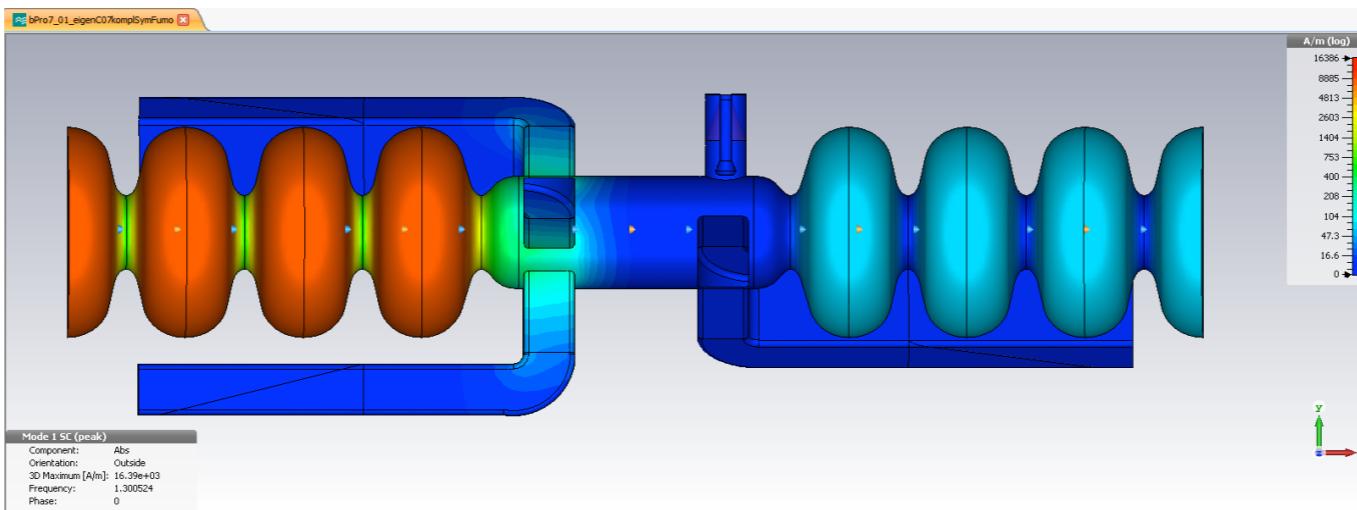


Questions and inputs:

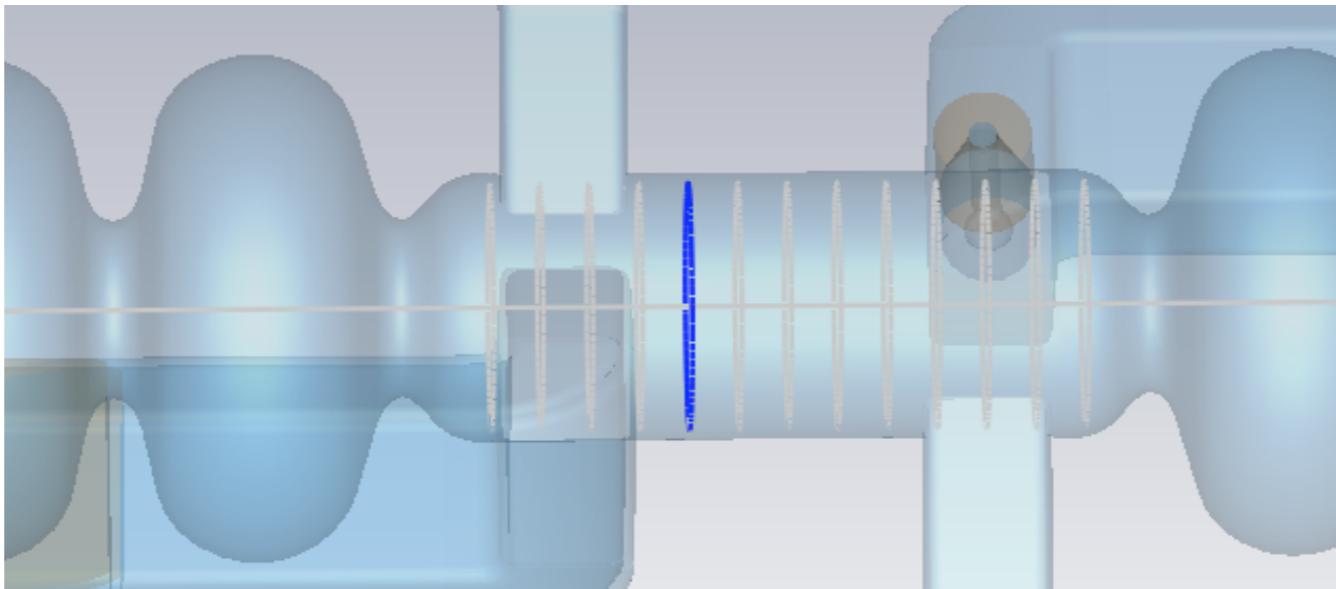
- How far to extend superconducting material from accelerating cavities into beam pipe?
- What is going to happen outside the LHe-vessel?
- Fundamental mode surface resistance $R_s(T)$ and thermal conductivity $\lambda(T)$ strongly depend on temperature. \Rightarrow Severely non-linear problem
- 1-dimensional approach to keep effort reasonable but gain "feeling" (also provide benchmark for any 3-dim).
- Include distributed fundamental mode losses, concentrated heat flux from "nc bellow" and fixed temperature boundary at "LHe bath".

Fundamental Loss Calculations

- eigenmode computation of fundamental mode, H_{tan} @ surface = j_{surf}

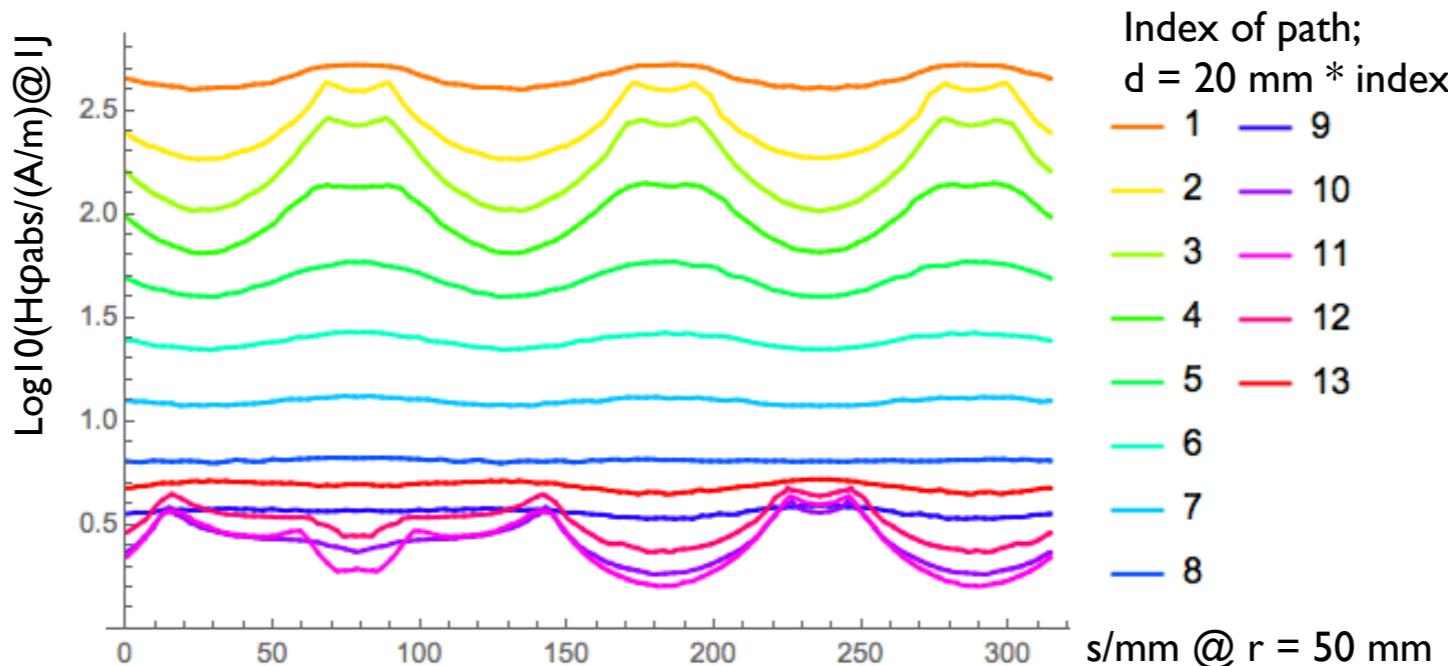


- sampling along axially equidistant circular paths, close to inner surface

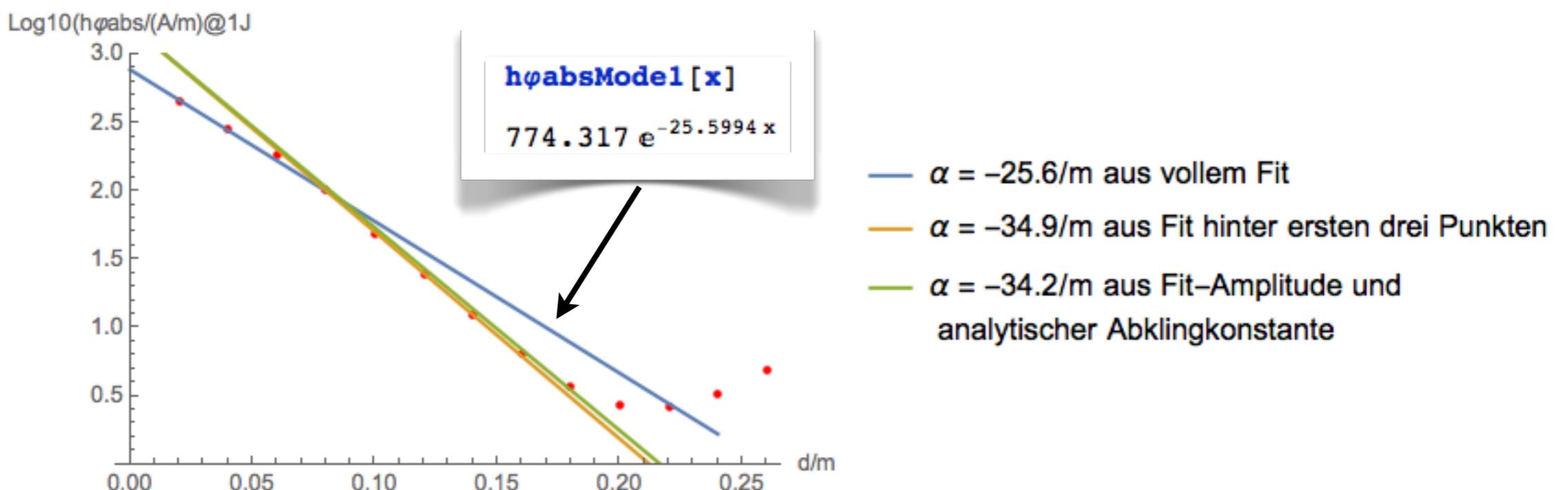


Fundamental Loss Calculations II

- taking average of circumferential field profiles to eliminate disturbances by WGs



- fit exponential dependence to sampled (average) values; compare to analytics



Fundamental Loss Calculations III

- scale field amplitude from CST-convention: "stored energy = $\int J^2$ "

CST - with transittime factor: energy gain of 1.8005×10^6 Volt in 3,5 cells.
calculation for 25 MV/m:

$$\text{feldSkalier} = \frac{25 \times 10^6 \text{ Volt / Meter} * 0.8 \text{ Meter}}{2 * 1.8005 \times 10^6 \text{ Volt}}$$

5.55401

$$h\varphi[x_] := \text{feldSkalier} * h\varphi_{absModel}[x]$$

$$\text{linienLeistung}[rs_, x_] := 2 \pi 0.055 \text{ Meter} \frac{rs}{2} (h\varphi[x] \text{ Ampere / Meter})^2$$

- for steel parts determine surface impedance from conductivity, frequency
(, permeability)

normaler Skineffekt liefert

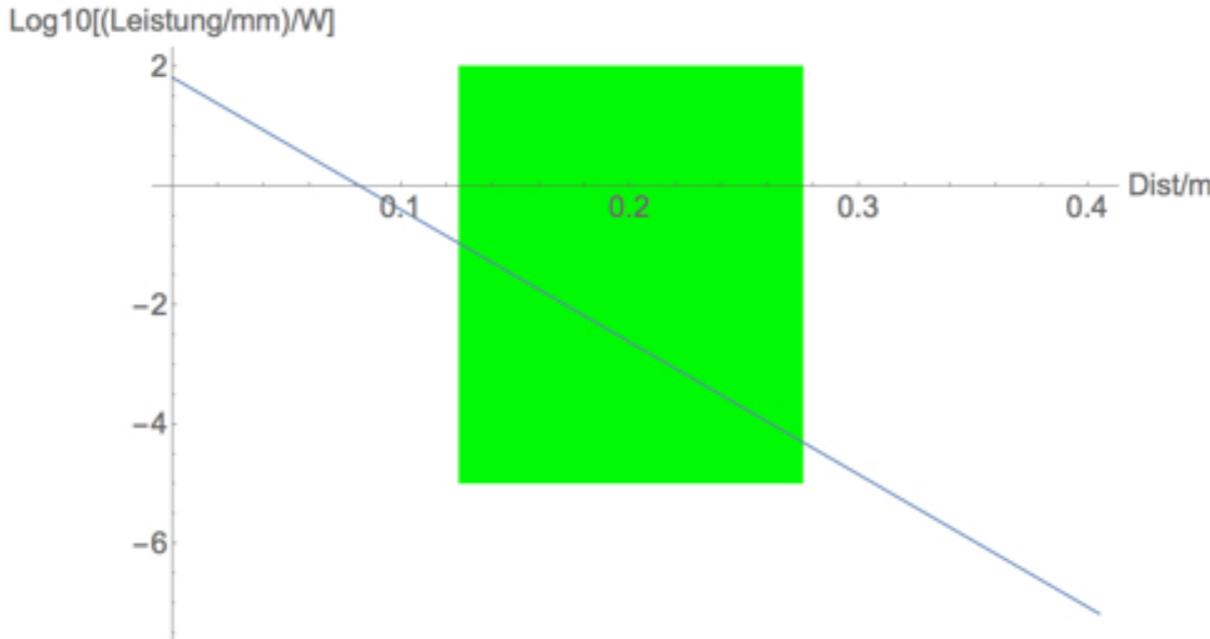
$$rSur[\omega_, \mu_r_, cond_] := \sqrt{\frac{\omega \mu_r 4 \pi 10^{-7} \text{ Volt Sekunde}}{2 cond \text{ Ampere Meter}}}$$

$$\frac{0.02096 \text{ Volt}}{\text{Ampere}}$$

... by the way: Is stainless steel „magnetic“ ?

Fundamental Loss Calculations IV

- dissipated fundamental power (no wakes) per mm straight beam pipe length @ 25 MV/m, **steel 316L**, excited by ONE cavity



- integrated over bellow (ignoring corrugation): 2.1 Watt

```
intPowSteel4K[{0.078 + 0.0475, 0.078 + 0.0475 + 0.150} Meter]  
2.11771 Ampere Volt
```

- hypothetically 20 mm closer to the cavity: 5.9 Watt

```
intPowSteel4K[{0.078 + 0.0475 - 0.02, 0.078 + 0.0475 + 0.150 - 0.02} Meter]  
5.89623 Ampere Volt
```

... by the way: What is the Carnot efficiency for a refrigerator cooling from 300 K to 2 K ?

Temperature-dependent thermal conductivity of niobium

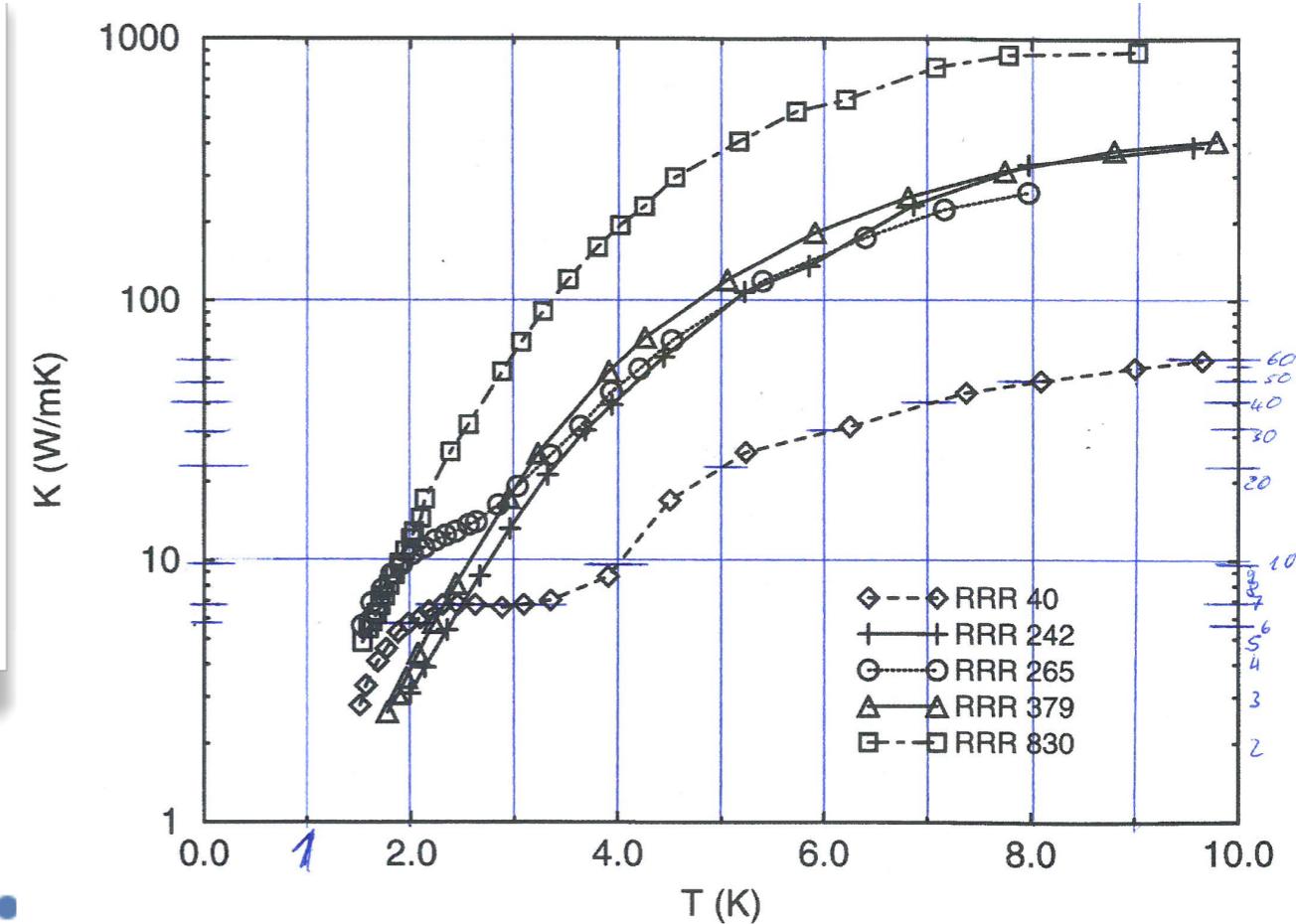
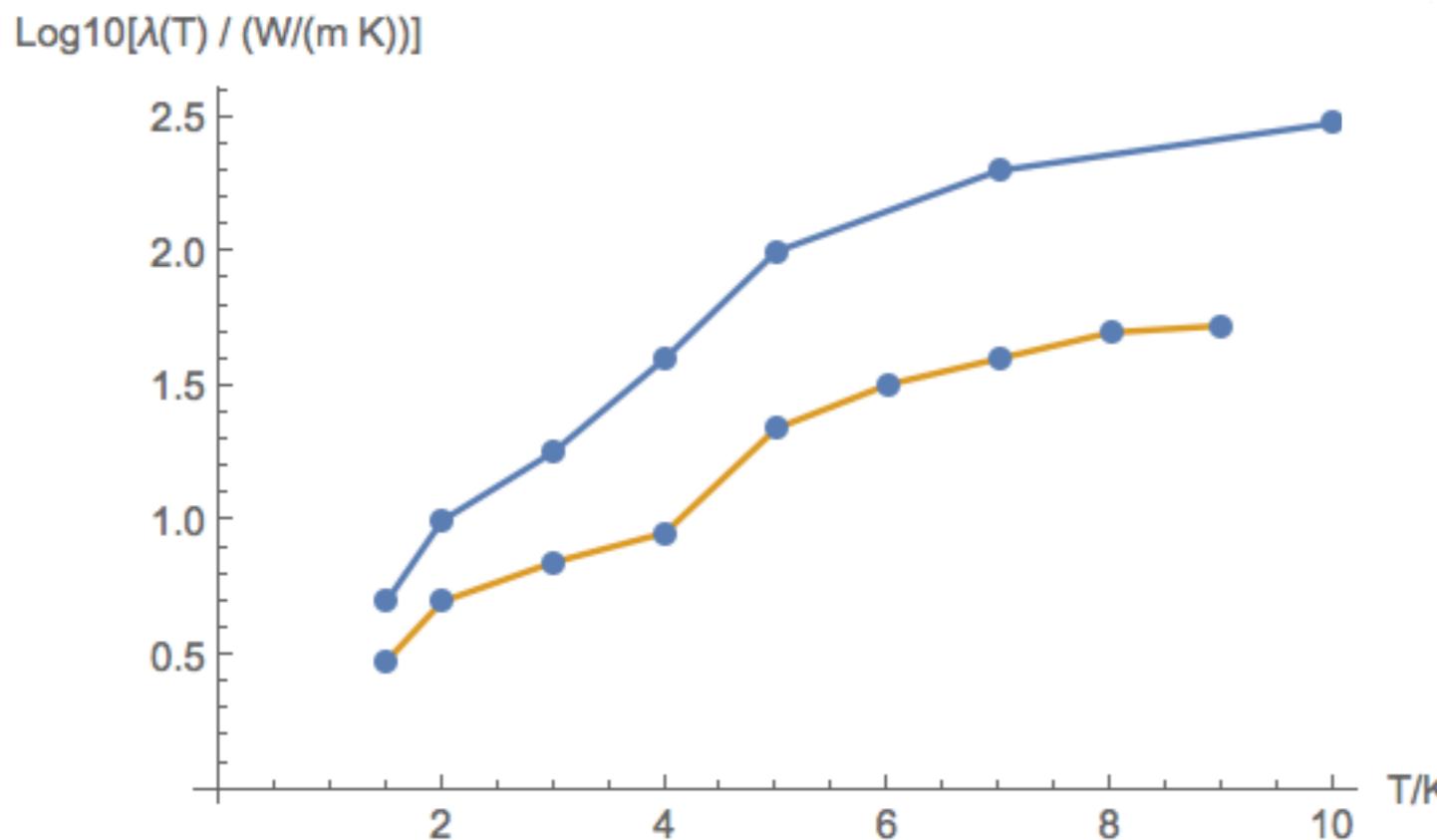
Supercond. Sci. Technol. 9 (1996) 453–460. Printed in the UK

Parametrization of the niobium thermal conductivity in the superconducting state

F Koechlin and B Bonin

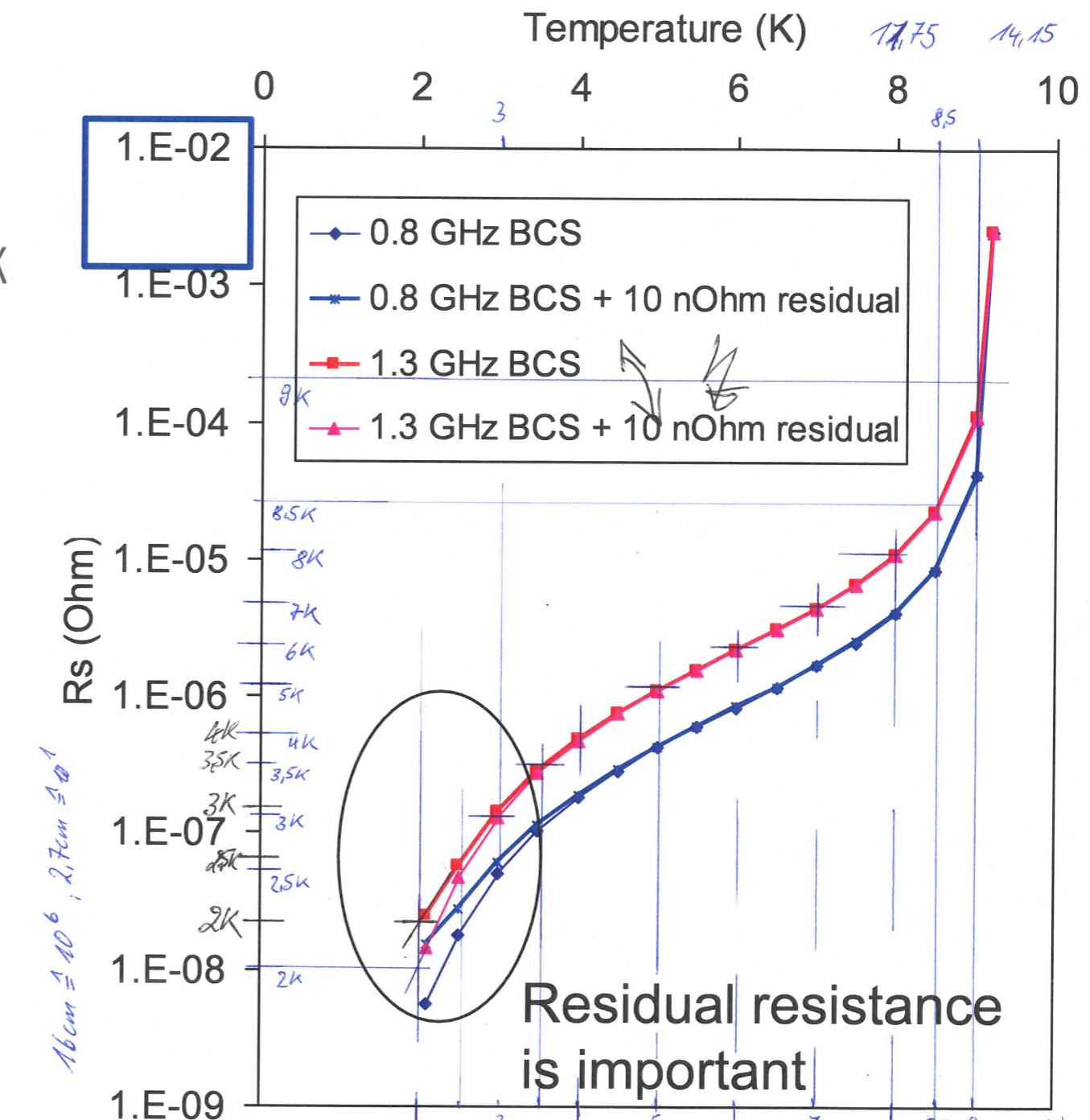
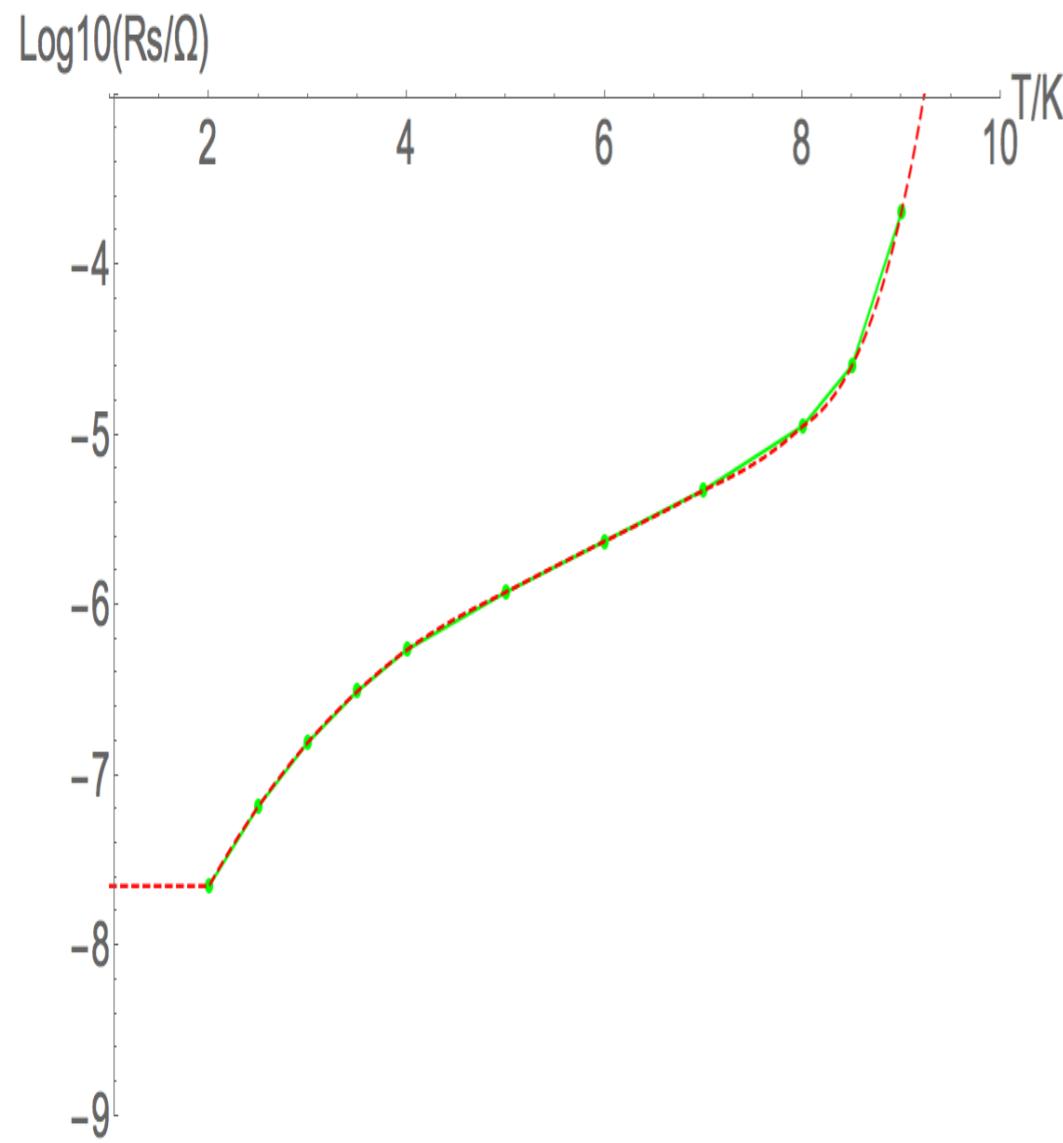
CEA, DSM/DAPNIA/Service d'Etudes d'Accelerateurs C E Saclay,
91191 Gif sur Yvette, France

Received 5 February 1996



— RRR 270 @ Singer/Koechlin+Bonin Fit
— RRR 40 @ Koechlin+Bonin exp.

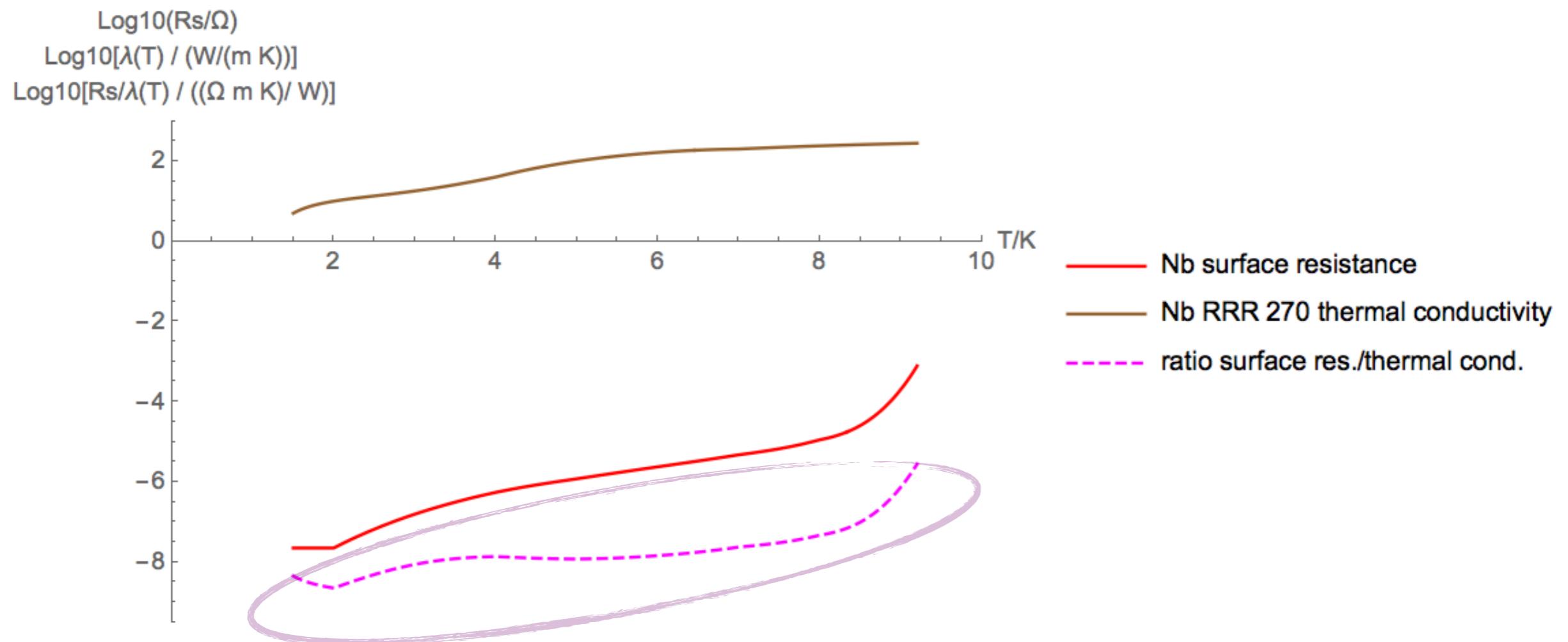
Temperature-dependent surface resistance of niobium



author ??, very recommendable source: uspas.fnal.gov/materials/13Duke/SCL_ChapI.pdf

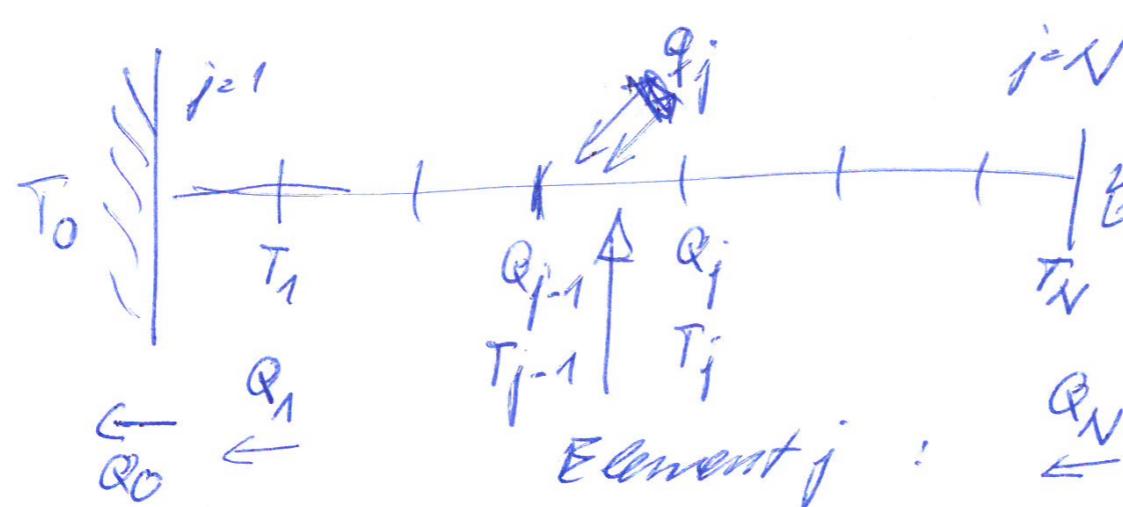
data close to Halbitter SRIMP, now online <https://www.classe.cornell.edu/~liepe/webpage/researchsrimp.html>

Temperature-dependent Nb surface resistance and thermal conductivity



surface resistance \sim dissipated power grows faster than thermal conductivity \Rightarrow the colder, the cooler

1-dimensional model of stationary heat flux



Folles
Stationar.

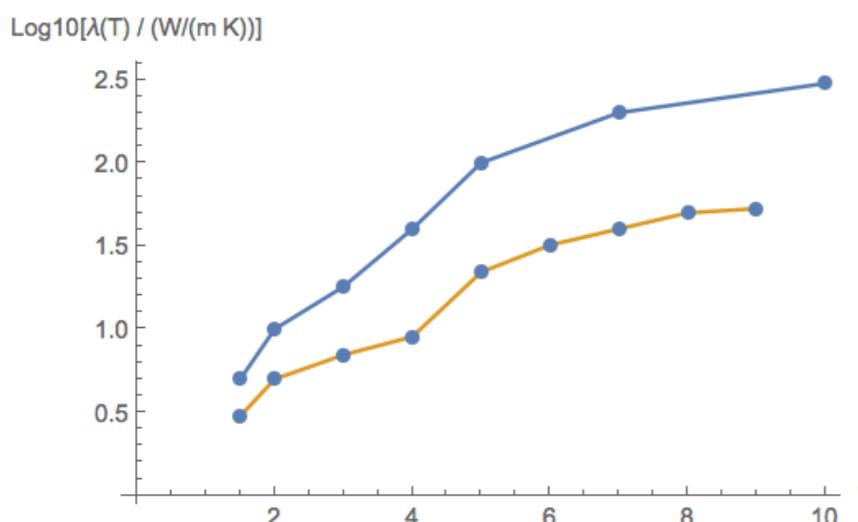
T1
25.11.15

$$Q_{j-1} = Q_j + q_j \quad q_j > 0 \text{ für abgewinkelte Wärmeleitung}$$

$$T_j = T_{j-1} + Q_j \cdot \frac{\ell_j}{R_j} + q_j \cdot \frac{\ell_j}{2 R_j}$$

↑
positiver Wärmestrom
bedeutet $T_j > T_{j-1}$
 T_0 : kalt, T_N warm

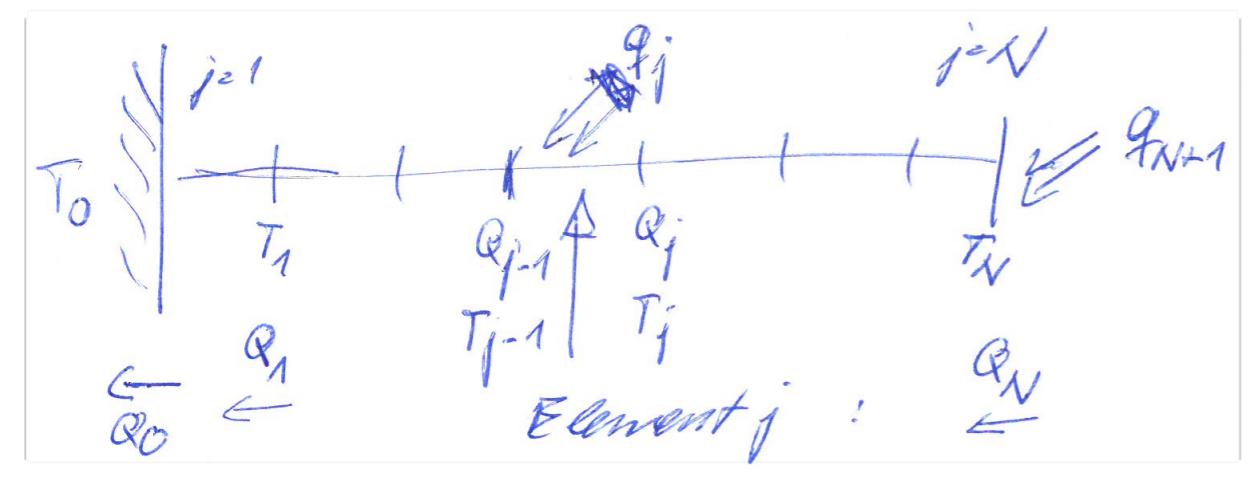
↑
zusätzlicher Wärme-
eintrag wird nur auf
halber Länge gezählt



— RRR 270
— RRR 40

$$R_j = R_j \left(\frac{T_j + T_{j-1}}{2} \right)$$

1-dimensional model of stationary heat flux



essentially a series of *heat flux resistors*,
unfortunately strongly temperature-dependent
and a chain of *heat flux sources*, temperature- and
EM-field-dependent

$$t_0 + \frac{11 \left(\frac{q_1}{2} + q_2 + q_3 + q_4 + q_5 \right)}{a_1 \lambda f_u \left[\frac{t_0 + t_1}{2} \right]}$$

$$t_0 + \frac{11 \left(\frac{q_1}{2} + q_2 + q_3 + q_4 + q_5 \right)}{a_1 \lambda f_u \left[\frac{t_0 + t_1}{2} \right]} + \frac{12 \left(\frac{q_2}{2} + q_3 + q_4 + q_5 \right)}{a_2 \lambda f_u \left[\frac{t_1 + t_2}{2} \right]}$$

$$t_0 + \frac{11 \left(\frac{q_1}{2} + q_2 + q_3 + q_4 + q_5 \right)}{a_1 \lambda f_u \left[\frac{t_0 + t_1}{2} \right]} + \frac{12 \left(\frac{q_2}{2} + q_3 + q_4 + q_5 \right)}{a_2 \lambda f_u \left[\frac{t_1 + t_2}{2} \right]} + \frac{13 \left(\frac{q_3}{2} + q_4 + q_5 \right)}{a_3 \lambda f_u \left[\frac{t_2 + t_3}{2} \right]}$$

$$t_0 + \frac{11 \left(\frac{q_1}{2} + q_2 + q_3 + q_4 + q_5 \right)}{a_1 \lambda f_u \left[\frac{t_0 + t_1}{2} \right]} + \frac{12 \left(\frac{q_2}{2} + q_3 + q_4 + q_5 \right)}{a_2 \lambda f_u \left[\frac{t_1 + t_2}{2} \right]} + \frac{13 \left(\frac{q_3}{2} + q_4 + q_5 \right)}{a_3 \lambda f_u \left[\frac{t_2 + t_3}{2} \right]} + \frac{14 \left(\frac{q_4}{2} + q_5 \right)}{a_4 \lambda f_u \left[\frac{t_3 + t_4}{2} \right]}$$

$$t_0 + \frac{11 \left(\frac{q_1}{2} + q_2 + q_3 + q_4 + q_5 \right)}{a_1 \lambda f_u \left[\frac{t_0 + t_1}{2} \right]} + \frac{12 \left(\frac{q_2}{2} + q_3 + q_4 + q_5 \right)}{a_2 \lambda f_u \left[\frac{t_1 + t_2}{2} \right]} + \frac{13 \left(\frac{q_3}{2} + q_4 + q_5 \right)}{a_3 \lambda f_u \left[\frac{t_2 + t_3}{2} \right]} + \frac{14 \left(\frac{q_4}{2} + q_5 \right)}{a_4 \lambda f_u \left[\frac{t_3 + t_4}{2} \right]} + \frac{15 q_5}{2 a_5 \lambda f_u \left[\frac{t_4 + t_5}{2} \right]}$$

$$\Rightarrow T_1 = T_0 + \frac{\ell_1}{R_1 \left(\frac{T_0 + T_1}{2} \right) A_1} \cdot \left(\frac{q_1}{2} + \sum_{j=2}^{N+1} q_j \right)$$

$$T_2 = T_1 + \frac{\ell_2}{R_2 \left(\frac{T_1 + T_2}{2} \right) A_2} \cdot \left(\frac{q_2}{2} + \sum_{j=3}^{N+1} q_j \right) =$$

$$= T_0 + \frac{\ell_1}{R_1 \left(\frac{T_0 + T_1}{2} \right) A_1} \cdot \left(\frac{q_1}{2} + \sum_{j=2}^{N+1} q_j \right) +$$

$$+ \frac{\ell_2}{R_2 \left(\frac{T_1 + T_2}{2} \right) A_2} \cdot \left(\frac{q_2}{2} + \sum_{j=3}^{N+1} q_j \right)$$

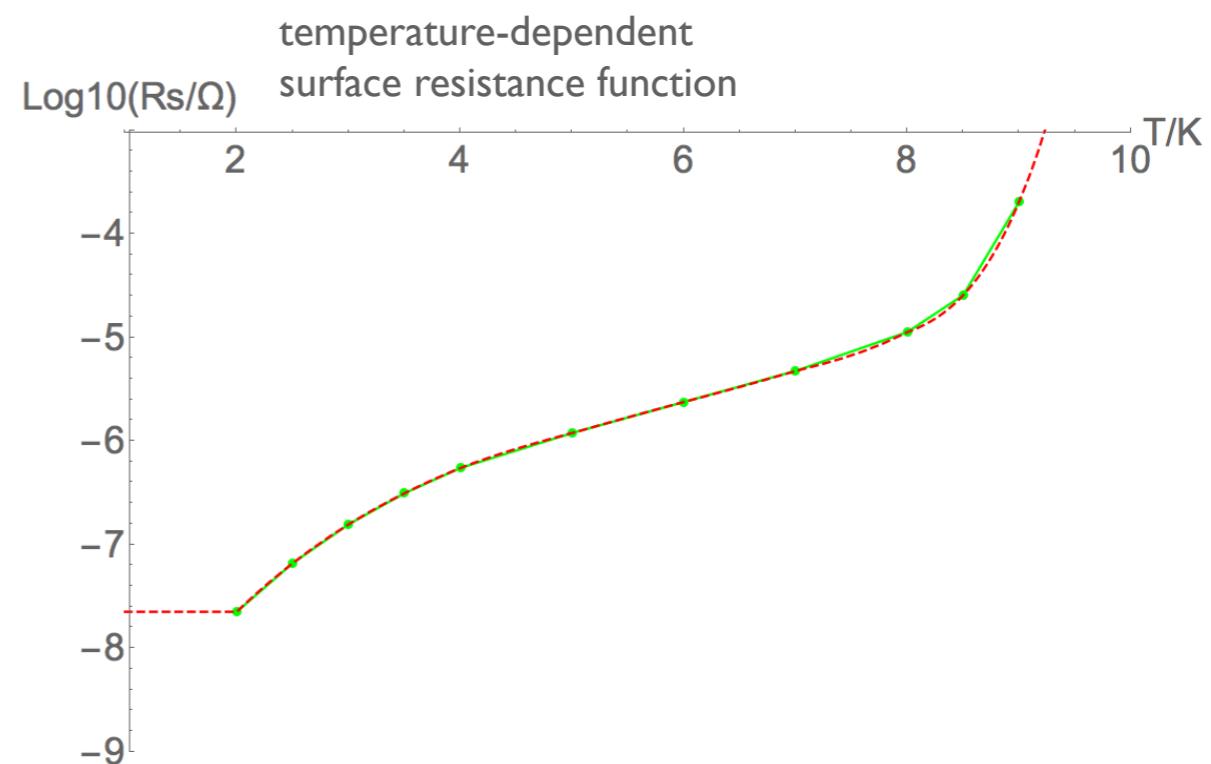
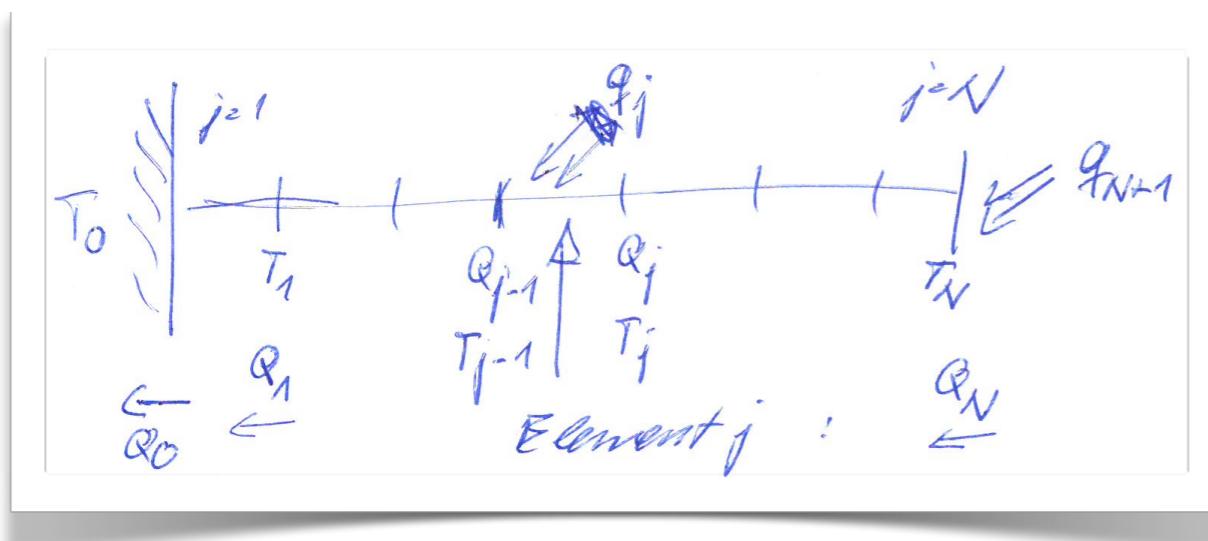
$$T_3 = T_2 + \frac{\ell_3}{R_3 \left(\frac{T_2 + T_3}{2} \right) A_3} \cdot \left(\frac{q_3}{2} + \sum_{j=4}^{N+1} q_j \right) =$$

$$T_3 = T_0 + \frac{\ell_1}{R_1 \left(\frac{T_0 + T_1}{2} \right) A_1} \cdot \left(\frac{q_1}{2} + \sum_{j=2}^{N+1} q_j \right) +$$

$$+ \frac{\ell_2}{R_2 \left(\frac{T_1 + T_2}{2} \right) A_2} \cdot \left(\frac{q_2}{2} + \sum_{j=3}^{N+1} q_j \right) +$$

$$+ \frac{\ell_3}{R_3 \left(\frac{T_2 + T_3}{2} \right) A_3} \cdot \left(\frac{q_3}{2} + \sum_{j=4}^{N+1} q_j \right)$$

1-dimensional model of stationary heat flux: sources



florer $q_k = B_k \cdot \frac{\pi}{4} (T_{k-1} + T_k) \cdot \frac{H^2}{\tan k}$
 Oberflächenwiderstand
 Innenfläche
 @ 1,3668 über B_k mittelk quadrat.
 Oberflächenstromdichte

linienLeistung[*rs_*, *x_*] := $2 \pi 0.055 \text{ Meter} \frac{rs}{2} (\text{hφ}[x] \text{ Ampere / Meter})^2$
 beam pipe radius

liLeiD110[*rs_*, *x_*] := $2 \pi 0.055 \frac{rs}{2} \text{ hφ}[x]^2$ position-dependent surface current density (cf. page 7)

temperature-dependent surface resistance function artificial power scaling factor for easing convergence

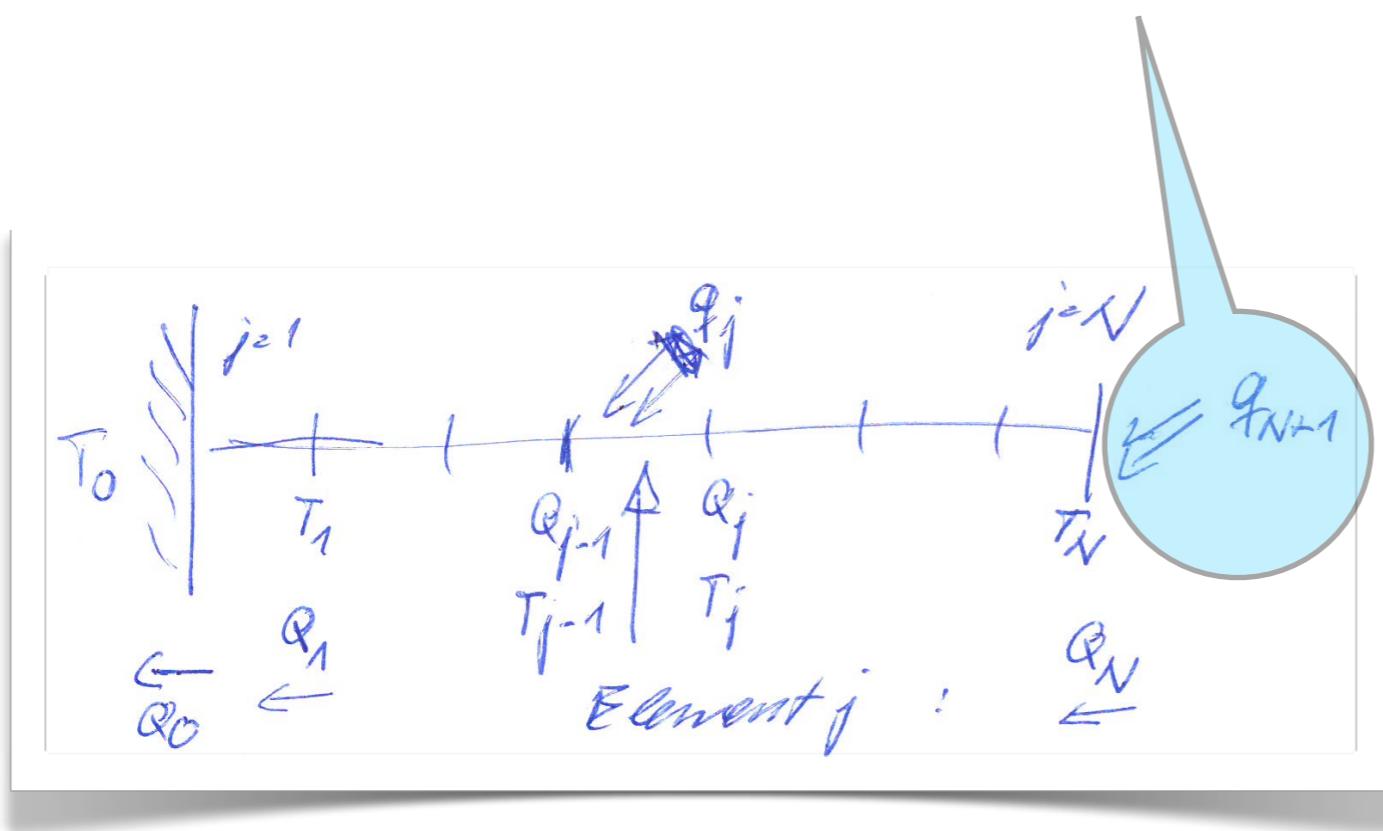
qvec = liLeiD110[nbBCS1p3GHzIP[[1]], [[2]]]*[[3]]*powerscale & /@

Transpose[{(tkvec + tksupvec)/2, absLkvec, lkvec}];
 average temperature of segments distances to reference plane lengths of individual segments

1-dimensional model of stationary heat flux: sources II

```
qvec = liLeiD110[nbBCS1p3GHzIP[[1]], #[[2]] * #[[3]] * powerscale & /@  
Transpose[{(tkvec + tksupvec) / 2, absLkvec, lkvec}];  
qvec = qvec + Join[Table[0, {Length[qvec] - 1}], {poweradd}];
```

additional power incident at the chain's end

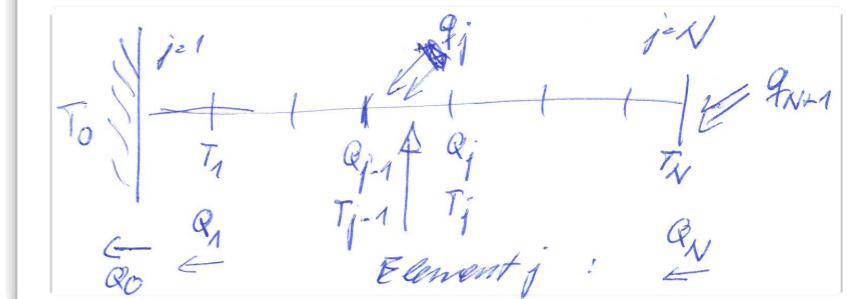


1-dimensional model of stationary heat flux: iterator

In[103]:= **increment** = 0.001

define the power growth rate
during iteration

Out[103]= 0.001



In[174]:= **iteRad** = NestList[do everything repeatedly and
store all intermediate steps

{**setSystemTkQkD110U25MV**[compute new temperature
distribution based on ...

