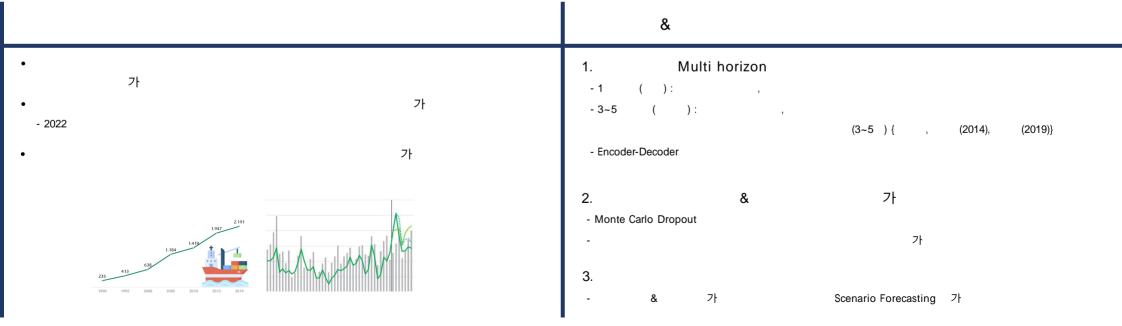
2021155151

1.
2.
3.
4. &
5.
6.
7.



ARIMA VAR - VEC , (2020)	ARIMA, VAR, VEC	,GDP,	ARIMA . VECM .
. (2019)	ARIMA, LSTM, GRU		LSTM & GRU7ት ARIMA . 7ት
. (2021)	ARIMA, VAR, LSTM, GRU	, , 가 ,	, RMSE 7ł
Prophet : , . , . , (2022)	ARIMA, LSTM, Prophet		 , ARIMA Prophet . LSTM

(20)

(16)

(8) 3. Encoder-Decoder & Attention

One-Step Ahead Prediction

&

2000.01 ~ 2022.06						
	(TEU) *	가	/		
	BDI()			Investing.com		
	SCFI()	*	E	n.macromicro.me		
	HRCI(Howe Robinson) *		가		
				Investing.com		
	/					
	가					
			가	1		

- 2000 TEU : [2001.01 ~ 2001.12 / TEU (1.23)] × [2000.01 ~ 2000.12 TEU]

: 2002.01 ~ 2022.06 가 --> 2000.01 ~ 2001.12 ARIMA

(2002.01.11 ~ 2009.10.09)] : [SCFI (2009.10.16 ~ 2022.06.24) + CCFI --> 2000.01 ~ 2001.12 ARIMA

2.



3. Multi Horizon

- $[17.07 \sim 18.06]$, $[18.07 \sim 19.06]$, $[19.07 \sim 20.06]$, $[20.07 \sim 21.06]$, $[21.07 \sim 22.06]$ --> 5 - 1
- $[2017.07 \sim 2020.06]$, $[2019.07 \sim 2022.06]$ --> 2 - 3
- [2017.07 ~ 2020.06] --> 1 - 5

4. Sliding Window & Min-Max Scaling

	Sequence Length [∟]
1년 단위 예측←	Input Sequence = 18, Prediction Length = 12
3년 단위 예측₽	Input Sequence = 18, Prediction Length = 364
5년 예측←	Input Sequence = 20, Prediction Length = 60€

- Train [2000.01 ~ 2017.06] & Test [2017.07 ~ 2022.06] --> Min-Max Scaler
- (B,T,D)

& 8 Multi Horizon

1. Encoder-Decoder Layer

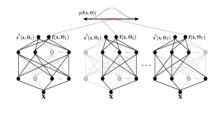
- LSTM, CNN-LSTM, TCN(Temporal Convolutional Network), LSTM-Attention

2. Prediction Uncertainty

- Monte Carlo Dropout
- 3. Probability Distribution Similarity
 - KL-Divergence, Negative Log-Likelihood
- 4. Probabilistic Forecast Measure
- CRPS(Continuous Ranked Probability Score), Coverage, Sharpness
- 5. Priority Prediction Value Set
- Mean MCD Pred, TEU Seasonality, Euclidean Distance, JS-Distance, DTW

Monte Carlo Dropout

- Epistemic Uncertainty [
- BNN, Gaussian Process, Variational Inference
- Dropout
- MC-Dropout