#[[1]], ... old temperature distribution ...,

2, ... T_0 at leftmost boundary, here $T_0 = 2\text{K}$, ...

Table[0.001, {100}], ... interval lengths, here 100 intervals of 1 mm length, ...

Table[$\pi * (0.058^2 - 0.055^2)$, {100}], ... table of interconnecting surfaces, here all 3 mm thick pipes of
55 mm inner radius, ...

nbRRR270tc, ← → nbRRR270tc, ...

1, ... overall scaling of powers, here no scaling ...

8, ... additional power at the chain's end, here 8 W ...

#[[2]], ... iteration dependent scaling of power.

If[#[[2]] + **increment** > 1, 1, #[[2]] + **increment**] increment power scaling in every step by 1 %.

} &,

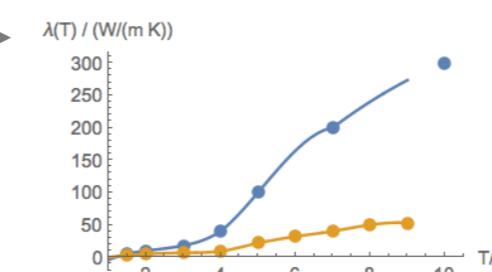
{**Table**[2, {100}], 0.001}, start iteration with overall temperature of 2 K for all
100 segments, initial power scaling 0.001
1100; do 1100 steps

(**Flatten**[{{#[[2]], #[[1]]}}] & /@ **iteRad**) [[1 ;; -1 ;; 50, 1 ;; -1 ;; 10]] // **TableForm**

write iteration-dependent scaling as first entry;

show every 50th iteration;

show every 10th segment



... temperature dependent
thermal conductivity, here of
Nb RRR 270, ...

1-dimensional model of stationary heat flux: typical result

write
iteration-
dependent
scaling as
first entry

all temperatures in K

show every 10th segment

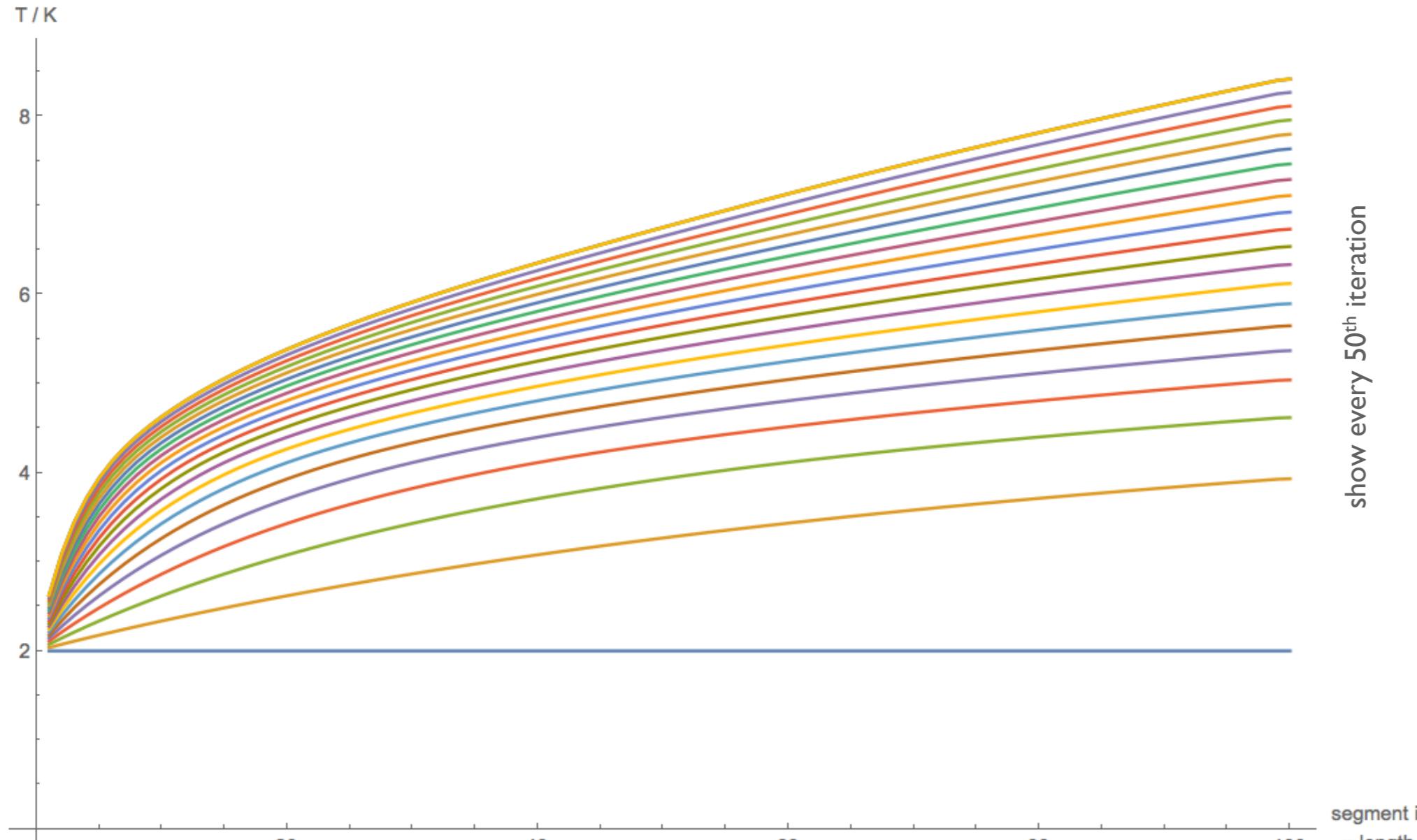
Out[175]//TableForm=

	0.001	2	2	2	2	2	2	2	2	2	2
	0.051	2.336	2.61874	2.86418	3.07858	3.26711	3.43336	3.58055	3.71168	3.82939	3.93078
	0.101	2.61829	3.07693	3.43034	3.70743	3.93064	4.11478	4.26788	4.39987	4.51684	4.6175
	0.151	2.86317	3.42982	3.82358	4.11331	4.3343	4.5149	4.66992	4.80722	4.93142	5.04005
	0.201	3.07698	3.70647	4.11295	4.3975	4.61986	4.80647	4.96965	5.11618	5.25023	5.36855
	0.251	3.26491	3.92938	4.3338	4.61979	4.849	5.0445	5.21748	5.37426	5.51884	5.64731
	0.301	3.4306	4.11328	4.51438	4.80645	5.04457	5.25002	5.43339	5.60083	5.75624	5.89517
	0.351	3.57727	4.26633	4.6696	4.96986	5.2178	5.43364	5.62771	5.80604	5.97256	6.12226
	0.401	3.70796	4.39841	4.80716	5.11672	5.37494	5.60144	5.80641	5.99589	6.17385	6.33479
	0.451	3.82545	4.51555	4.9317	5.25115	5.51991	5.75726	5.97334	6.17427	6.36413	6.53689
	0.501	3.93171	4.62159	5.04625	5.37595	5.65544	5.90382	6.13126	6.34403	6.54636	6.73176
	0.551	4.0287	4.71892	5.15284	5.49303	5.7834	6.04299	6.28211	6.50721	6.72278	6.92189
	0.601	4.11641	4.80925	5.25291	5.60376	5.90515	6.1762	6.42739	6.66545	6.89523	7.1085
	0.651	4.19648	4.89389	5.34761	5.70925	6.02183	6.3046	6.56834	6.82015	7.06508	7.28874
	0.701	4.27033	4.97376	5.43779	5.81034	6.13429	6.42912	6.70599	6.97251	7.23001	7.46296
	0.751	4.33879	5.04941	5.52396	5.90755	6.24309	6.55039	6.8411	7.12231	7.38975	7.63182
	0.801	4.40337	5.12181	5.60696	6.00171	6.34908	6.66931	6.97471	7.26792	7.54506	7.79612
	0.851	4.46405	5.19102	5.68694	6.09301	6.4525	6.78623	7.10644	7.40956	7.69627	7.9562
	0.901	4.52151	5.25754	5.76436	6.1819	6.55386	6.90175	7.23485	7.5477	7.84385	8.11254
	0.951	4.57668	5.32199	5.83975	6.26893	6.65373	7.01658	7.36043	7.68288	7.98836	8.26571
1	4.62906	5.38413	5.913	6.35406	6.75218	7.12951	7.48319	7.81515	8.12987	8.41581	
1	4.62826	5.38322	5.912	6.353	6.75106	7.12834	7.48195	7.81384	8.12849	8.41437	
1	4.62826	5.38322	5.912	6.353	6.75106	7.12834	7.48195	7.81384	8.12849	8.41437	

iteration stabilizes well after 1000 steps with increasing power and 100 more steps with constant power (probably also less steps sufficient); computing takes a few seconds

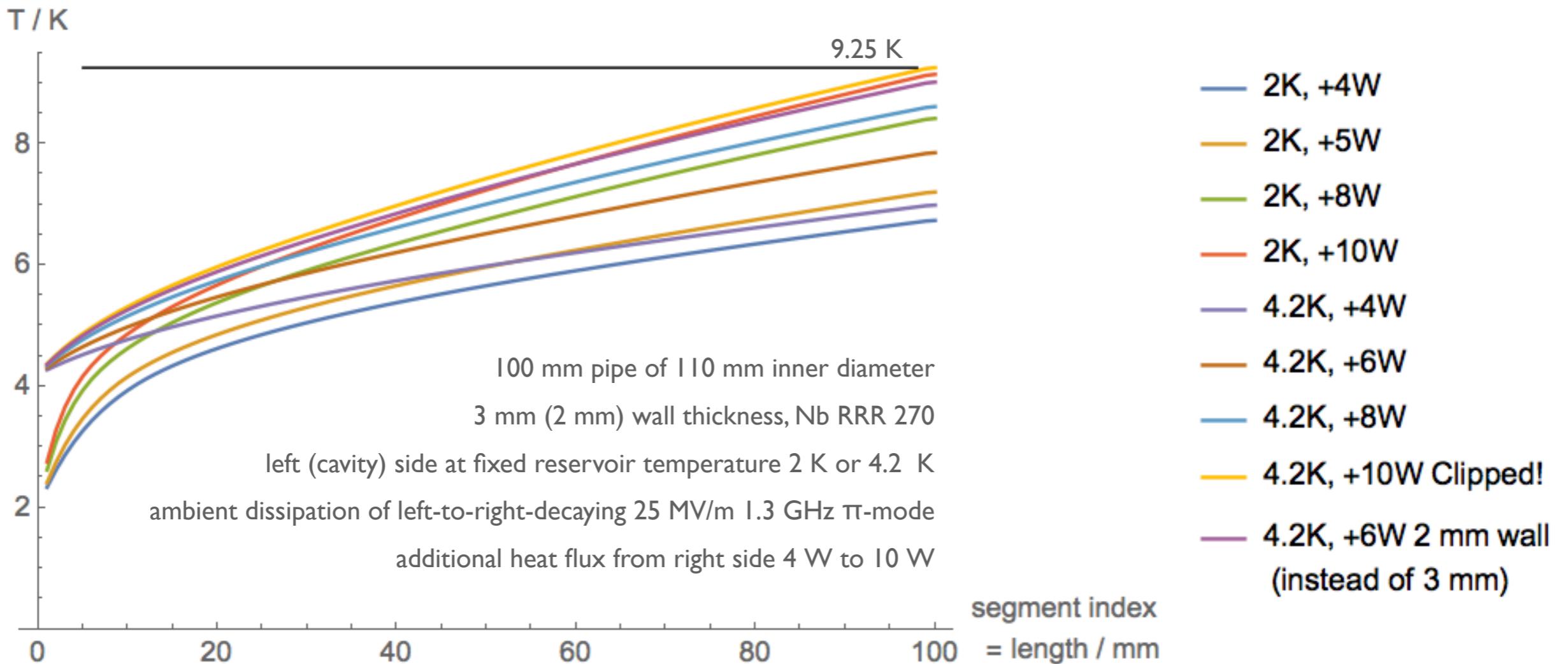
1-dimensional model of stationary heat flux: typical result

```
ListPlot[#[[1]] & /@ iteRad)[[1 ;; -1 ;; 50]], Joined → True, AxesLabel → {"segment index \n = length / mm", "T / K"}]
```



iteration stabilizes well after 1000 steps with increasing power and 100 more steps with constant power (probably also less steps sufficient); computing takes a few seconds

1-dimensional model of stationary heat flux: different scenarios



Superconducting limit (almost) reached either by:

- 10 W additional power, 2 K reservoir temperature
- 8 W additional power, 4.2 K reservoir temperature
- 6 W additional power, 4.2 K reservoir temperature, 2 mm wall thickness

Conclusions:

fundamental mode decay in a D110 mm circular pipe causes $\sim 4\text{ W}$ additional losses if the inner 150 mm (of 405 mm) are made of stainless steel

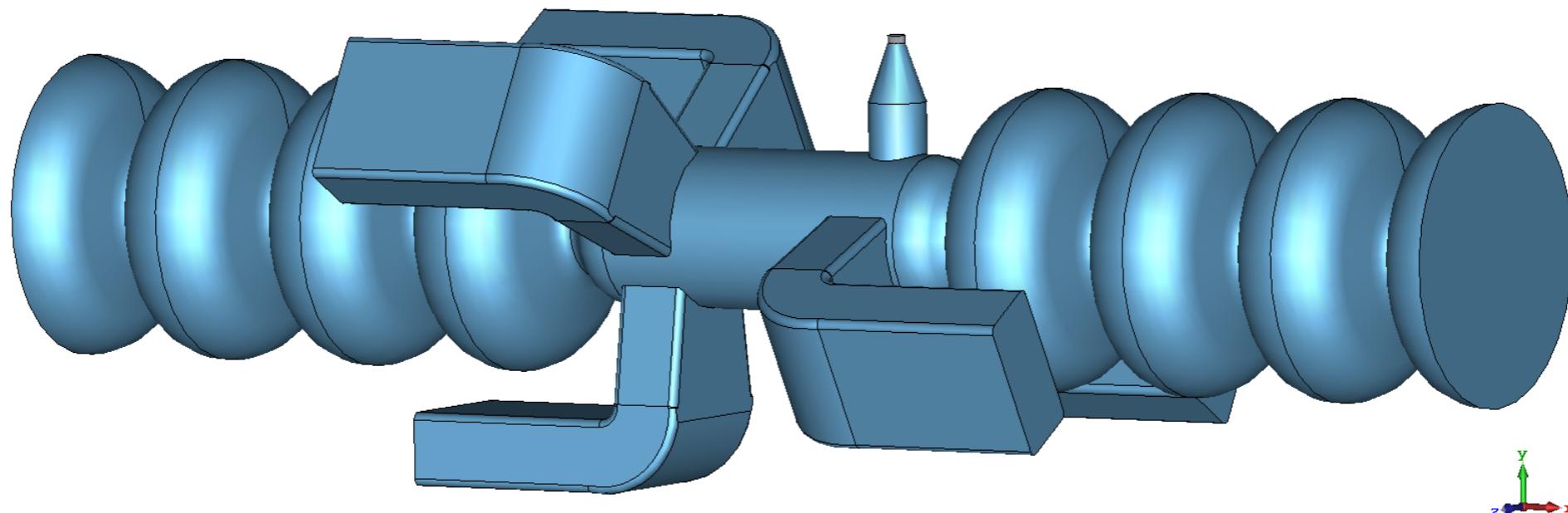
a straight beam pipe of 100 mm length and attached to the 25 MV/m, 1.3 GHz π -mode *can be bridged remaining superconducting without additional cooling if*

- a high RRR (here 270) is used
- wall thickness of 3 mm is used
- cavity side has reservoir temperature of 2 K (or lower)
- additional heat load remains below 10W

higher

... so, let us compute some eigenmodes of a:

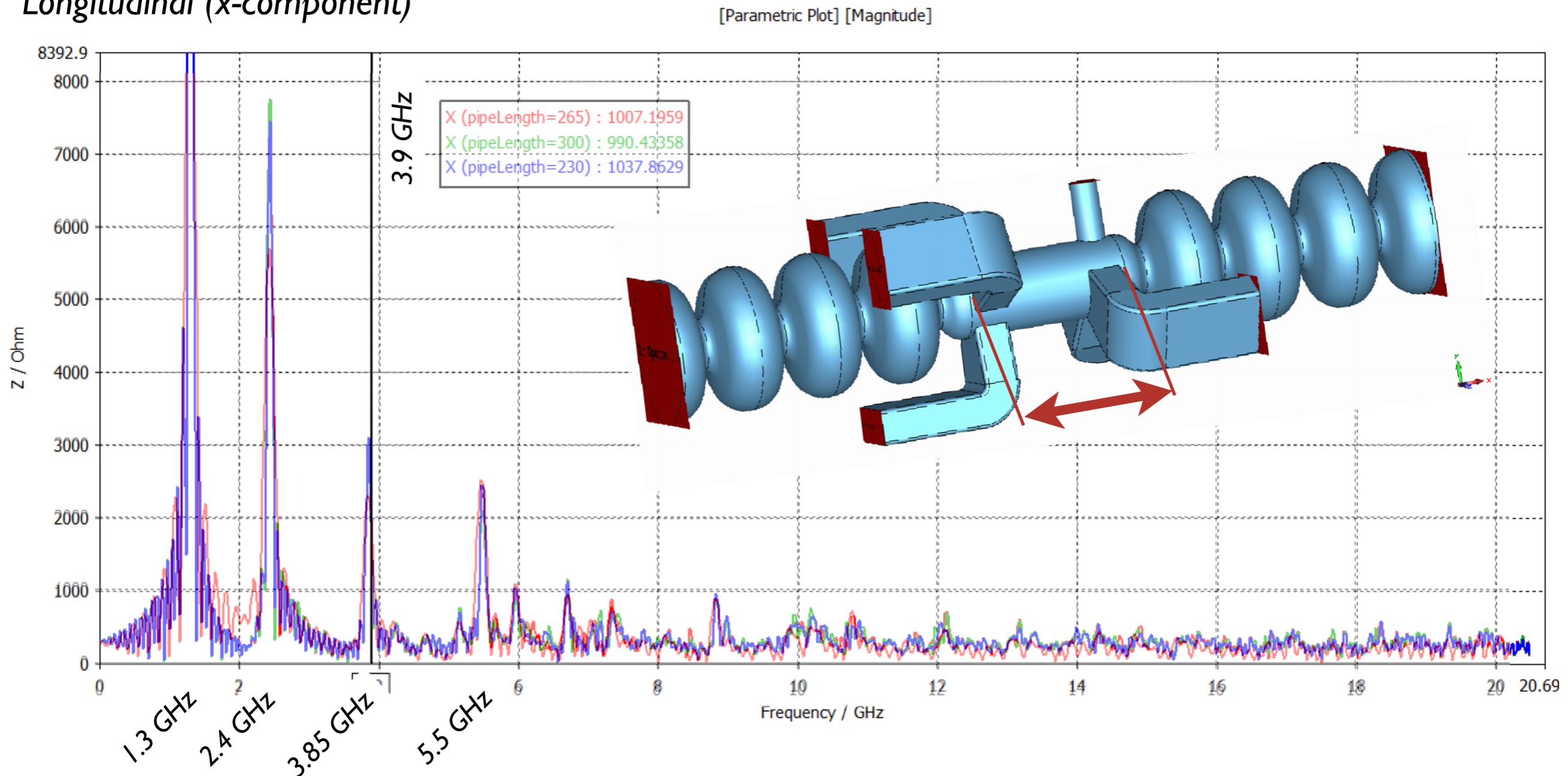
- 7-cell elliptical cavity
- strongly HOM-damped with 5 waveguides
- a fundamental power coupler
- and a beam pipe



- which is going to be placed in a chain of identical neighbors, so we would like to study the beam-pipe-coupling as well

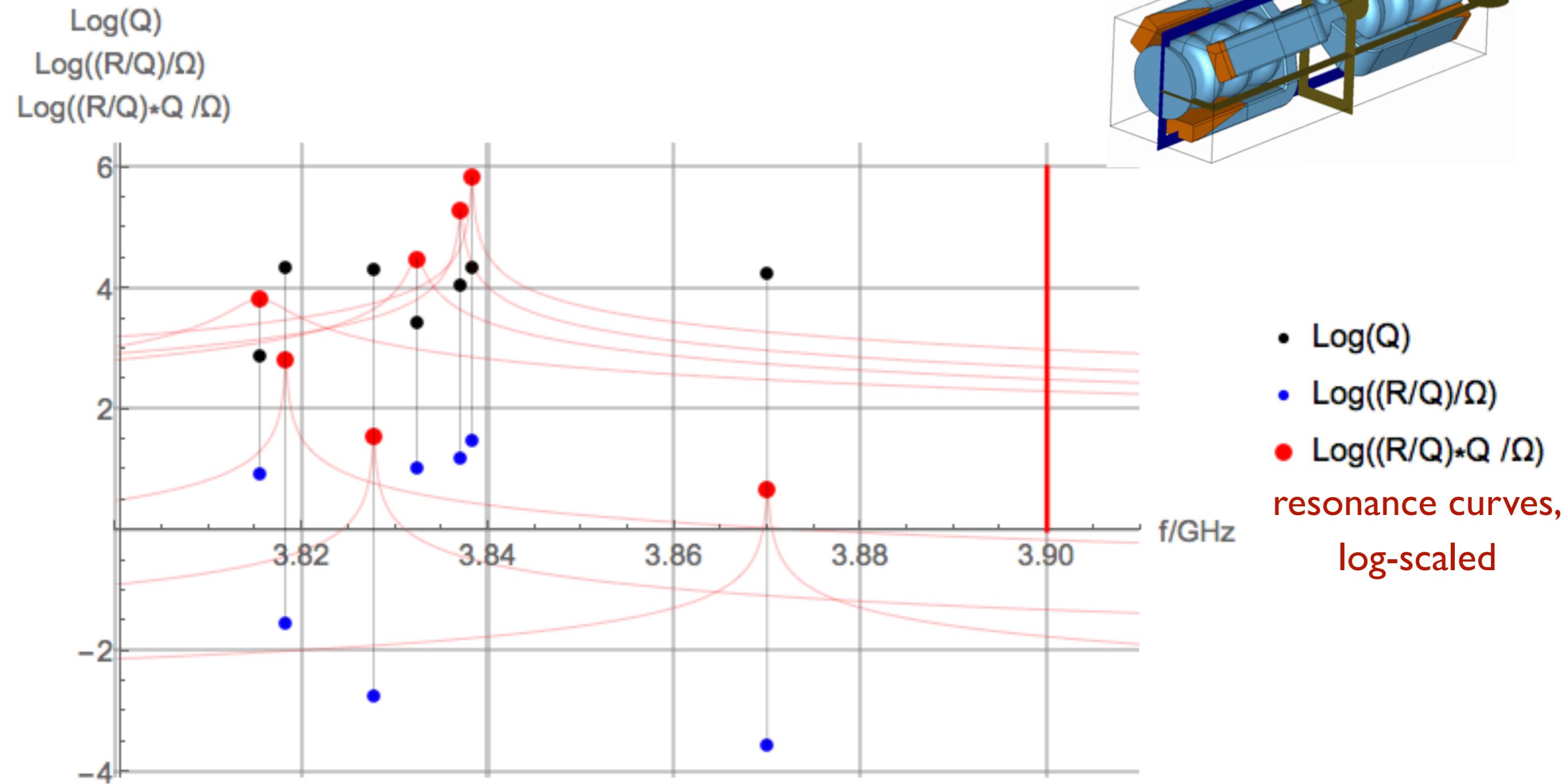
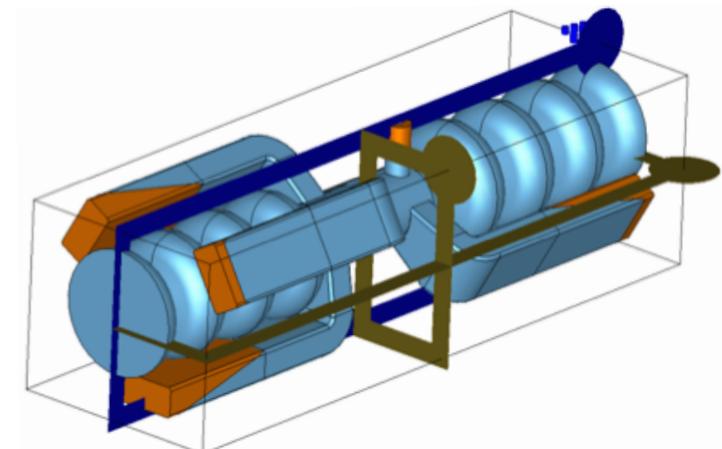
A wake-solver result: Impedance Simulations with variation of pipe length

Longitudinal (x-component)



- longitudinal impedance independent on pipe length \Rightarrow no pipe-trapped fields contributing
- few, but significant peaks; none of them on bERLinPro's beam harmonics $N \cdot 1.3 \text{ GHz}$, but two very close (@ $\approx 3.85 \text{ GHz}, \approx 5.15 \text{ GHz}$)

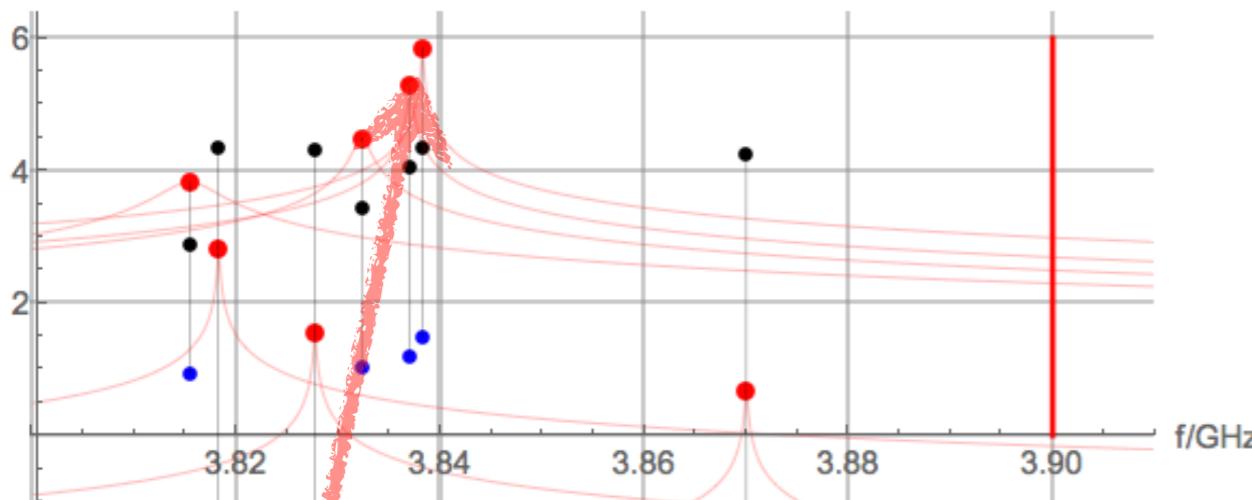
Eigenmode computations close to 3.9 GHz



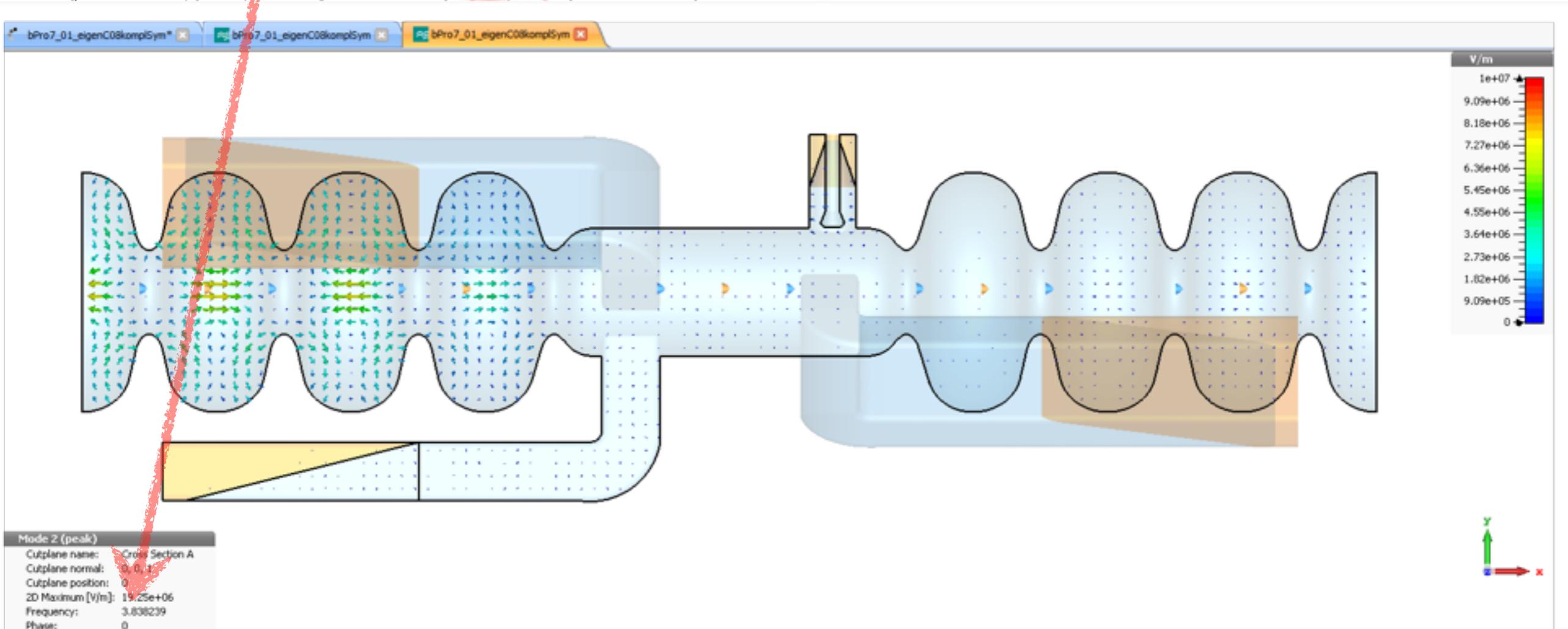
- no Q's $> 2.5 \cdot 10^4$ observed
- set of relevant (R/Q)'s $\sim 10 \dots 30 \Omega$ found
- close, but not too close to 3.900 GHz

$\text{Log}(Q)$
 $\text{Log}((R/Q)/\Omega)$
 $\text{Log}((R/Q)*Q / \Omega)$

Eigenmode computations close to 3.9 GHz



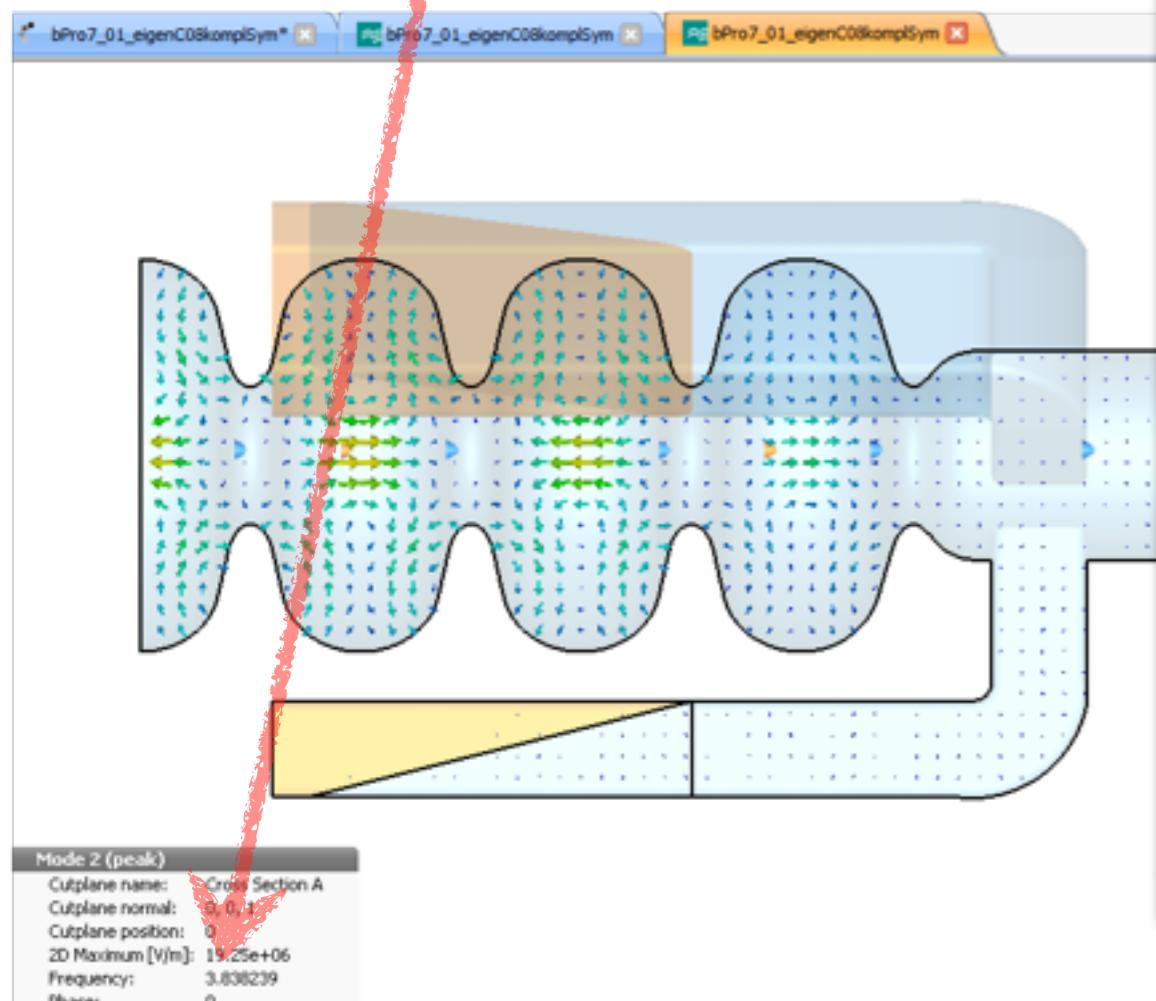
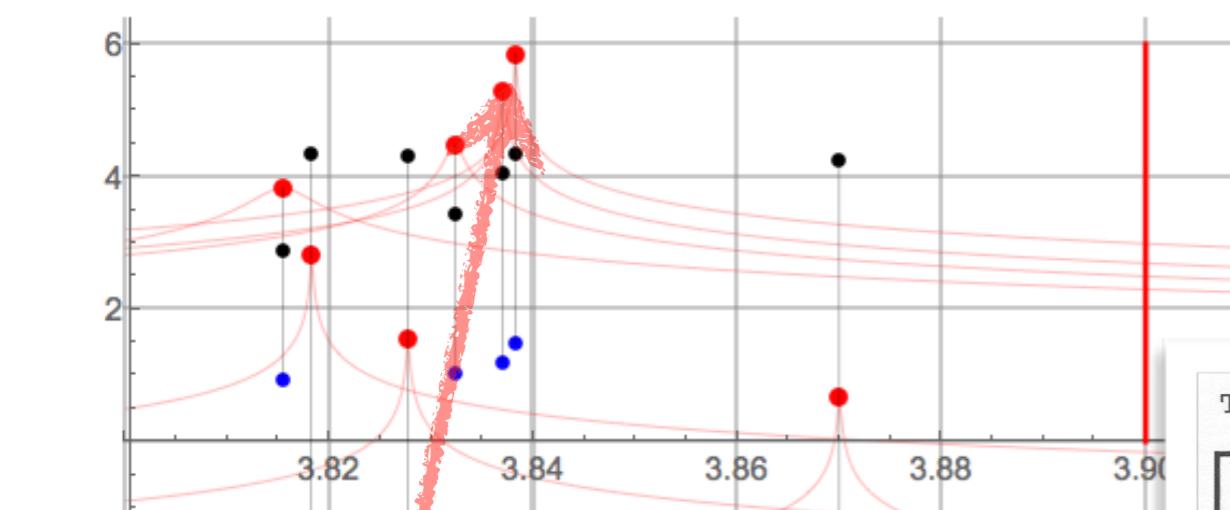
- Log(Q)
- Log((R/Q)/Ω)
- Log((R/Q)*Q / Ω)



- $\text{TM}_{\varphi=0, r=1, z=2}$ –type: monopole, on axis longitudinal E-field
- $f = 3.838239 \text{ GHz}$, $Q = 2.286 \cdot 10^4$, $R/Q = 31.4 \Omega$

Log(Q)
 Log((R/Q)/Ω)
 Log((R/Q)*Q / Ω)

Eigenmode computations close to 3.9 GHz



HIGHER ORDER MODE COUPLER FOR TESLA TESLA-Report 1994-07

- Log(Q)
- Log((R/Q)*Q / Ω)

Jacek Sekutowicz
DESY, Notkestraße 85, 22607 Hamburg, FRG

Table 2 Values of Q_{ext} for the monopole modes

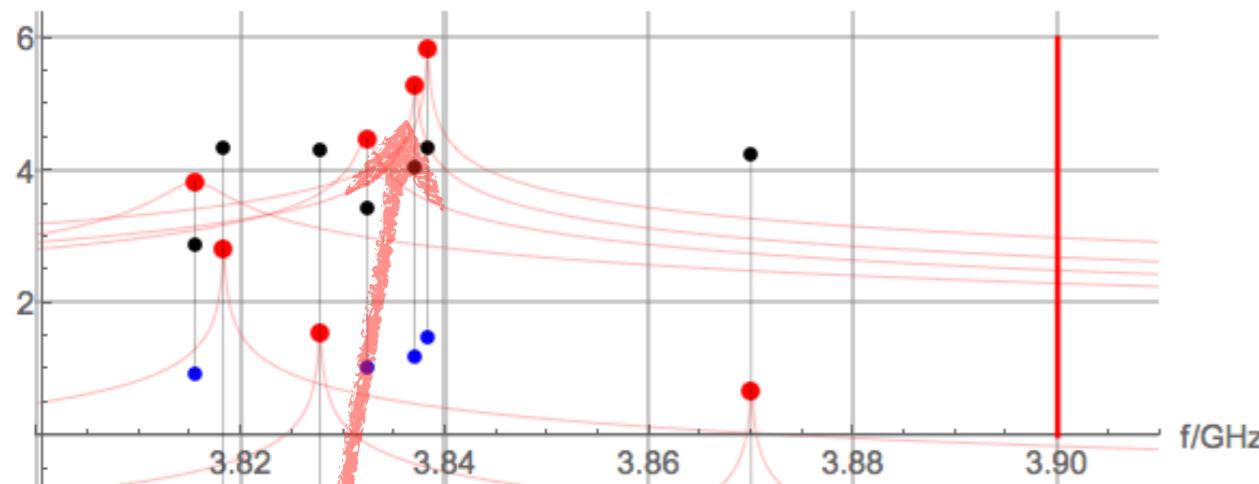
MODE	FREQ.	R/Q	2 welded	2 demount.	2 demount.	Q _{ext} Limit
			couplers on asymmetric cavity	couplers on asymmetric cavity	couplers on symmetric cavity	
	[MHz]	[Ω]	[1.0E+3]	[1.0E+3]	[1.0E+3]	[1.0E+3]
TM011	1	2379,6	0,00	350,0	1150	1600
	2	2384,4	0,17	72,4	360	460
	3	2392,3	0,65	49,5	140	220
	4	2402,0	0,65	84,0	68	110
	5	2414,4	2,05	32,0	70	97
	6	2427,1	2,93	29,1	81	59
	7	2438,7	6,93	20,4	66	49
	8	2448,4	67,04	27,4	58	51
	9	2454,1	79,50	58,6	110	100
TM012	1	3720,0	1,26	3,0		
	2	3768,9	0,07	5,1		
	3	3792,2	0,75	5,2		
	4	3811,7	1,43	3,9		
	5	3817,5	0,18	15,2		
	6	3829,2	2,33	11,3		
	7	3830,6	0,77	40,0		
	8	3845,3	22,04	240,0		300
	9	3857,3	6,85	6,1		1000

- TM_{φ=0, r=1, z=2} -type

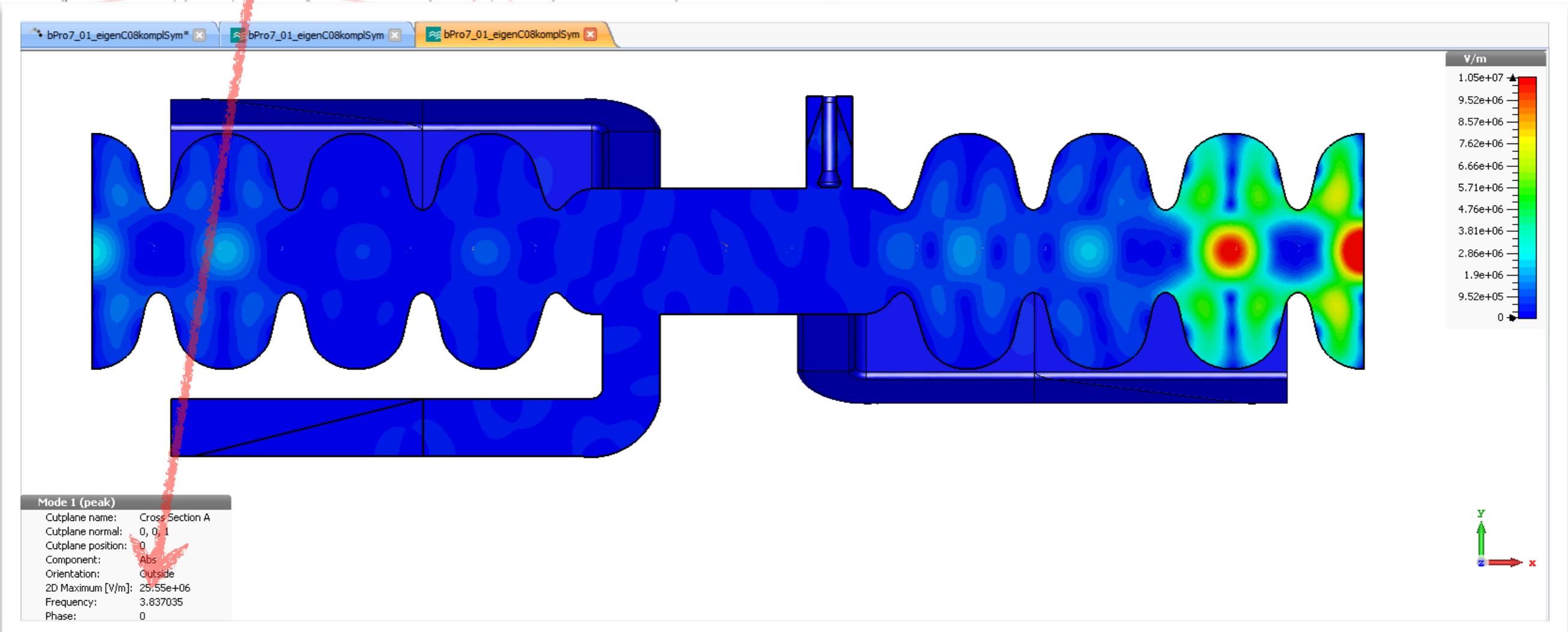
- f = 3.838239 GHz, Q = 2.286 · 10⁴, R/Q = 31.4 Ω

Log(Q)
Log((R/Q)/Ω)
Log((R/Q)*Q /Ω)

Eigenmode computations close to 3.9 GHz



- Log(Q)
- Log((R/Q)/Ω)
- Log((R/Q)*Q /Ω)

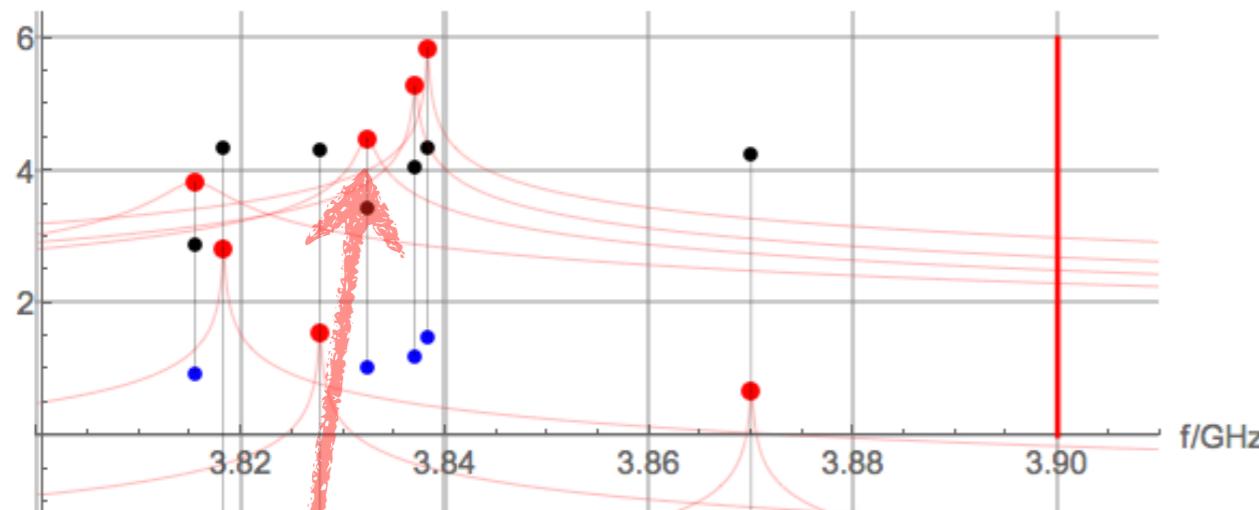


– $\text{TM}_{\varphi=0, r=1, z=2}$ –type

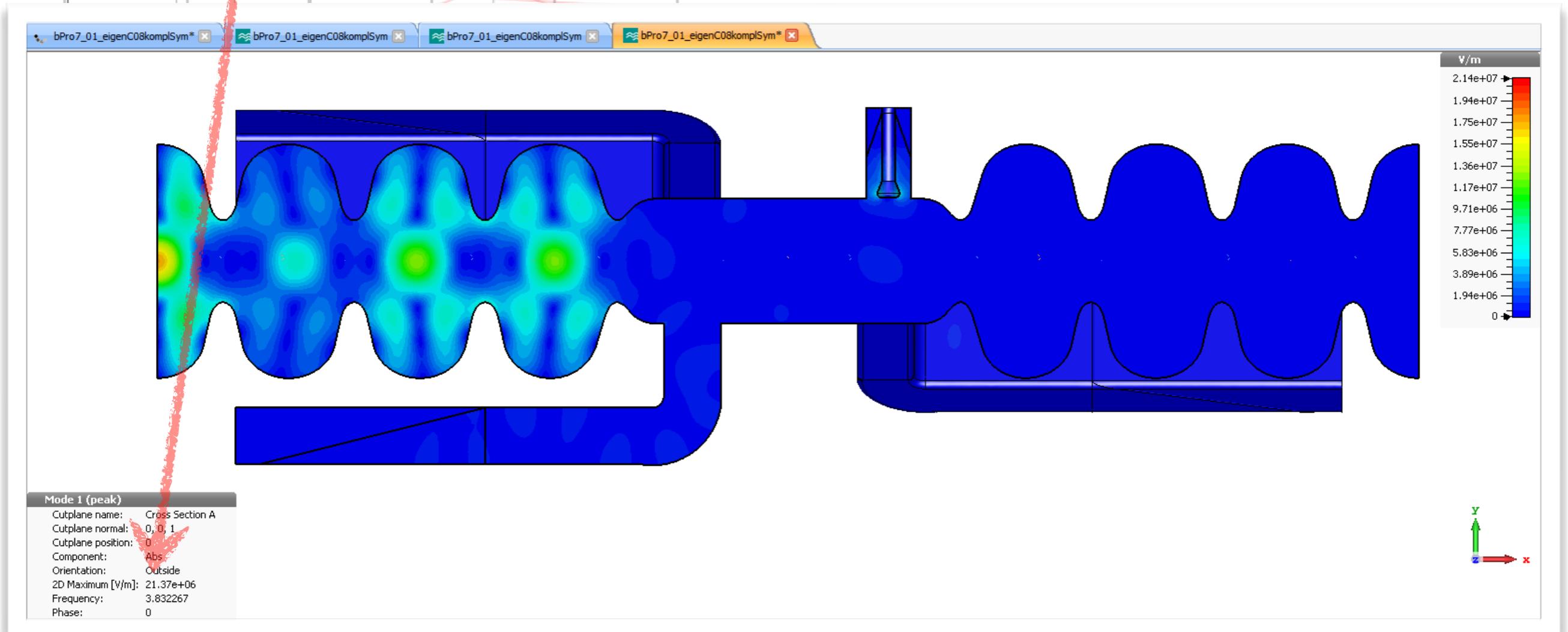
– $f = 3.837035 \text{ GHz}, Q = 1.166 \cdot 10^4, R/Q = 16.2 \Omega$