Monte Carlo Dropout Predictions

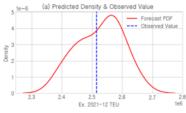
Uncertainty Quantification

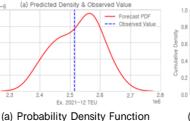
MC-Dropout =0.8 N = 30

CRPS(Continuous Ranked Probability Score)

- Multi Horizon

N = 30





 $crps_{F,y} = \int_{-\infty}^{\infty} [F(t) - I(t \ge y)]^2 dt$

- (b) Cumulative Density Function

가

$$CRPS = \frac{1}{T} \sum_{i=1}^{T} crps(F_i, y_i)$$

Coverage(Prediction Interval Coverage Probability)

- (ex. 95% Prediction Interval)

-

$$\textit{Coverage} = \frac{1}{T} \sum_{i=1}^{T} \{ (Y_i > Lower PI_i) \cap (Y_i < Upper PI_i) \}$$

가

Sharpness(Mean Prediction Interval Width)

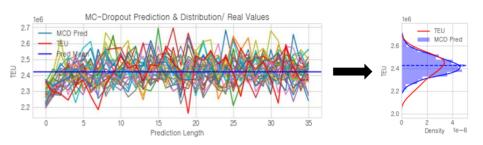
(ex. 95% Prediction Interval)

 $Sharpness = \frac{1}{T} \sum_{i=1}^{T} (Upper PI_i - Lower PI_i)$

가

CRPS

1. MLE MC-Dropout



가

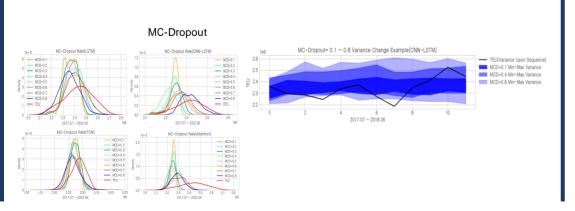
MC-Dropout 0.1~0.8

- MLE 가 MC-Dropout

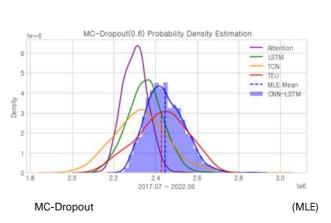
- & Horizon N=30

• , MC-Dropout 가

MC-Dropout=0.8



• CNN-LSTM Layer



가

• Monte Carlo Dropout=0.8 & N=30

- MC-Dropout=0.8 & N=30

KL-Divergence,

Negative Log-Likelihood

, CNN-LSTM

가

CNN-LSTM Encoder-Decoder(MCD=0.8) 가

KL-Divergence							
MC-Dropout=0.8 Encoder-Decoder							
예측기간~	LSTM₽	CNN-LSTM₽	TCN←	Attention□			
2017.07~2018.06	382774₽	654165↩	399003₽	536973₽			
2018.07~2019.064	603162₽	326301₽	9935054	997807₽			
2019.07~2020.06	389196≓	551593₽	618384₽	281291₽			
2020.07~2021.0643	977680≓	551098₽	1469896₽	930074₽			
2021.07~2022.06 ⁽²⁾	680140₽	383917₽	1083607₽	760118₽			
2017.07~2020.0643	1354819₽	1045959₽	2763750₽	4458365₽			
2019.07~2022.064	1142756⊖	1387508₽	4641674₽	1578009₽			
2017.07~2022.06 ⁽²⁾	4445308₽	1529650₽	5457136₽	72654505₽			
평균↩	1246979.375	803773.875	2178369.375	2101005.254			

Negative Log-Likelihood□								
MC-Dropout=0.8 Encoder-Decoder								
예측기간데	LSTM⊖	CNN-LSTM↔	TCN∈	Attention⊲				
2017.07~2018.06	4548⊲	4640⊲	4607←	4513⊲				
2018.07~2019.06	4648₽	4613€	4726₽	4640₽				
2019.07~2020.06	4616⋳	4644⊲	4642€	4513⊲				
2020.07~2021.06	4725₽	4682₽	4819₽	4660₽				
2021.07~2022.06	4676↩	4656₽	4757↩	4614₽				
2017.07~2020.06	13721₽	13862₽	14317₽	14379₽				
2019.07~2022.06	13875₽	13995₽	14771₽	13783₽				
2017.07~2022.06	23549	23216₽	24417₽	23952₽				
평균↩	9294.75₽	9288.5₽	9632₽	9381.75₽				

2. Uncertainty Quantification

• 3-Sigma Based(Gaussian) Prediction Interval [

± 2 95%

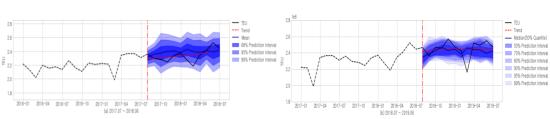
± 1 68%

• Quantile Based Prediction Interval [

95%

- [0.025,0.975]

- [0.15,0.85] 70%



2. **CRPS**

CNN-LSTM

가

Coverage Sharpness 가

(a)

€ J				
평가 지표↩	E	ncoder-Decoder	٥	LSTM [←]
	LST M ←	CNN-LSTM	T CN⊖	Attention =
평균값 MAPE←	4.183↩	3.823₽	5.36↩	5.03←
평균값 RMSE←	120882₽	113658↩	153969↩	1444462↩
중앙값 MAPE←	4.267←	3.813↩	5.63₽	5.067←
중앙값 RMSE4	125704↩	113605↩	161813₽	145607⊄
2o 95% PI Coverage⊖	0.651←	0.842↩	0.8461↩	0.3837⊄
2o 95% PI Sharpness⊖	270785↩	306066.90↩	4850404.51↔	110372.87↩
[0.025,0.975] 95% PI Coverage⊖	0.603₽	0.749₽	0.821₽	0.359₽
[0.025,0.975] 95% PI Sharpness	236327.4₽	266479.06↩	428196.63₽	151226.09↩
CRPS₽	78728.533↩	66868.954₽	97022.659↩	104242.804€

2.

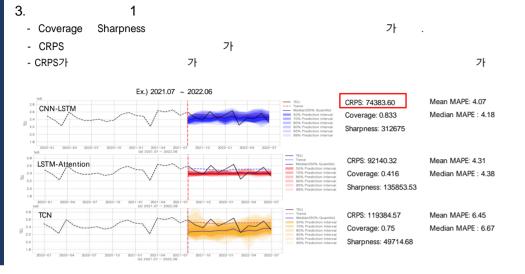
CRPS CNN-LSTM

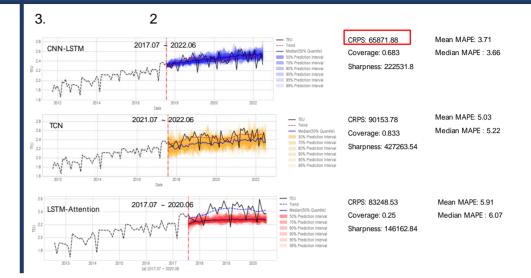
가

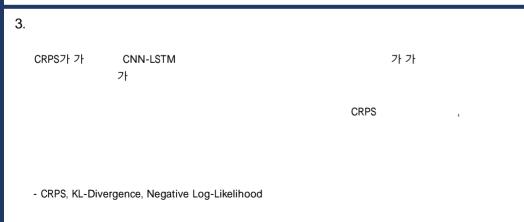
(b)

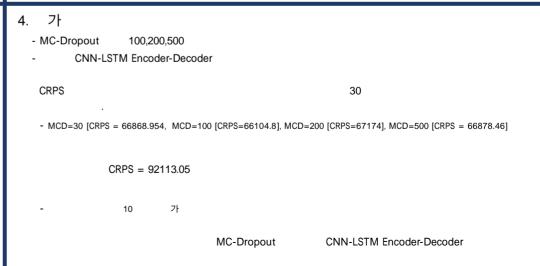
가

Monte Carlo Dropout Prediction						
^실 평가 지표 [△]		Encoder-Decoder				
	LSTM₽	Ī	CNN-LSTM	T CN⊕	Attention	
평균값 MAPE⊄	2.3487₽	Г	1.3756₽	4.729₽	3.9737↩	
평균값 RMSE⊄	64725.83↩	Г	40801.33↔	121286.39↩	101930.74↩	
중앙값 MAPE⊲	2.4612₽	П	1.467←	5.126₽	4.069₽	
중앙값 RMSE⊄	65475.2874	П	43459.0567₽	131797.97↩	101984.5334	
1¢ 68% PI Coverage⊖	0.5397₽	Г	0.9159₽	0.5096↩	0.17123↩	
1¢ 68% PI Sharpness⊖	135390.587	-	153033.327↩	242520.276	89885.6617↩	
[0.15,0.85] 70% PI Coverage⊖	0.5994↩	П	0.9151₽	0.4454₽	0.12248↩	
[0.15,0.85] 70% PI Sharpness⊖	130906.848	9	150622.45↩	211314.88₽	83988.73234	
CRPS₽	78728.5334		66868.954	97022.659⊄	104242.804	