Log(Q)
Log((R/Q)/Ω)
Log((R/Q)*Q /Ω)

Eigenmode computations close to 3.9 GHz



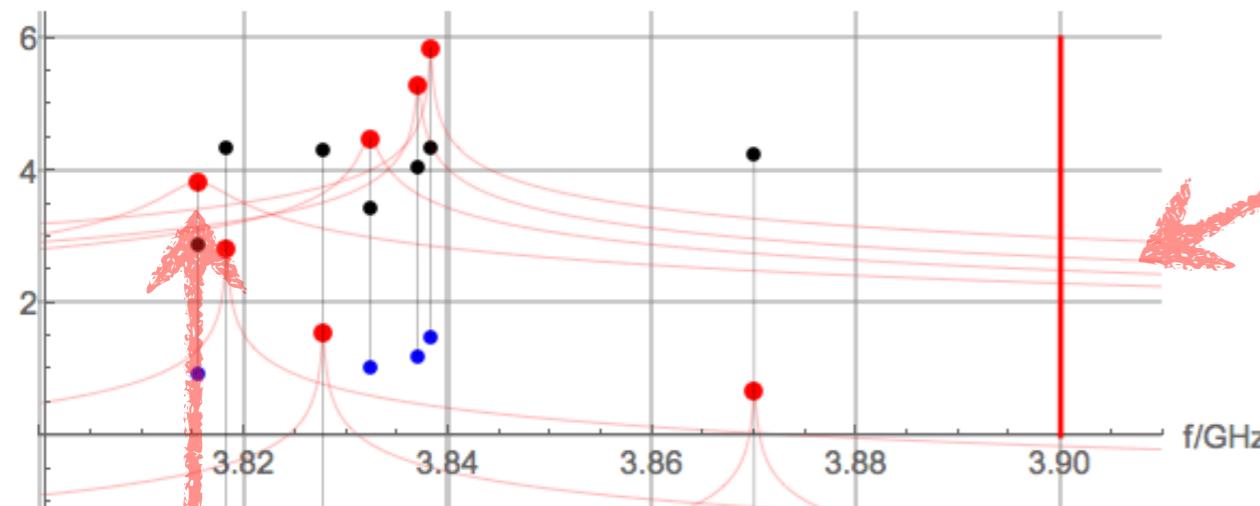
- Log(Q)
- Log((R/Q)/Ω)
- Log((R/Q)*Q /Ω)



- TM $_{\varphi=0, r=1, z=2}$ -type

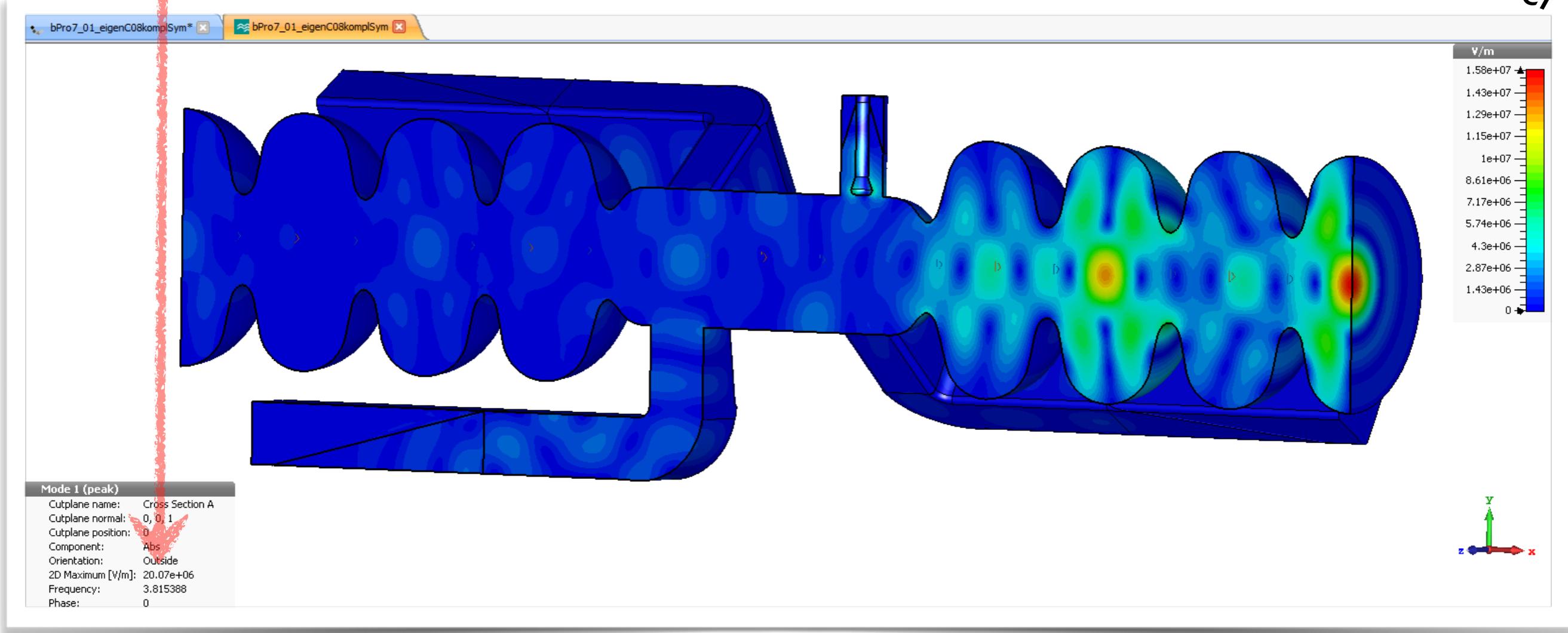
- $f = 3.832267 \text{ GHz}$, $Q = 2802$, $R/Q = 11.1 \Omega$

$\text{Log}(Q)$
 $\text{Log}((R/Q)/\Omega)$
 $\text{Log}((R/Q)*Q / \Omega)$



Eigenmode computations close to 3.9 GHz

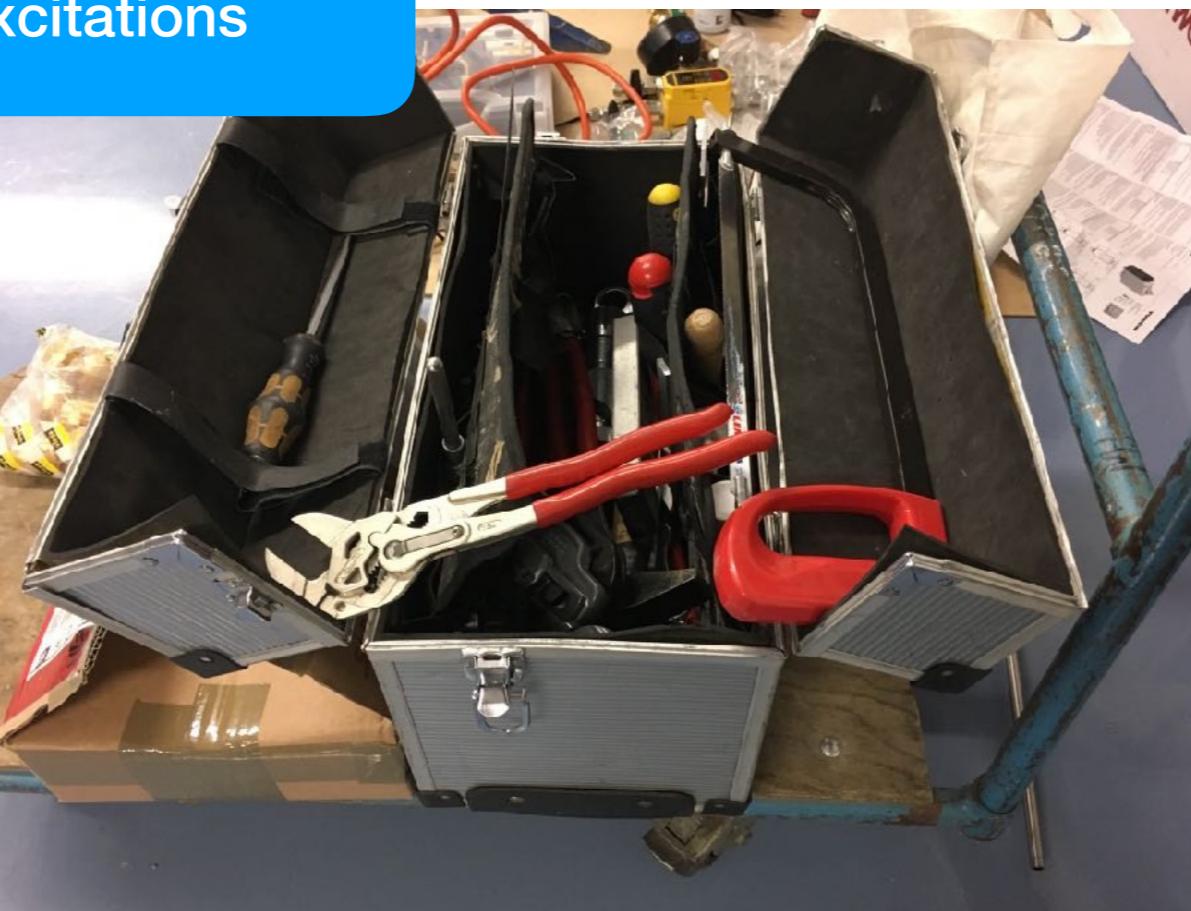
Low Q 's are not necessarily harmless
weaker reaction, but covering broader spectrum !



- $\text{TM}_{\varphi=0, r=1, z=2}$ -type
- $f = 3.815388 \text{ GHz}$, $Q = 758$, $R/Q = 8.85 \Omega$:

The tool box: You should have ...

a frequency domain solver to
compute the reaction of a cavity or
an open structure on externally
given driving excitations

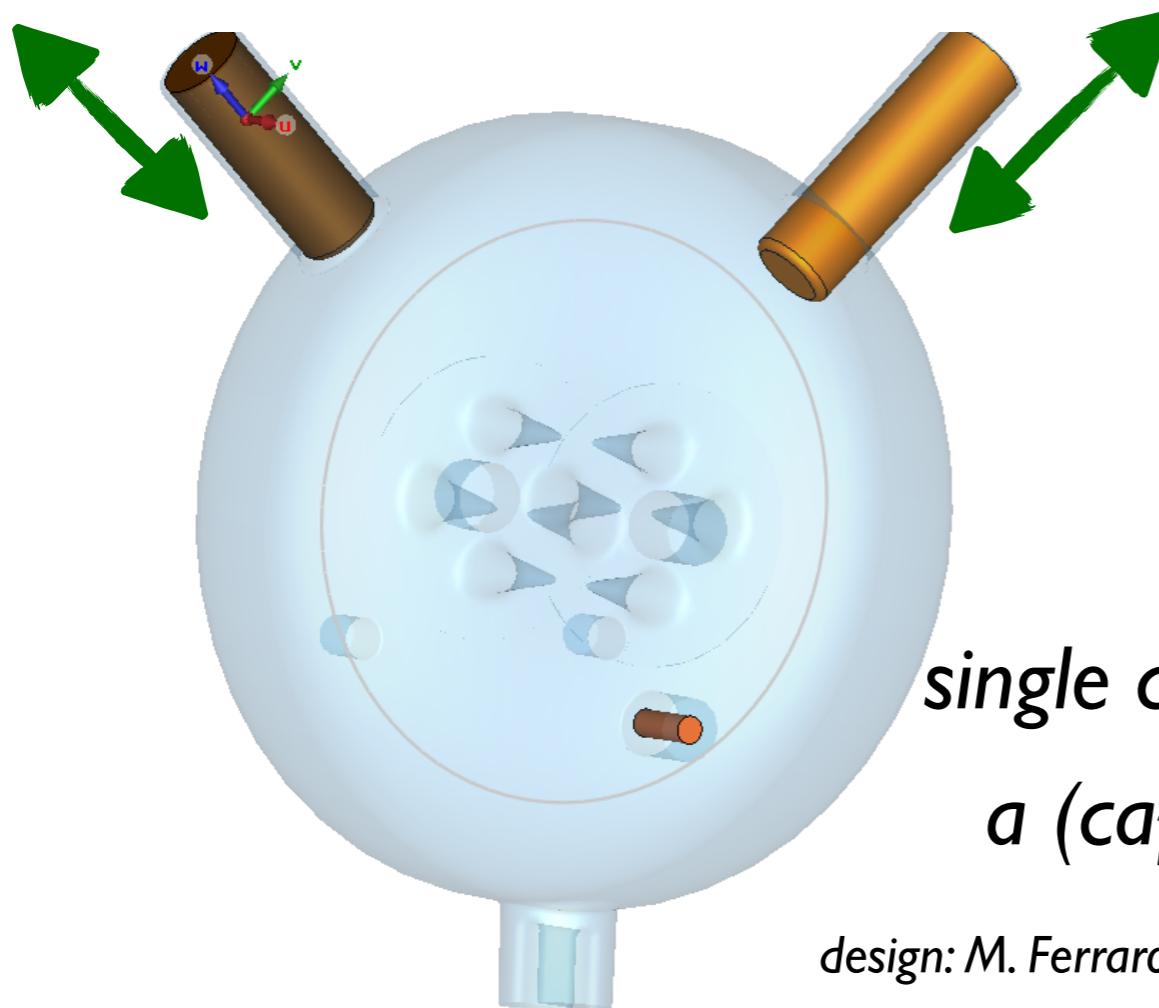


,,Frequency-domain“-field solver:

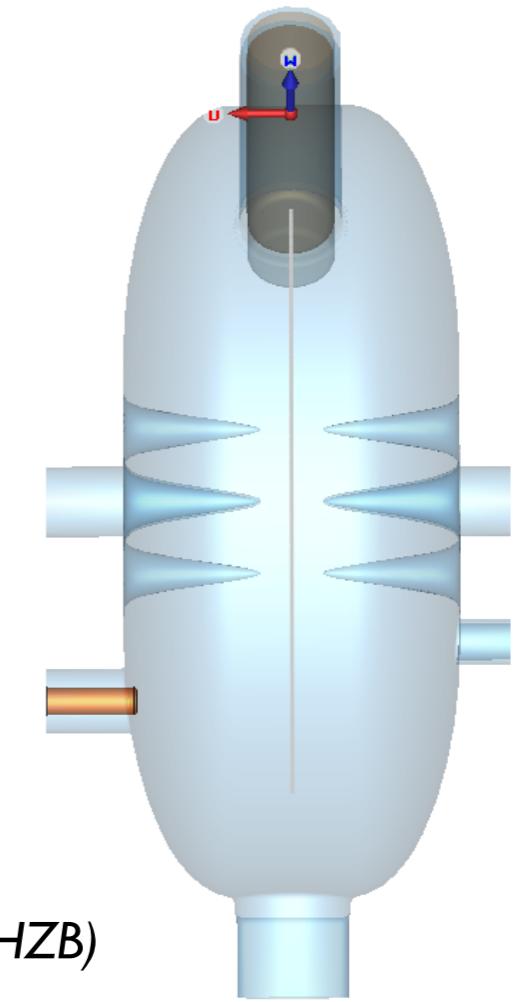
1. *Excites a cavity-like or waveguide-like structure (or anything between) with at least one port through a monochromatic wave of given frequency and simulates the stationary (not: static!) response.*
2. *Such a response is ...*
 - a) *the electromagnetic field inside the structure, and ...*
 - b) *the scattered waves at the port of excitation and at all other ports. By normalization with the incident wave amplitude, (complex-valued) S-parameters are computed.*
3. *It also computes (typically) the appropriate waveguide modes of the port(s) as solutions of 2-dimensional eigen-problem(s).*
4. *Frequency spectra are computed by repetition (slow) or (sophisticated) model-order-reduction-miracles.*

Example:

Double-plunger-tuned Cu cavity for transversal deflection



*single coaxial port feeding
a (capacitive) antenna*



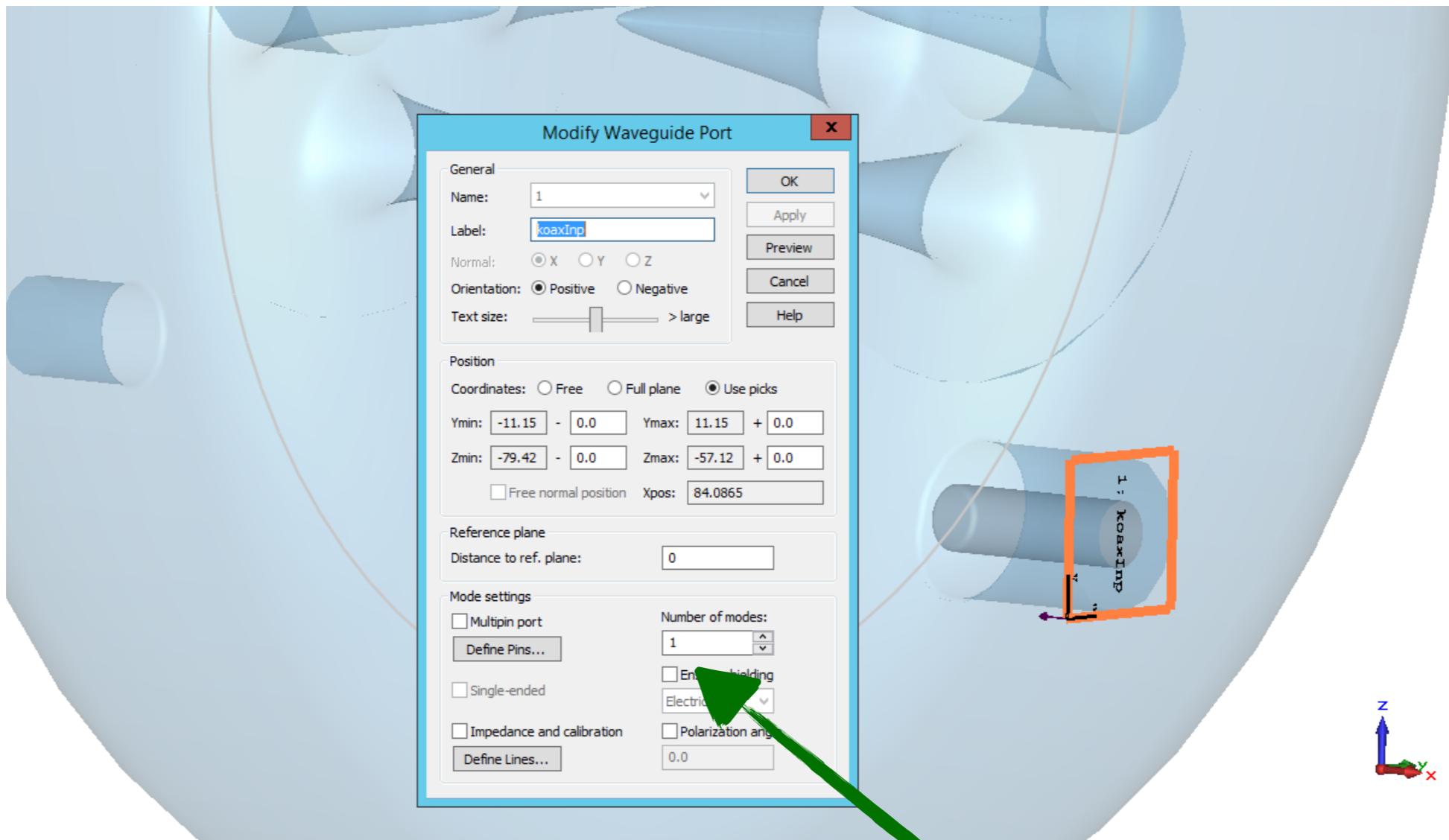
design: M. Ferrarotto (TU Dortmund), F. Pfloksch (HZB)

*Task: Determine the internal field patterns and input reflection
depending on plunger depths and antenna length.*

(we will skip the multi-dimensionality, handled in practice by geometry parameters)

... by the way: What determines the TEM-impedance of a vacuum coaxial line ?

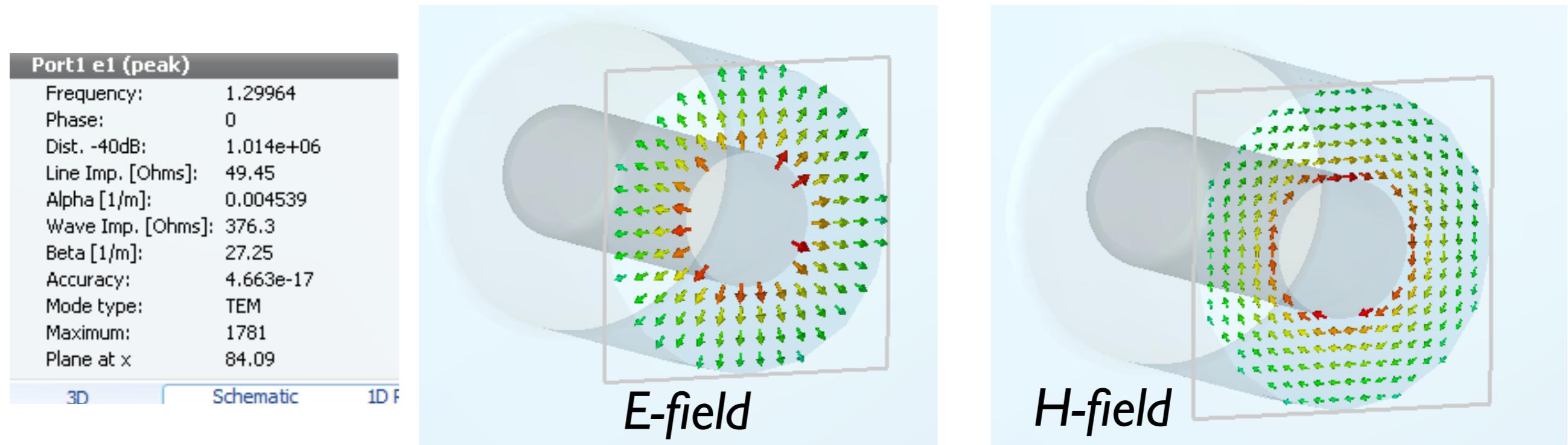
Frequency-domain-solver definitions I: Port location(s) and parameters



most essential: How many modes to be considered.

... by the way: What is the cut-off frequency of a TEM mode ?

Frequency-domain-solver outcome I: Mode pattern(s) at the port(s)



... by the way: What is the ratio E/H in free space ?

Frequency-domain-solver definitions II:

Frequency sampling points/ranges, fields to keep, excitations

The screenshot shows a 3D model of a coaxial cable system with a green bounding box around the central conductor. Below the model is a monitor summary table:

Monitor	e-field (f=1.29946)
Type	E-Field (peak)
Frequency	1.29946

At the bottom of the interface, there are tabs: 3D, Schematic, 1D Results\Parameters\S1,1, and Parameter View.

To the right is the "Frequency Domain Solver Parameters" dialog box:

- Method:** Broadband sweep:
 - General purpose
 - Tetrahedral
- Results:**
 - Store result data in cache
 - Calculate port modes only
 - Normalize S-parameter to 50 Ohms
- Excitation:** Source type: Port 1 (koaxInp), Mode: 1
- Frequency samples:**

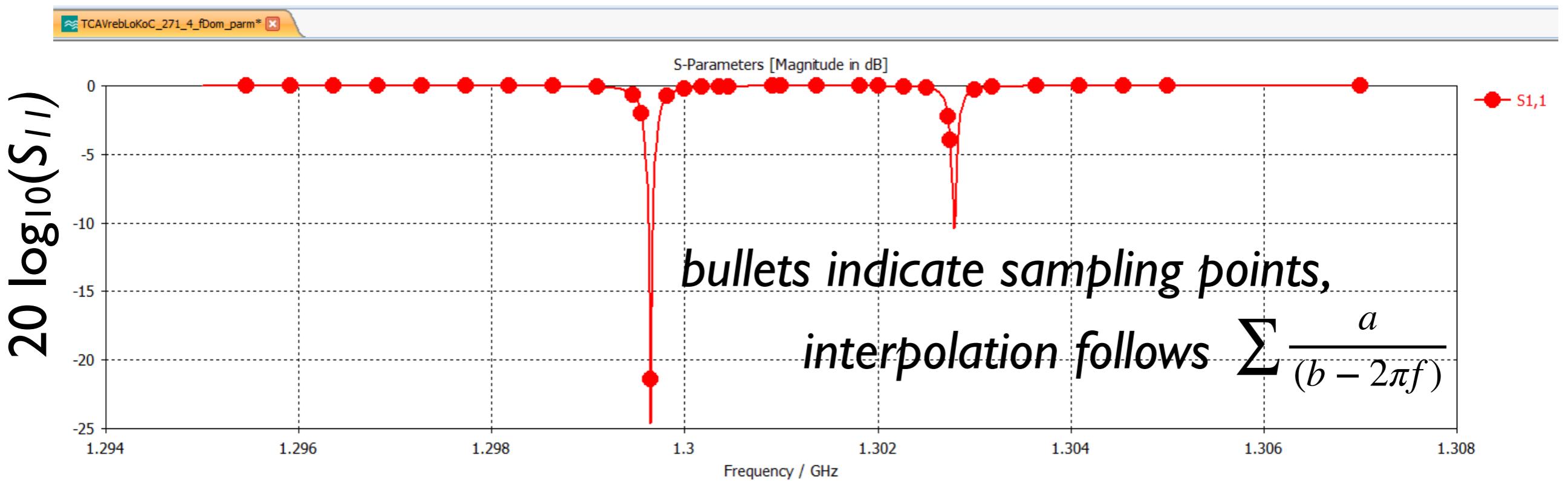
Active	Type	Adapt.	Samples	From	To	Unit
	Max.Range			1.293	1.307	GHz
<input checked="" type="checkbox"/>	Monitors					GHz
<input checked="" type="checkbox"/>	Equidistant	<input type="checkbox"/>	23	1.295	1.305	GHz
<input type="checkbox"/>	Automatic	<input type="checkbox"/>				GHz
<input type="checkbox"/>	Single	<input type="checkbox"/>	1			GHz
- Adaptive mesh refinement:** Adaptive tetrahedral mesh refinement (checked)
- Sensitivity analysis:** Use sensitivity analysis (unchecked)

Buttons on the right side of the dialog box include Start, Optimizer..., Par. Sweep..., Acceleration..., Specials..., Simplify Model..., Apply, Close, and Help.

Below the dialog box, three labels with arrows point to it: "stored volume" (pointing to the 3D model), "frequencies" (pointing to the "Frequency samples" table), and "excitations" (pointing to the "Excitation" section).

... by the way: How to compute a stationary H-field from a given E-field ?

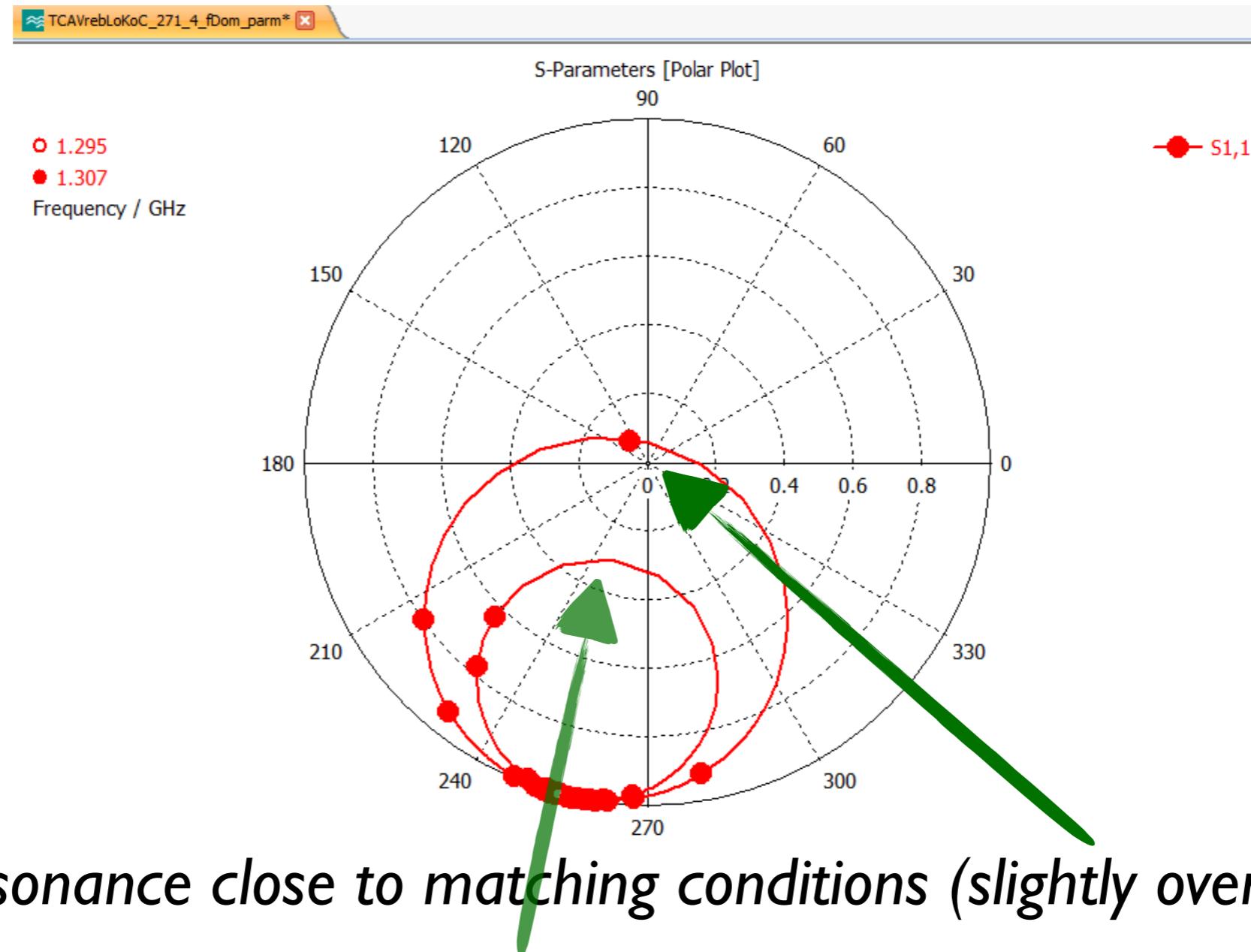
Frequency-domain-solver outcome II: Scattering parameters – in case of single-moded one-port device only S_{11} exists



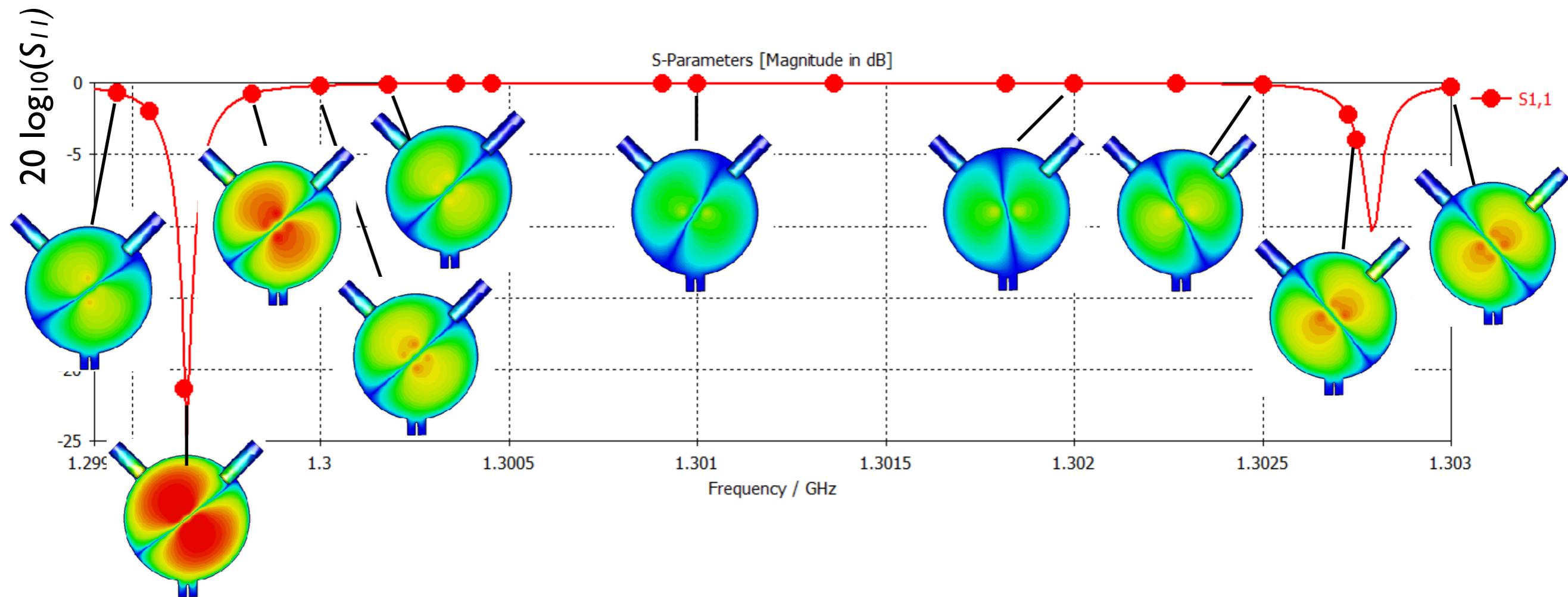
Cavity dissipates most energy in the wall, if in resonance, i.e. minima of S_{11}
(1.2996 GHz and 1.3028 GHz)

... by the way: How much of the energy is reflected if $|S_{11}| = -3$ dB ?

Frequency-domain-solver outcome III: Complex-valued scattering parameters in polar representation



Frequency-domain-solver outcome IV: Field patterns for different driving frequencies



Driven field pattern shifts its orientation and takes different amplitudes depending on the frequency.

... by the way: What is a degenerated mode ?

The tool box: You should have ...

a wakefield solver to observe the time-domain reaction of a beam line element on a driving bunch



,,Wake“-field solver:

1. *Excites a cavity-like or waveguide-like structure (or anything between) with (typically) one traversing gaussian bunch of given length and simulates the time-dependent response.*
2. *Such a response is ...*
 - a) *the electromagnetic field inside the structure, and ...*
 - b) *the outgoing waves at all ports, and ...*
 - c) *the integral force, that would be experienced by witness charges following the bunch in fixed distances („wake potentials“)*
3. *It also computes (typically) the appropriate waveguide modes of the port(s) as solutions of 2-dimensional eigen-problem(s).*
4. *Fourier-transformation of the wake potentials give „beam impedances“, integral deposited energy „loss factors“.*

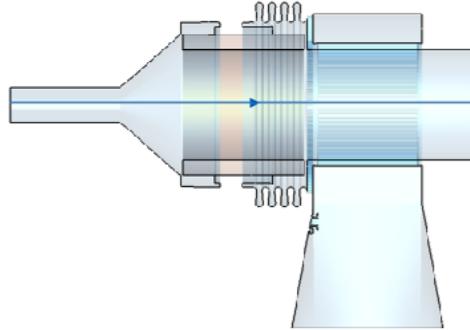
Again for comparison: „Frequency-domain“-field solver:

1. *Excites a cavity-like or waveguide-like structure (or anything between) with at least one port through a monochromatic wave of given frequency and simulates the stationary (not: static!) response.*
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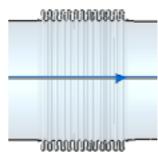
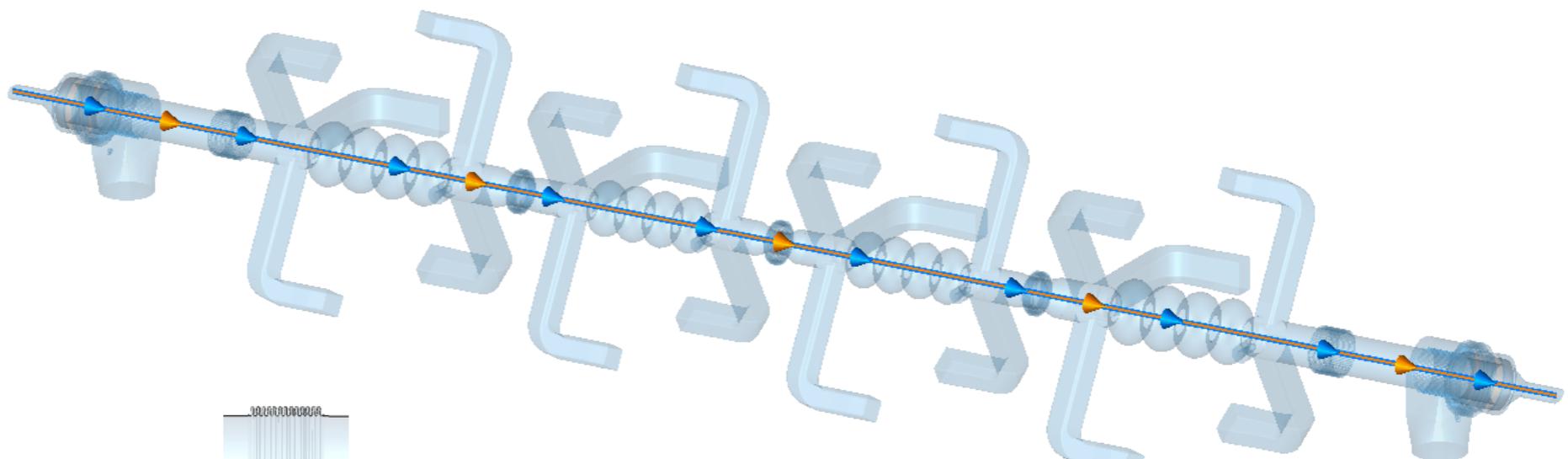
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4. *Fourier-transformation of the wake potentials give „beam impedances“, integral deposited energy „loss factors“.*

Example (a really big one): BESSY-VSR-upgrade module



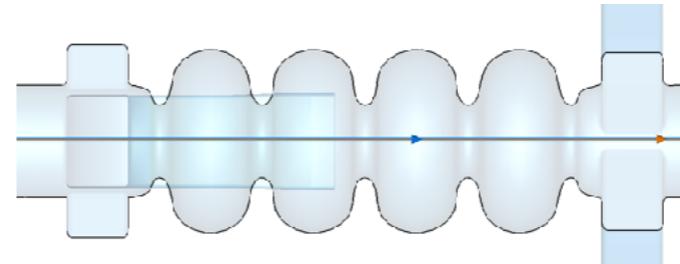
**Warm End Group
(not recent design)**

- absorber
- cross section adaption
- mech. compensation
- pumping



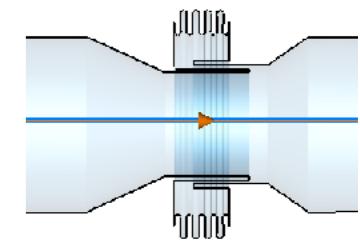
**Module End Bellow
(not recent design)**

- mech. compensation
- thermal insulation



Cavity 1.5 / 1.75 GHz

- alternating bunch lengthening/shortening



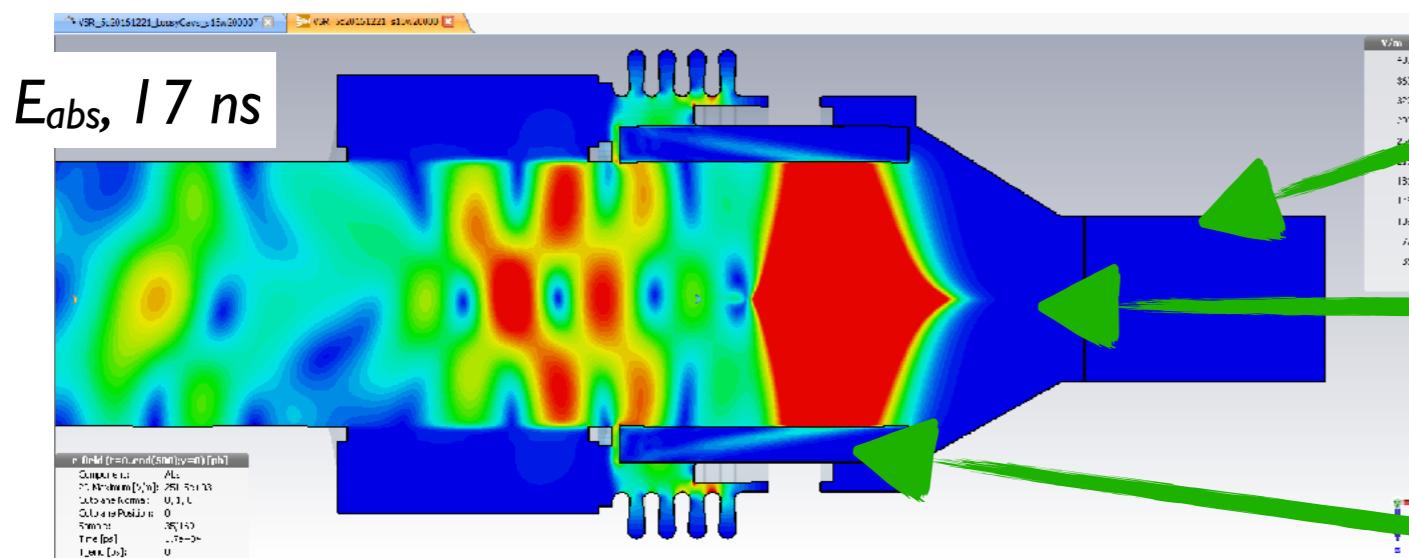
Shielded Belows

- mech. compensation
- synchrotron light collimation
- while not affecting cavity Qs

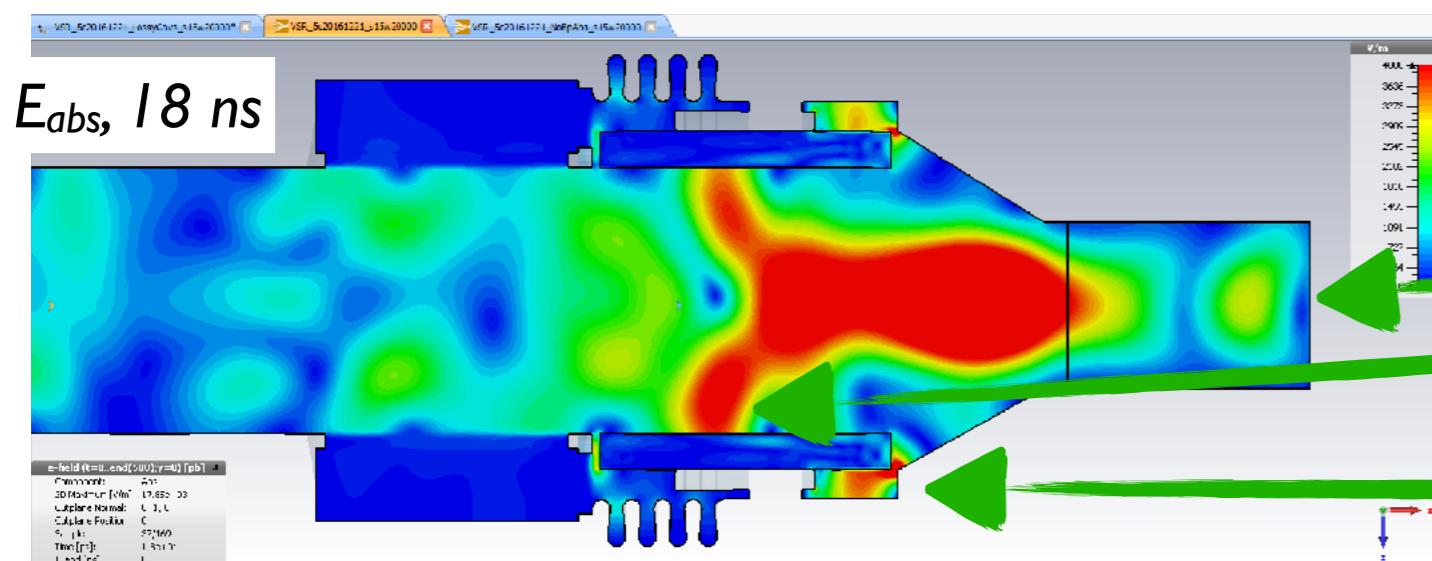
Task: Determine the power to be damped in the waveguides and endgroups when operating in 300 mA CW synchrotron operation

... by the way: How many bunches with 4 ns spacing are together in a structure of 5 m length ?

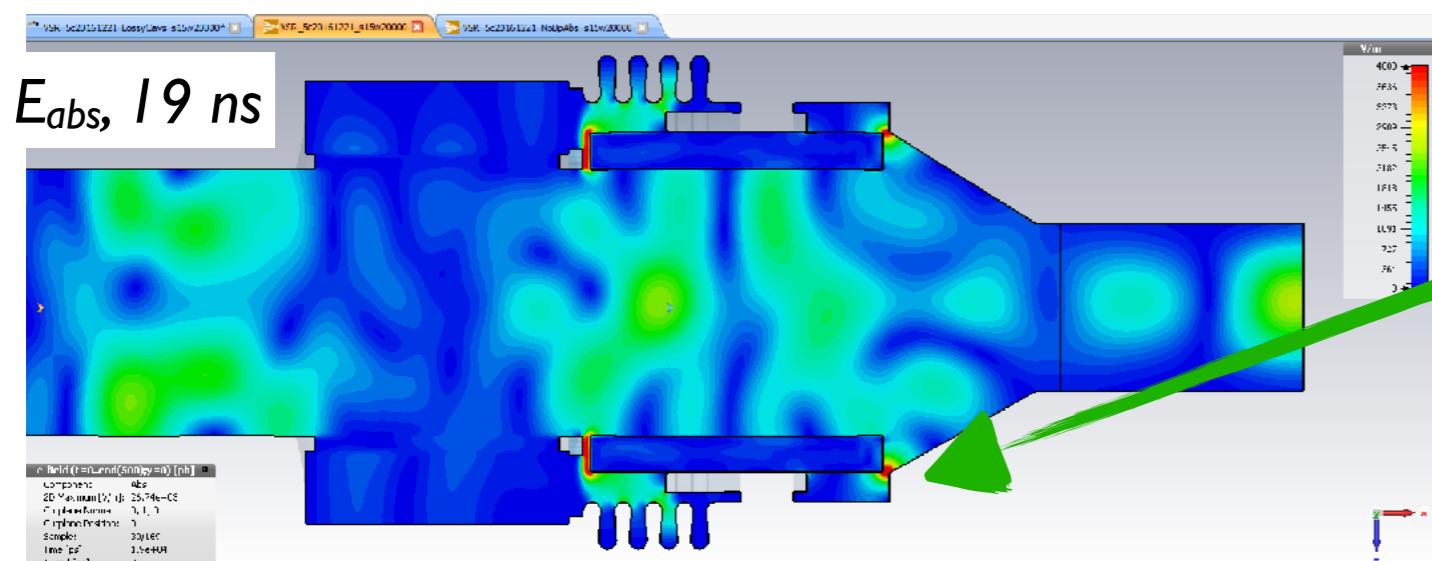
How do wake fields look like (e.g. at the module end)?



field-free volume ahead the bunch
(ideally only if $v_{bunch} = c_0$)



scattered fields propagate
up- and
downstream

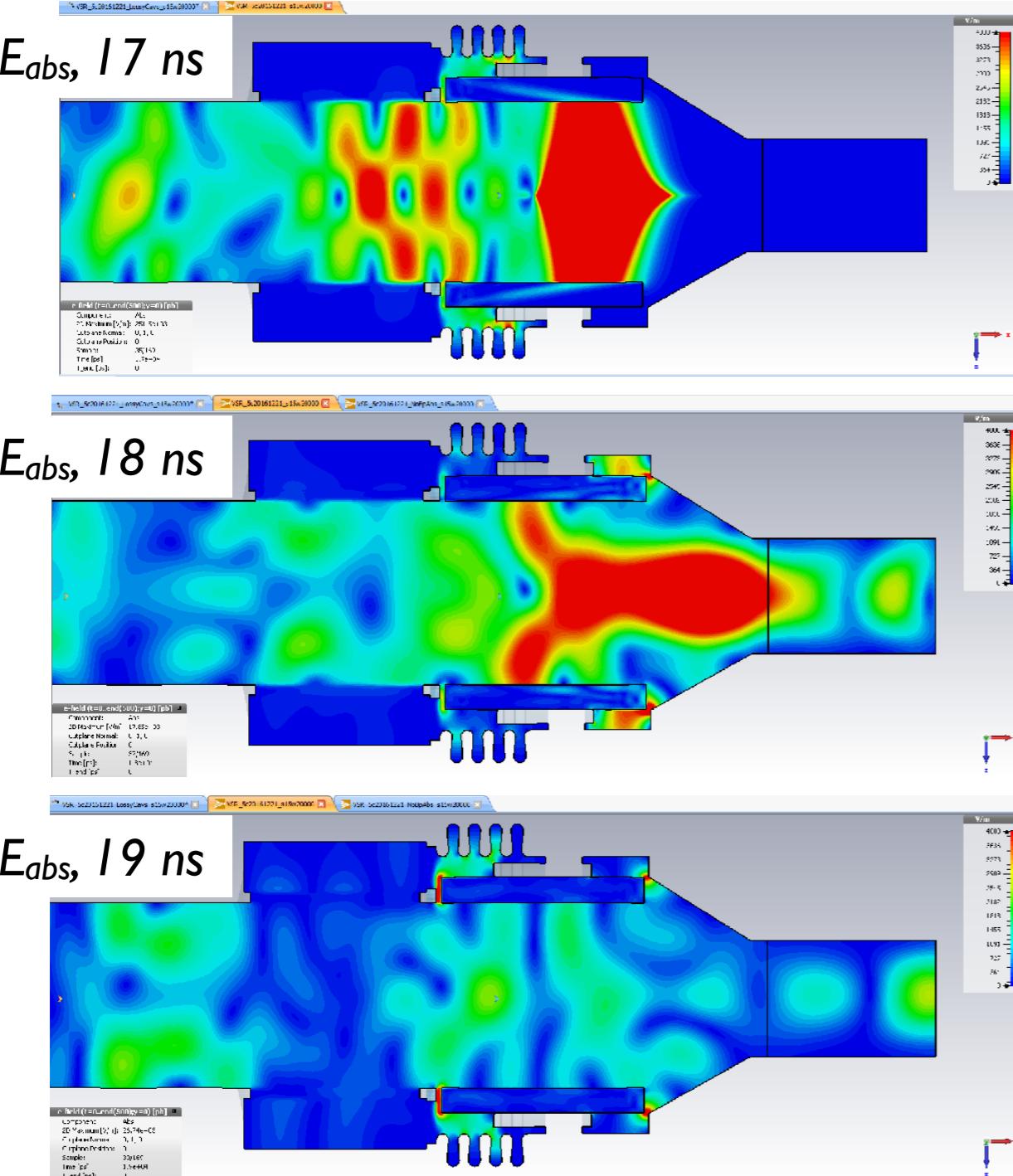


localized field patterns („modes“)
ring and ...

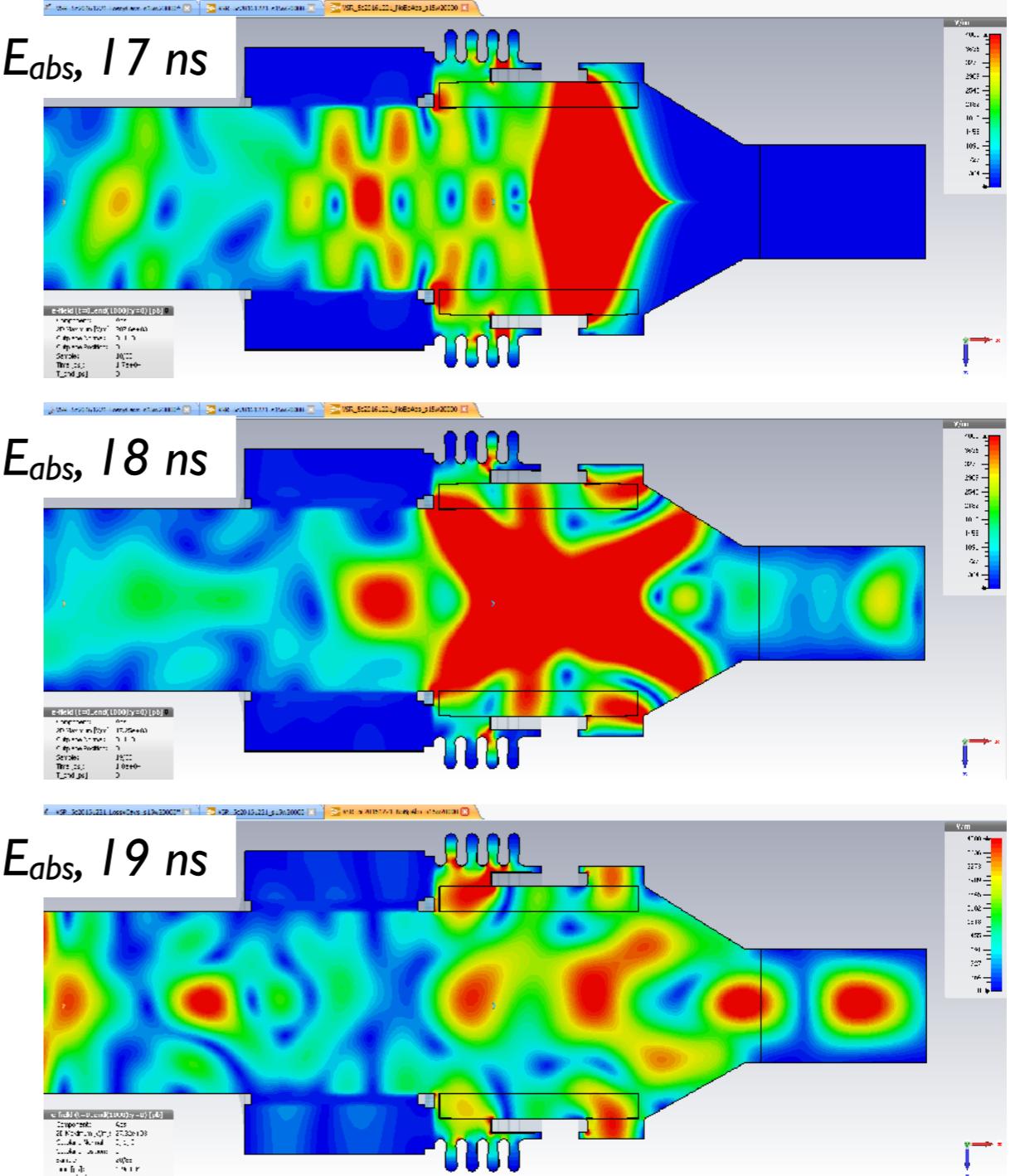
... decay; Q depending on energy
sinks = ports, wall losses,
dielectric losses)

Side note: How damps the dielectric absorber the fields?

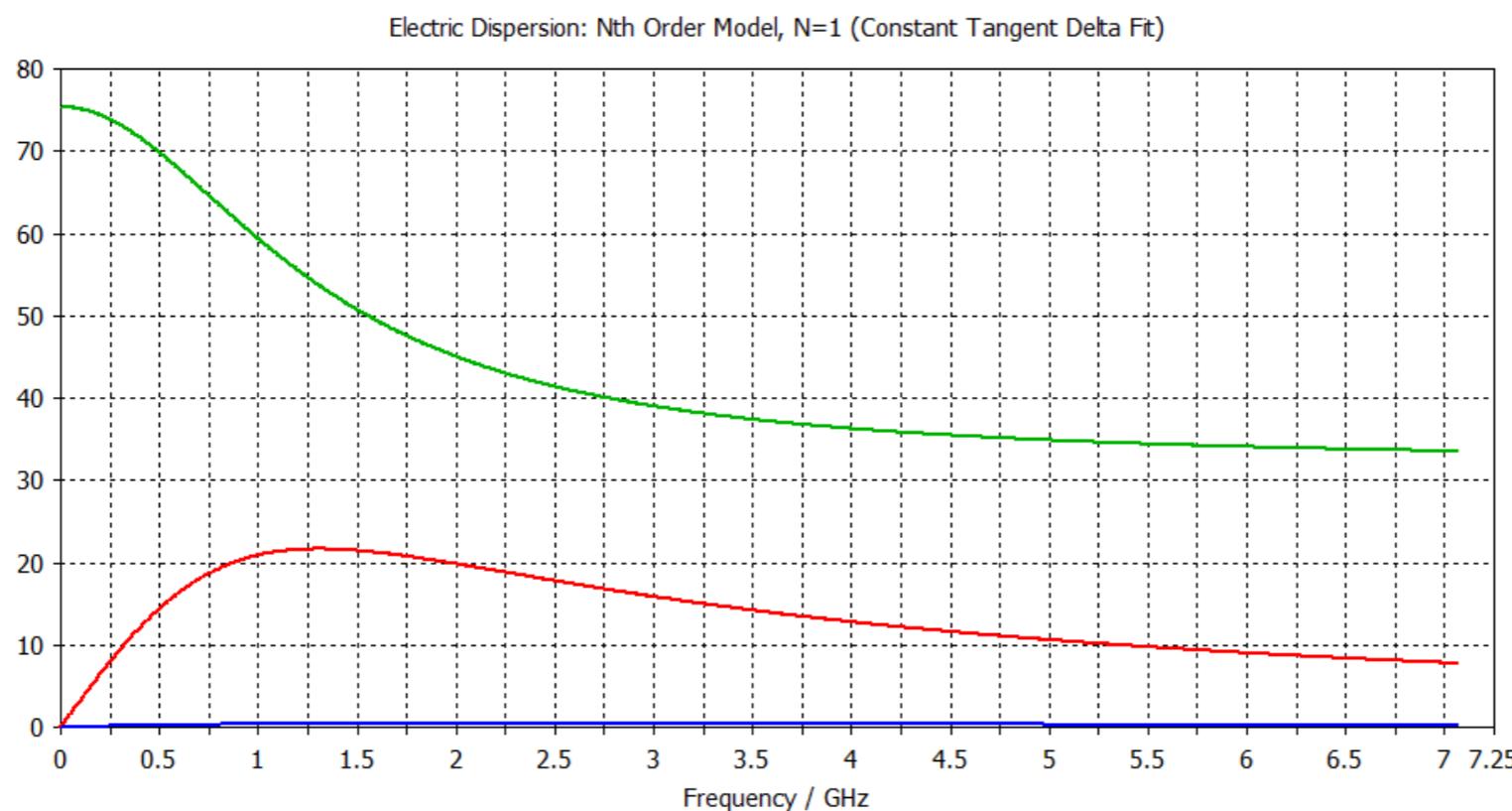
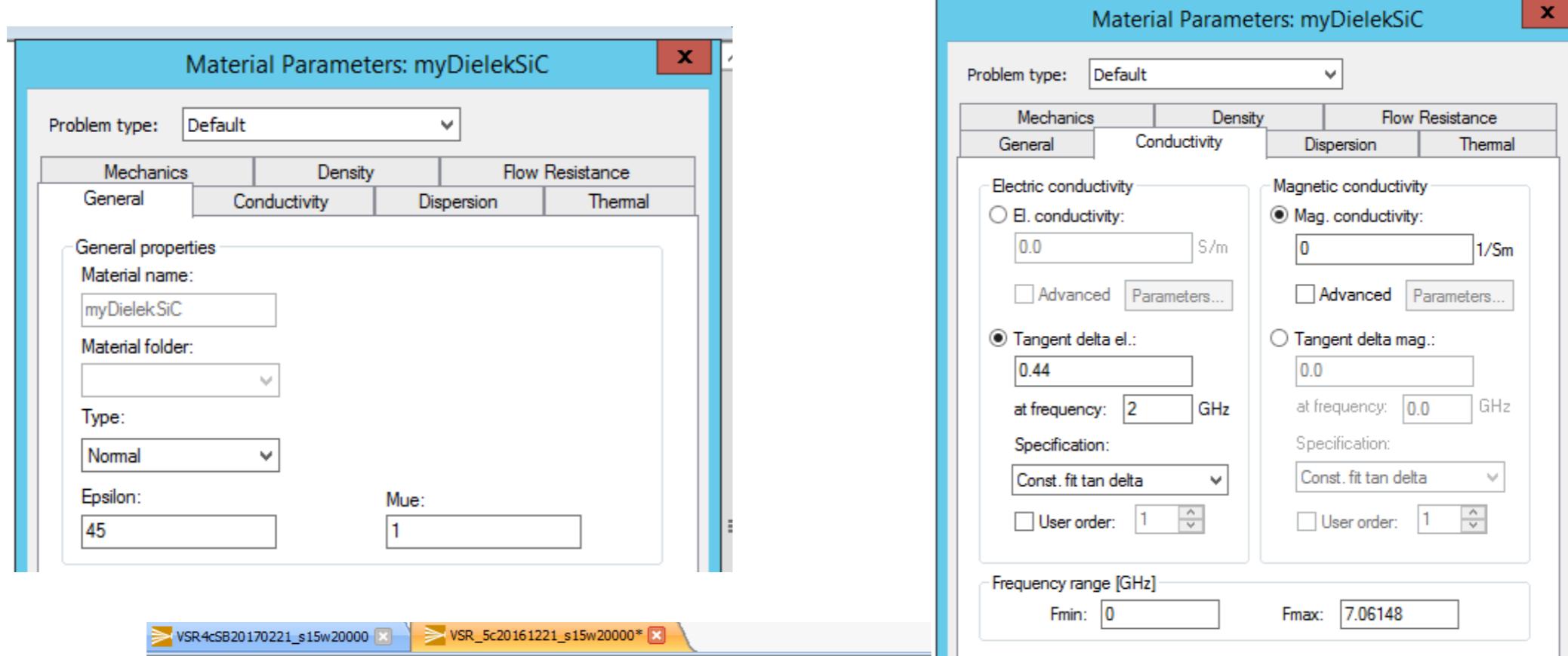
dielectric $\epsilon_r = 45$, $\mu_r = 1$, $\tan \delta = 0.44$ @ 2.0 GHz



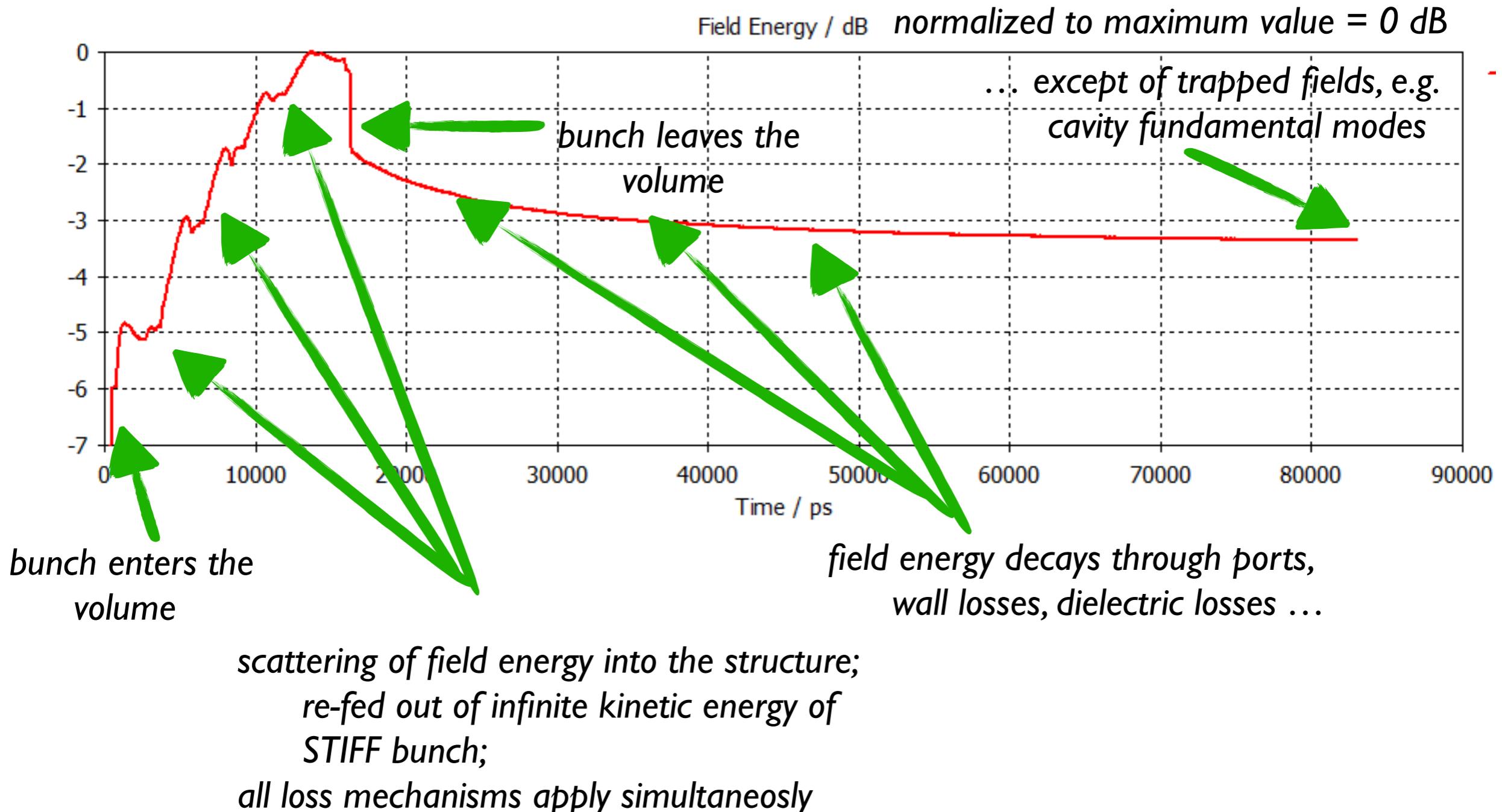
vacuum $\epsilon_r = 1$, $\mu_r = 1$, $\tan \delta = 0$



Side note II: Definition of dispersive materials needs care !

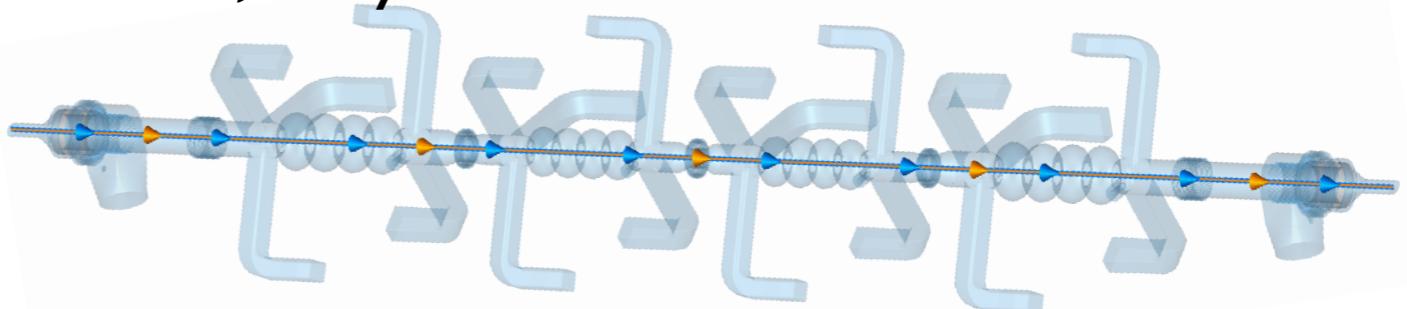


How develops the total energy in the system?

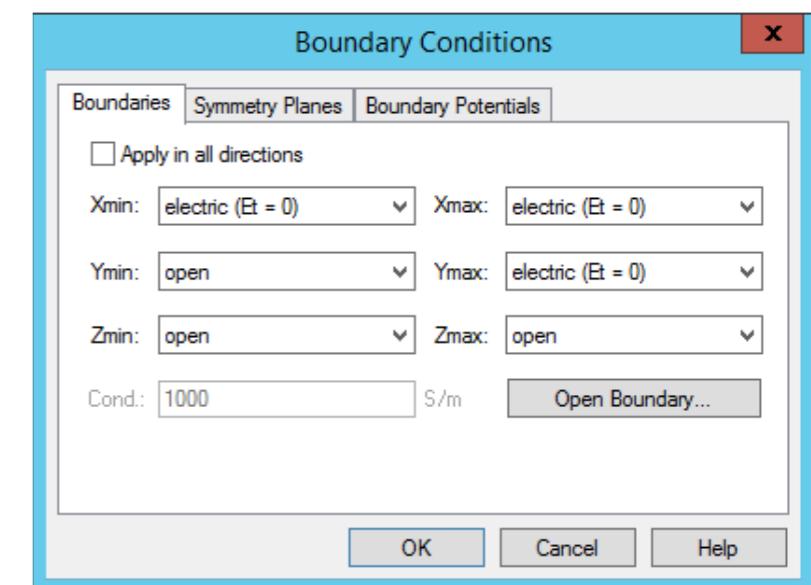
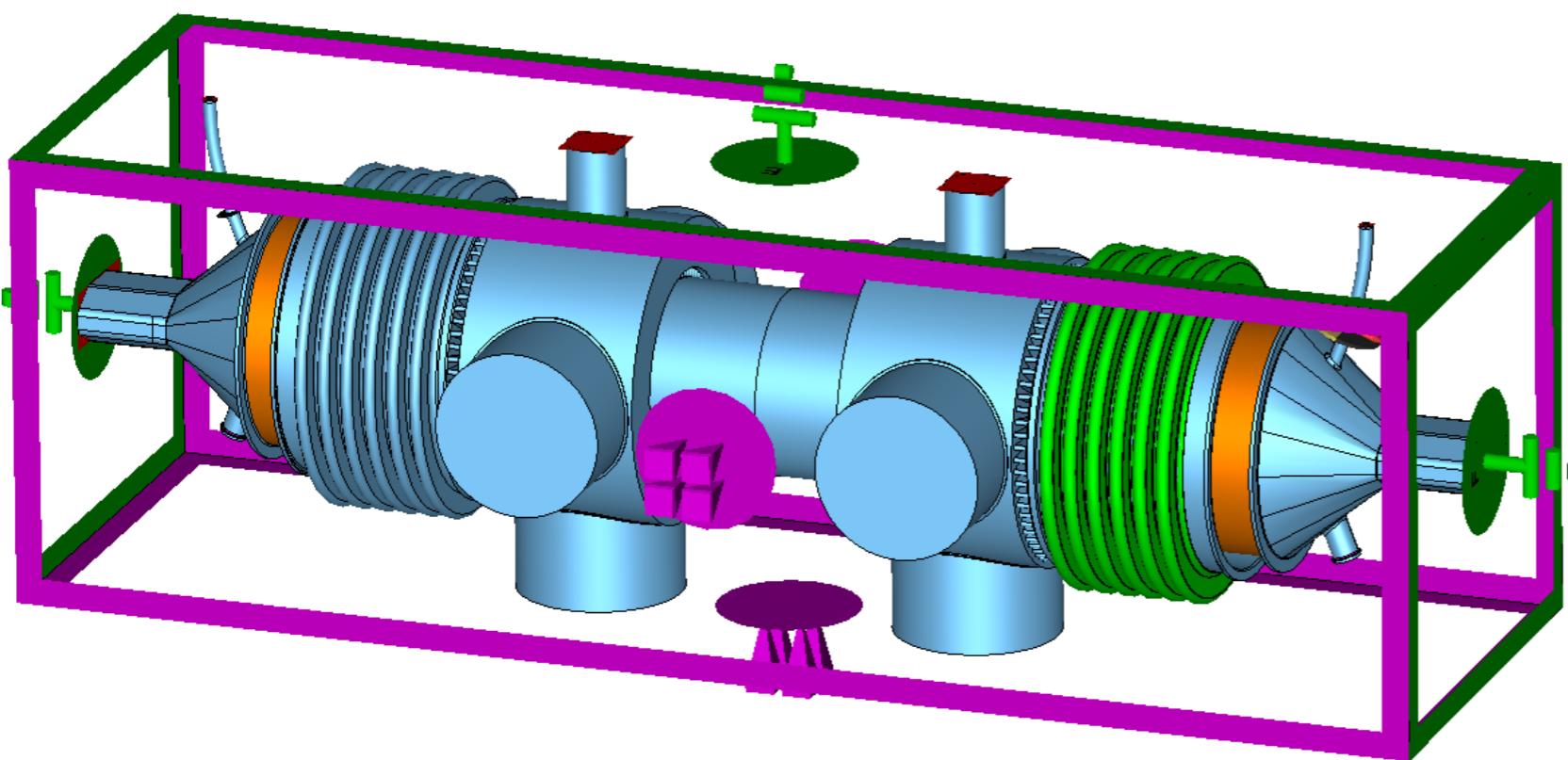


So, what to tell the wakefield solver ?

1. the geometry, i.e. the inner vacuum, lossy metal walls, dielectrics



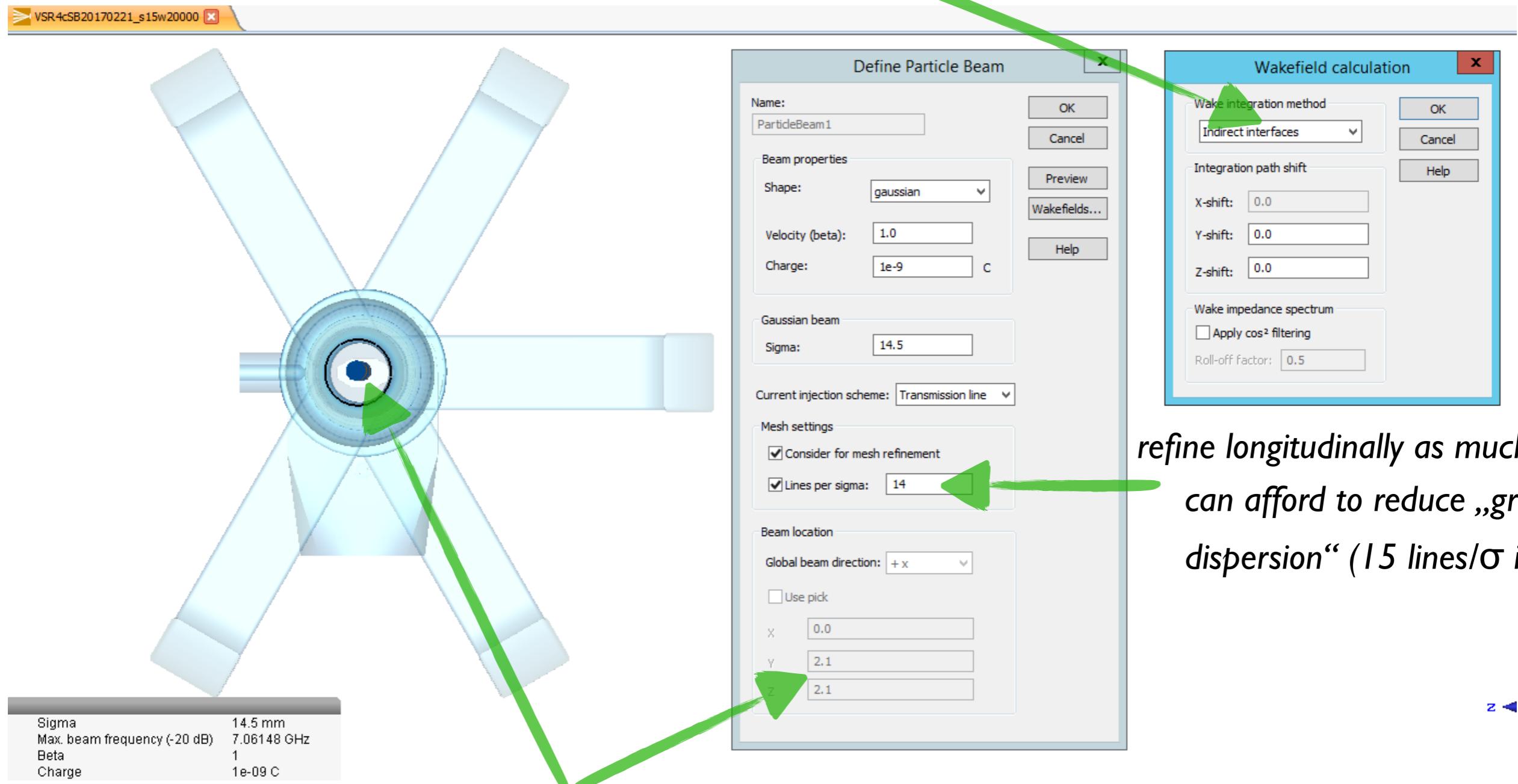
2. the boundary conditions, esp. at the beam pipes (preferably waveguide ports overlaying PEC) and large openings like pumping ports (preferably open boundary)



So, what to tell the wakefield solver ?

3. the beam parameters

3a. the wake integration scheme (avoid „direct“ unless $v < c_0$ or you can afford very long beam pipes !)

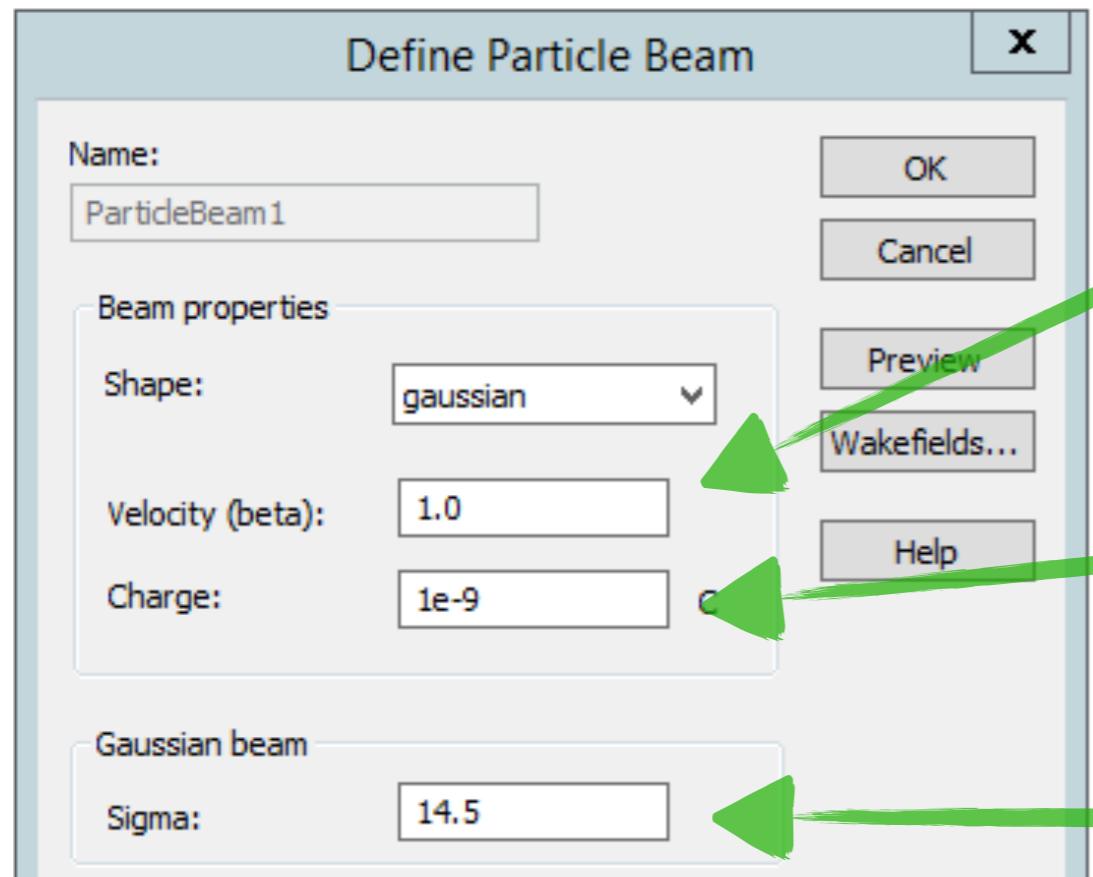


refine longitudinally as much you can afford to reduce „grid dispersion“ (15 lines/ σ is ok)

put it slightly off-axis to excite also dipole (quadrupole ...) modes

So, what to tell the wakefield solver ?

3. the beam parameters (cont.)



things get difficult if $v < c_0$

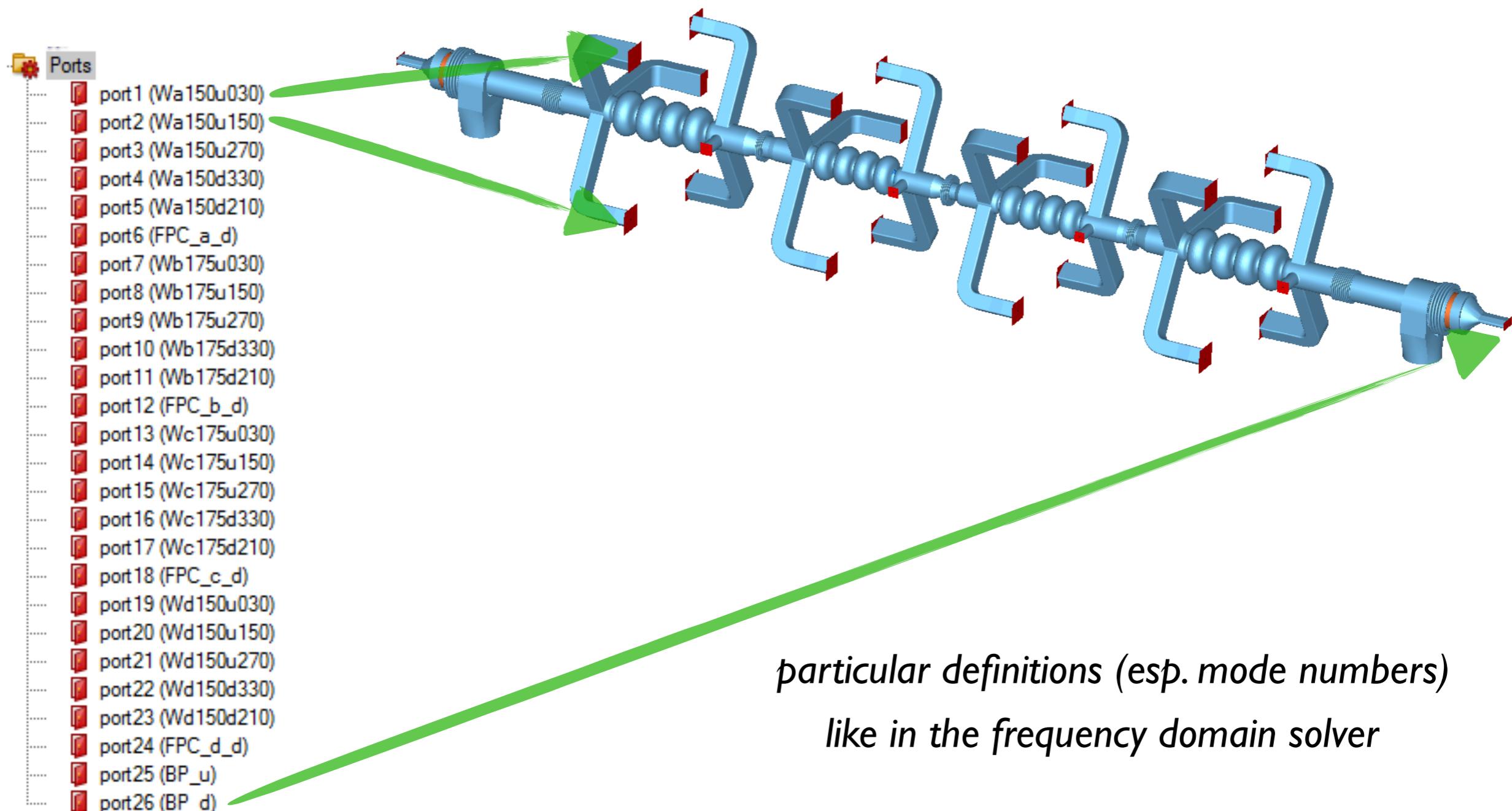
relevant only for absolute field amplitudes

the longer the bunch, the lower the frequency range covered: $\sigma = 14.5 \text{ mm}$ correspond to $\sim 7 \text{ GHz}$

... by the way: How scale wake fields if the bunch charge is doubled ?

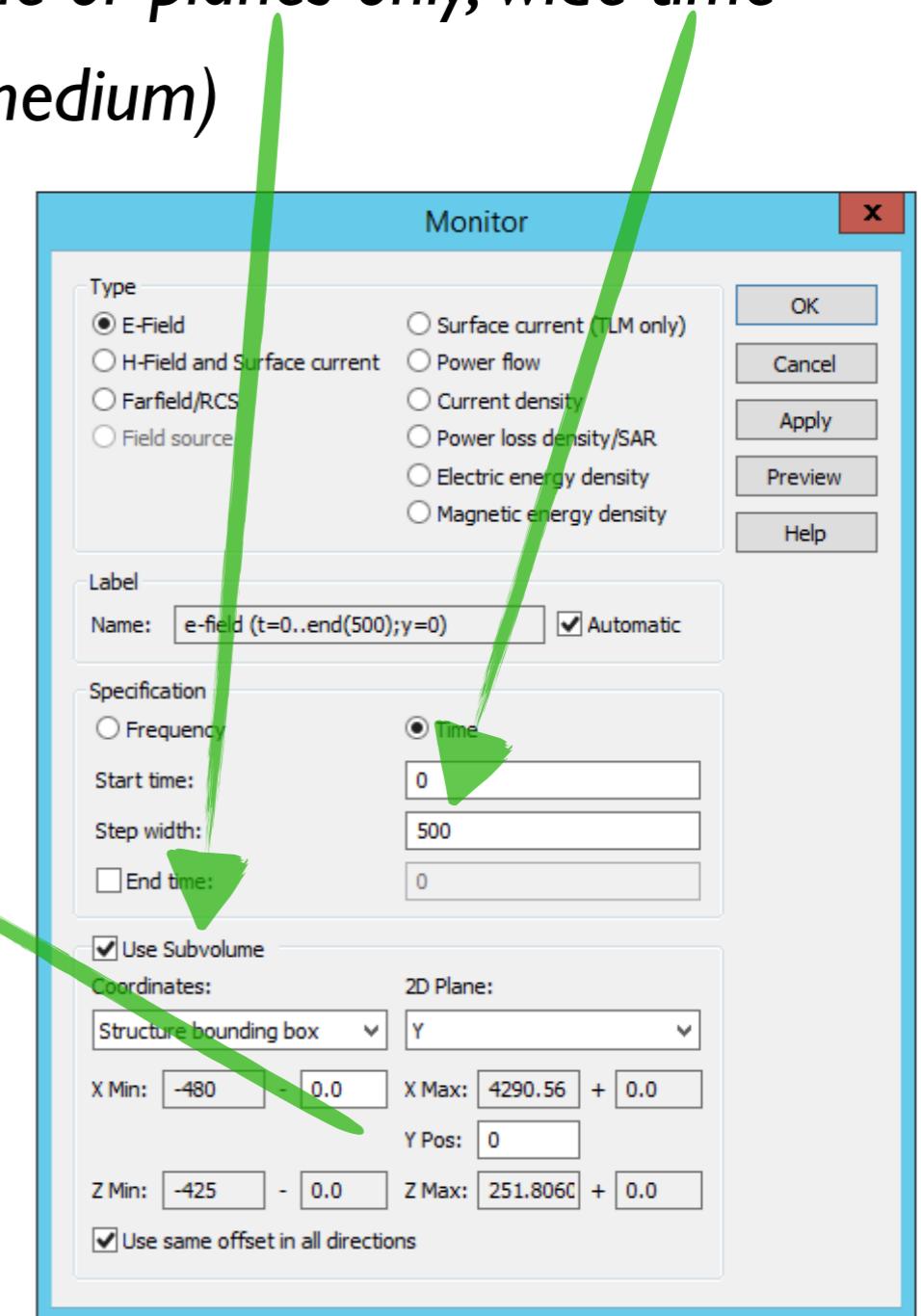
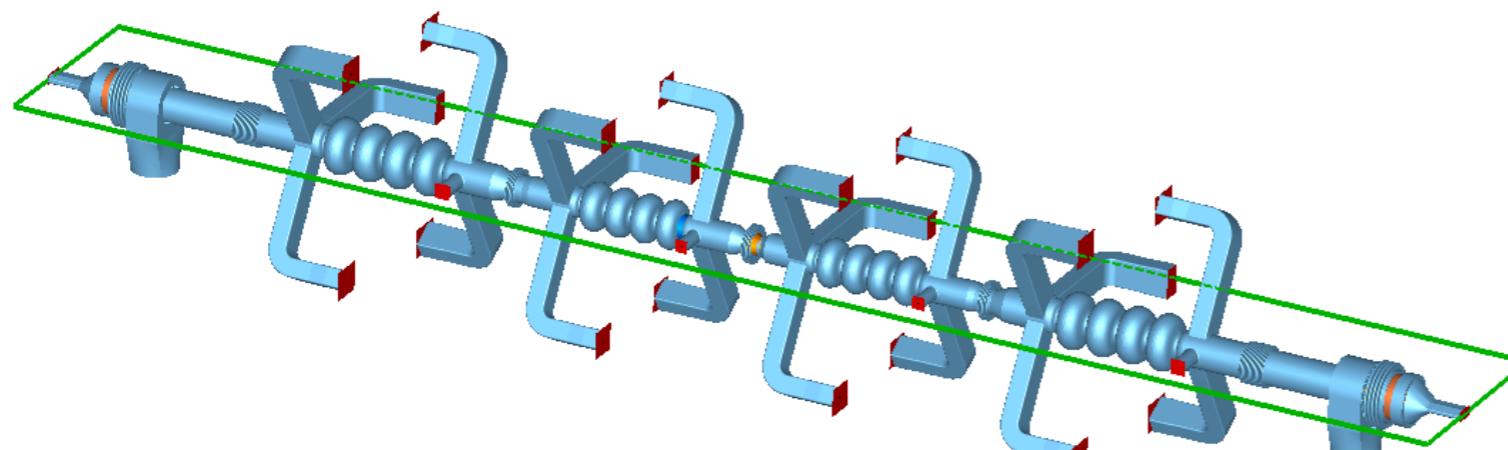
So, what to tell the wakefield solver ?

4. the ports



So, what to tell the wakefield solver ?

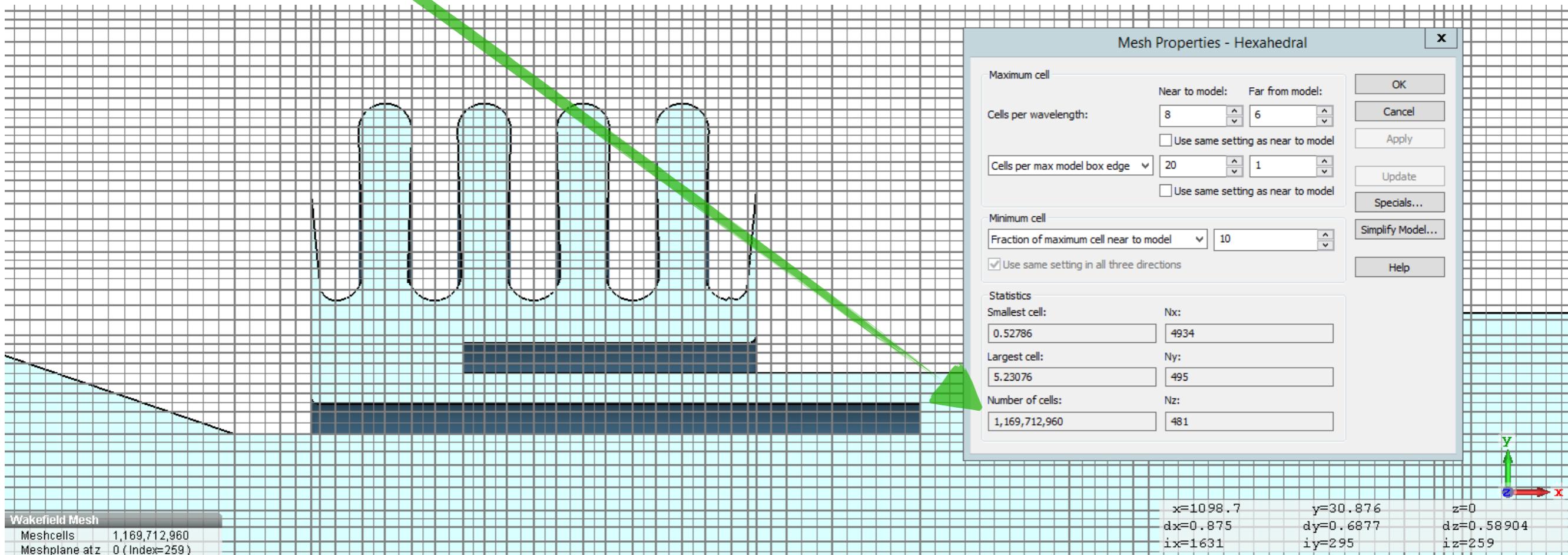
5. the field monitors (very carefully = reduce volume or planes only, wide time stepping, otherwise you can fill up any storage medium)



So, what to tell the wakefield solver ?

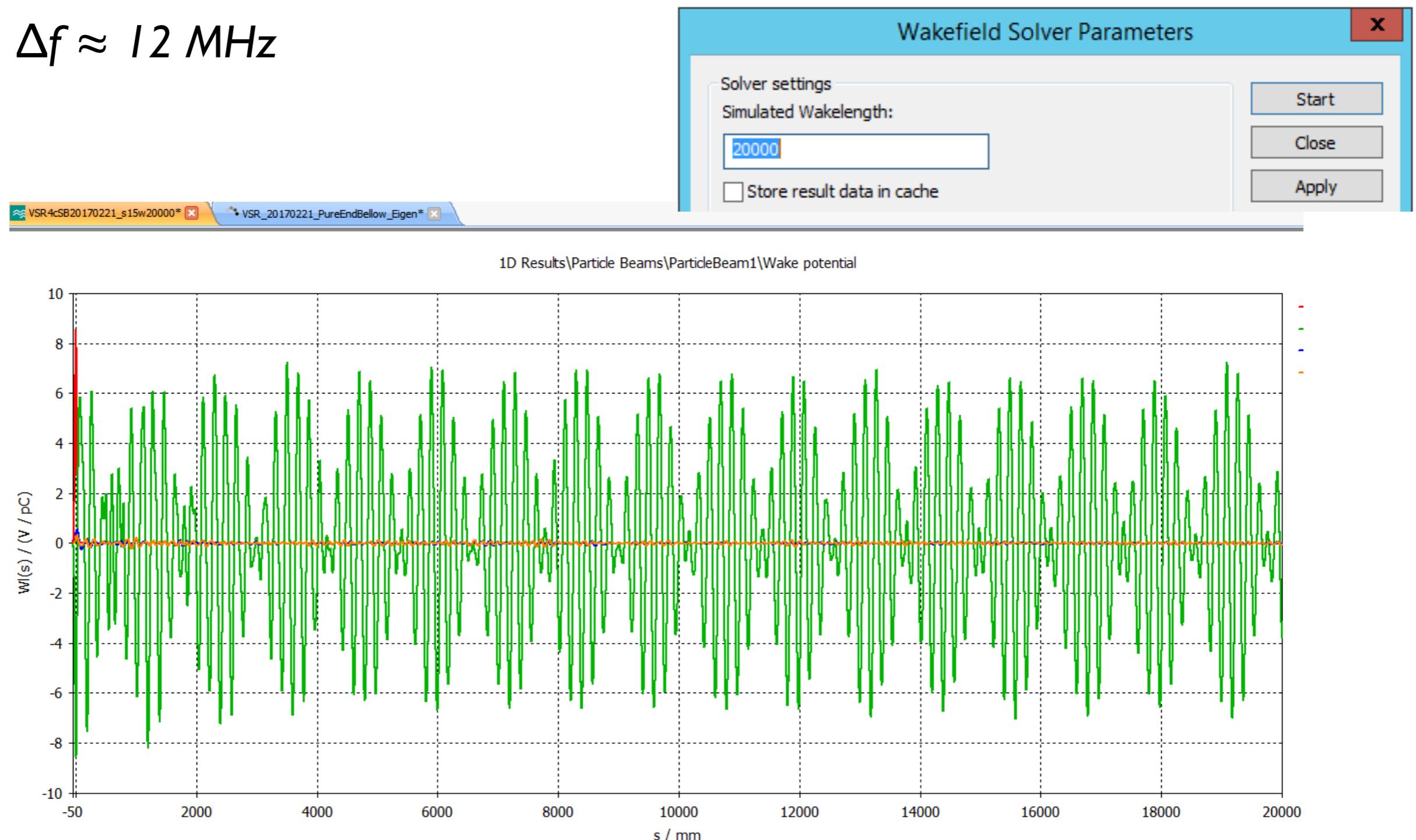
6. check the mesh (hex-mesh only, constructed automatically and appropriate for the beam, but all geometrical details need to covered)

$N_{\text{cells}} \sim 10^9$ is close to the limit of 256GB / 12 core workstation; lengthen bunch as $N_{\text{cells}} \sim (l/\sigma)^3$; computing time $\sim (l/\sigma)^4$



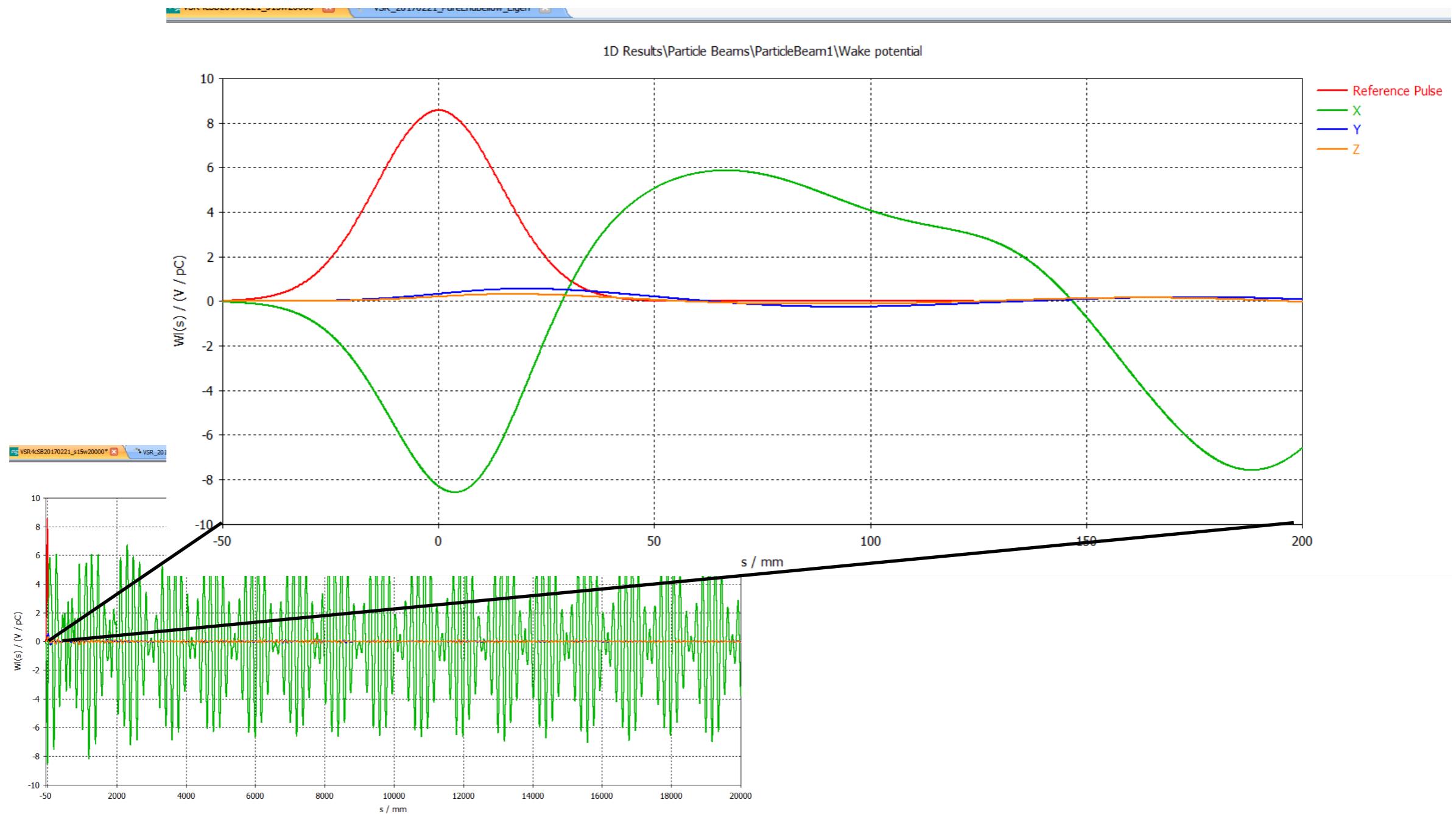
So, what to tell the wakefield solver ?

7. the wake integration length L_{wake} . This determines the resolution of the impedance spectrum by $\Delta f = c_0 / L_{\text{wake}}$. $L_{\text{wake}} = 20 \text{ m}$ corresponds to $\Delta f \approx 12 \text{ MHz}$



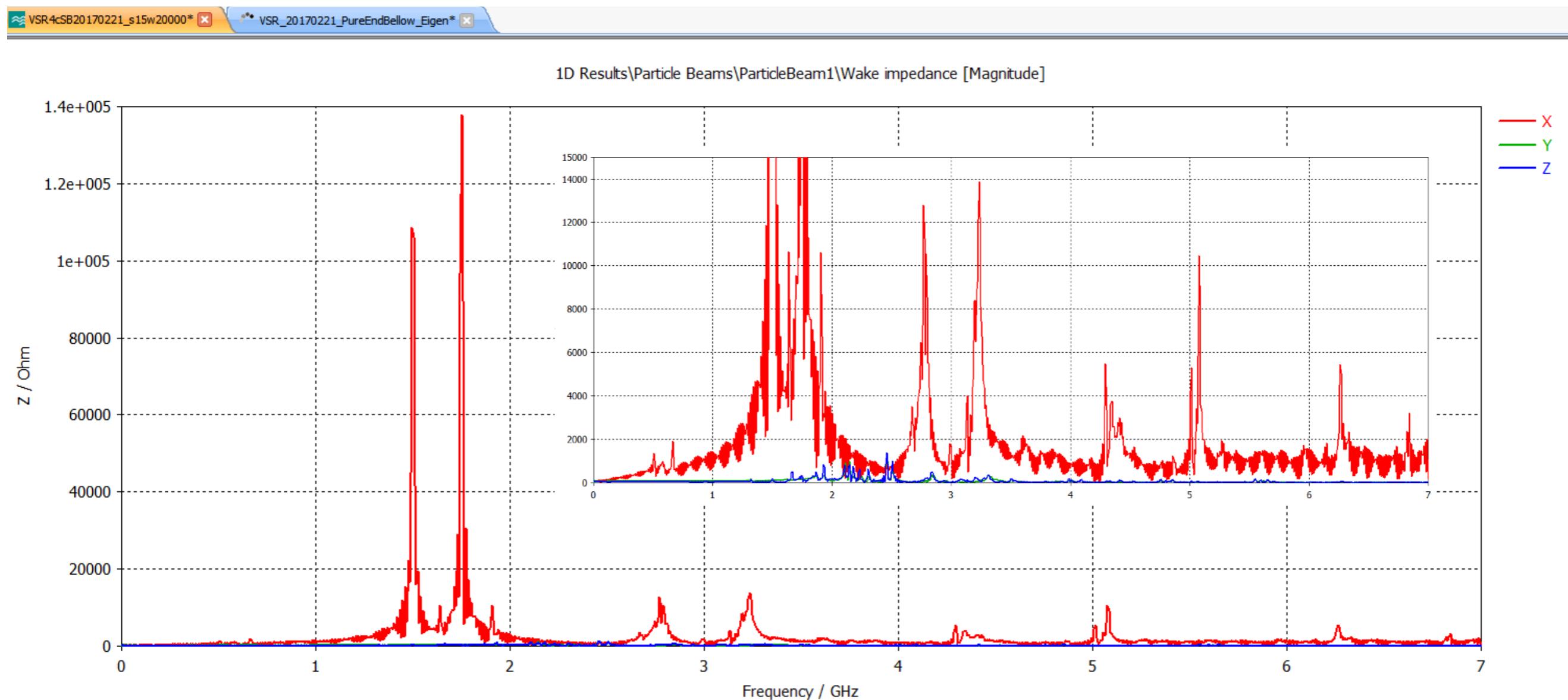
So, what to tell the wakefield solver ?