4. 가

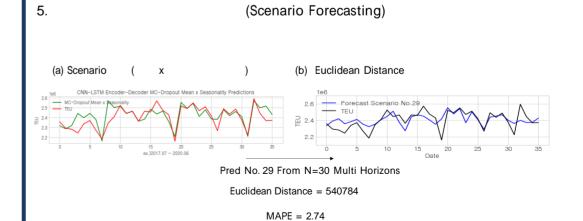
Continuous Ranked Probability Score							
세호기기	MC-Dropout 출력 개수⊲						
예측 기간의	30₽	100₽	200₽	500₽			
17 ↔	67890.706₽	67089.4	69315⊄	68405.4₽			
3Y ←	66844.275⊖	64944₽	65913₽	65660			
5Y ←	65871.88₽	66281∉	66294₽	66570₽			
전체 평균⊖	66868.954	66104.8⊲	67174	66878.46₽			

Monte Carlo Dropout Prediction ^{c2}						
평가 지표↔	CNN LSTM Encoder-Decoder					
	Univariate∈	Multivariate←				
평균값 MAPE⊲	4.79←	3.823←				
평균값 RMSE←	137746←	113658↩				
중앙값 MAPE₽	4.84←	3.813₽				
중앙값 RMSE←	138532←	113605↩				
2σ 95% PI Coverage⊖	0.582←	0.842←				
2σ 95% PI Sharpness⇔	219508.9←	306066.90⊄				
[0.025,0.975] 95% PI Coverage	0.568↩	0.749←				
[0.025,0.975] 95% PI Sharpness	226618.19↩	266479.06↩				
CRPS↩	92113.05←	66868.954←				

4. 기 (Multi Horizon ARIMA, VECM, Prophet One-Step Ahead DL)
5 , MC-Dropout CNN-LSTM Encoder-Decoder

성능 비교~							
방법론↩	MAPE←	RMSE←					
LSTM-	4.31←	128746↩					
GRU⇔	4.14	125469↩					
CNN-LSTM←	3.75↩	118493⋳					
TCN←	4.93↩	145384					
VECM [←]	4.28	125623↩					
ARIMA⊲	5.78↩	181322↩					
Prophet←	4.06↩	181322↩					
MCD-CNN-LSTM Encoder-Decoder (Mean)다	3.71↩	111060					
MCD-CNN-LSTM Encoder-Decoder (Median)↔	3.66⊲	109749⊲					





5.

2019.07 ~ 2022.06							
MC_Dropout Best Predictions△							
Pred No.	17↩	6←	25⊄	4←	21↩		
MAPE₽	3.91∂	4.00₽	4.02₽	4.13⊖	4.34		
		JS-Di:	stance□				
Distance□	0.012044	0.013709↩	0.014641↩	0.014931	0.015454		
Pred No	21∂	7←	1↩	17⊲	6∈		
MAPE	4.34	4.94↩	4.84←	3.91₽	4.00		
		Euclidear	nDistance□				
Distance	567127₽	612222₽	615392₽	649793⊲	679009⊍		
Pred No⊖	21₽	1↩	7←	4↩	25∂		
MAPE□	4.34	4.84←	4.94←	4.13	4.02₽		
		Dynamic Ti	me Warping	3			
Distance⊖	401886↩	423161↩	423403₽	431783₽	435740↩		
Pred No	18↩	13↩	21↩	25∈	12←		
MAPE⊲	6.77⊄	5.05↩	4.34∈	4.02	4.74←		

x MC-Dropout , 가 5 1

MC-Dropout 가 가 5 Scenario / 1.

Multi Horizon
Monte-Carlo Dropout

CRPS(Continuous Ranked Probability Score)7†

7† (MC-Dropout &)

Scenario

2.

2000 1 100%

가 &

DeepAR, NHITS 가

End