7b. If you only need a loss factor 200 mm wake length are sufficient, as k_{loss} is determined by the short range effect only.



And what do you get out - most we already saw

- except of the impedance



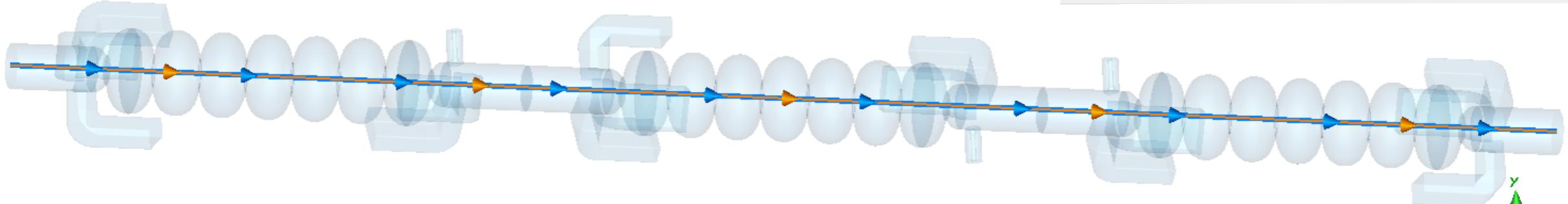
... by the way: Which cavity modes should show the highest impedances ?

Supplement:

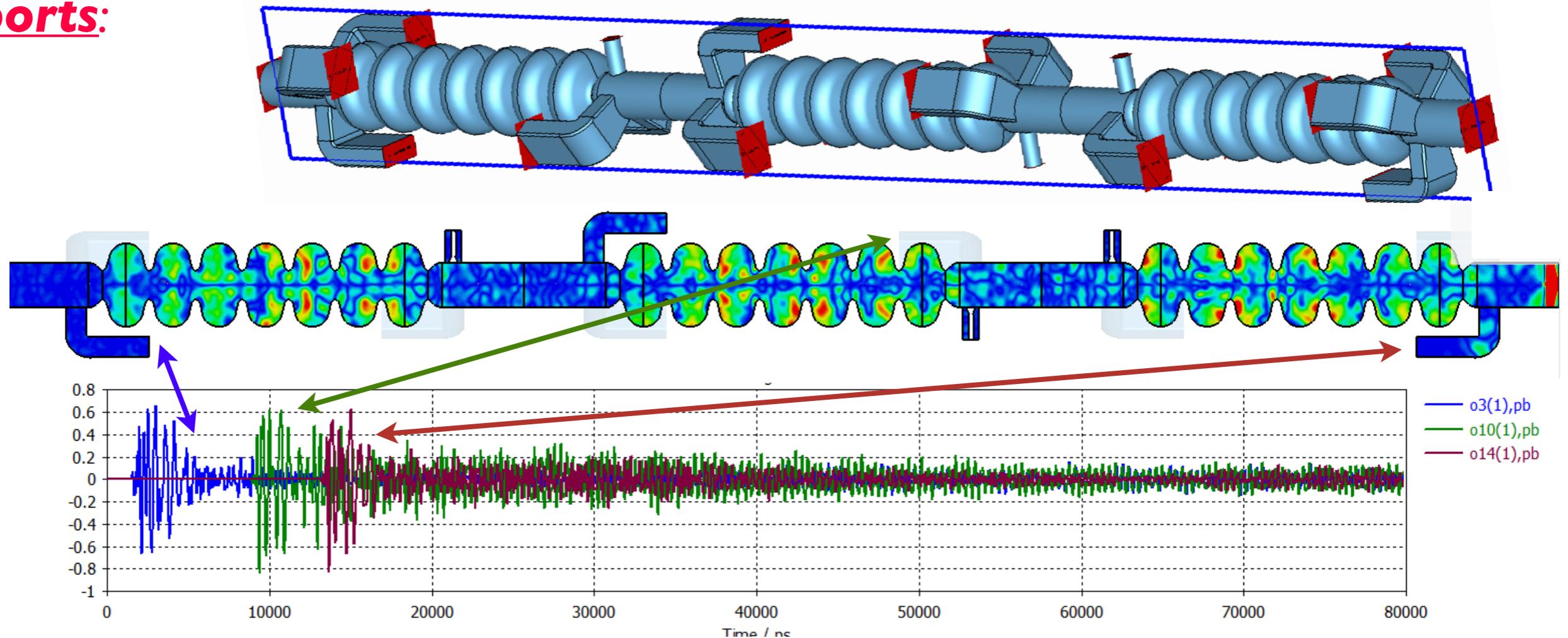
*Continuous-Wave HOM Load Power Computations
Based on Single-Bunch Wake Simulations*

CST wake-to-absorber calculations (here bERLinPro Linac):

I.) numerically pass a *single bunch* ((reasonably) off-axis) through the cavity (chain)



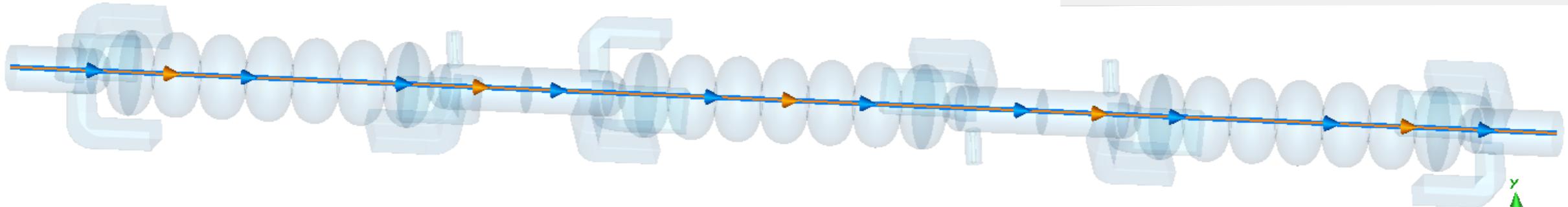
2.) monitor (sufficiently many) waveguide mode amplitudes (dimension $W^{1/2}$) at all **ports**:



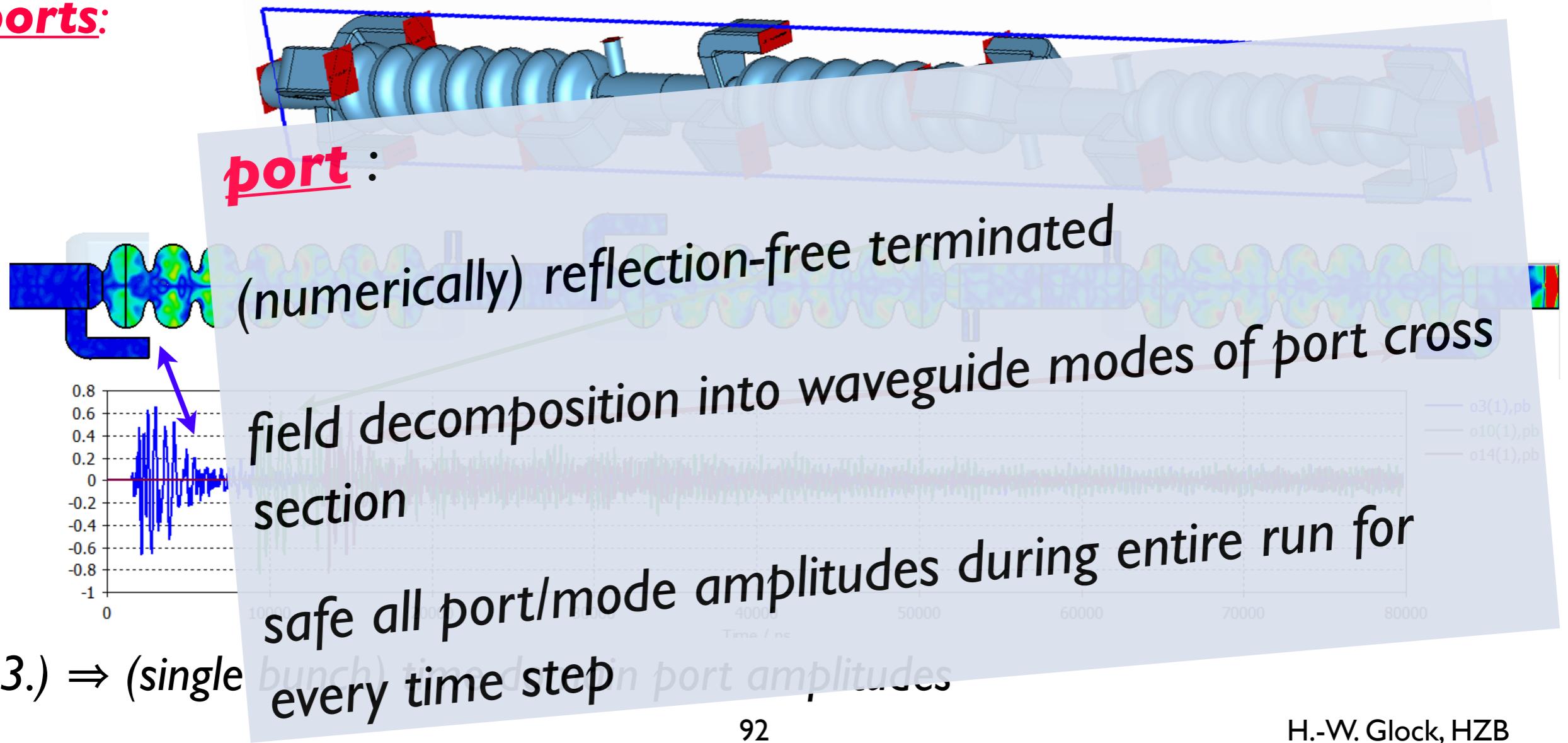
3.) \Rightarrow (single bunch) time domain port amplitudes

CST wake-to-absorber calculations:

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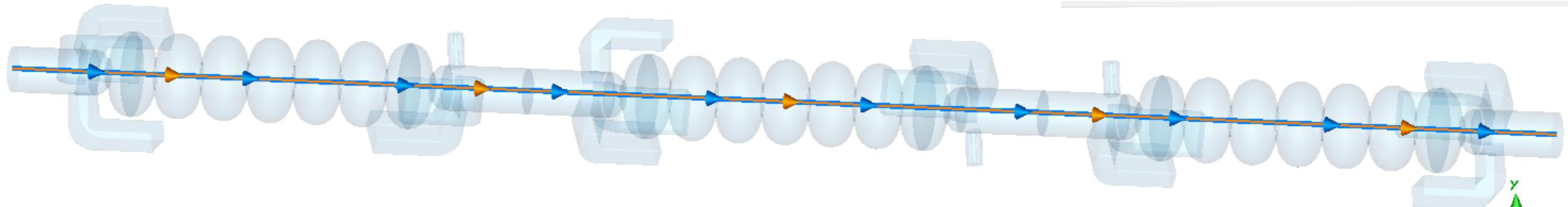


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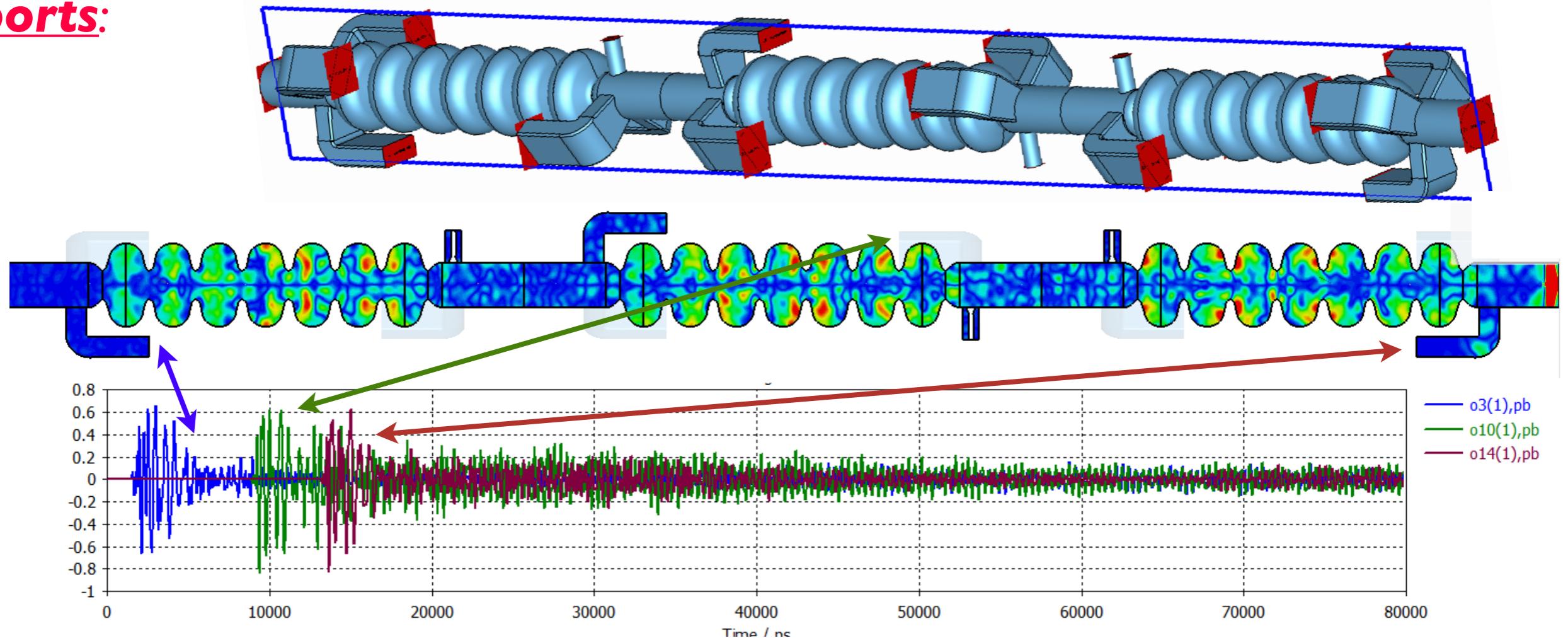


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3.) \Rightarrow (single bunch) time domain port / mode amplitudes

CST wake-to-absorber calculations:

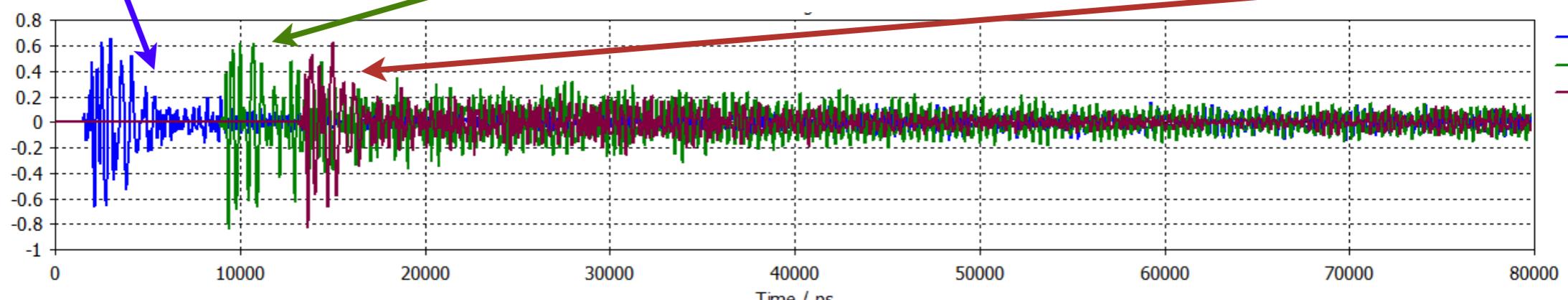
- 1.) numerically pass a *single bunch* ((reasonably) off-axis) through the cavity (chain)



- 2.) monitor (sufficiently many) waveguide mode amplitudes (dimension $W^{1/2}$) at all invariant **ports**:

⇒ linear convolutions of excitations / reactions allowed

⇒ Fourier transforms allowed



- 3.) ⇒ (single bunch) time domain port amplitudes

How do we get the
multi-bunch port/mode power P_{pm} (averaged over ΔT)
from the single-bunch excited port/mode amplitude A_{pm} ?

1.) Fourier-transform A_{pm} and interpolate it on frequency points ($j/\Delta T$)

$$\alpha_{pm}(j) = \text{Interpolate}\{ \text{DiscreteFourierTr.}\{A_{pm}\} @ (j/\Delta T) \}, \quad j = 1 \dots N_{max}, \quad N_{max} = f_{max} \cdot \Delta T$$

2.) Sample a single Gaussian bunch current of simulated σ , zero-padded to ΔT . Fourier-transform, take the first N_{max} values:

$$Y(j) = \text{DiscreteFourierTr.}\{\text{Gauss}_{\sigma}+000\}$$

3.) Sample the given train of (Gaussian?) bunch currents. Fourier-transform, take the first N_{max} values:

$$\beta(j) = \text{DiscreteFourierTr.}\{\text{bunchtrain}\}$$

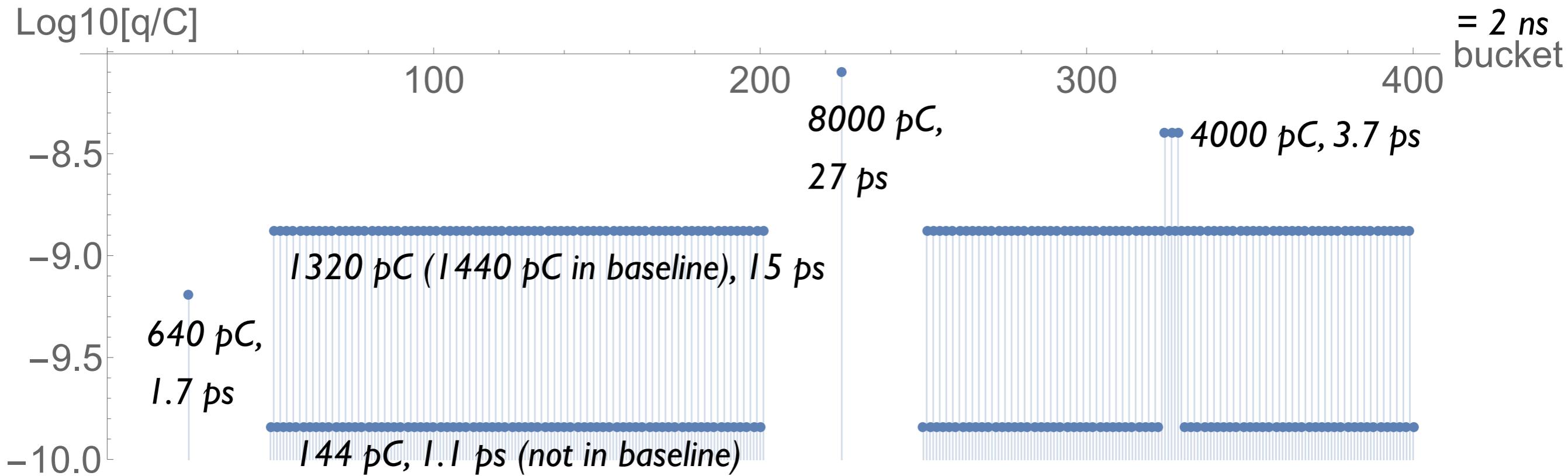
4.) Compute for each frequency step j the excitation-scaled, frequency-domain port / mode amplitude:

$$\tilde{A}_{pm}(j) = \beta(j) / Y(j) \cdot \alpha_{pm}(j)$$

5.) Compute for each frequency step j (of width $1/\Delta T$), the frequency-domain port / mode power $P_{pm}(j)$:

$$P_{pm}(j) = \tilde{A}_{pm}(j) \cdot \tilde{A}_{pm}^*(j)$$

VSR (Variable pulse length Storage Ring) beam time structure:



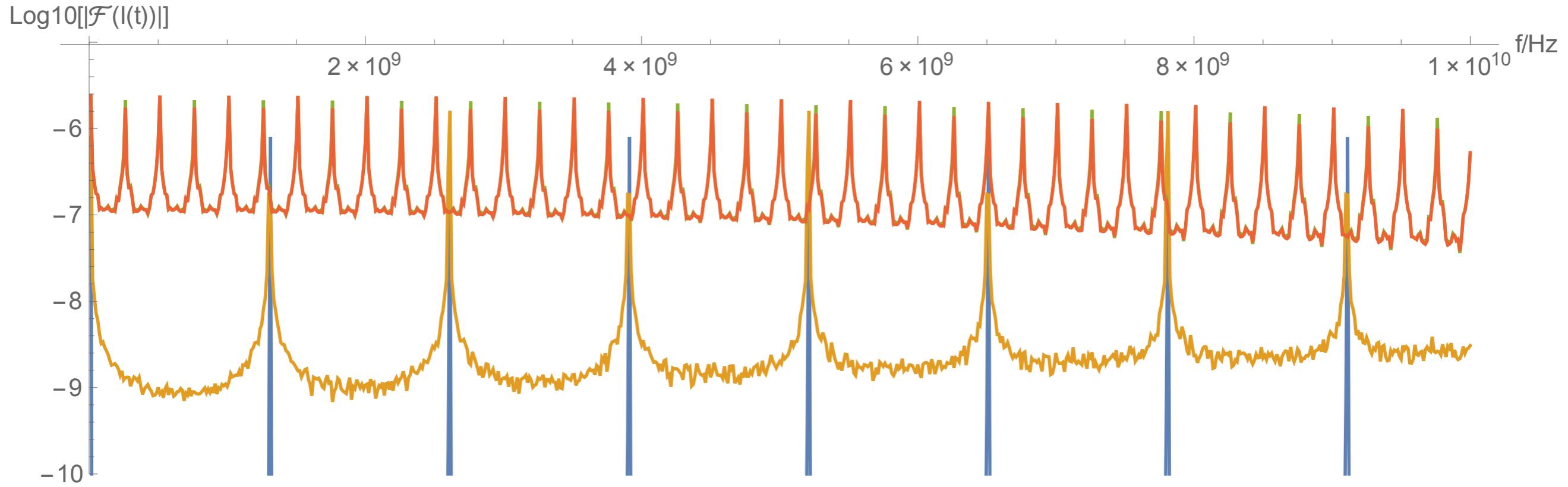
All bunches Gaussian shaped, sampled with 0.1 ps time step,
time signal of $\Delta T = 8 \mu s$ length = 80 Mio sampling points Discrete-Fourier-transformed.

VSR — NO: beam dynamics, phase shifts, noise

bERLinPro — $\sigma = 2 \text{ ps}$, 1.3 GHz cw, recirculation, white noise charge jitter $\pm 2\%$,
phase jitter $\pm 1^\circ$, assumed gapping: 2080 bunches + 520 empty buckets

Spectral amplitude comparison up to 10 GHz:

bERLinPro / bERLinPro-worst case / VSR-baseline / VSR-extended



bERLinPro: recirculation not included, therefore $n \times 1.3$ GHz

bERLinPro-w.c.: recirculation included $\Rightarrow n \times 2.6$ GHz, but also gaps \Rightarrow (weaker) $n \times 2.6$ GHz + 1.3 GHz

VSR: 4 ns-gaps dominant $\Rightarrow n \times 250$ MHz

VSR-extended: interlaced 1.1 ps – low charge does not hurt, but $n \times 500$ MHz a little bit more exposed

- bERLinPro cw beam NO repetition,
NO jitter
- bERLinPro cw beam with repetition,
2080 bunches + 520 gaps, jitter $\pm 1^\circ$, $q \pm 2\%$
- bessy VSR beam
NO 1.1 ps, no jitter
- bessy VSR beam
WITH 1.1 ps, no jitter

Interpolation of port signal spectra ... unfortunately needed:

*Typical workstation (12 cores, 256 GB RAM),
wake simulation acting on $\sim 10^9$ mesh cells (hexagonal grid),
response times $\sim 10^1$ days :*

$\Rightarrow \sim 20\text{ m wake length}$

$\Rightarrow \sim 80\text{ ns integration time}$

$\Rightarrow \sim 12.5\text{ MHz frequency resolution}$

REMEMBER: Beam spectra available e.g. with 125 kHz

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Interpolation options:

- \Rightarrow linear
 - in tests significant power deficit
- \Rightarrow black-box spline x^{th} order
 - we use $x = 5$, seems acceptable
- \Rightarrow pole fitting
 - recommendable

Interpolation of port signal spectra ... unfortunately needed:

*Typical workstation (12 cores, 256 GB RAM),
wake simulation acting on $\sim 10^9$ mesh cells (hexagonal grid),
response times $\sim 10^1$ days :*

*Interpolating the spectrum of the port signals means a
virtual prolongation of missing wake integration time.*

$\Rightarrow \sim 80$ ns integration time

$\Rightarrow \sim 12.5$ MHz frequency resolution

REMEMBER: Beam spectra available e.g. with 125 kHz

Interpolation options:

\Rightarrow linear

– in tests significant power deficit

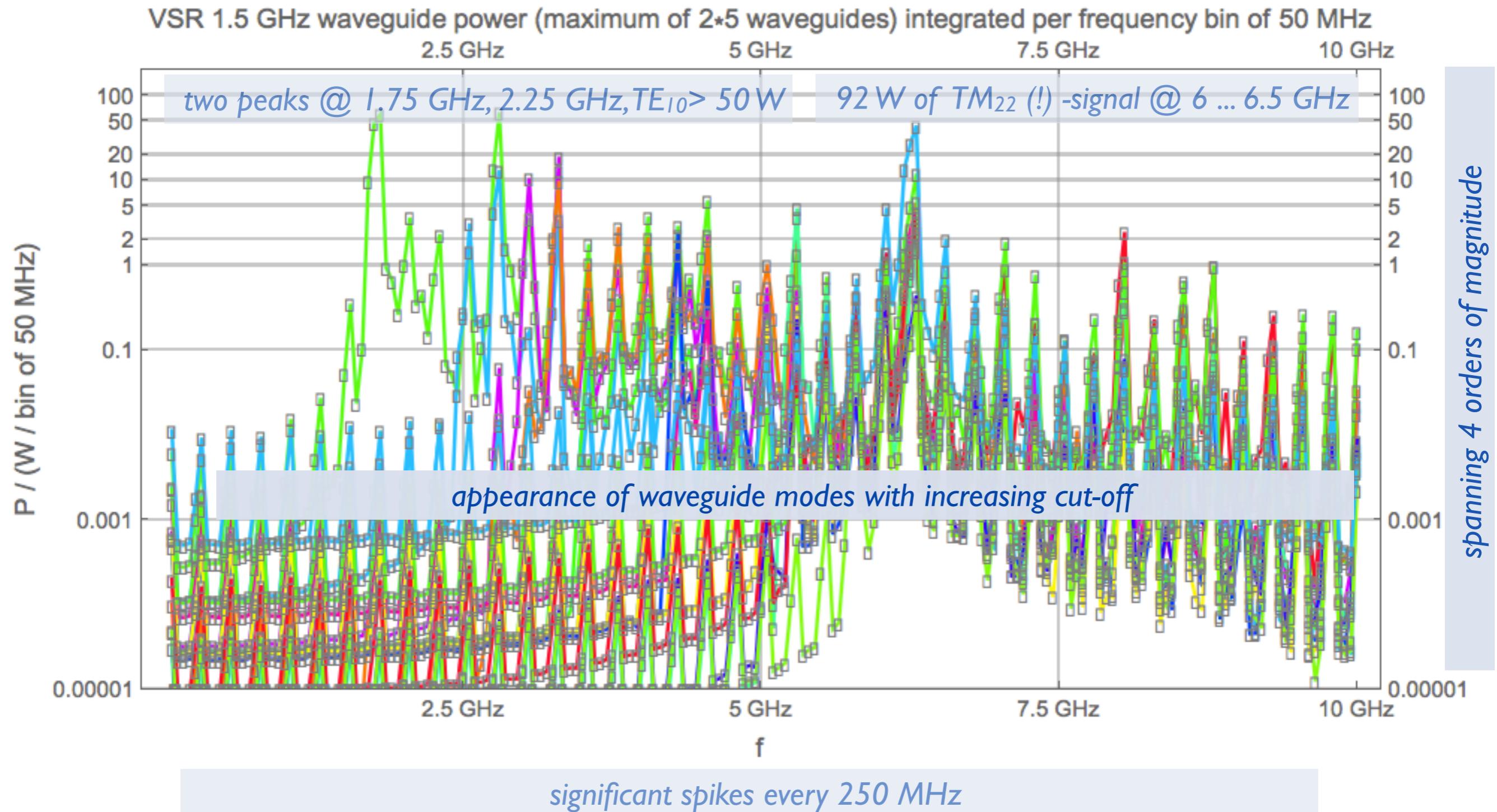
\Rightarrow black-box spline x^{th} order

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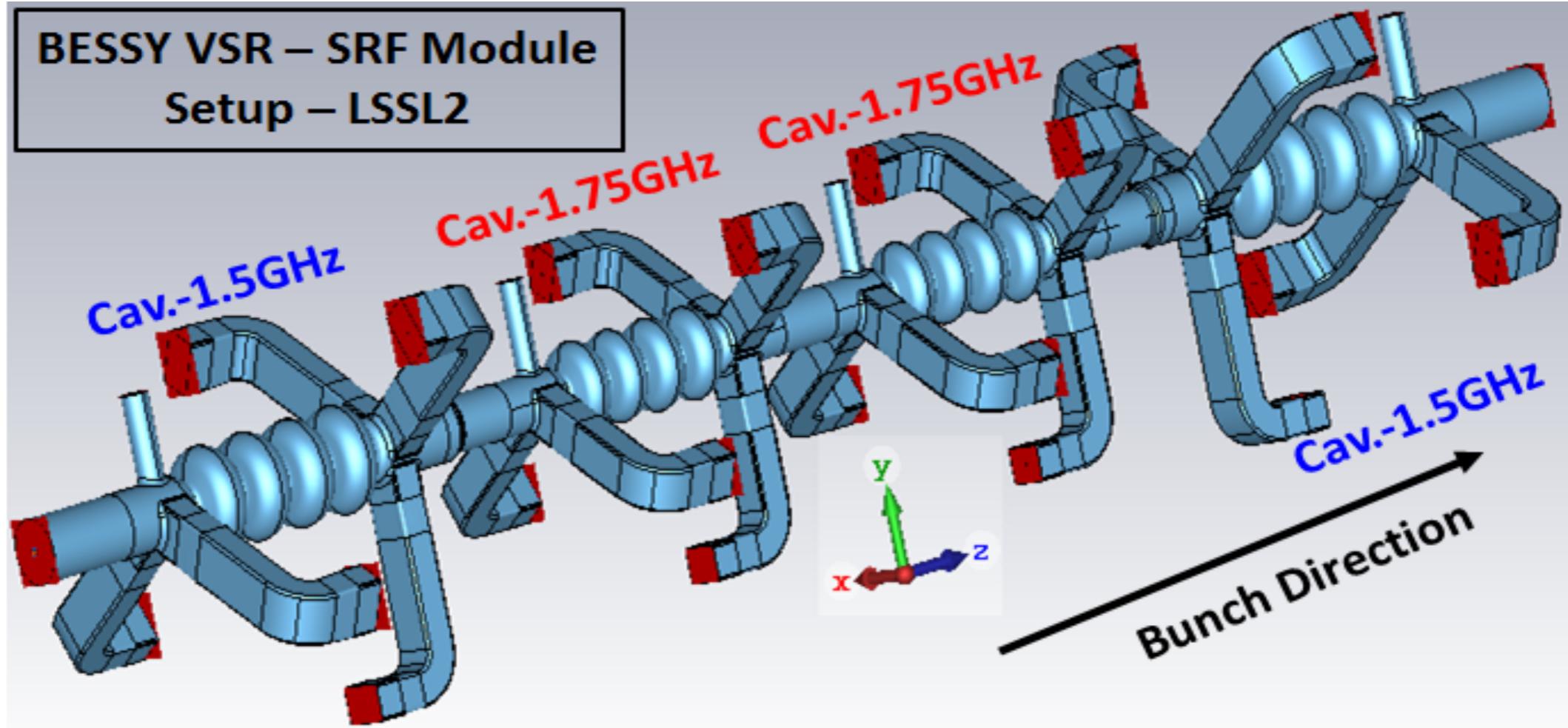
– recommendable

Result example: VSR 4-cavity chain, 1.5 GHz: Waveguide port power analysis – using maximum values per frequency of any of 10 waveguides



Full String Wake Simulations in Various Setups

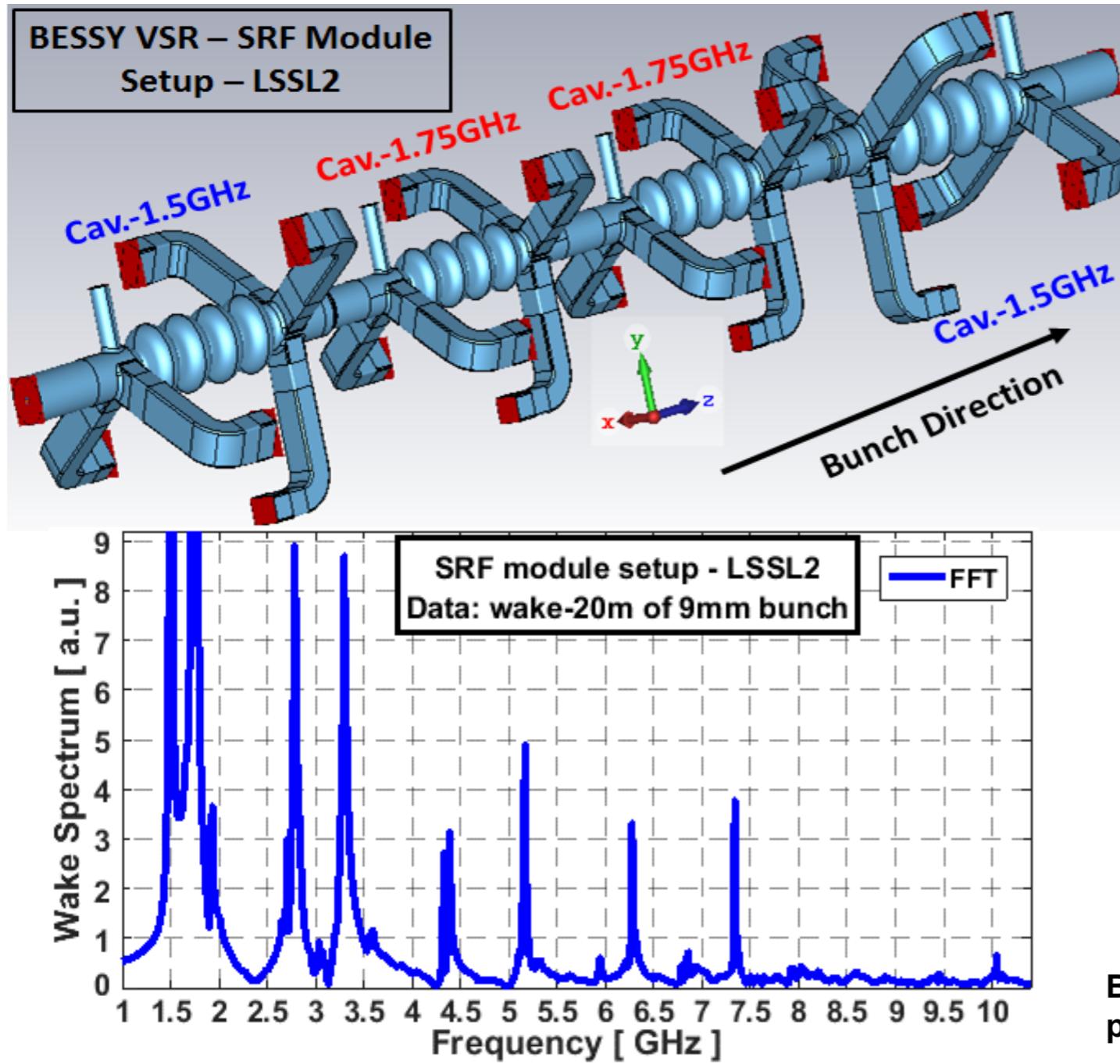
results, slide courtesy of Andranik Tsakanian



- ... to reduce and equilibrate power flow in HOM loads
- ... especially to reduce power flow in fundamental power couplers to avoid issues of the ceramic windows.

HOM Power Levels in Entire Module

results, slide courtesy of Andranik Tsakanian



VSR Module Power Levels: Baseline Filling Pattern

Port	LSSL1	LSSL2	SSLL1	SSLL2
1	28,9	28,9	102,2	58,6
2	102,2	102,1	216,0	217,4
3	102,2	102,1	216,0	217,4
4	157,0	157,1	178,7	179,0
5	157,0	157,1	178,7	179,0
6	195,6	195,5	204,6	231,7
7	46,3	45,8	25,7	25,4
8	230,3	230,1	140,2	140,1
9	230,3	230,1	140,2	140,1
10	163,2	163,7	165,5	165,9
11	163,2	163,7	165,5	165,9
12	221,8	221,3	225,7	223,6
13	52,6	53,0	53,1	52,4
14	249,6	247,2	254,2	251,8
15	249,6	247,2	254,2	251,8
16	185,2	163,9	195,2	171,1
17	185,2	163,9	195,2	171,1
18	240,9	199,9	263,6	207,6
19	96,2	24,2	59,7	23,7
20	201,5	115,1	210,2	116,2
21	201,5	115,1	210,2	116,2
22	86,0	159,5	90,0	167,6
23	86,0	159,5	90,0	167,6
24	97,3	202,8	96,5	208,5
25	246,6	246,1	227,6	225,0
26	269,4	330,2	299,0	357,7
Total	4245 W	4225 W	4457 W	4432 W

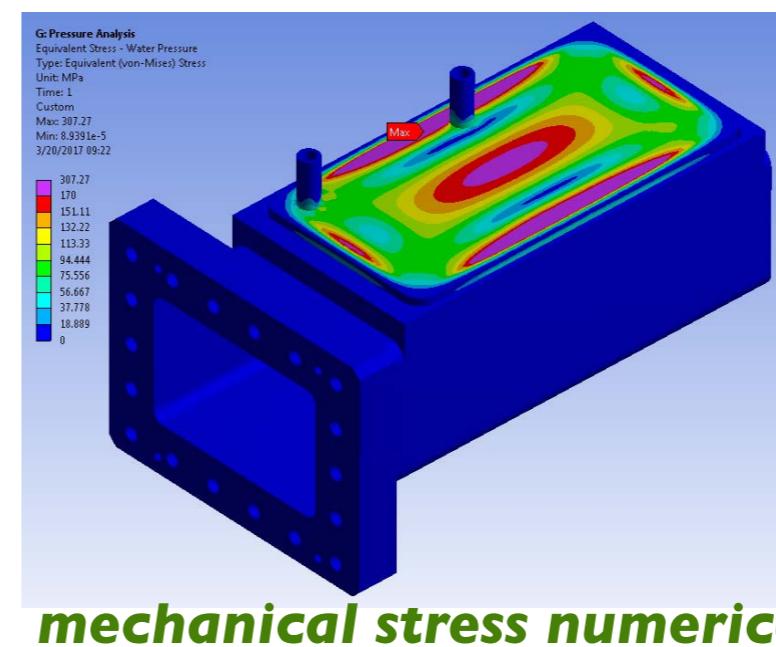
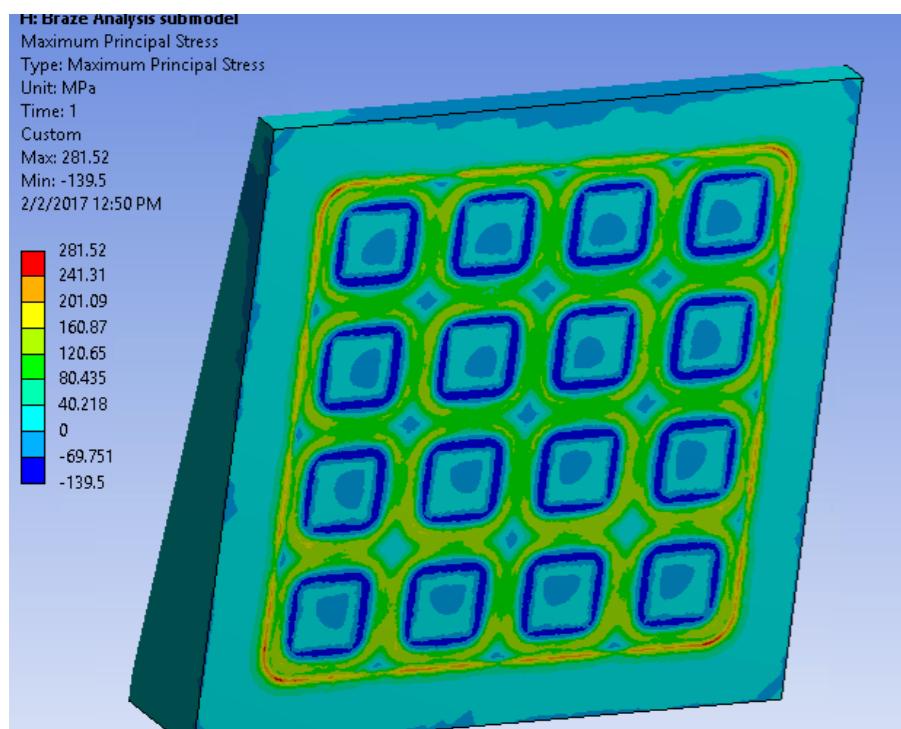
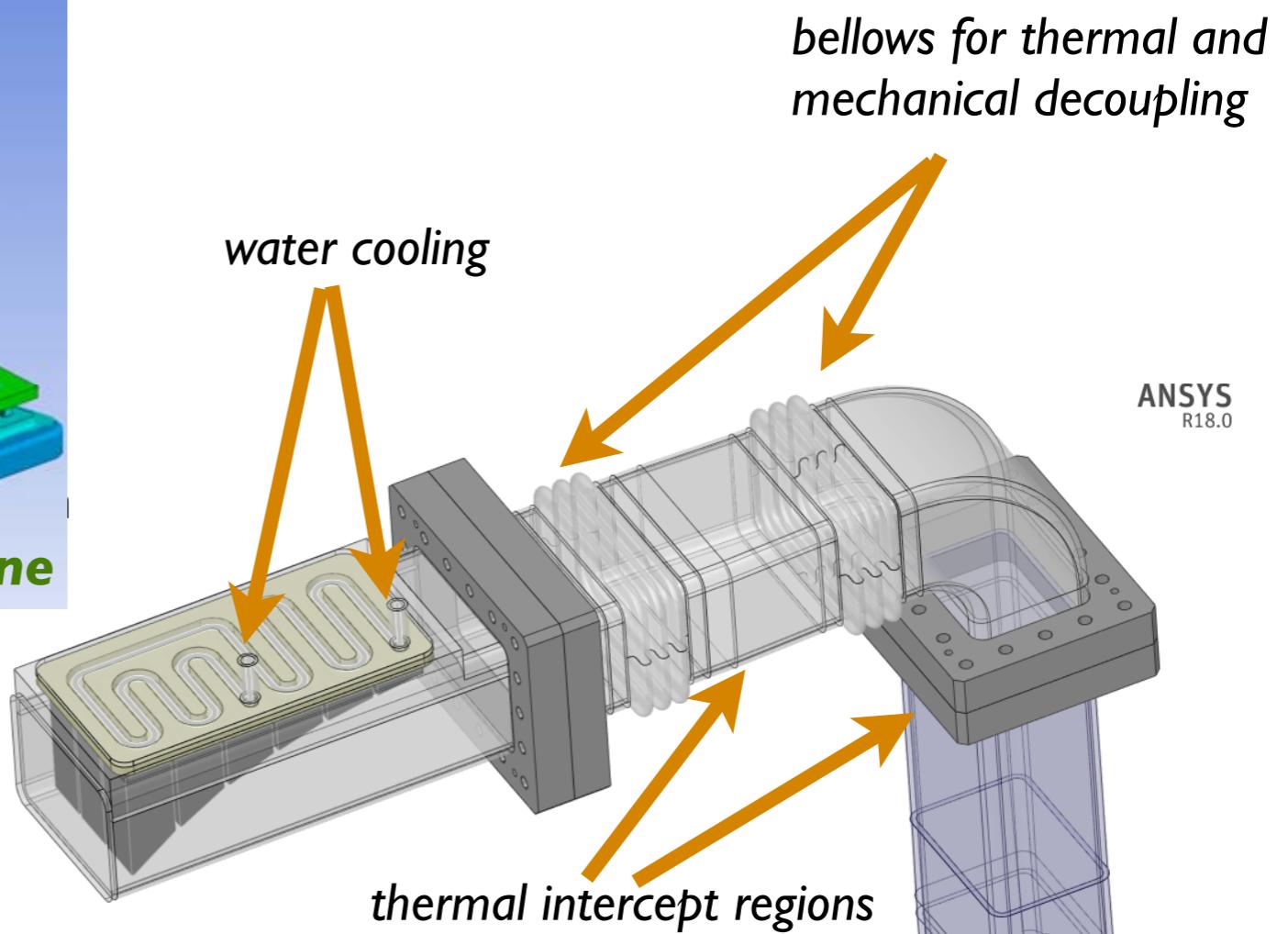
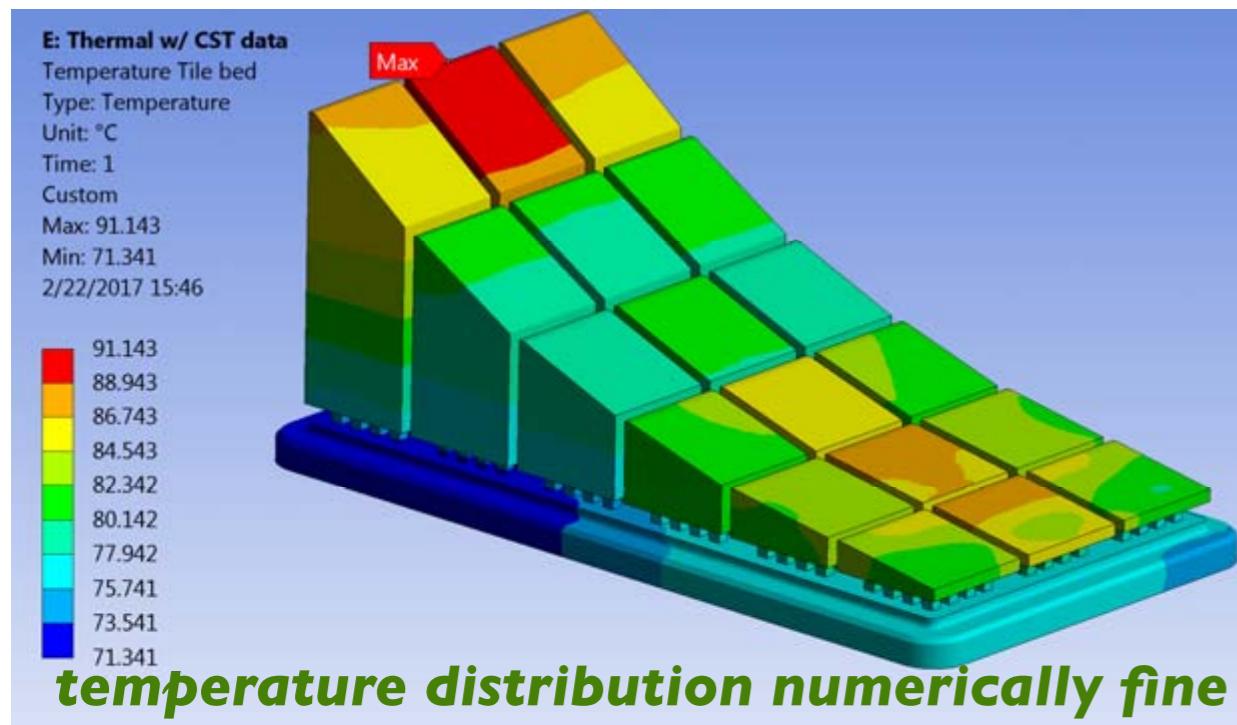
Beam pipes {

1.5 GHz 1.75 GHz Cavities 1.5 GHz

... we have to face ~5 kW of RF power to be dumped.

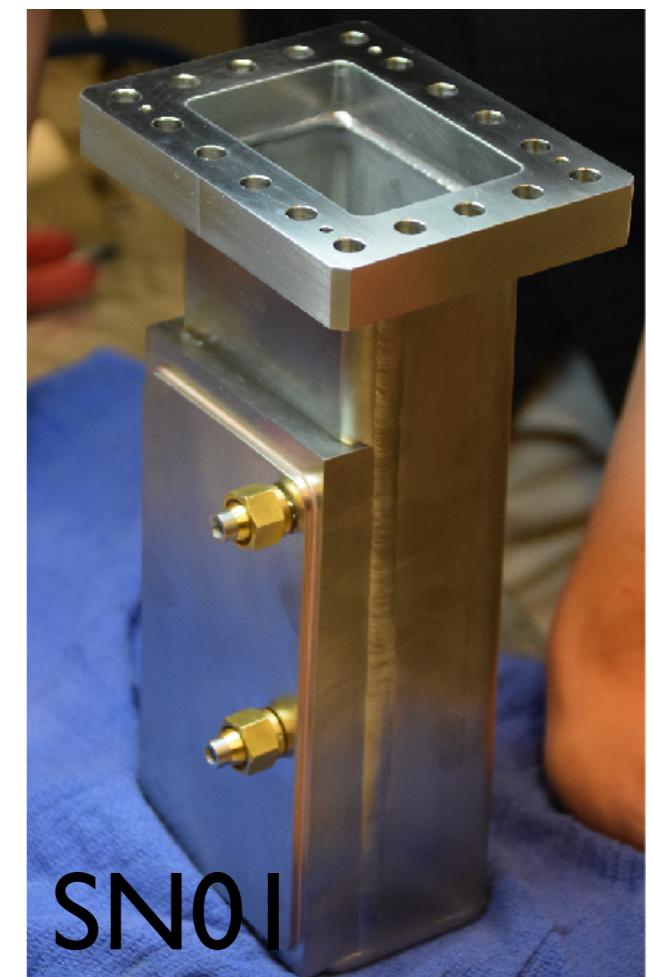
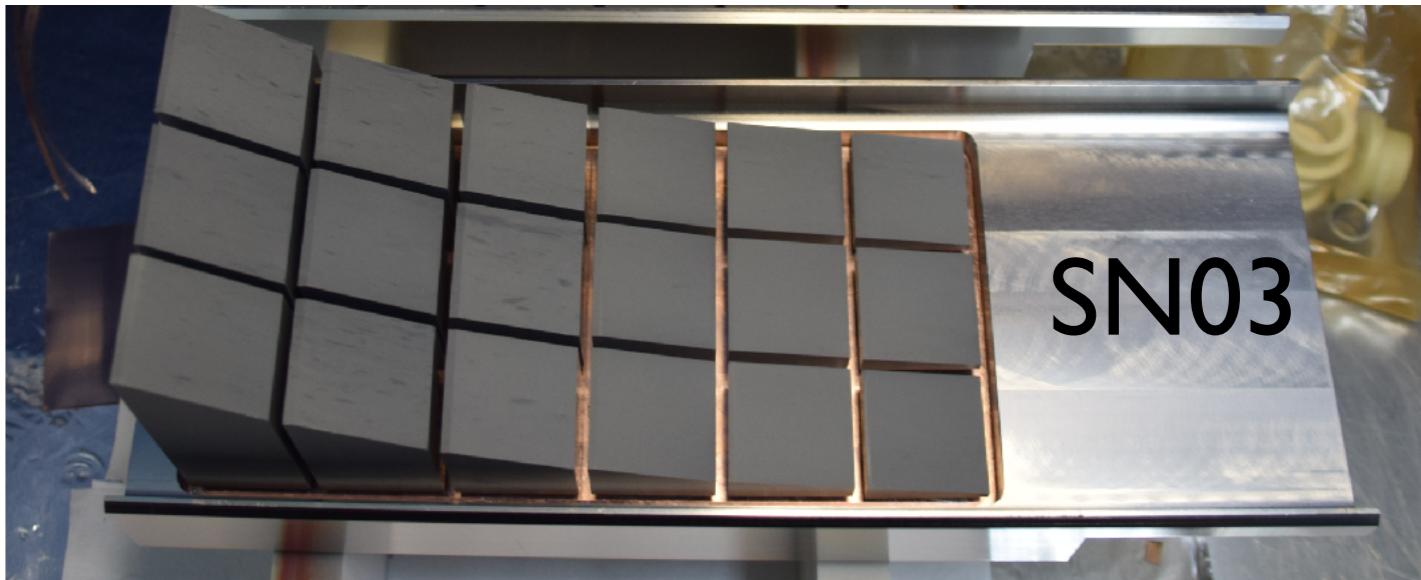
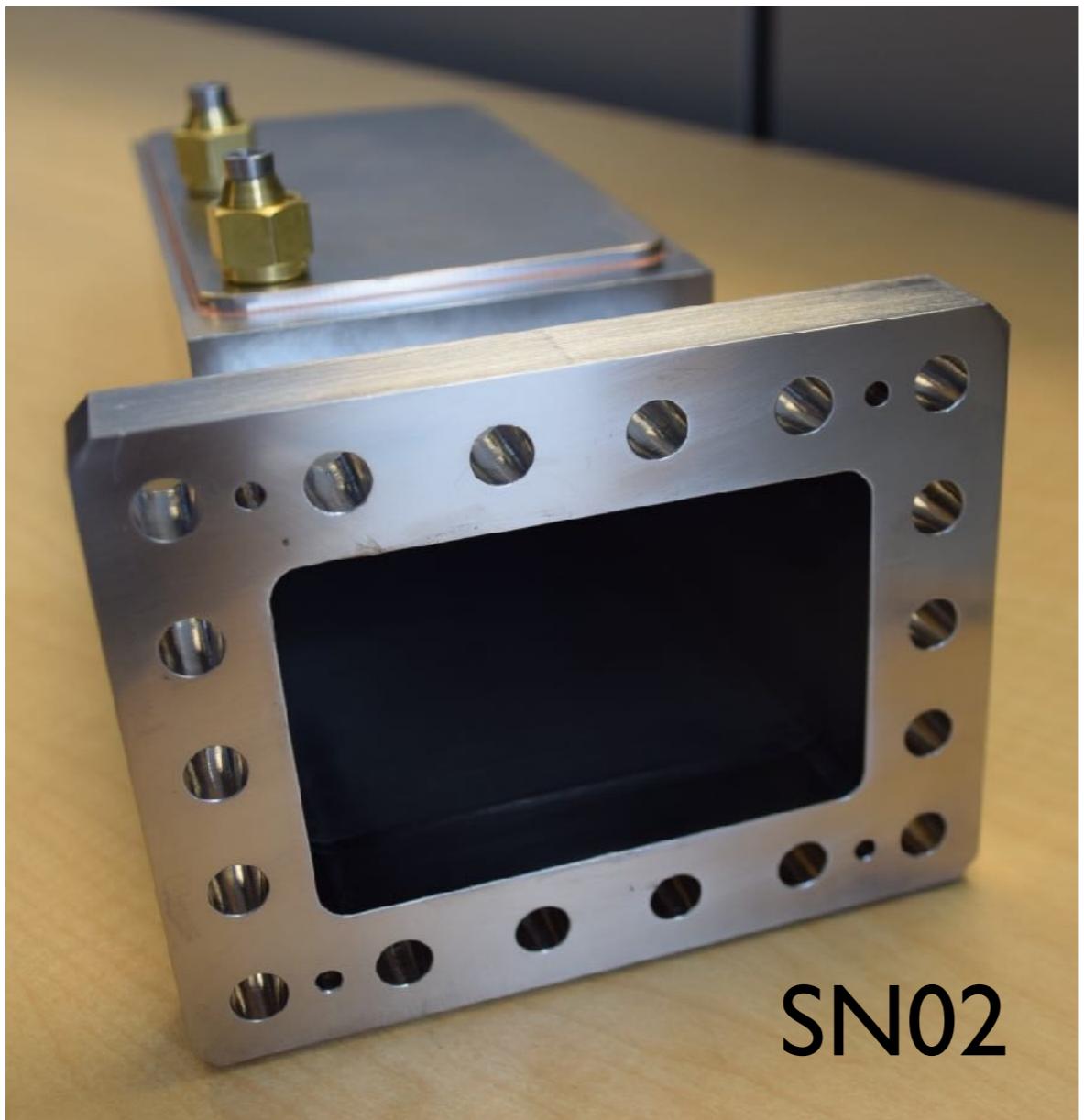
Warm absorber / waveguides

modeling, simulation, viewgraphs
courtesy Fredrik Fors, Jiquan Guo, JLab



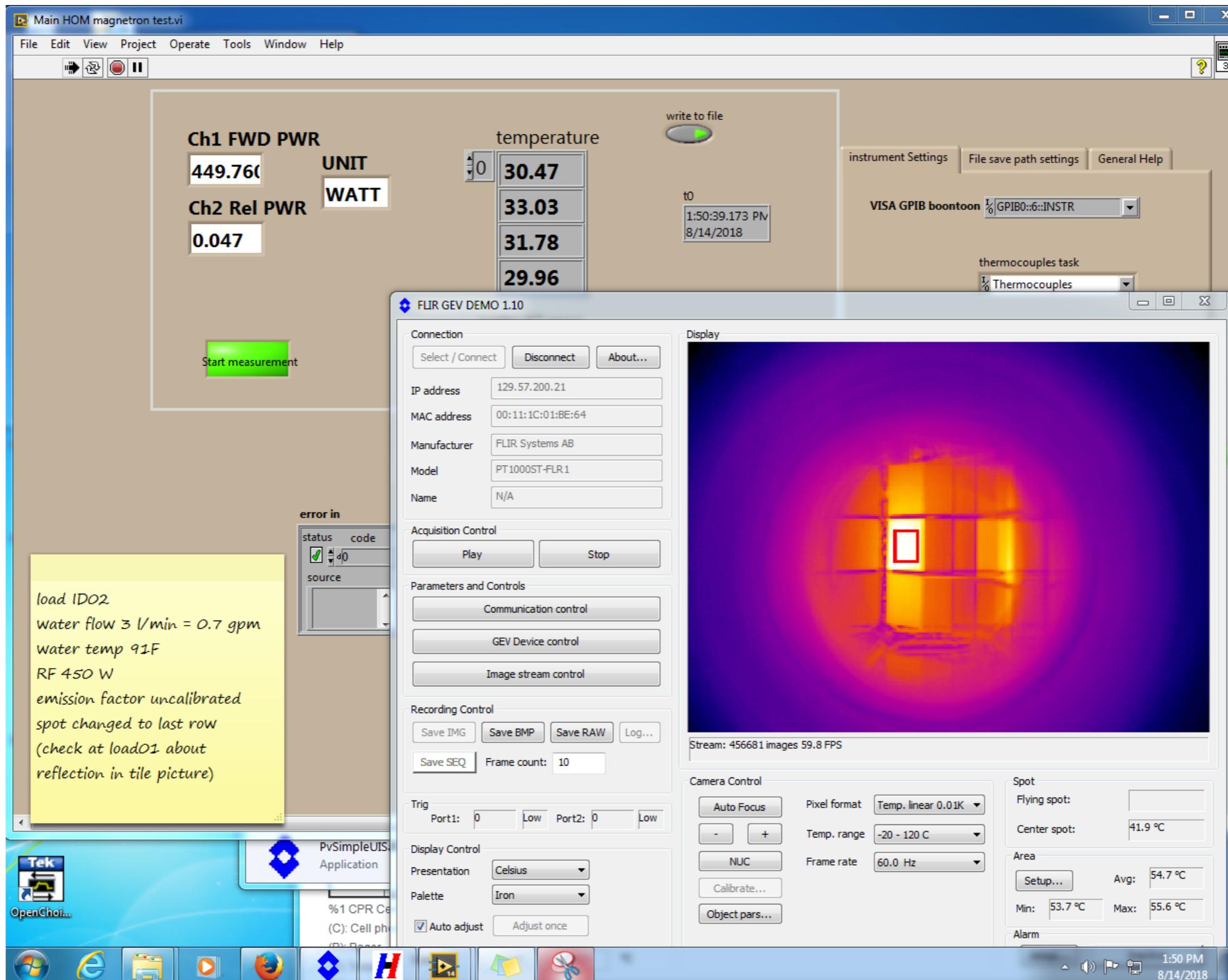
We do have

- 2 VSR load prototypes (1.5 GHz) welded (*including top, flange*)
- 1 VSR load prototypes (1.5 GHz) *not* welded



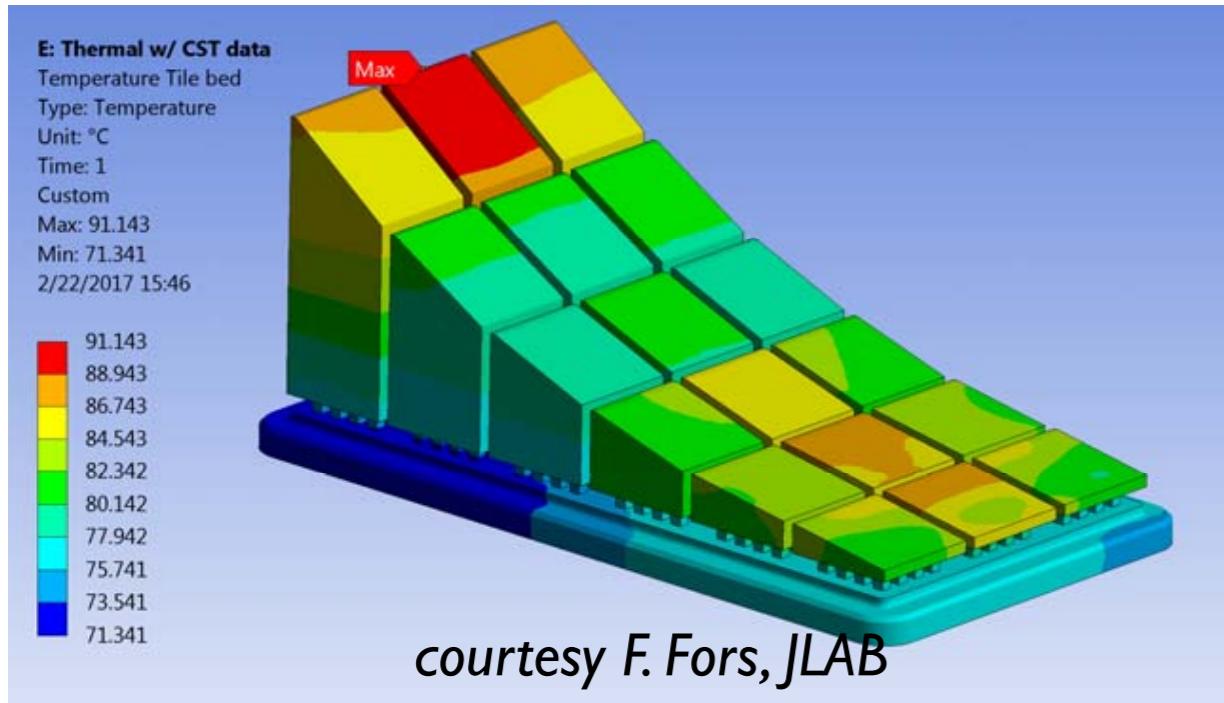
High-power RF test

– ceramic temperatures $\leq 56^\circ\text{C}$ (uncal.), water $\leq 32^\circ\text{C}$ (@ 30°C inlet, 3 L/min) @ 450 W (design)



High-power RF test

– good coincidence with simulation result (leftmost row is reflection at waveguide inner surface)

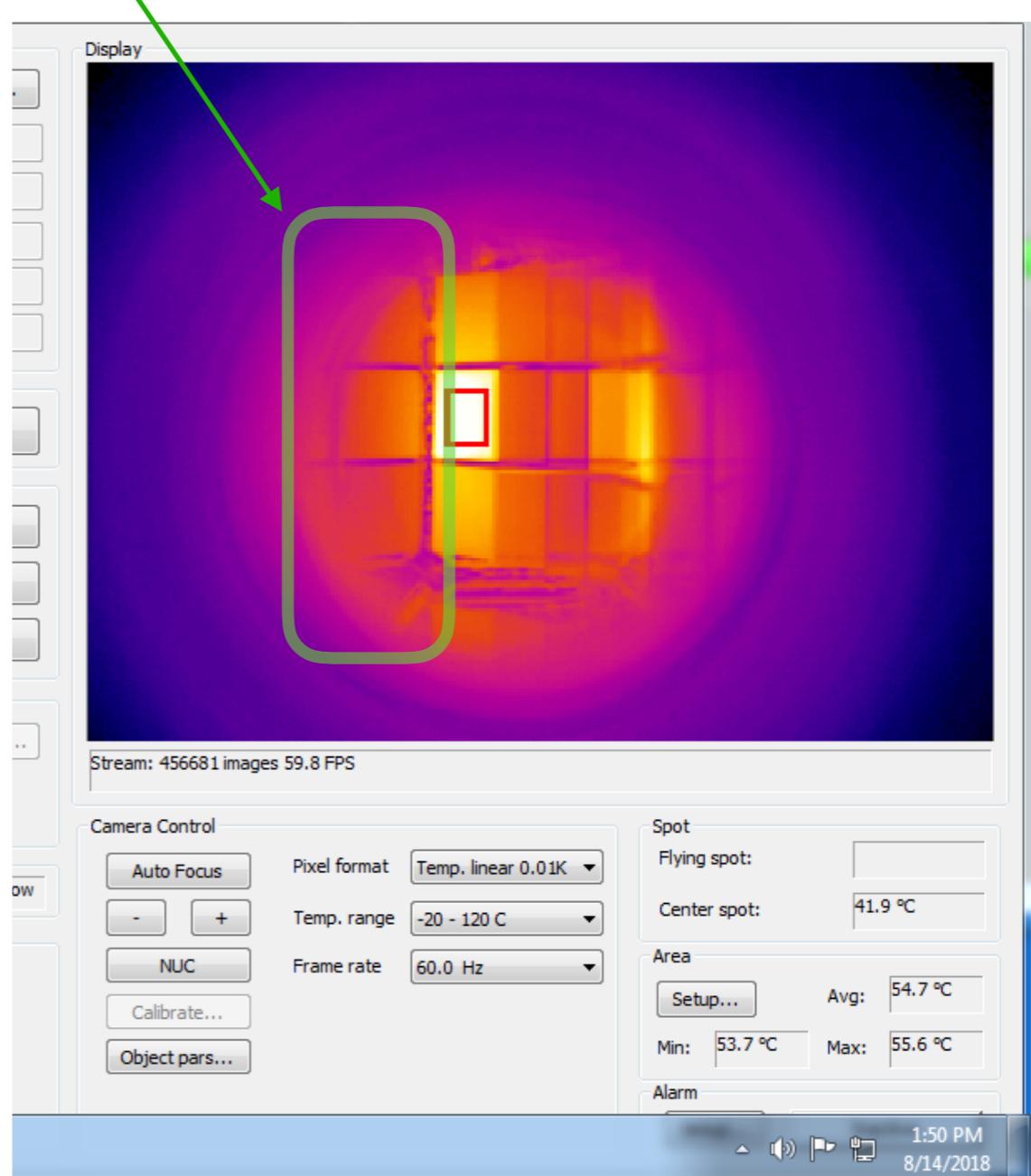


Thermal analysis results

temperature level of copper backplate
unexpectedly high @30°C cooling
water

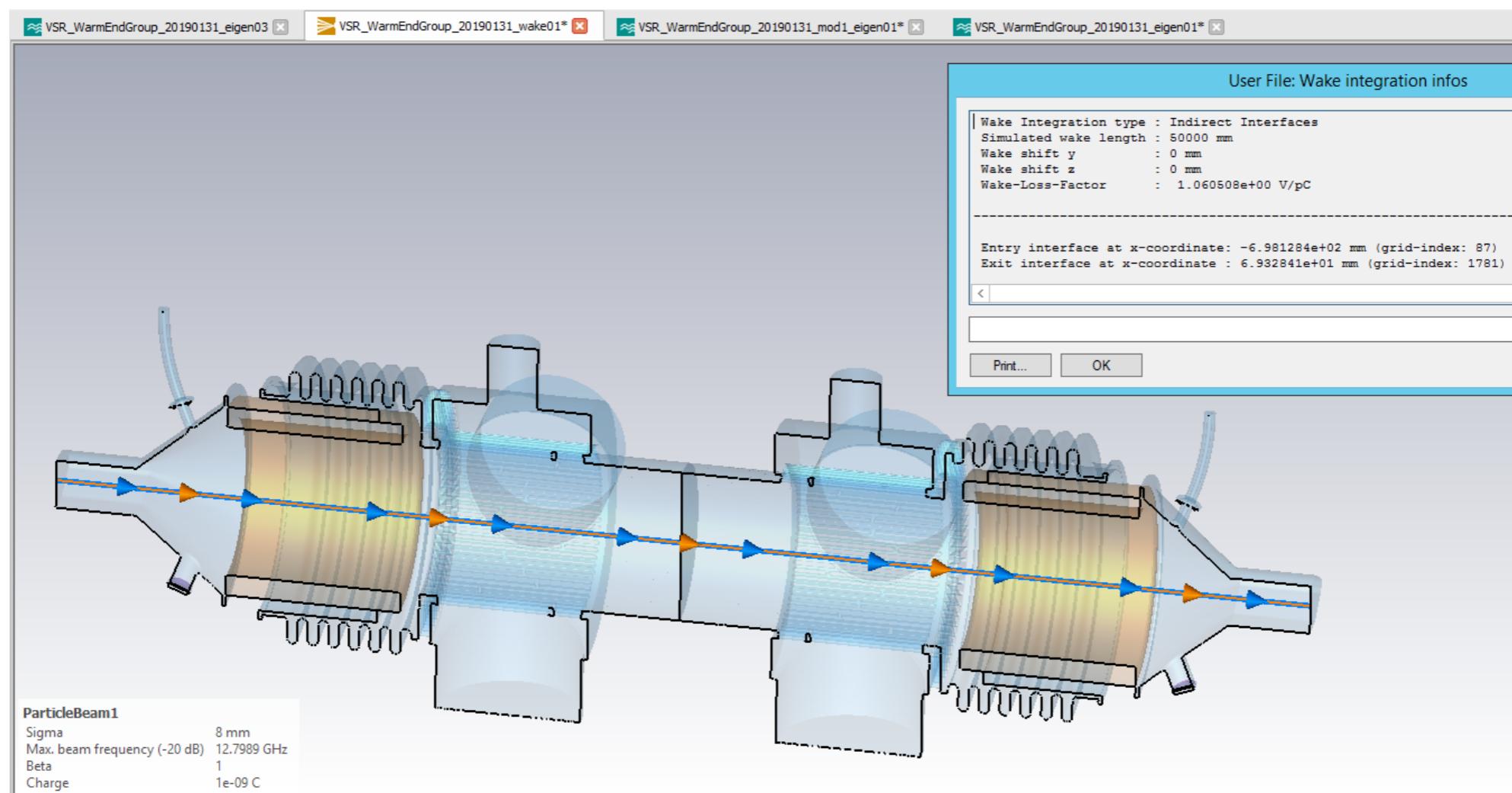
temperature gradient from backplate to
ceramic in good coincidence with
measurement

optical reflection of last row

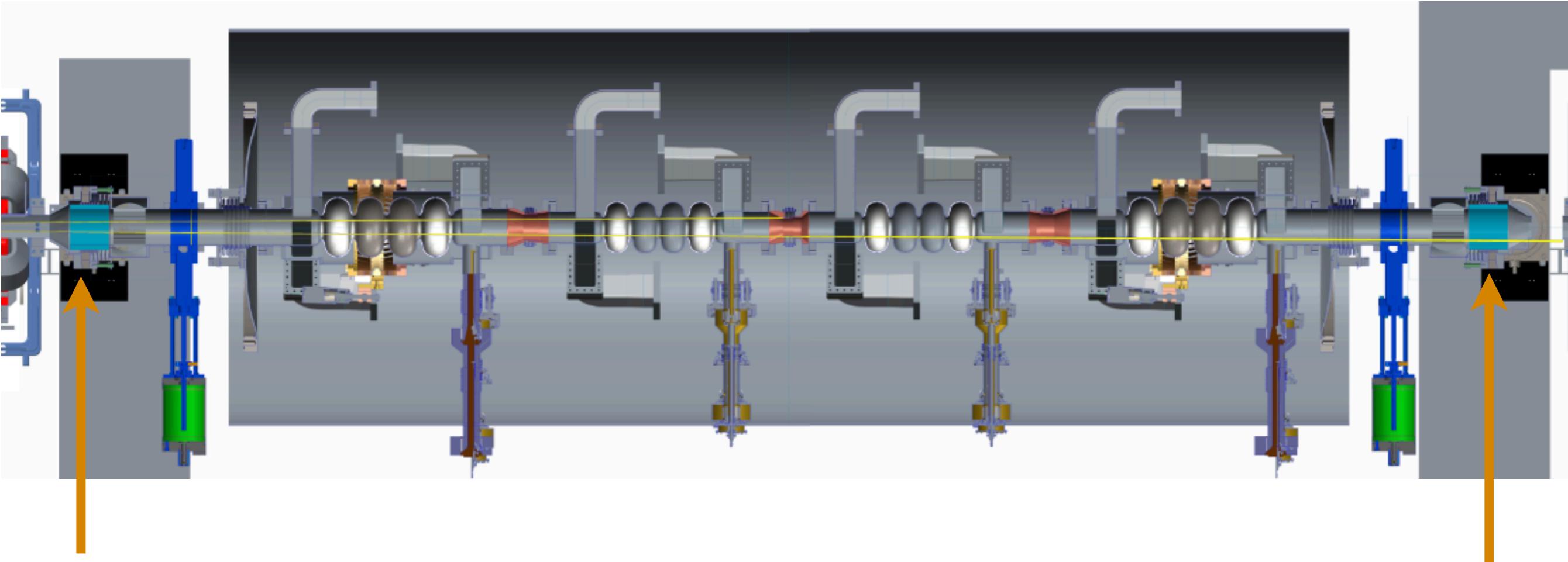


Supplement:

The Warm End Group as Example for Rescaling of Dielectric Losses



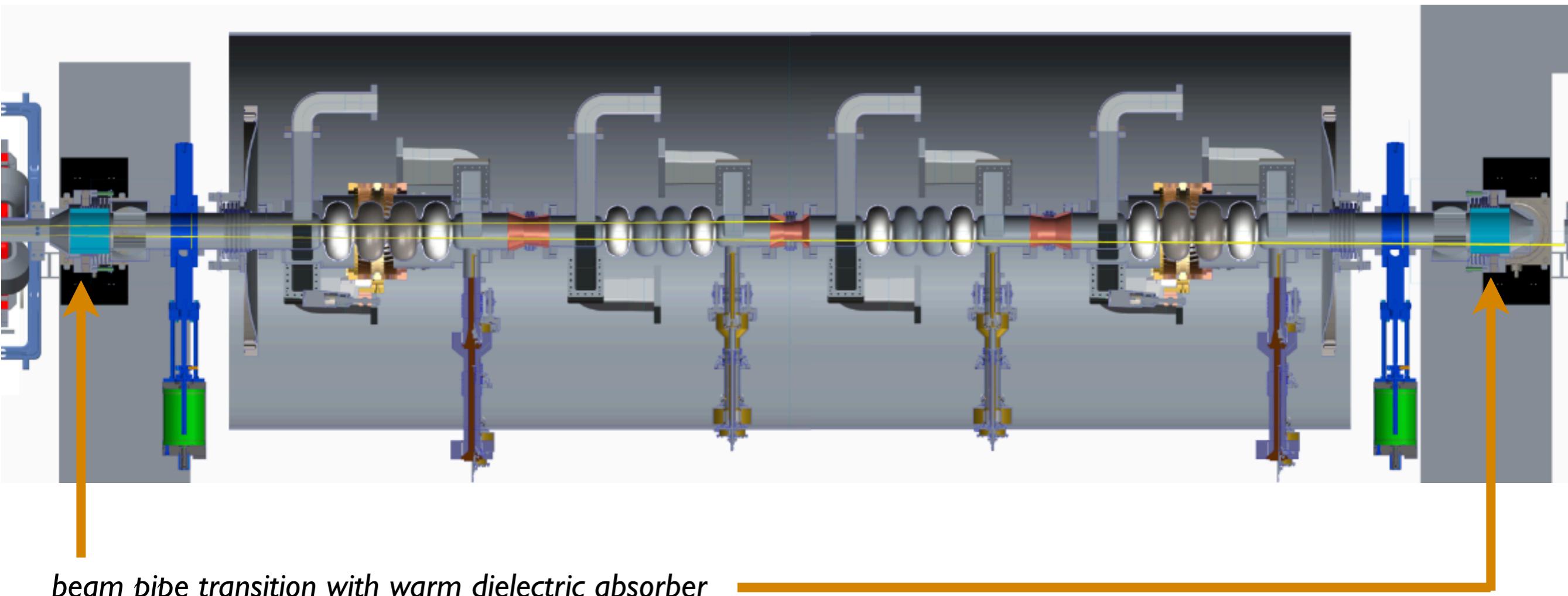
Beam pipe transitions with warm dielectric absorbers etc.



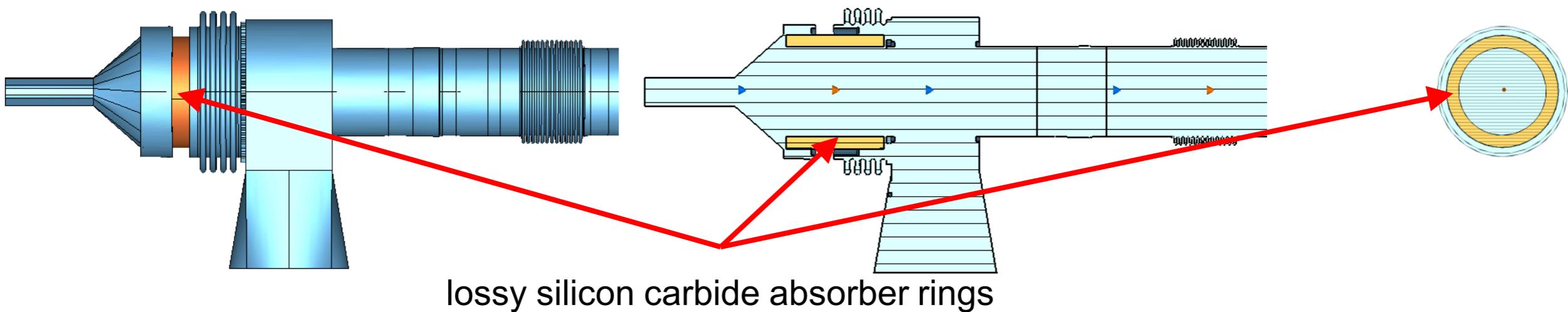
beam pipe transition with warm dielectric absorber

- space restrictions enforce step-like beam pipe cross section transitions \Rightarrow local wake power generation
- significant ($\sim 1 \dots 2$ kW) HOM power known to travel outwards the module
- further functionality: longitudinal compensation, attached getter pump dome, shutter valves (in vicinity), moveable collimator for synchrotron light (upstream only)
- use of dielectric absorbers identical to bERLinPro gun and booster devices very preferred (but water cooling applied)

Beam pipe transitions with warm dielectric absorbers (bulk dielectric available)

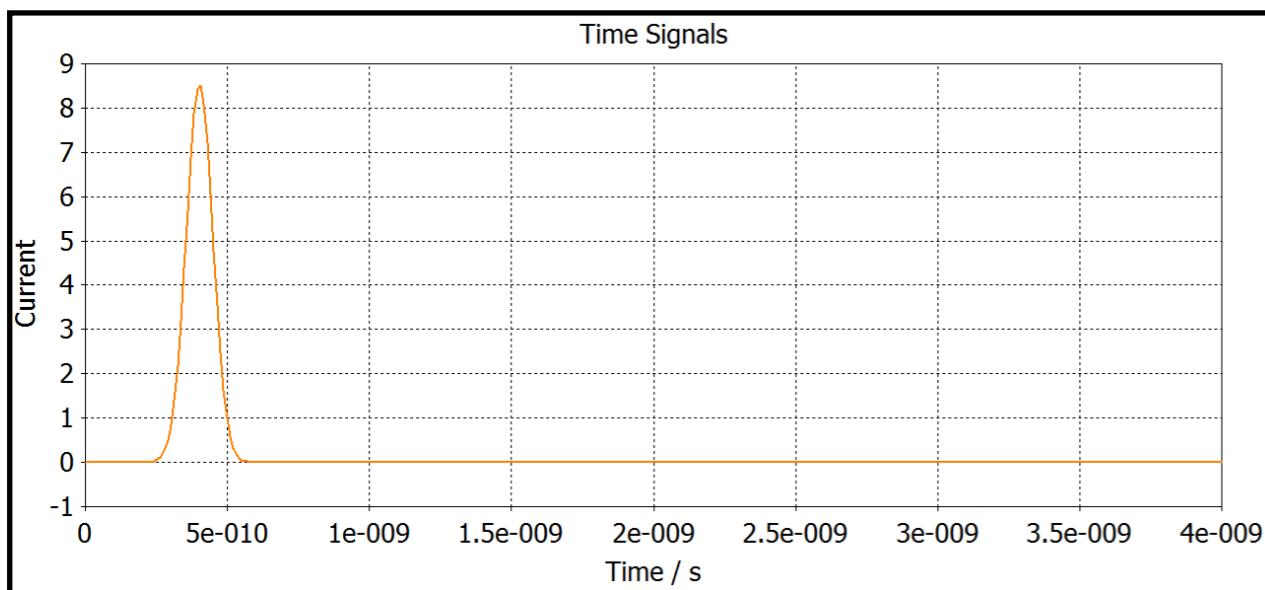
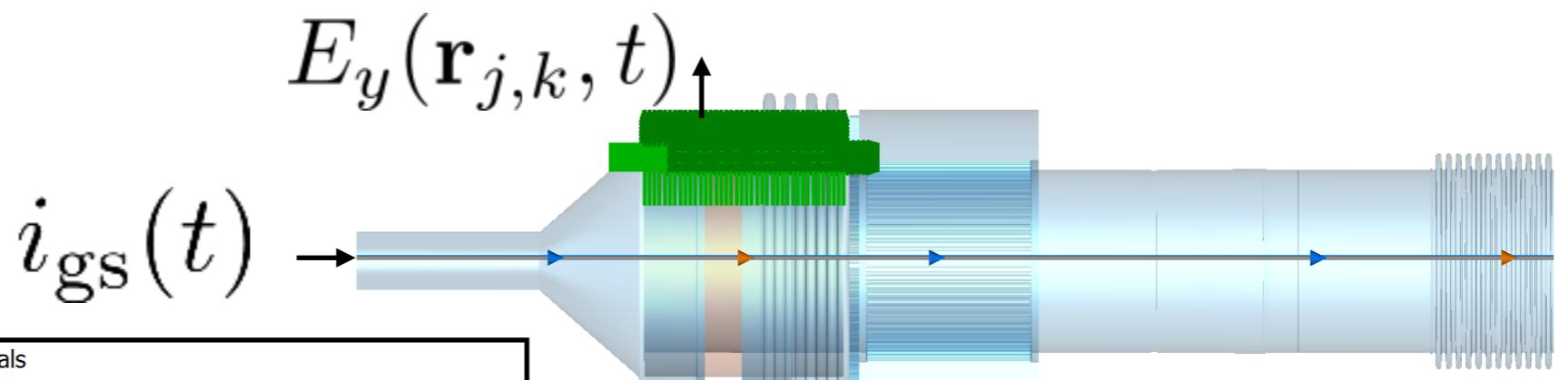
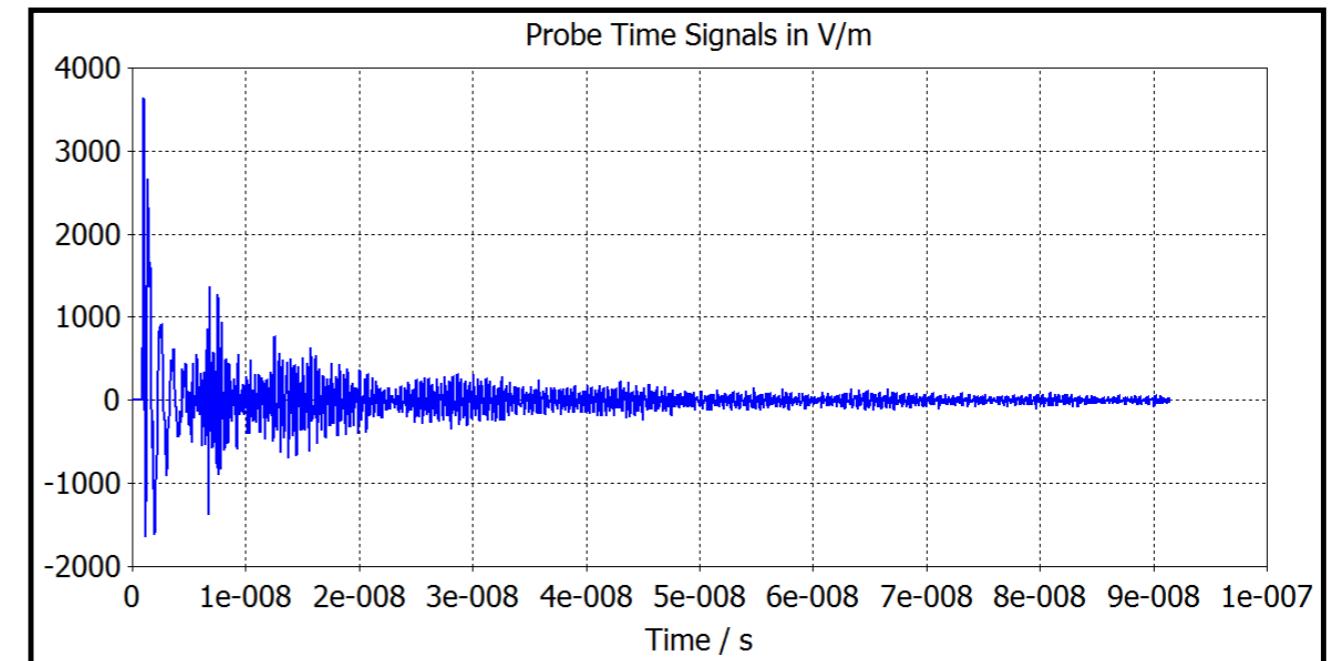


beam pipe transition with warm dielectric absorber



BROADBAND EXCITATION WITH A GAUSSIAN BUNCH

- excitation of the structure using broadband Gaussian bunch
- monitor electric field strengths arising from Gaussian bunch excitation using time domain field probes



method, results, slides courtesy of Thomas Flisgen

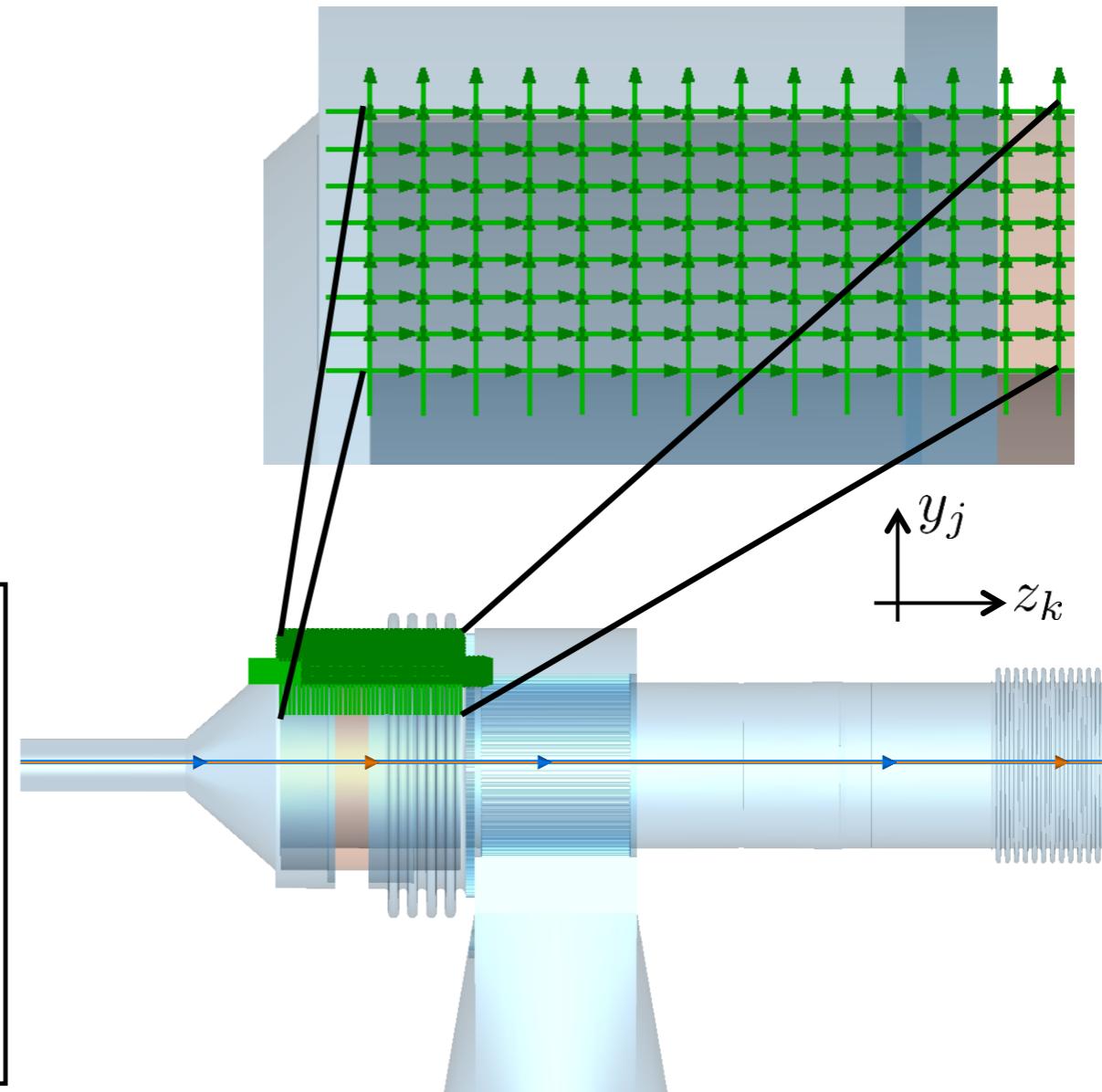
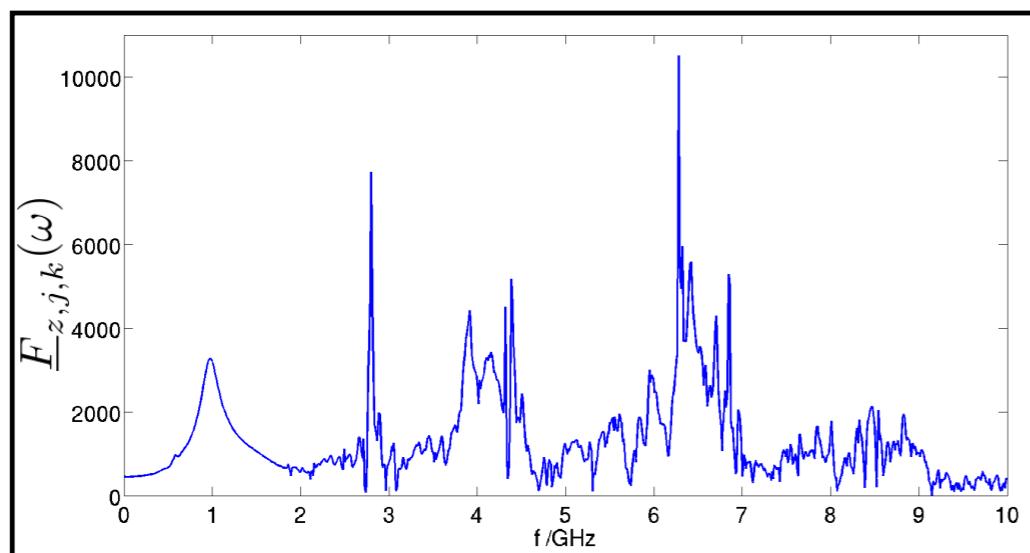


FREQUENCY DOMAIN TRANSFER FUNCTIONS

$$F_{x,j,k}(\omega_n) = \frac{\text{FFT}[E_x(\mathbf{r}_{j,k}, t)]}{\text{FFT}[i_{\text{gs}}(t)]}$$

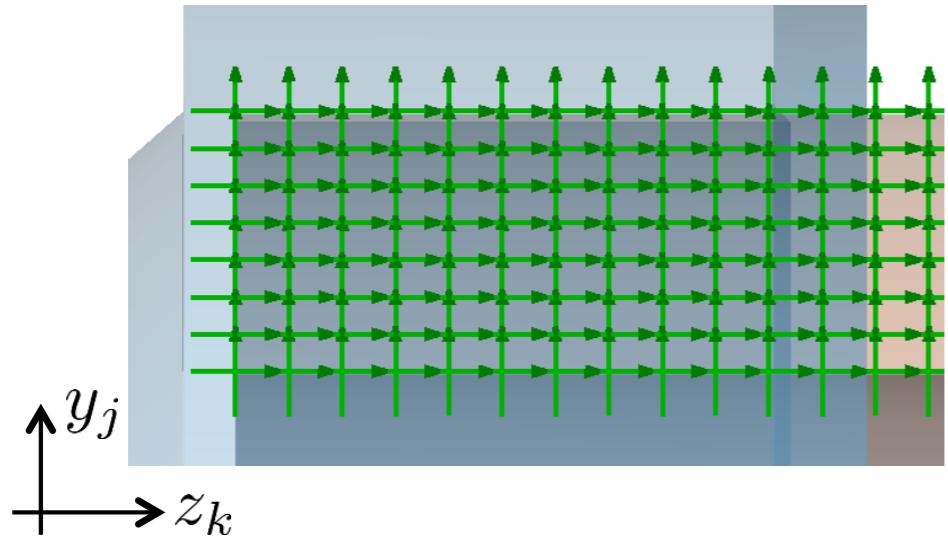
$$F_{y,j,k}(\omega_n) = \frac{\text{FFT}[E_y(\mathbf{r}_{j,k}, t)]}{\text{FFT}[i_{\text{gs}}(t)]}$$

$$F_{z,j,k}(\omega_n) = \frac{\text{FFT}[E_z(\mathbf{r}_{j,k}, t)]}{\text{FFT}[i_{\text{gs}}(t)]}$$



transfer function(s) translate(s) beam current into field components

ELECTRIC FIELDS ARISING FROM THE BESSY VSR FILLING PATTERN



Evaluation of the electric field strengths at the locations of the field probes by means of:

$$\underline{\mathbf{E}}_n(\mathbf{r}_{j,k}) = \begin{pmatrix} \underline{F}_{x,j,k}(\omega_n) \\ \underline{F}_{y,j,k}(\omega_n) \\ \underline{F}_{z,j,k}(\omega_n) \end{pmatrix} I_{\text{vsr}}(\omega_n)$$

Approximation of the volume integrals by surface integrals assuming rotational symmetry:

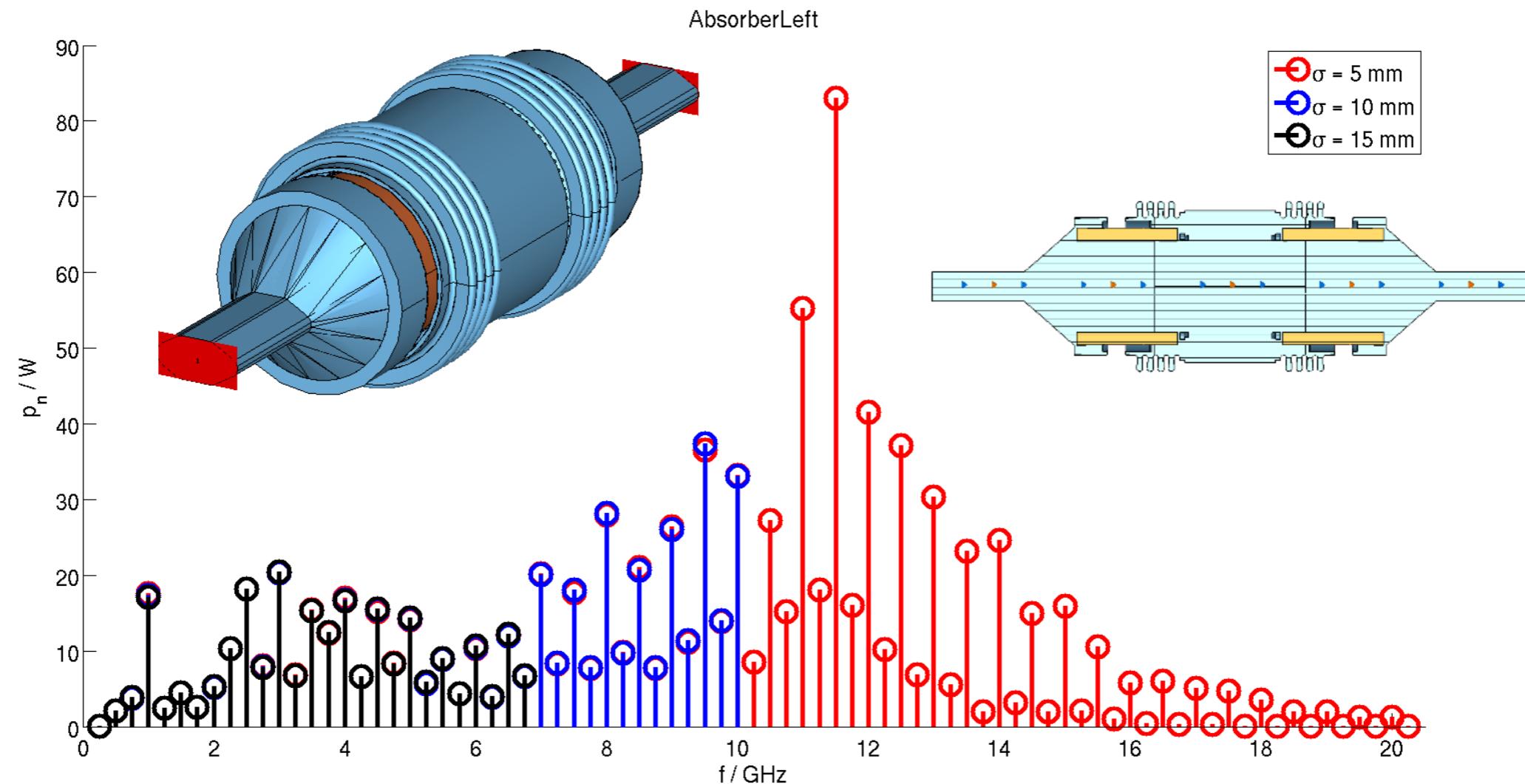
$$p_n = \iiint_{\Omega_{\text{abs}}} \frac{1}{2} \omega_n \varepsilon''(\omega_n) |\underline{\mathbf{E}}_n(\mathbf{r})|^2 dV$$

$$= \pi \int_{y_{\min}}^{y_{\max}} \int_{z_{\min}}^{z_{\max}} r \omega_n \varepsilon''(\omega_n) |\underline{\mathbf{E}}_n(\mathbf{r})|^2 dy dz$$

final determination of the 2D integrals using trapezoidal rule.

approximation for spectral- and spatial-distributed dielectric wake loss for periodic beams

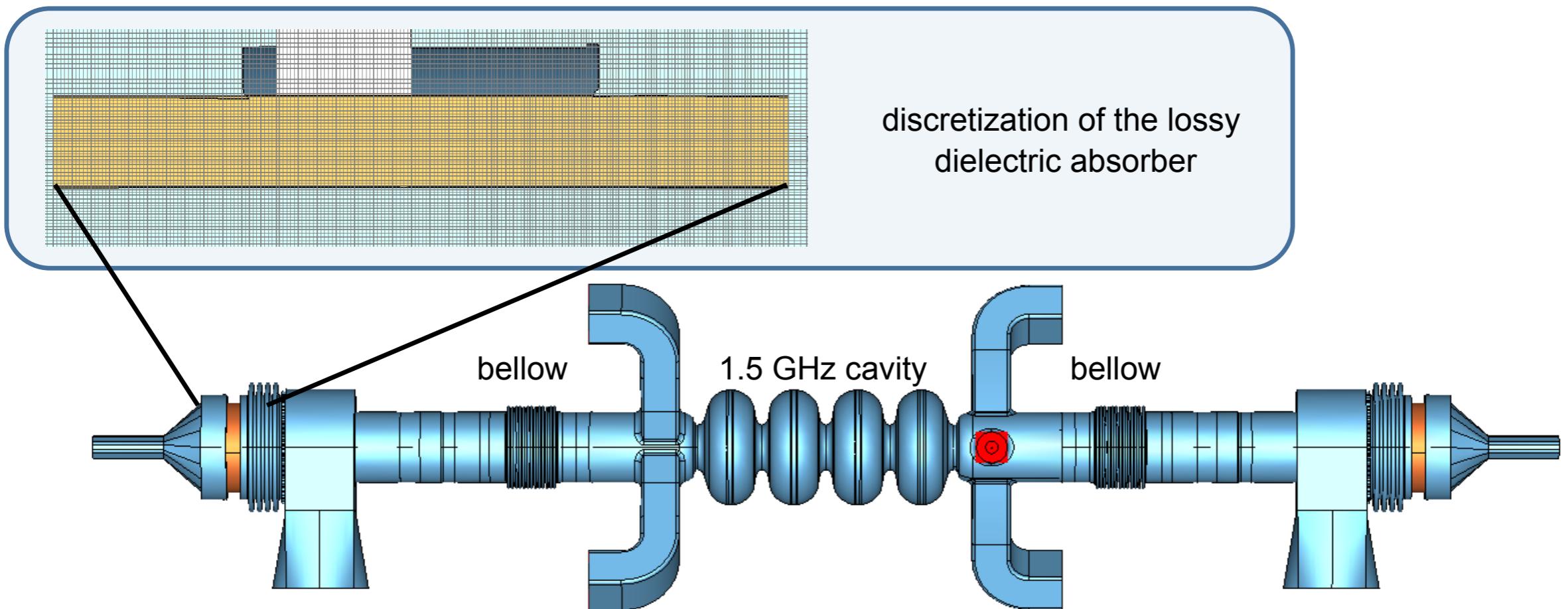
TEST STRUCTURE TO INVESTIGATE LOSSES AT HIGHER FREQUENCIES



Filling Pattern	Power Left Absorber $\sigma = 15 \text{ mm} / 10 \text{ mm} / 5 \text{ mm}$			Power Right Absorber $\sigma = 15 \text{ mm} / 10 \text{ mm} / 5 \text{ mm}$		
VSR Baseline	282 W	549 W	1064 W	446 W	861 W	1353 W

simulations should reach at least 15 GHz, better 20 GHz, but ...

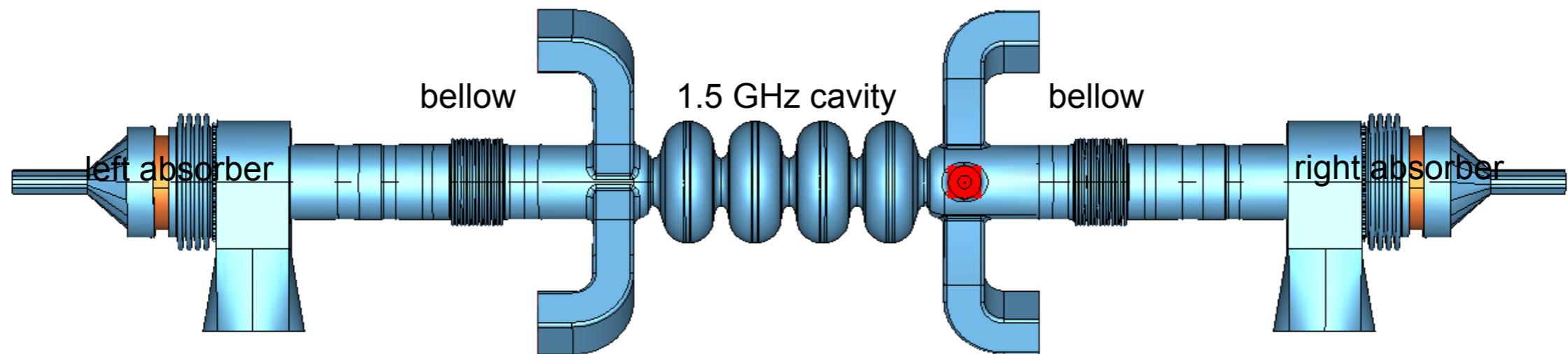
DIELECTRIC LOSSES IN SIMPLIFIED “STRING”



	σ / mm	f_{\max} / GHz	N_{mesh}	T_{comp}
Model 1	14	7.3136	426,809,958	2 d 20 h 12 min
Model 2	10	10.2391	1,075,099,752	7 d 3 h 11 min

- 112 2D port modes
- 320 field probes for E_x , E_y , and E_z per beam pipe absorber
- transversal offset of the bunch $\Delta x = \Delta y = 2.1 \text{ mm}$

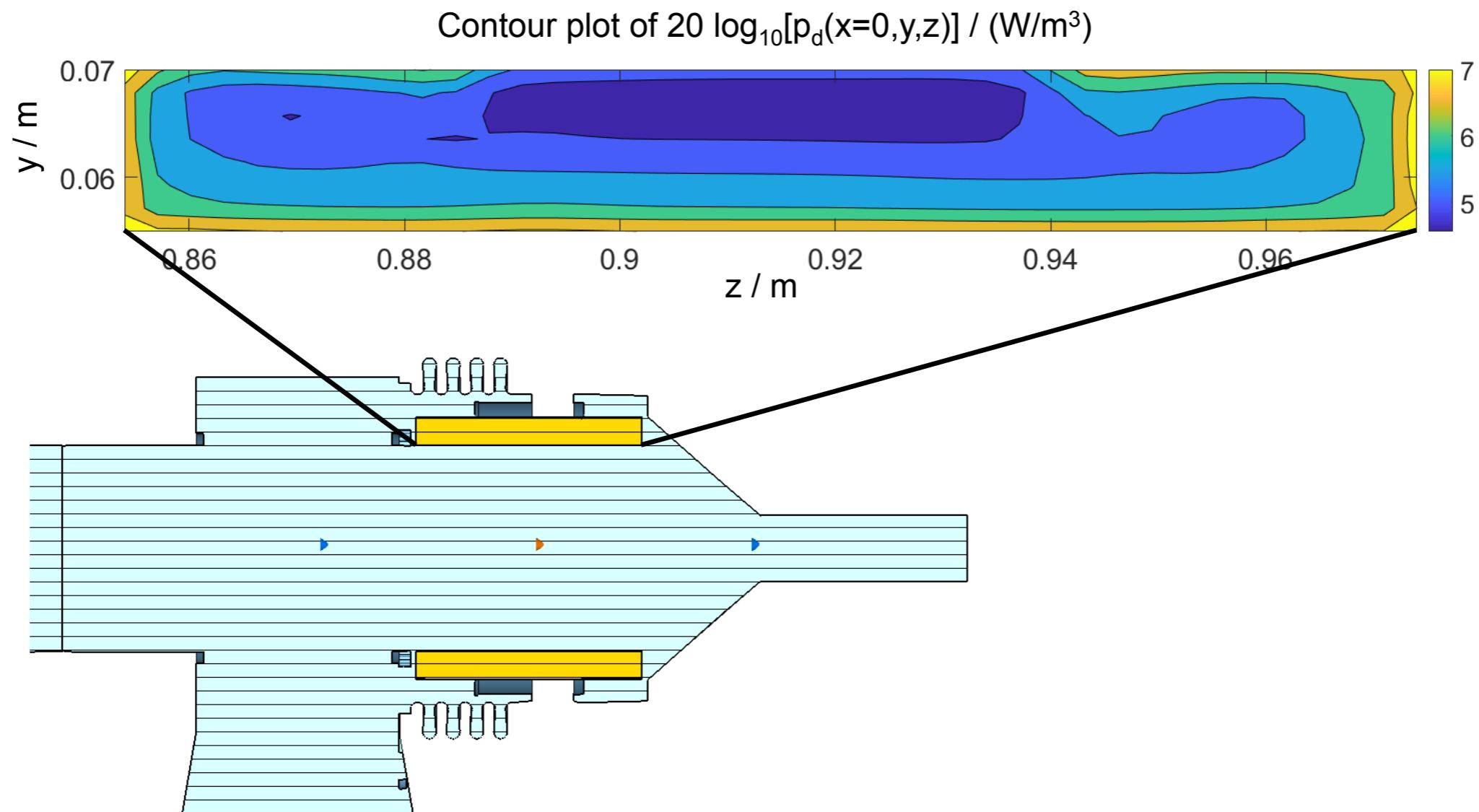
RESULTS DIELECTRIC LOSSES IN SIMPLIFIED “STRING”



Filling Pattern	Power Left Absorber	Power Right Absorber
baseline	801 W	1371 W
extended	716 W	1250 W

- losses are in the expected order ☺ but depend heavily on the considered frequency range ☹
- losses arising from baseline fill pattern are slightly higher than from extended pattern
- losses in the right absorber are ≈ 1.7 times higher than in the left absorber

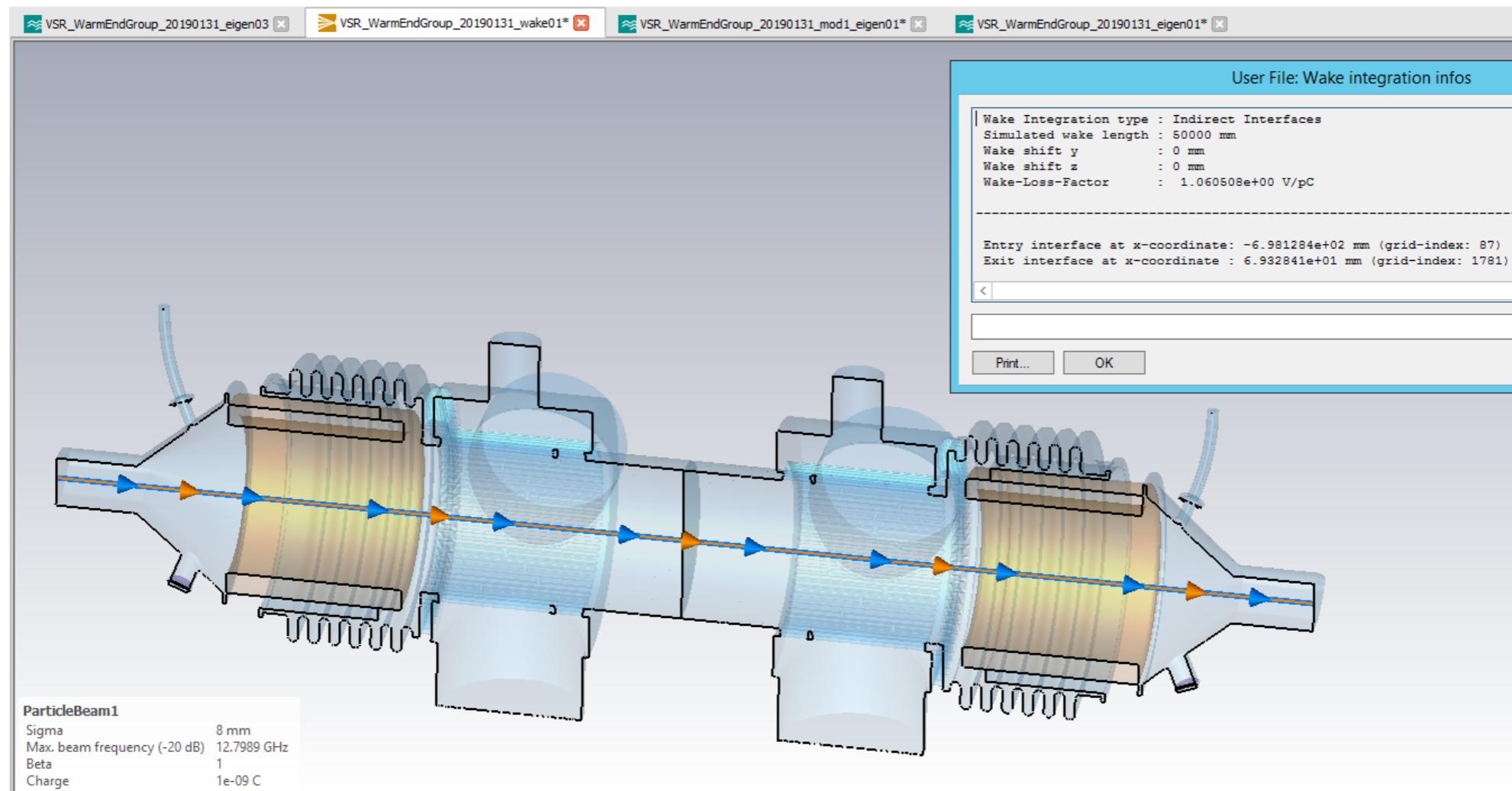
POWER DENSITY DISTRIBUTION RIGHT ABSORBER RING FROM MODEL 6



*dissipation strongly concentrated close to surface; stress ??
with contingency, we expect 2 kW per absorber*

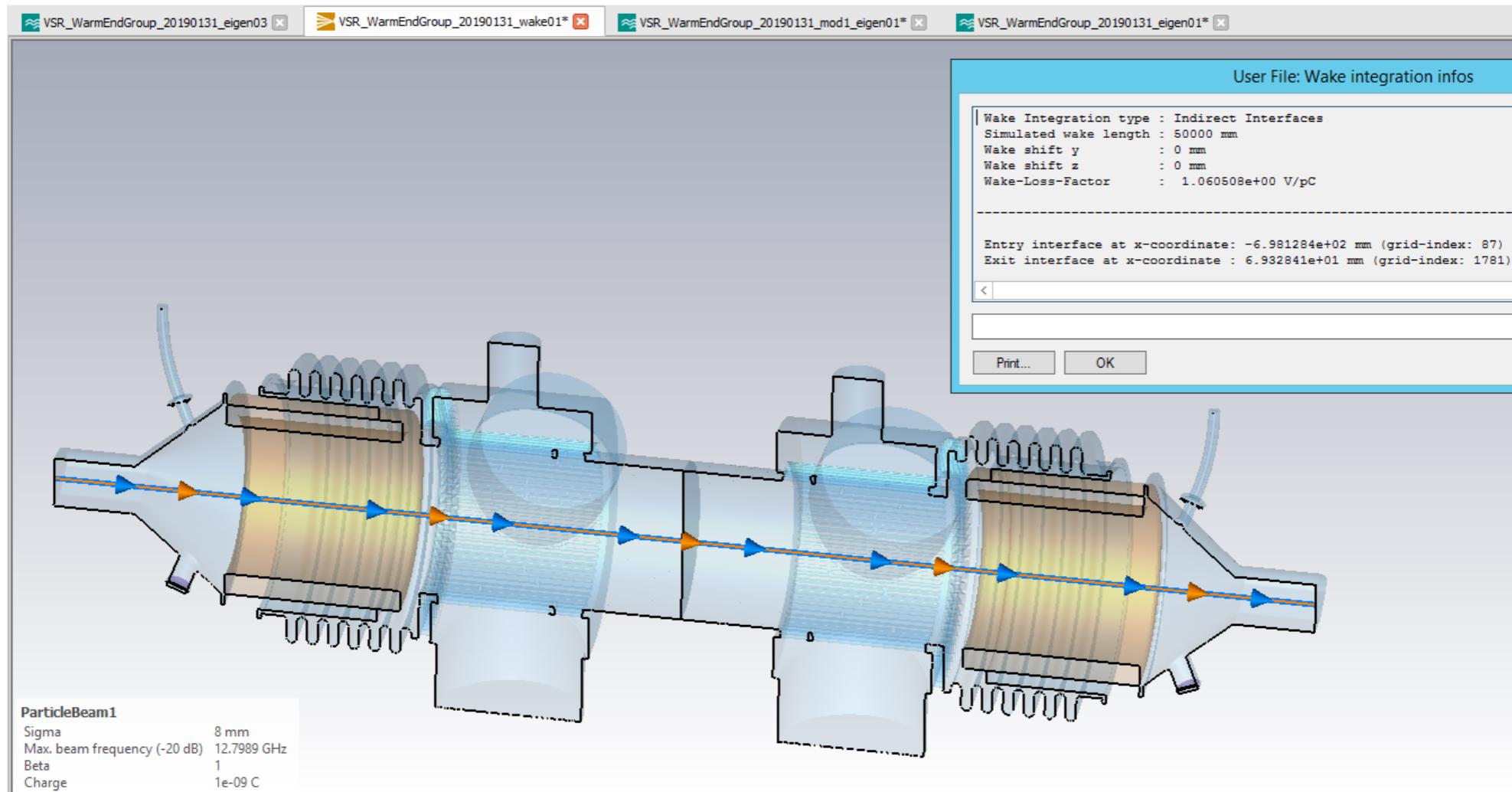
Supplement:

Redesign of the Warm End Group based on wake and eigenmode simulations



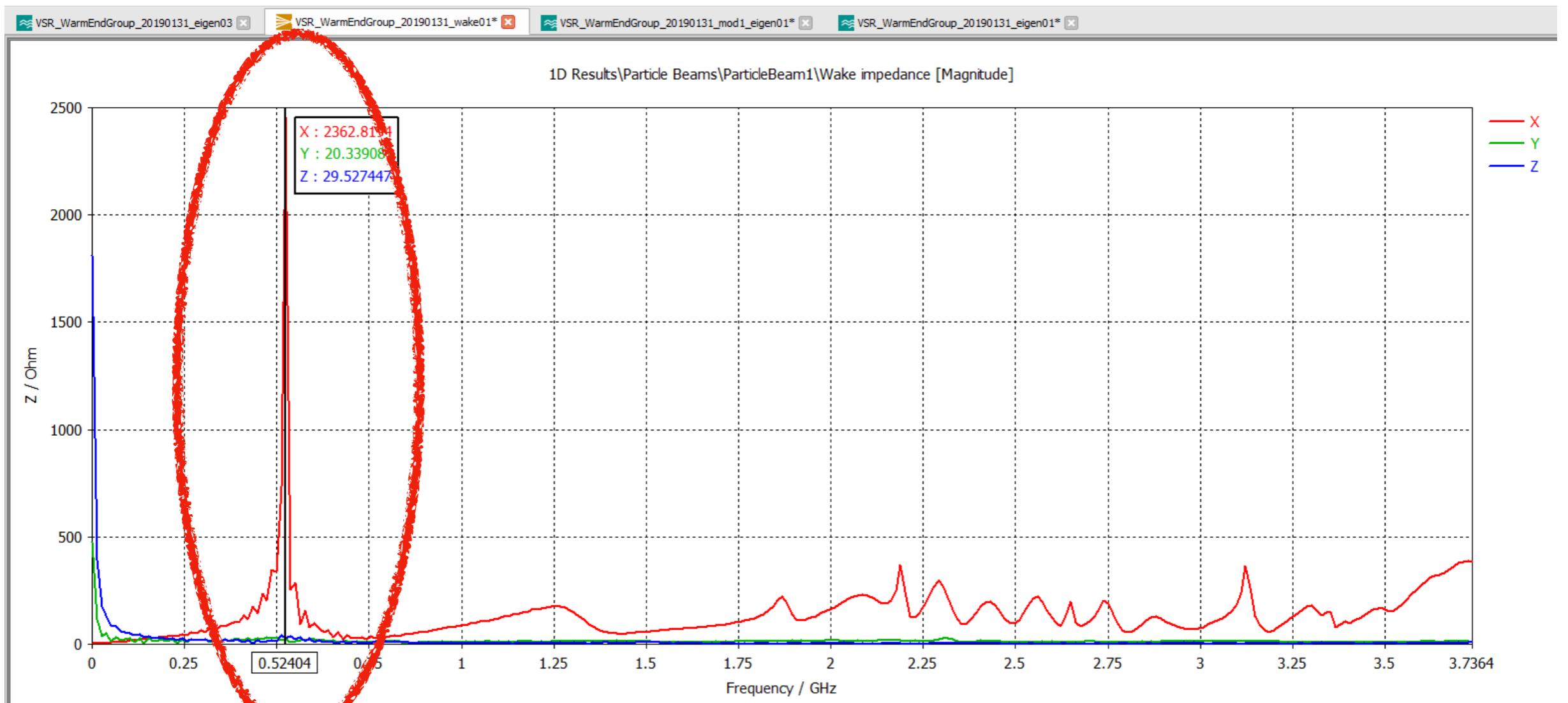
Warm end group (without additional synchrotron light collimator)

- engineered (NW) with several modifications: 3 + 1 pumping ports, increased gap and compensation capabilities for mounting, “decoherent“ slots, IR monitoring window, RF pick-up, etc..
- check-up wake run revealed dangerous resonance very close 500 MHz, ...
- ..., which needs to be avoided, options under numerical evaluation



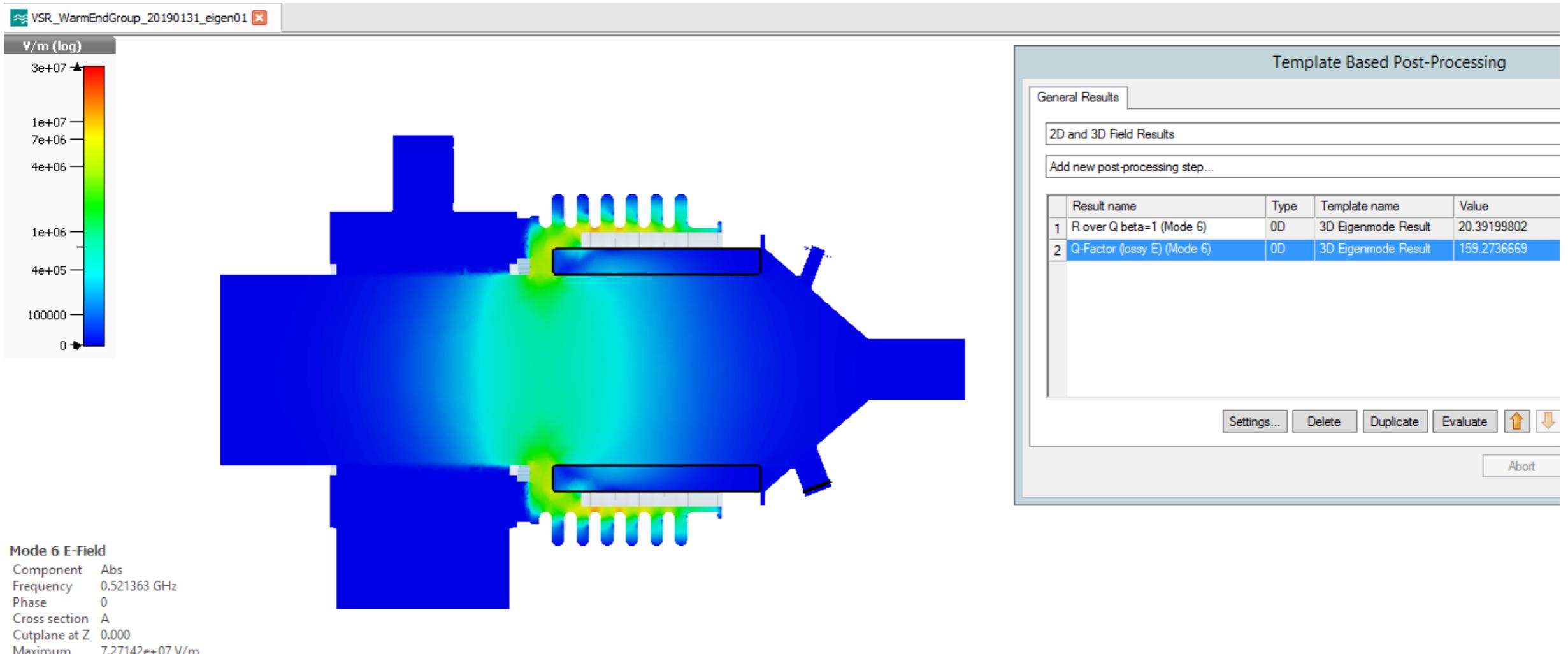
Warm end group

– check-up wake run revealed dangerous resonance very close 500 MHz, ...



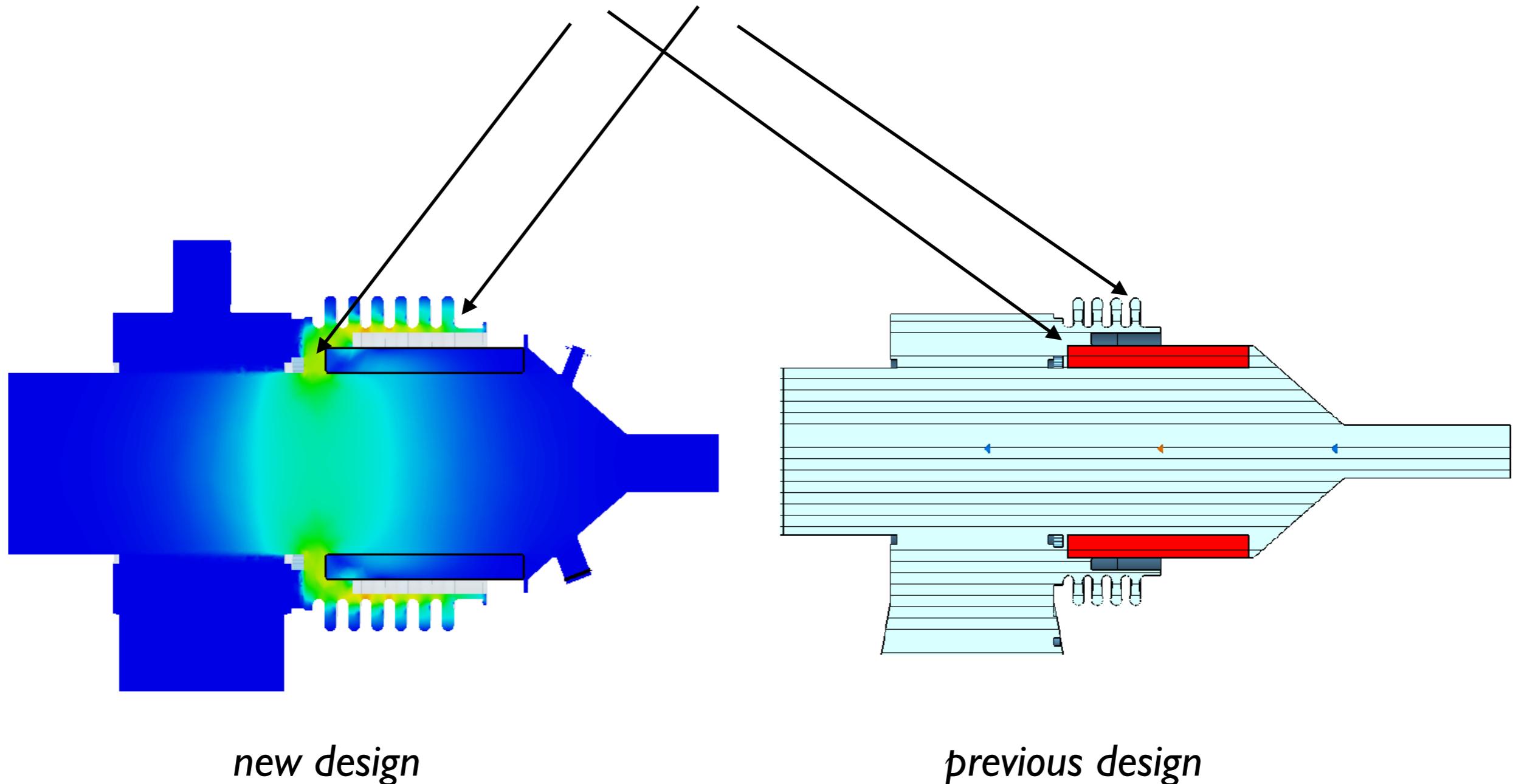
Warm end group

- check-up wake run revealed dangerous resonance very close 500 MHz, ...
- confirmed by eigenmode run: 521 MHz, $R/Q = 20.4 \Omega$, $Q = 159$



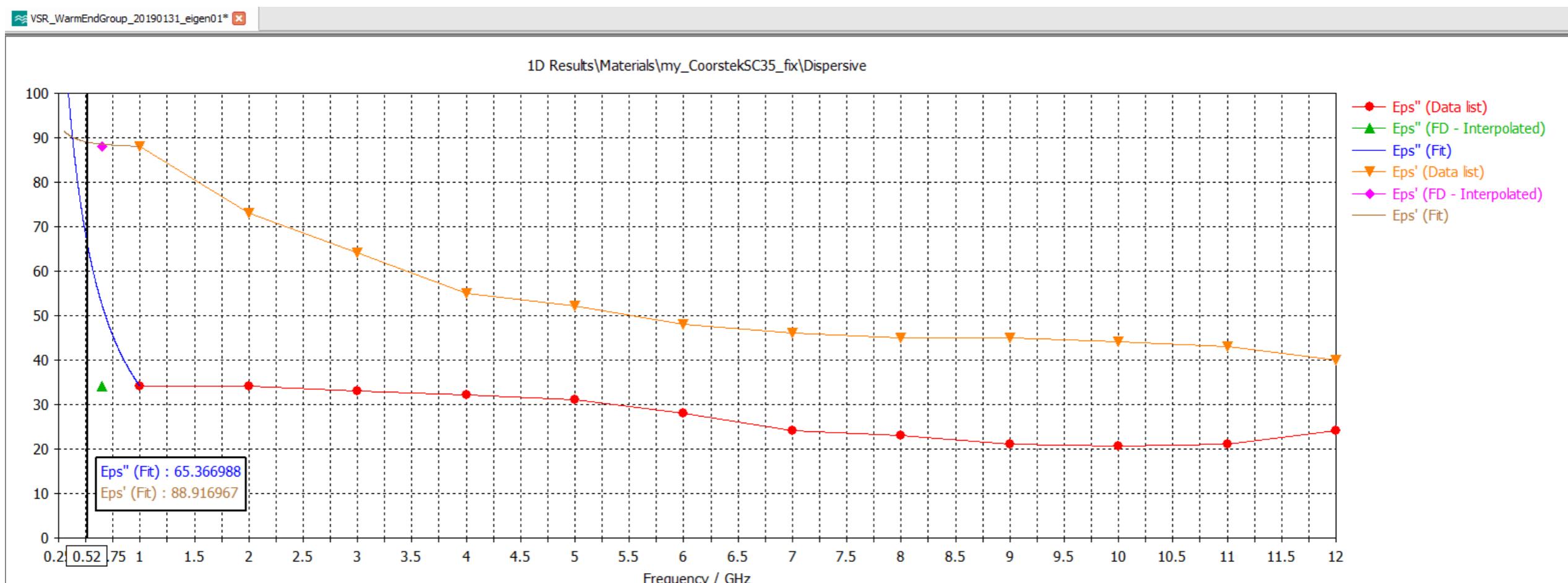
Warm end group – what made the difference ?

bigger gap, longer bellow



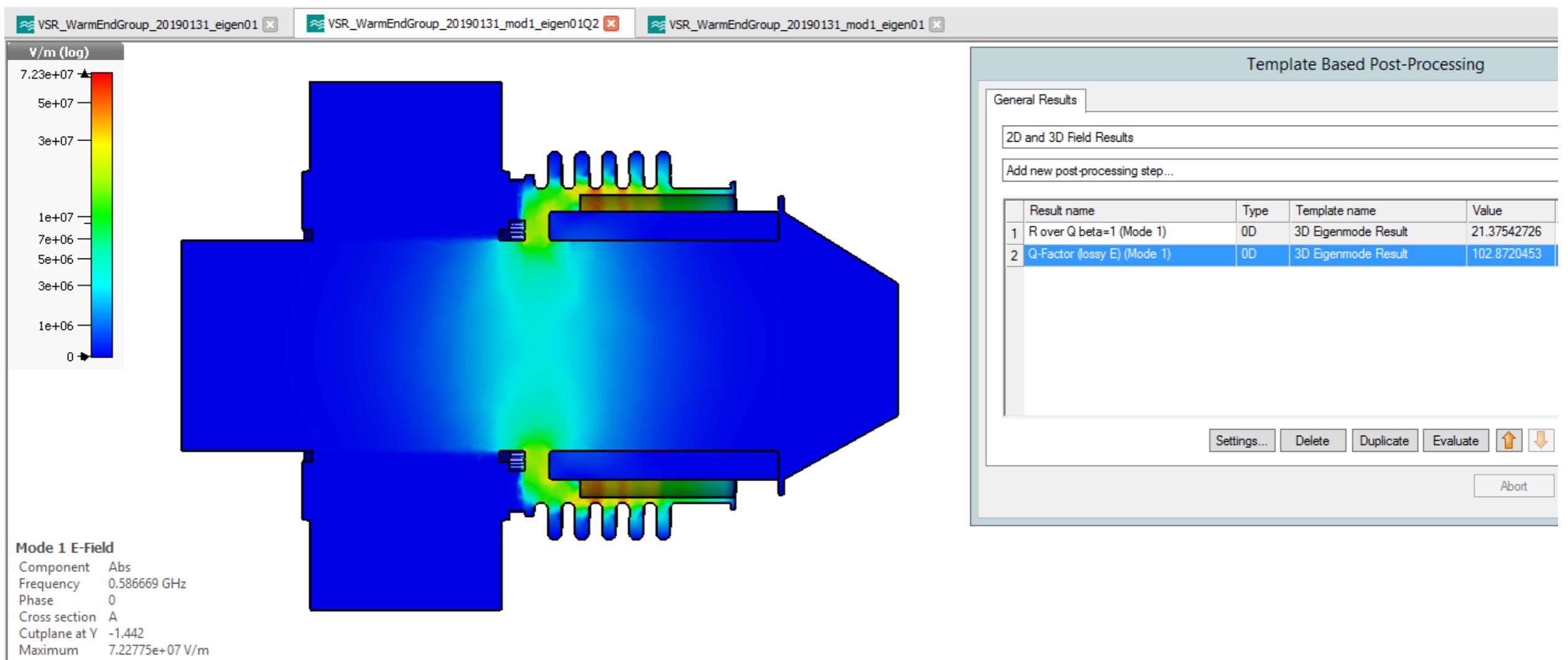
Warm end group

- check-up wake run revealed dangerous resonance very close 500 MHz, ...
- confirmed by eigenmode run: 521 MHz, $R/Q = 20.4 \Omega$, $Q = 159$
- but: dielectric material parameters (cf. Eichhorn priv.com.) may vary



Warm end group

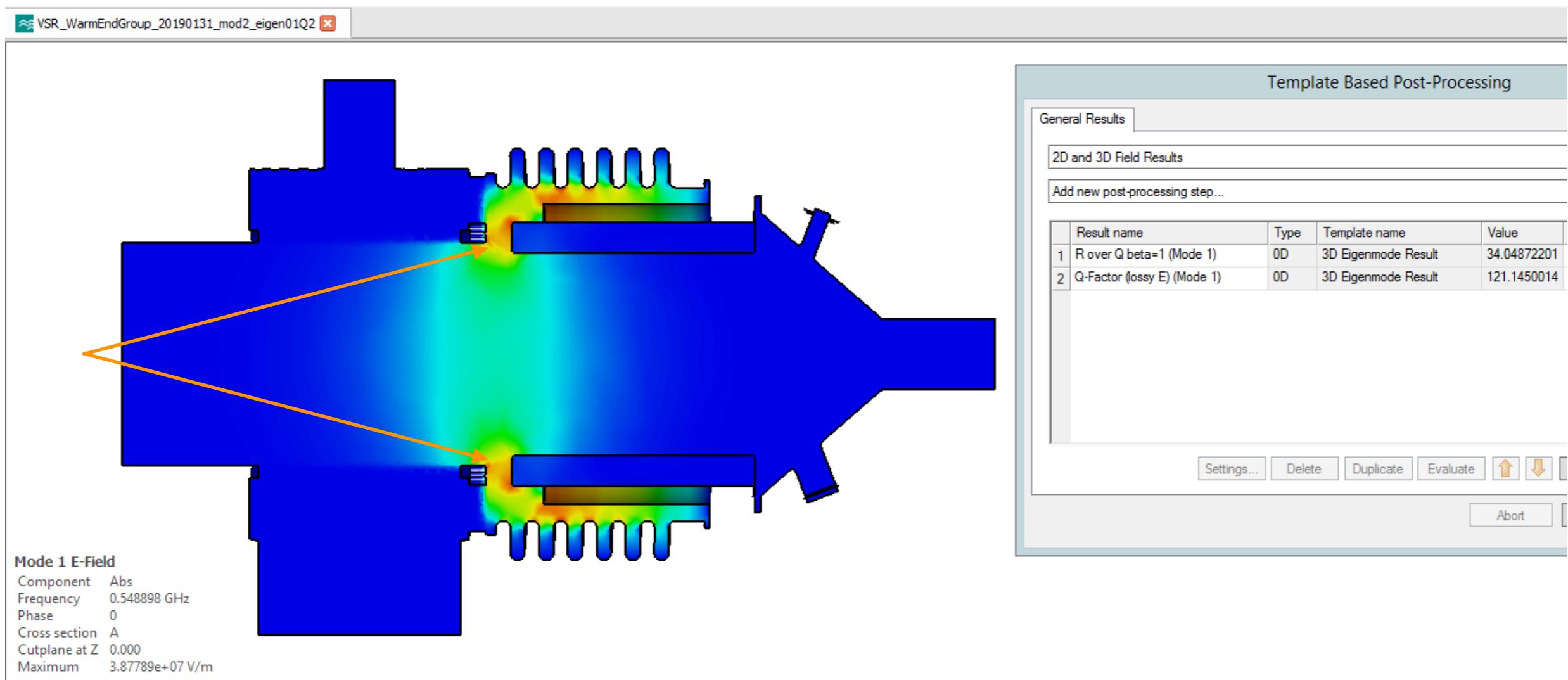
- check-up wake run revealed dangerous resonance very close 500 MHz, ...
- ..., which needs to be avoided, options under numerical evaluation
- Mod 1: one less convolution: 587 MHz, 21.3Ω , $Q = 103$, $E_{peak@IJ} 7.2 \text{ MV/m}$



Warm end group

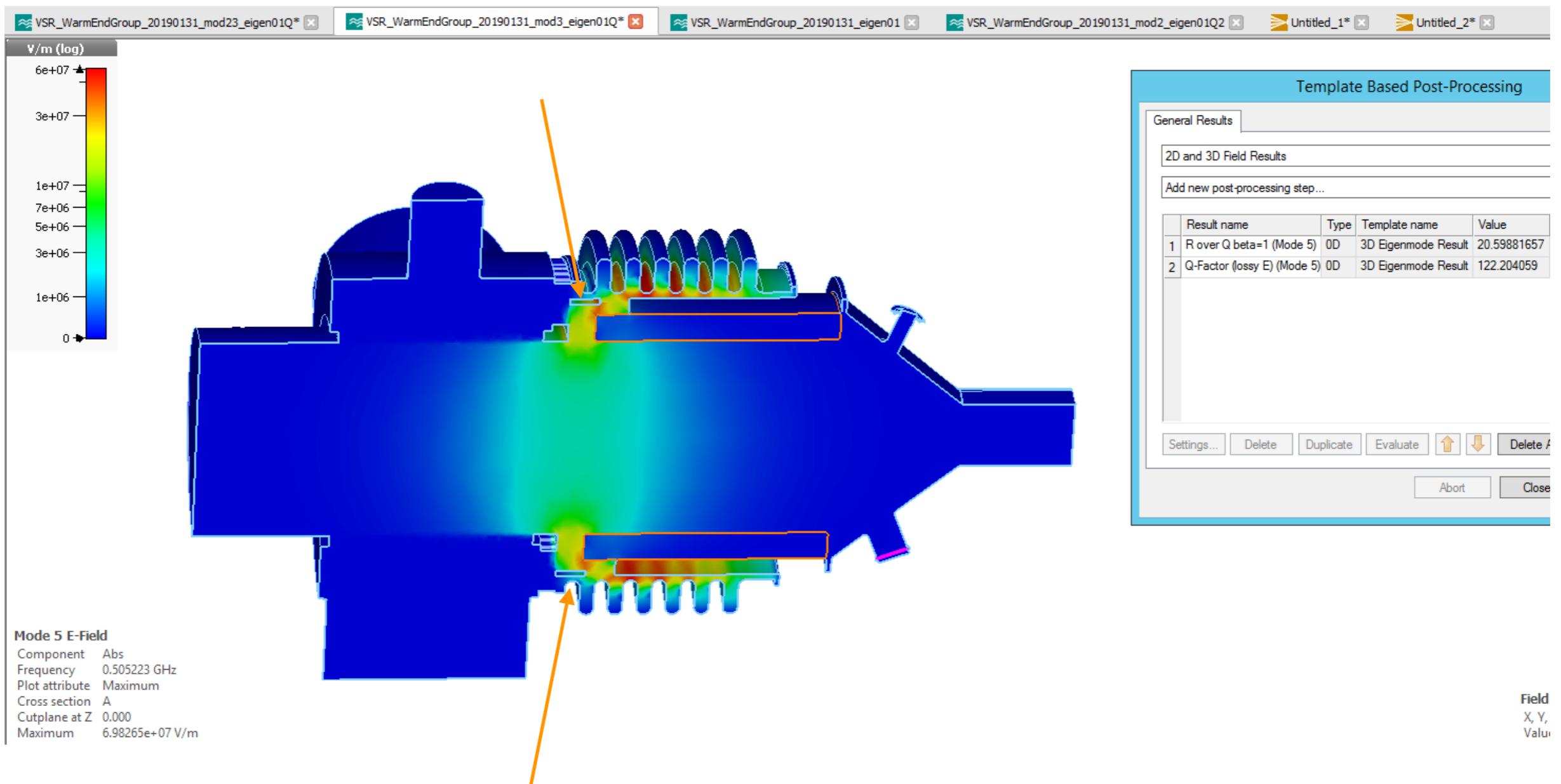
- check-up wake run revealed dangerous resonance very close 500 MHz, ...
- ..., which needs to be avoided, options under numerical evaluation
- Mod 2: reduce diameter of toroid and jacket by 10 mm: 549 MHz,

$$R/Q = 34 \Omega, Q = 121, E_{\text{peak@IJ}} 3.9 \text{ MV/m}$$



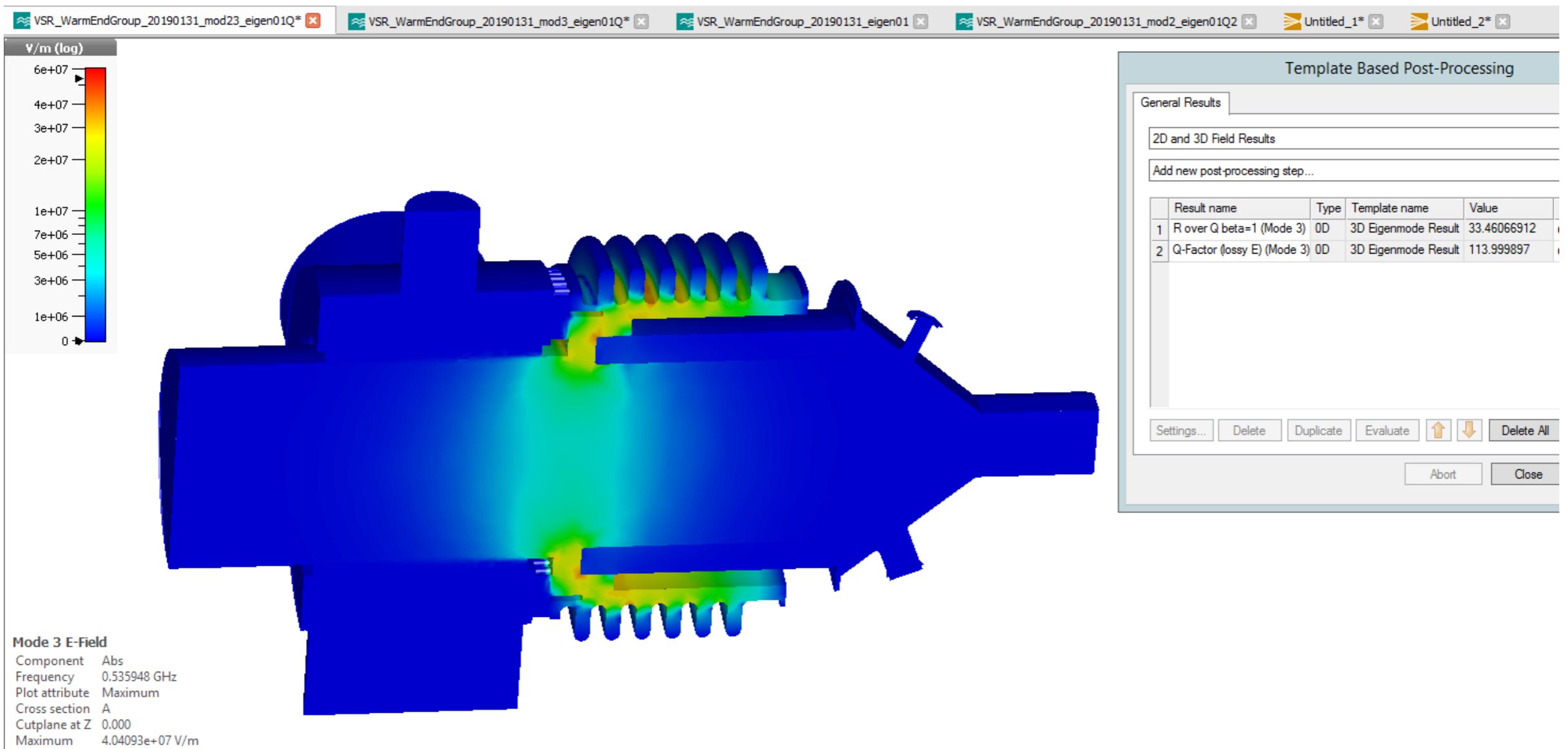
Warm end group

- check-up wake run revealed dangerous resonance very close 500 MHz, ...
- ..., which needs to be avoided, options under numerical evaluation
- Mod 3: introduce a small shielding ring at the pumping grid: **505 MHz**,
 $R/Q = 20.6 \Omega$, $Q = 122$, $E_{\text{peak}}@I_J = 7.0 \text{ MV/m}$



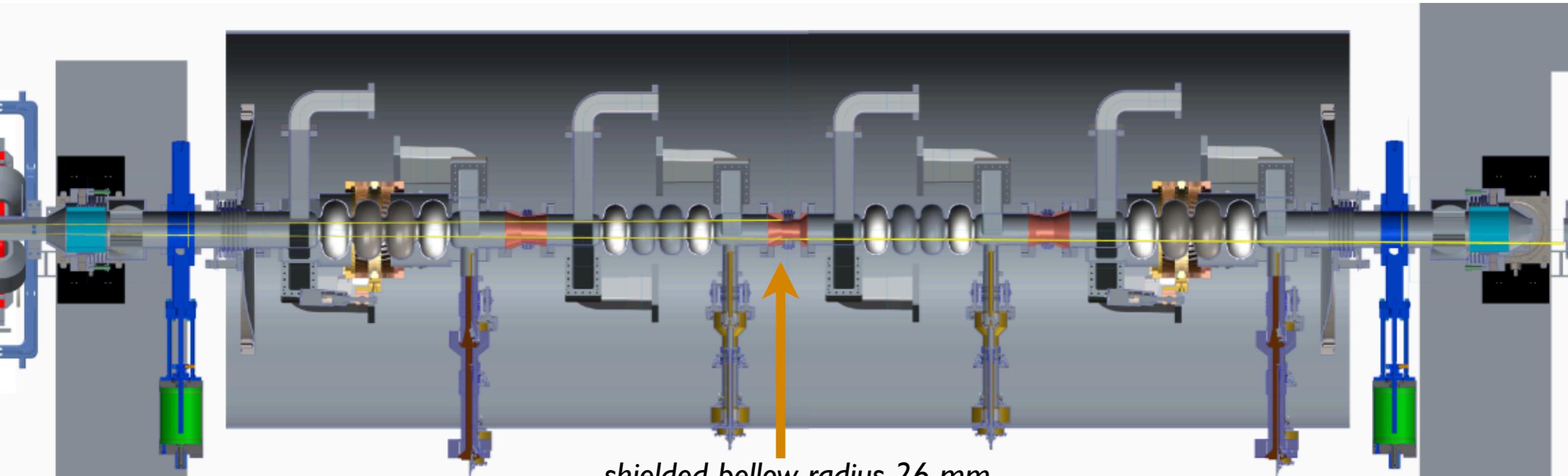
Warm end group

- check-up wake run revealed dangerous resonance very close 500 MHz, ...
- ..., which needs to be avoided, options under numerical evaluation
- Mod 23: combine mod 2 and mod 3: 536 MHz, $R/Q = 33.5 \Omega$, $Q = 114$,
 $E_{\text{peak}}@I_J 4.0 \text{ MV/m}$



Supplement:

Design Aspects of the Collimating Shielded Bellow

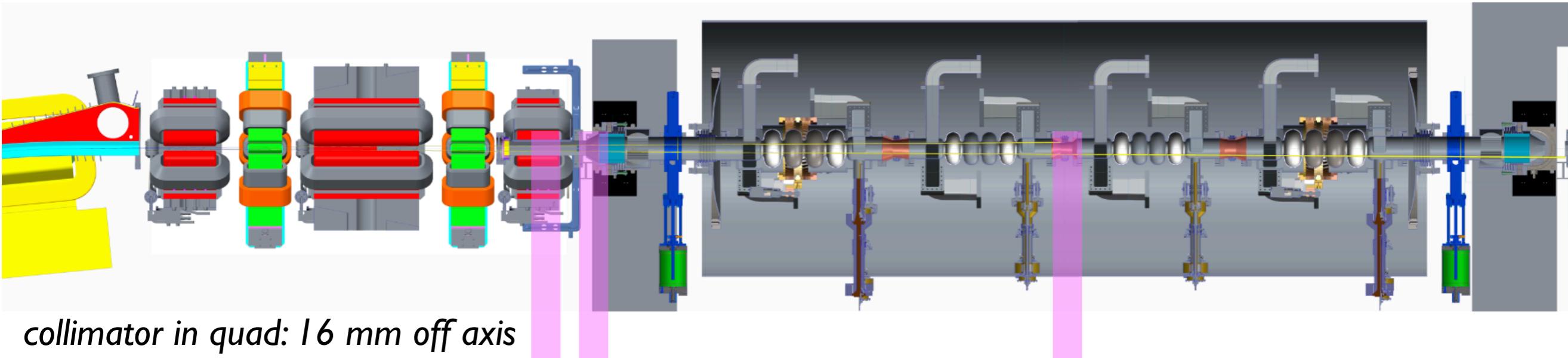


*shielded bellow radius 26 mm
with taper, collimating
synchrotron light*

Synchrotron light power deposition

data courtesy Markus Ries

mandatory to fetch power outside the module or at 5K-level



collimator in quad: 16 mm off axis

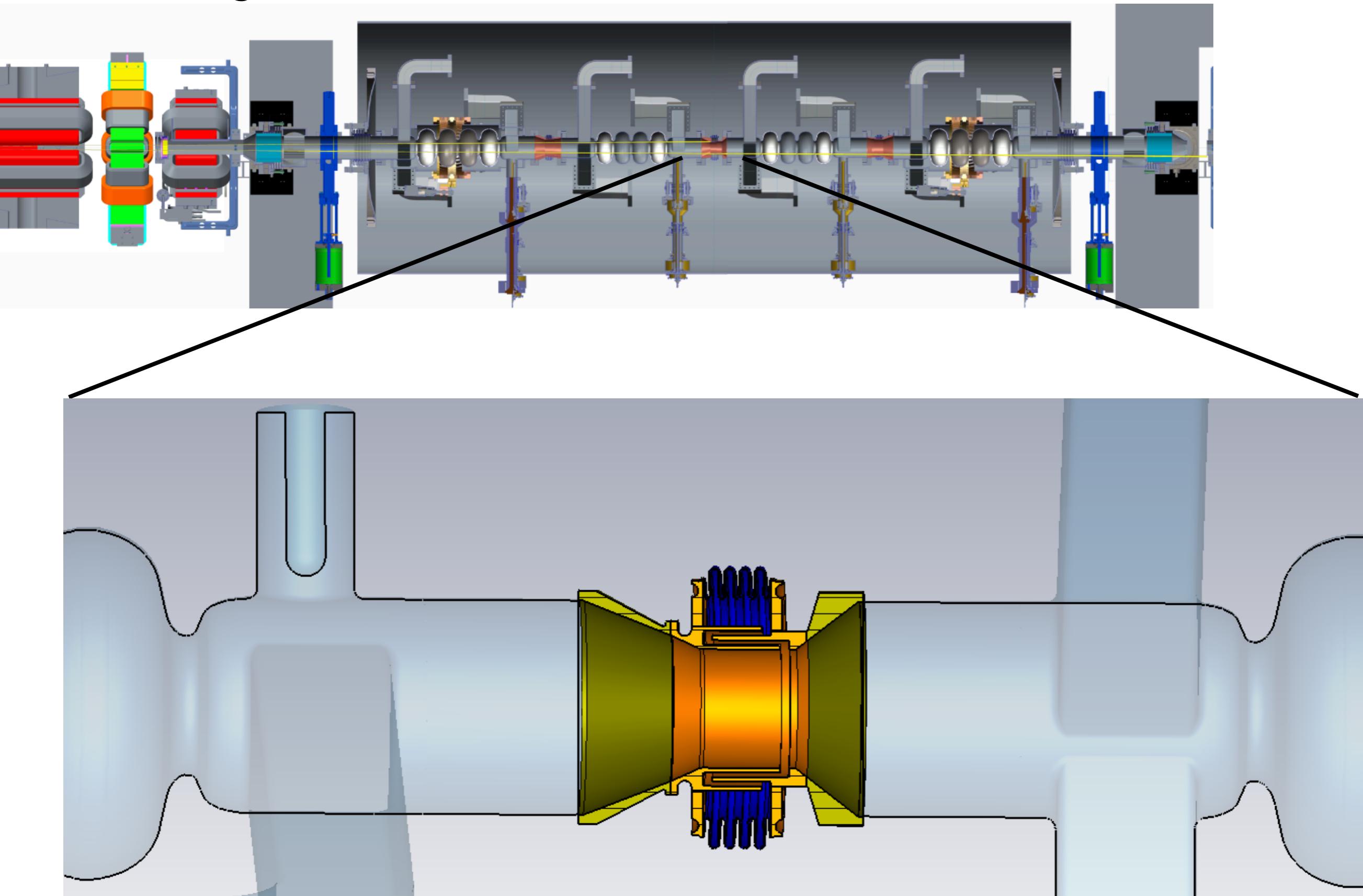
moveable collimator in taper:
 $\leq 16 \text{ mm off axis}$

collimating shielded bellow:
26 mm radius

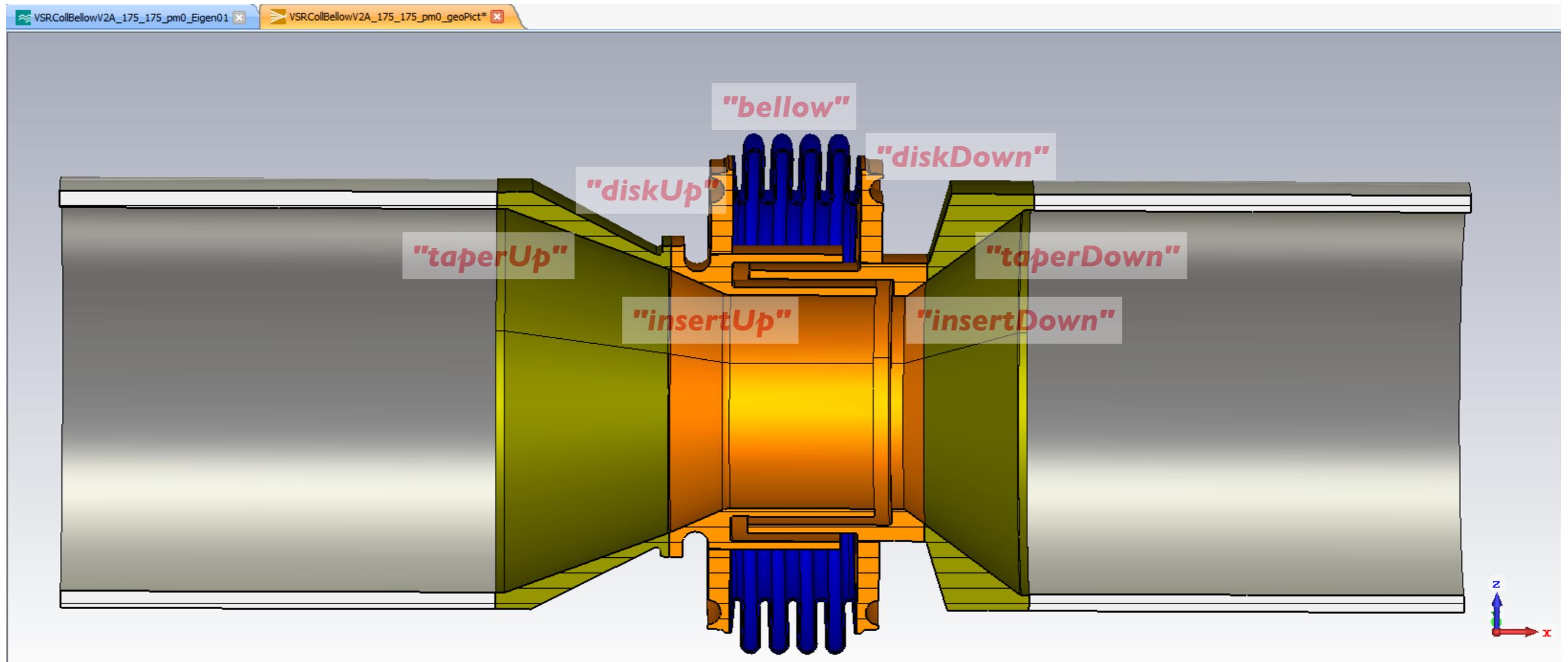
P_{rad} @ collimator in quadrupole	... on moveable collimator	... collimating bellow	... leaving cold module
moveable not activated	63 W	0 W	11 W	15.3 W

data courtesy Markus Ries

Collimating shielded bellow, inner radius 26 mm

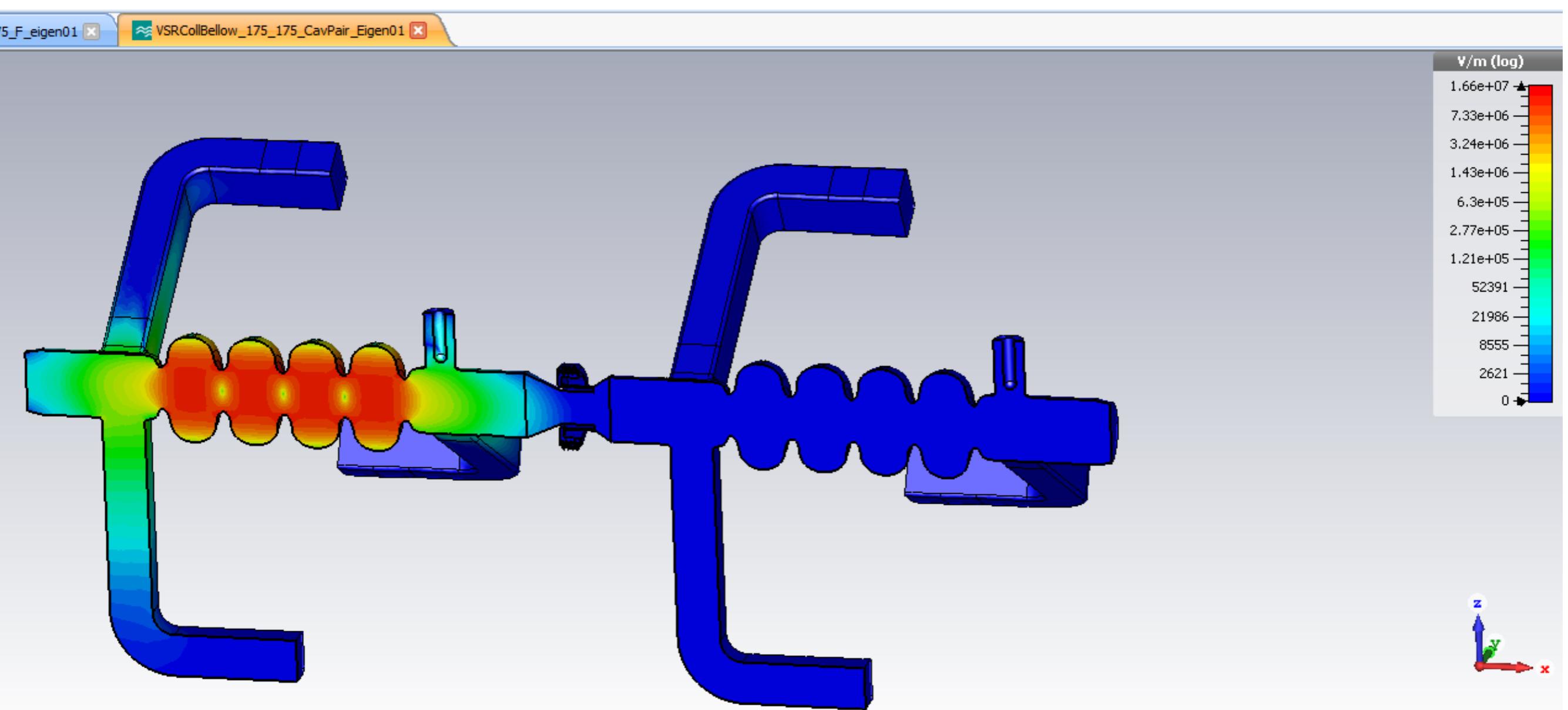


Collimating shielded bellow, inner radius 26 mm



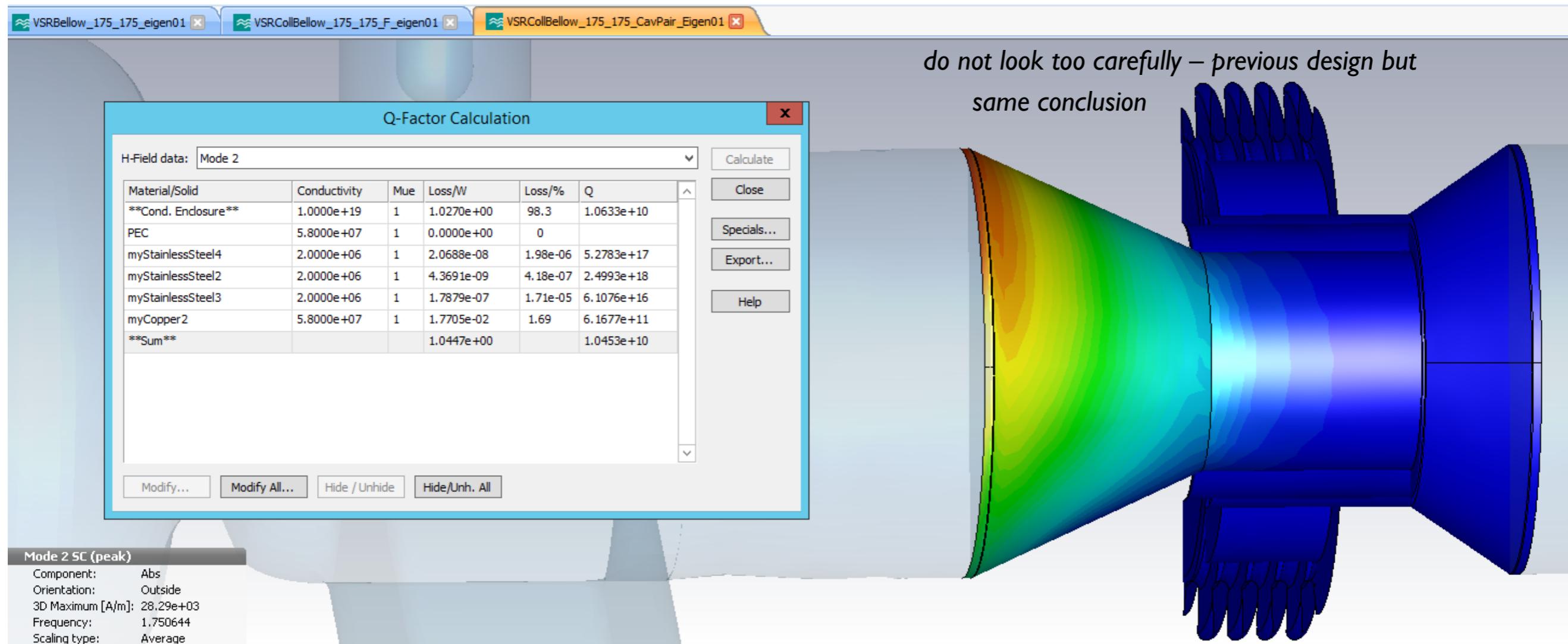
- seven sections for spatial resolution of power loss:
 - massive copper**
 - stainless steel**
 - stainless with inner copper coating / plating**

Collimating shielded bellow, fundamental mode losses



some part of evanescent fundamental mode reaches bellow
(from either side; here logarithmic color scaling)

Collimating shielded bellow, fundamental mode losses

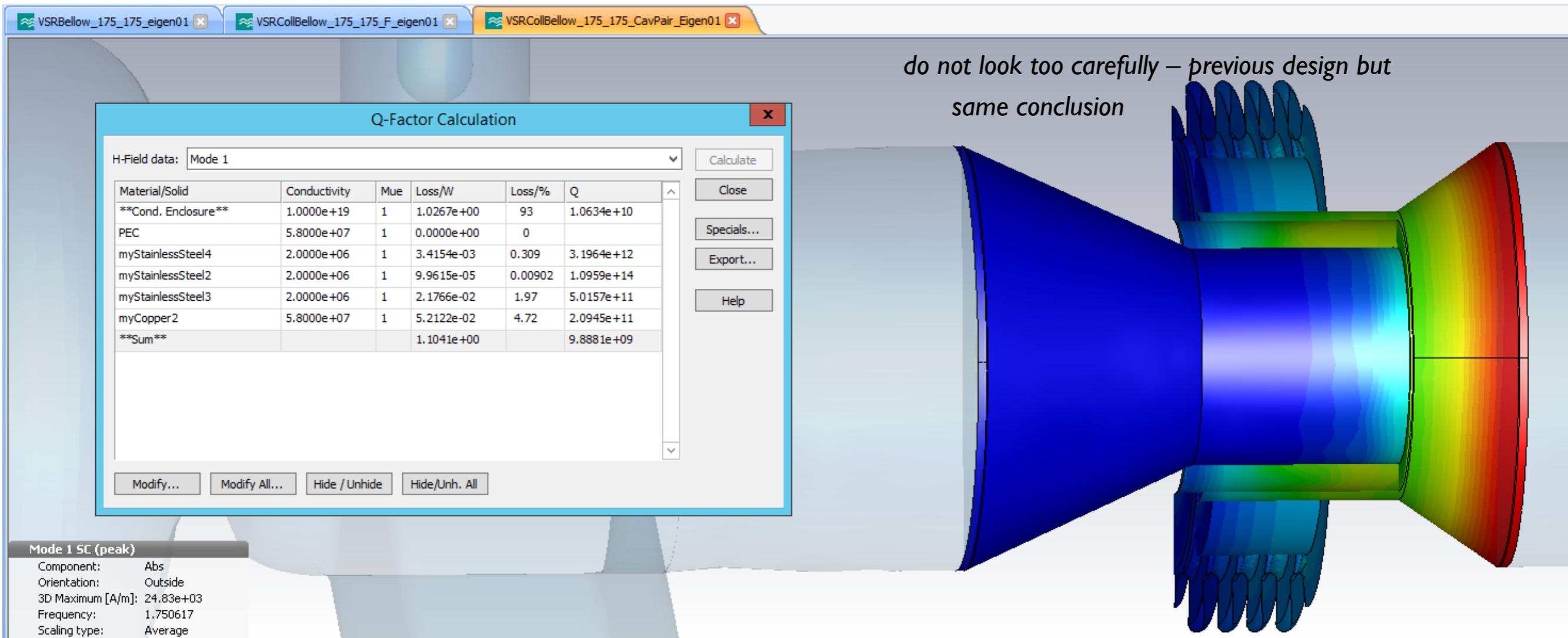


do not look too carefully – previous design but
same conclusion

some part of evanescent fundamental mode reaches bellow (from either side; here logarithmic color scaling)
"left side": $Q_{load,bellow} = 6.1 \cdot 10^{11}$, $P_{loss Cu @ 7MV/cav} = 0.28 W$, $P_{loss Steel @ 7MV/cav} \approx 0 W$

3	R over Q beta=1 (Mode 1)	0D	3D Eigenmode Result	380.7802724
4	R over Q beta=1 (Mode 2)	0D	3D Eigenmode Result	380.8026181
5	Voltage beta=1 (Mode 1)	0D	3D Eigenmode Result	2.0384628689e+06
6	Voltage beta=1 (Mode 2)	0D	3D Eigenmode Result	2.0391897604e+06

Collimating shielded bellow, fundamental mode losses



do not look too carefully – previous design but
same conclusion

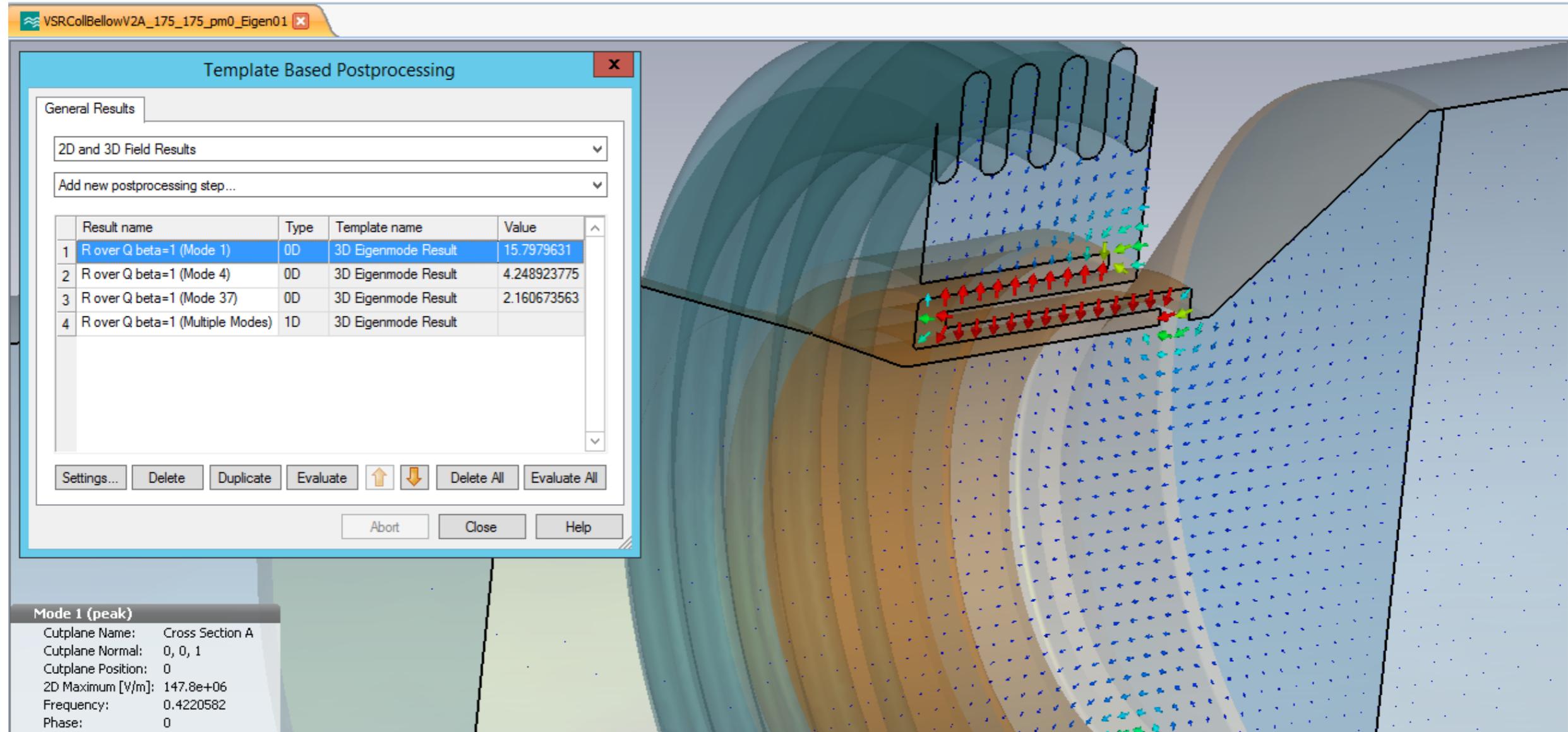
some part of evanescent fundamental mode reaches bellow (from either side; here logarithmic color scaling)

"right side": $Q_{load,bellow} = 2.09 \cdot 10^{11}$, $P_{loss Cu @7MV/cav} = 0.83 W$, $P_{loss Steel @7MV/cav} = 0.35 W$

3	R over Q beta=1 (Mode 1)	0D	3D Eigenmode Result	380.7802724
4	R over Q beta=1 (Mode 2)	0D	3D Eigenmode Result	380.8026181
5	Voltage beta=1 (Mode 1)	0D	3D Eigenmode Result	2.0384628689e+06
6	Voltage beta=1 (Mode 2)	0D	3D Eigenmode Result	2.0391897604e+06

\Rightarrow total fundamental mode loss: $0.28 W + 0.83 W + 0.35 W = 1.46 W \approx 1.5 W$

Collimating shielded bellow: Parasitic modes I – 422 MHz

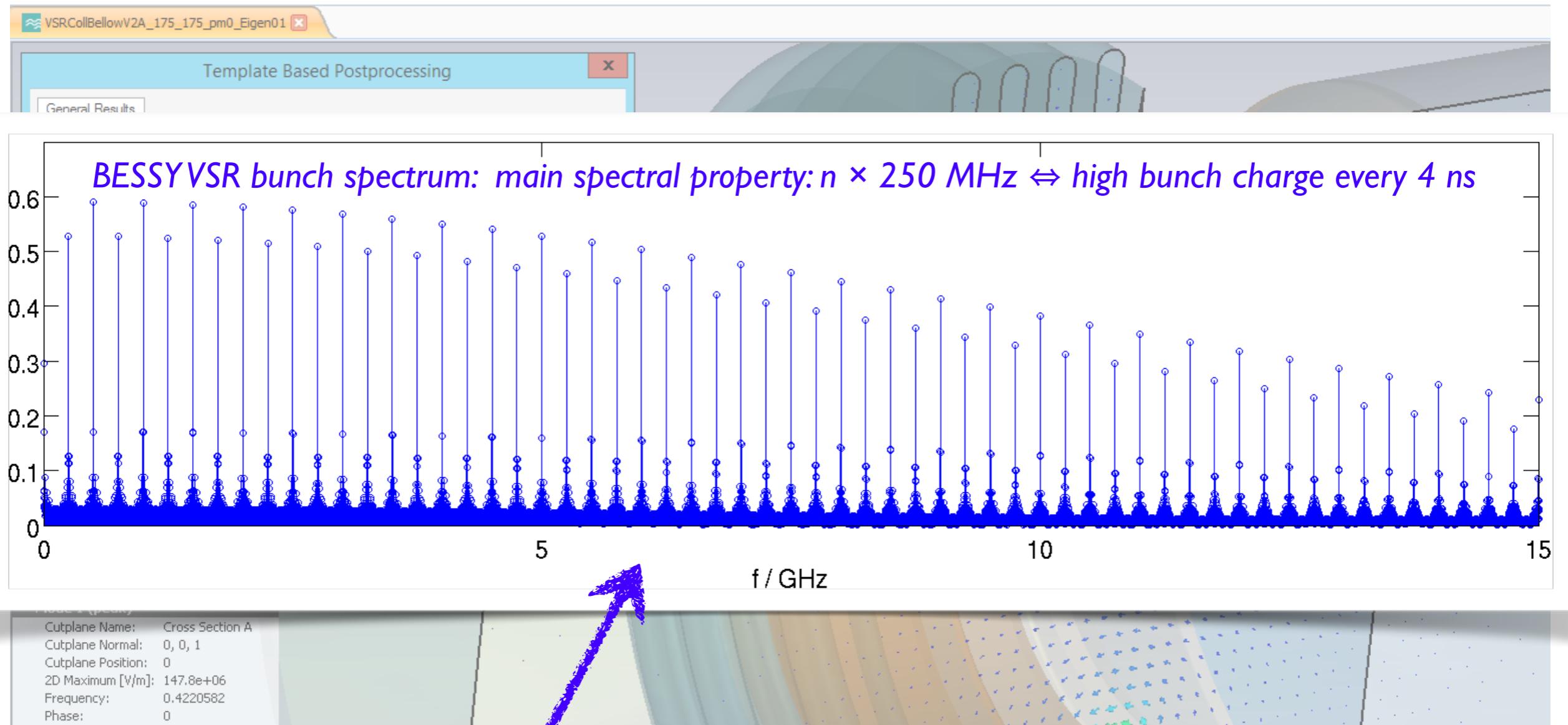


$\lambda/4$ -line-like field pattern, accessing beam, $R/Q = 15.80 \Omega$, $Q = 497$,
not relevant with standard fill patterns, but in case of single puls mode (20 mA):

$P_{beamloss} = 6.70 \text{ W}$, mainly dissipated in steel bellow:

Bellow	5.52429 Watt
InsertUp	0.541045 Watt
taperUp	0.
taperDown	0.
DiskDown	0.188161 Watt
DiskUp	0.179456 Watt
InsertDown	0.262487 Watt

Collimating shielded bellow: Parasitic modes I – 422 MHz

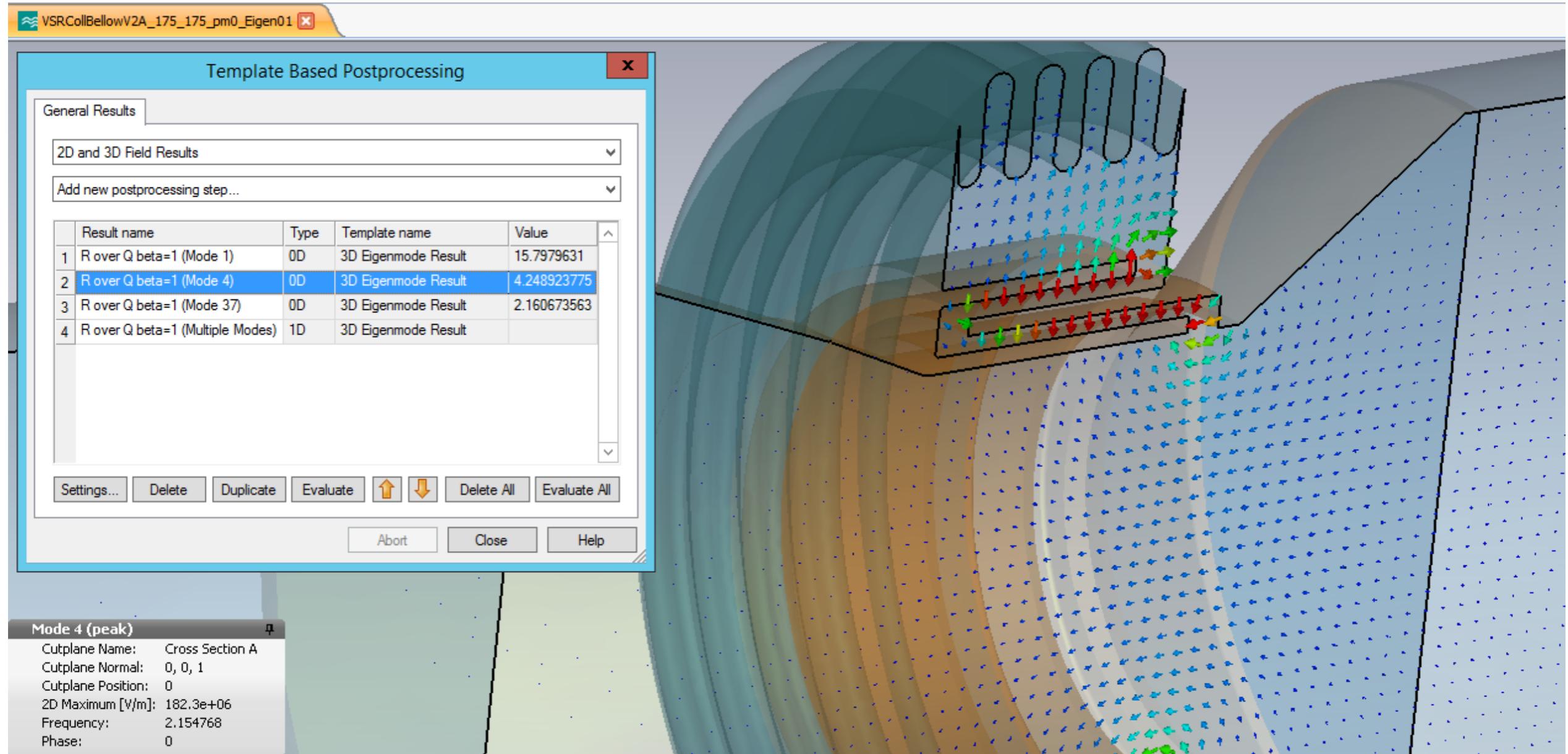


$\lambda/4$ -line-like field pattern, accessing beam, $R/Q = 15.80 \Omega$, $Q = 497$,
not relevant with standard fill patterns, but in case of single puls mode (20 mA):

$P_{beamloss} = 6.70 \text{ W}$, mainly dissipated in steel bellow:

Bellow	5.52429 Watt
InsertUp	0.541045 Watt
taperUp	0.
taperDown	0.
DiskDown	0.188161 Watt
DiskUp	0.179456 Watt
InsertDown	0.262487 Watt

Collimating shielded bellow: Parasitic modes II – 2.155 GHz



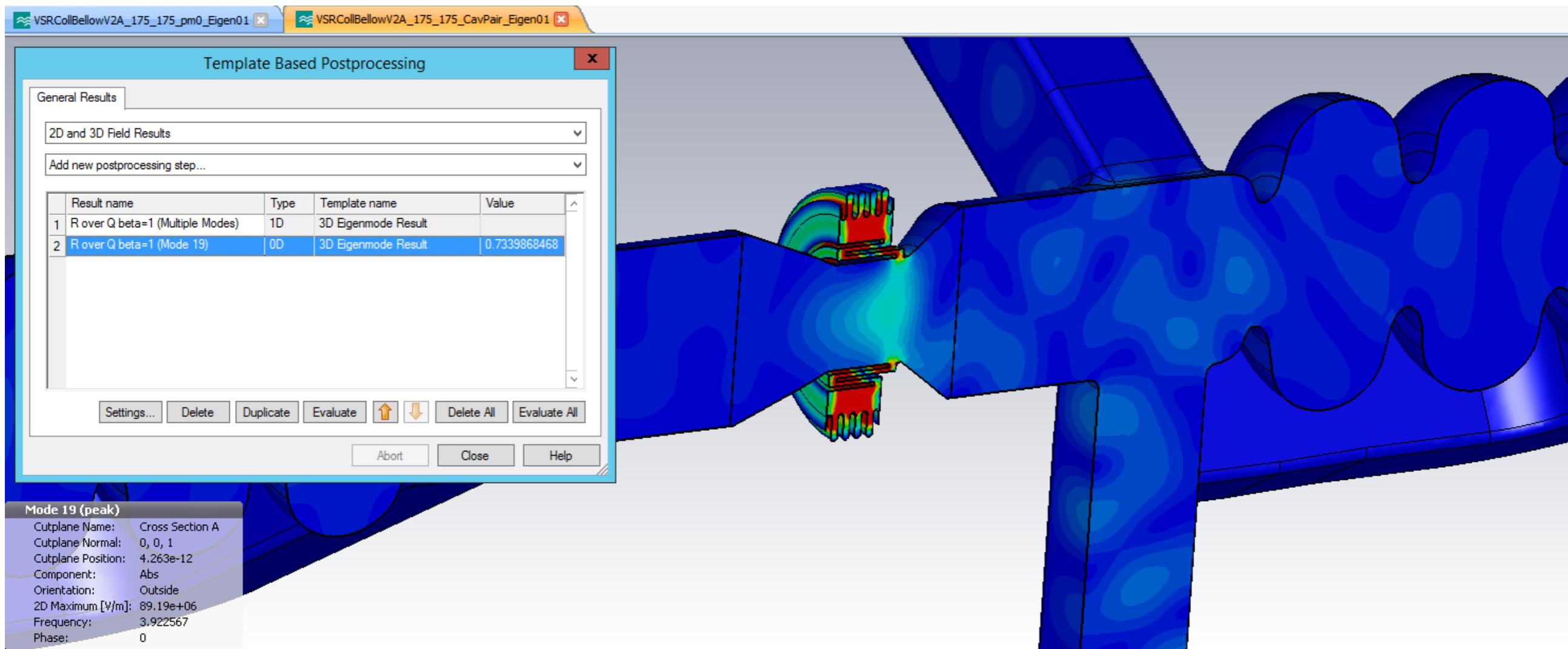
$3\lambda/4$ -line-like field pattern, accessing beam, $R/Q = 4.25 \Omega$, $Q = 1490$

not relevant with standard fill patterns, but in case of single puls mode (20 mA):

$P_{beamloss} = 9.16 \text{ W}$, mainly dissipated in copper inserts:

Bellow	1.19021 Watt
InsertUp	4.69675 Watt
taperUp	0.
taperDown	0.
DiskDown	0.
DiskUp	0.0539257 Watt
InsertDown	3.21357 Watt

Collimating shielded bellow: Parasitic modes III – 3.923 GHz



distributed field pattern, accessing beam, $R/Q = 0.734 \Omega$, $Q = 1038$ (no HOM dampers)

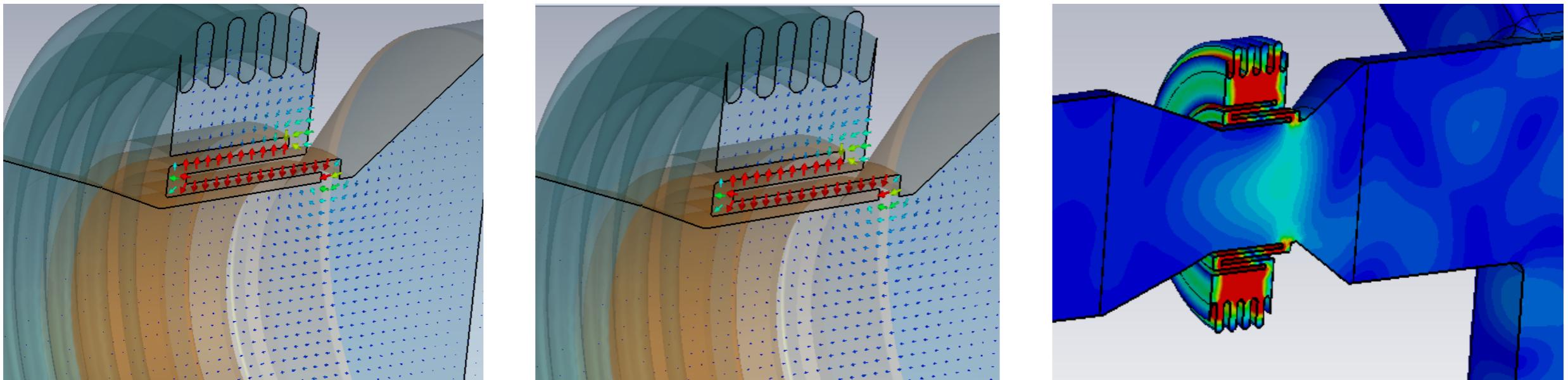
not relevant with standard fill patterns, in case of single puls mode (20 mA):

$P_{beamloss} = 2.90 \text{ W}$, mainly dissipated in steel bellow:

Bellow	2.50393 Watt
InsertUp	0.140266 Watt
taperUp	0.
taperDown	0.
DiskDown	0.0591205 Watt
DiskUp	0.0570919 Watt
InsertDown	0.125486 Watt

this and higher modes are well coupled to the absorbers

Collimating shielded bellow: Length dependence of parasitic modes



-2 mm	± 0	+ 2mm
415.8 MHz	422.1 MHz	423.0 MHz
14.3Ω	15.8Ω	17.1Ω

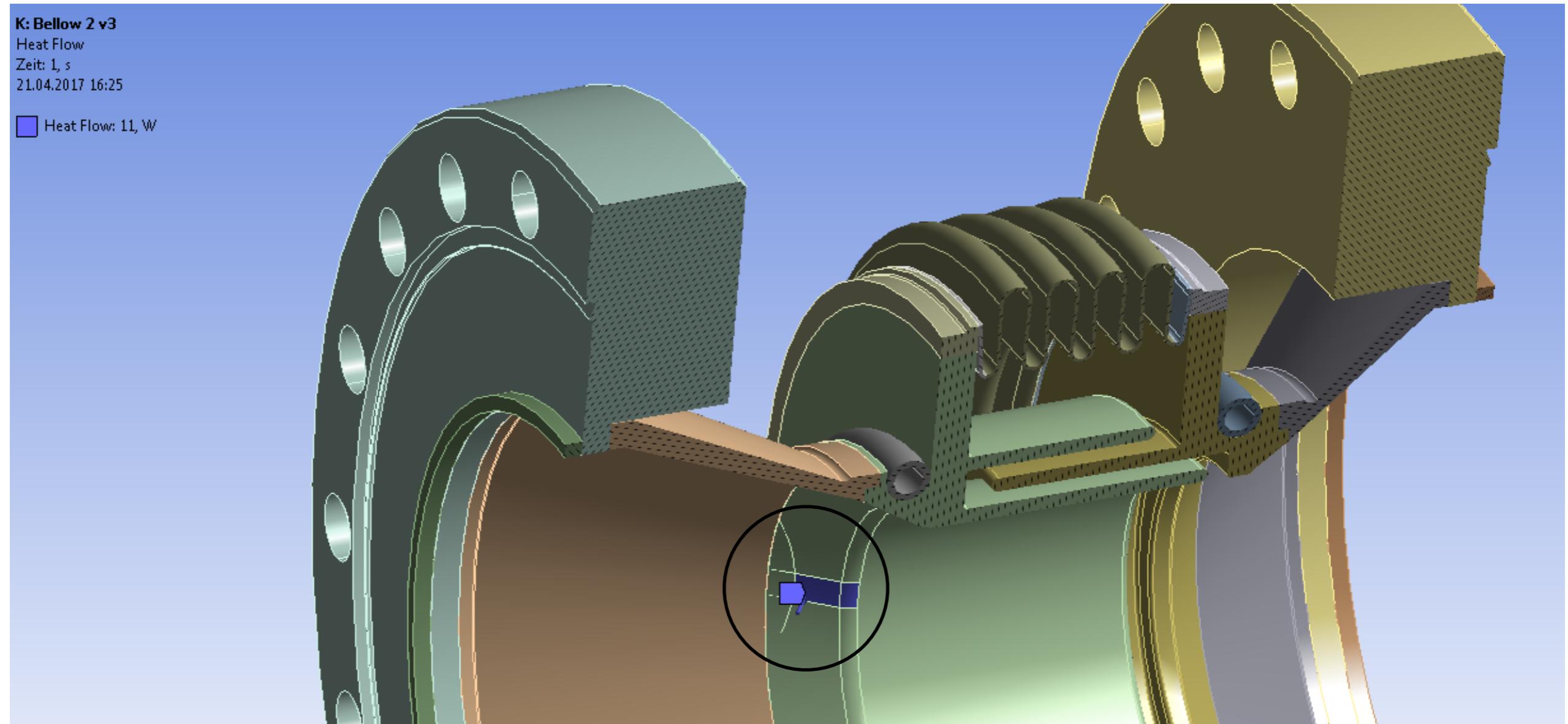
-2 mm	± 0	+ 2mm
2125.1 MHz	2154.8 MHz	2135.4 MHz
4.3Ω	4.2Ω	4.2Ω

-2 mm	± 0	+ 2mm
3976.4 MHz	3928.0 MHz	3784.4 MHz
5.2Ω	2.2Ω	2.2Ω

(computed without cavities;
influenced by finite beam pipes)

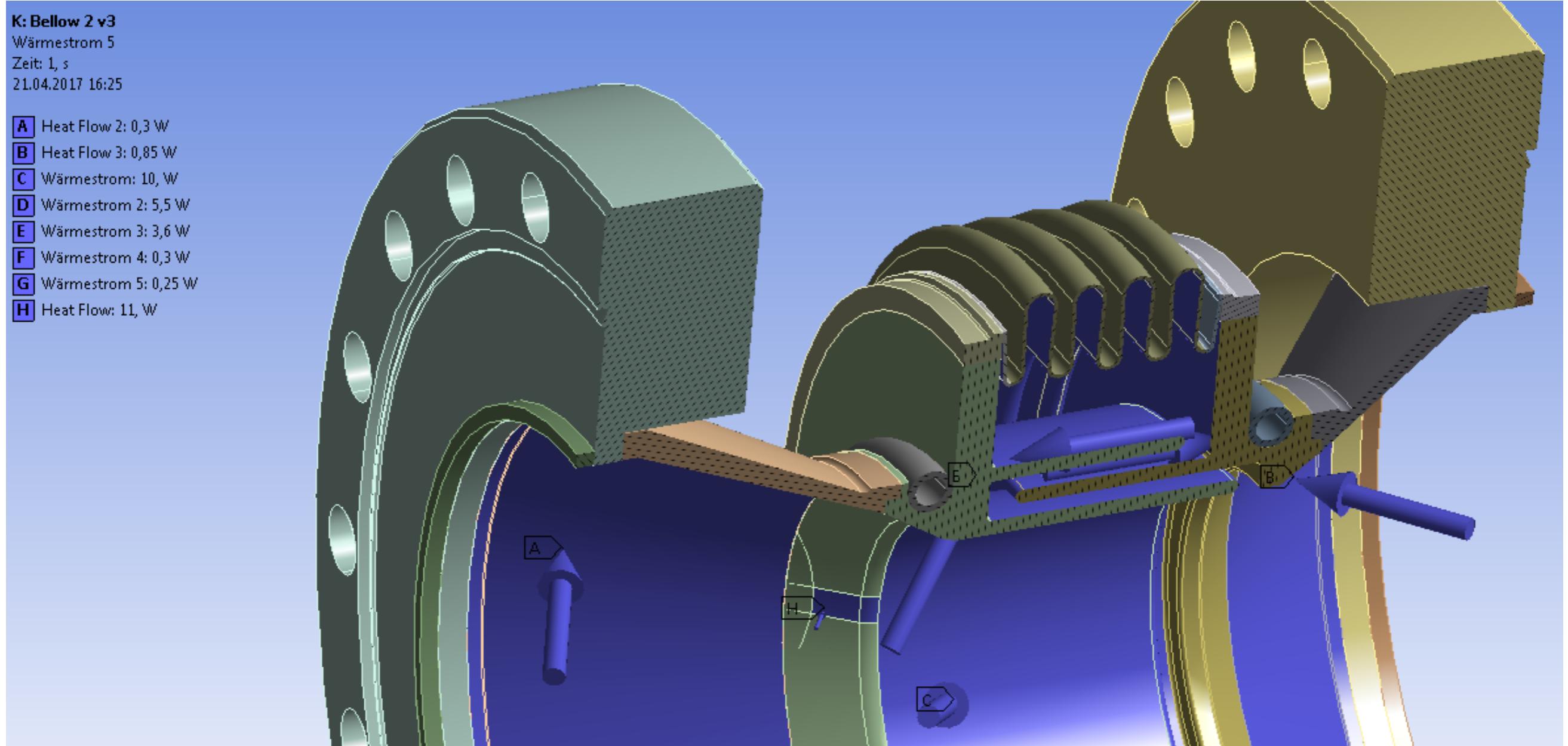
- no issues from stretching / shortening
- not necessarily monotonous dependence

Thermal simulation of collimating shielded bellow: Synchrotron light



Incidence of synchrotron light beam of $\sim 2 \times 2 \text{ mm}^2$ cross section and 11 W power

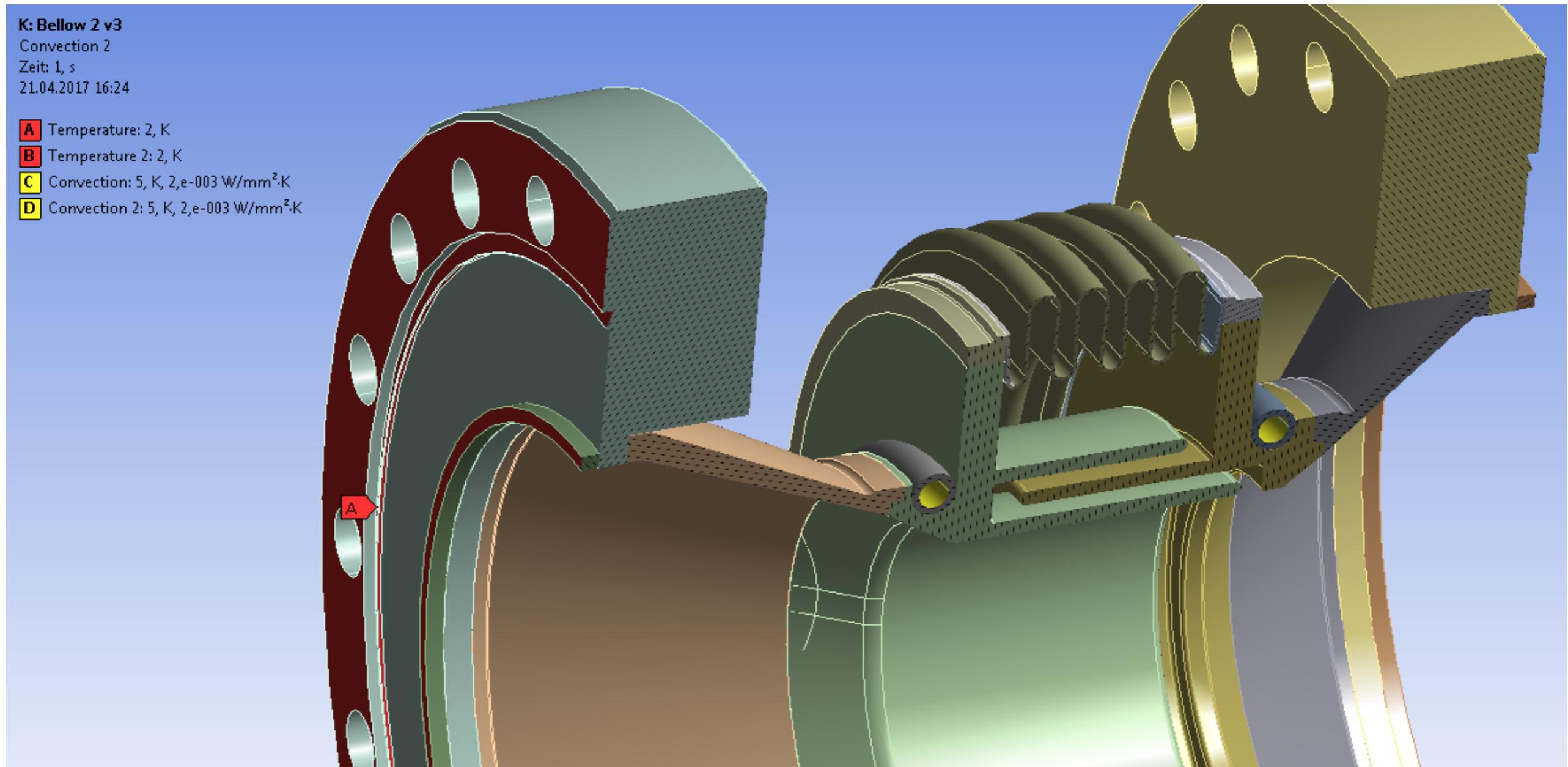
Thermal simulation of collimating shielded bellow: Fundamental + parasitic modes + synchrotron light



Total dissipated power of 31.8 W, assuming

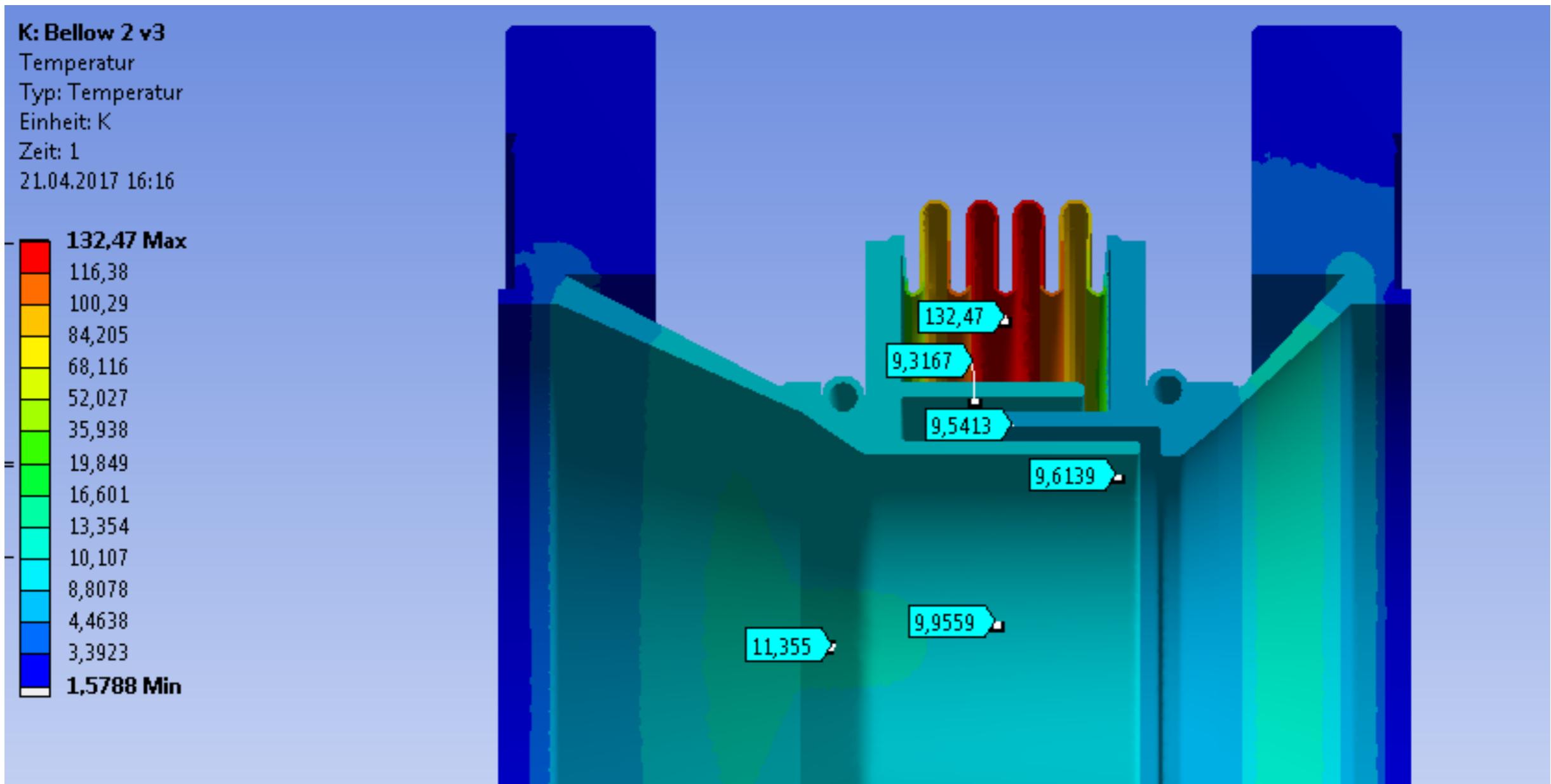
- all beam-deposited wake power is absorbed locally*
- synchrotron light is fully absorbed*
- homogeneous rf dissipation over surface elements*

Thermal simulation of collimating shielded bellow: Temperature and convective boundaries = heat sinks



- 2 K boundaries on contact planes to the neighboring cavities
- 5 K boundaries with $0.002 \text{ W}/(\text{mm}^2 \text{ K})$ convective heat transfer to circular pipes

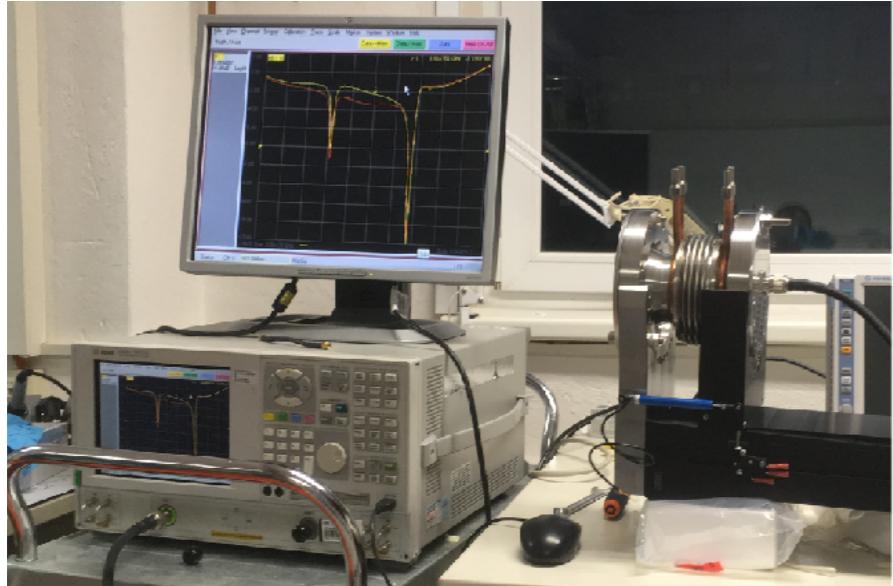
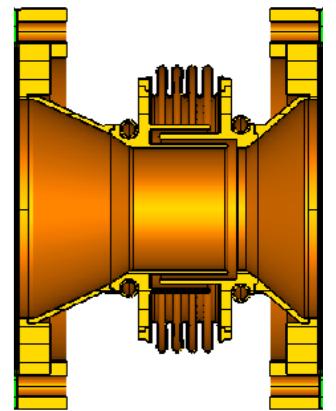
Thermal simulation of collimating shielded bellow: Temperature distribution



- synchrotron light power well distributed by copper
- total heat flux to the cavities < 1 W
- in (rare) single bunch operation bellow exceeds 130 K, outgassing triggered ...
- ... but labyrinth could work as cold gas trap

Collimating Shielded Bellow (CsB)

- prototype in house
- network analyzer measurements at default length done, results in (very) good agreement with simulations (dedicated run with closed beam pipes)



Eigenmode solver results:

Mode	Frequency	Accuracy
1	0.422017503820 GHz	4.815e-09
2	1.61651890959 GHz	1.505e-09
3	1.61660683476 GHz	1.848e-09
4	2.15390260456 GHz	5.946e-07
5	2.66492439661 GHz	7.97e-07
6	2.66507610941 GHz	8.177e-07
7	2.92504757426 GHz	3.033e-07
8	3.07292294057 GHz	3.693e-09
9	3.07302474842 GHz	4.112e-09
10	3.10802492374 GHz	6.663e-09
11	3.22143179174 GHz	4.217e-08
12	3.22143792905 GHz	3.796e-08



Conclusion, summary and recommendation:

„Ihr wißt, auf unsern deutschen Bühnen
Probiert ein jeder, was er mag;
Drum schonet mir an diesem Tag
Prospekte nicht und nicht Maschinen.
Gebraucht das groß, und kleine Himmelslicht,
Die Sterne dürfet ihr verschwenden;
An Wasser, Feuer, Felsenwänden,
An Tier und Vögeln fehlt es nicht.
So schreitet in dem engen Bretterhaus
Den ganzen Kreis der Schöpfung aus,
Und wandelt mit bedächt'ger Schnelle
Vom Himmel durch die Welt zur Hölle.“

J. W. von Goethe, Faust: Eine Tragödie