

# A Generalized Signal Quality Estimation Method for IoT Sensors

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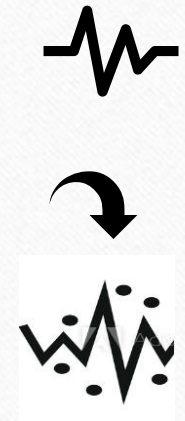


# Context

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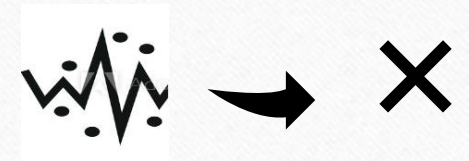
- Current healthcare scenarios-  
shift of care/ monitoring from  
hospitals to homes.
- Ambulatory healthcare monitoring-  
IoT sensors.
- Corrupted by noise.



# Context

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- Signal quality analysis.
- Quality assessment at the edge.
- Confidence metric.

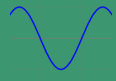


# Research Gap

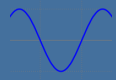
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- No general definition of signal quality.
  - Designed for a specific signal or noise scenario.
  - Instantaneous signal quality assessment method not discussed.
- a. Any stage of signal acquisition and processing.
  - b. Applicable to a number of signals and noise scenarios.
  - c. Instantaneous signal quality.

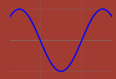
## Curve SQI (cSQI)



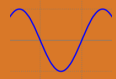
A generalized signal quality indicator - any periodic or quasi-periodic signals.



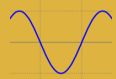
Amount of noise contained in the signal.



A monotonically increasing function of SNR.



Based on the waveform morphology - curve SQI (cSQI).



Performance on ECG signals.

# Methodology

- Template Generation



Generation of a single cycle template.



Template generation use  $N$  cycles of clean data .



Example: ECG signals



# Methodology - Template Generation

**Table 1: Algorithm for Template Generation**

**Setup:**

- A. Signal sequence of interest  $\mathbf{x}$
- B. Signal vector  $\mathbf{X}_n$  of length  $2M+1 \triangleq [\mathbf{x}[n-M], \dots, \mathbf{x}[n], \dots, \mathbf{x}[n+M]]$  where  $M$  has been decided based on the time period.
- C. Let  $\mathbf{X}_{n(c)}$  be the correlation Toeplitz matrix of  $\mathbf{X}_n$  of dimensions  $(2M+1, 4M+1)$  where  $\mathbf{X}_{n(c)} =$

$$\begin{bmatrix} \mathbf{x}[n+M] & \dots \mathbf{x}[n] & \dots \mathbf{x}[n-M] & \dots 0 & 0 \\ 0 & \mathbf{x}[n+M] & \dots \mathbf{x}[n] & \mathbf{x}[n-M] & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & \dots \mathbf{x}[n+M] & \dots \mathbf{x}[n] & \dots \mathbf{x}[n-M] \end{bmatrix}$$

, where the  $k^{\text{th}}$  column of  $\mathbf{X}_{n(c)}$  is indicated by  $\mathbf{X}_n^{(k)(c)}$  where  $k \in [0, 4M]$

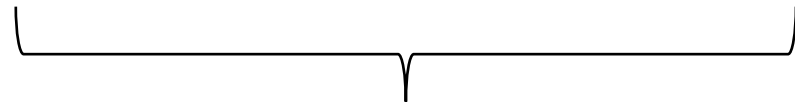
- D. Let  $\mathbf{X}_n^{(t)}$  be  $t^{\text{th}}$  circular shifted version of  $\mathbf{X}_n$  i.e.,  $\mathbf{X}_n^{(t)} = [\mathbf{x}[n-M+t] \ \mathbf{x}[n-M+t+1] \dots \mathbf{x}[n+M] \ \mathbf{x}[n-M] \dots \mathbf{x}[n-M+t-1]]$

**Template Generation:**

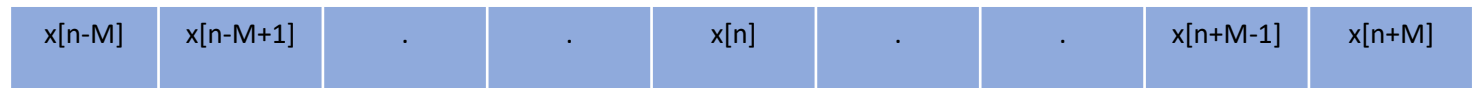
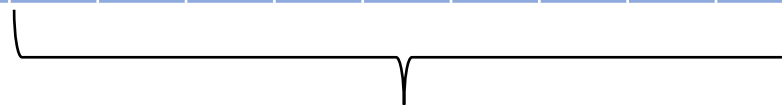
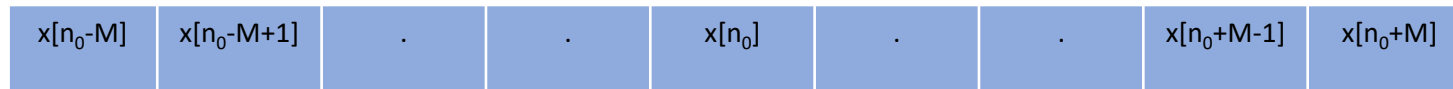
1. Identify a signal segment containing  $N$  consecutive fiducial features of interest (From the time period or otherwise).
  2. Let  $\mathbf{n}_0$  be the center of the first segment of length  $2M+1$ ,  $\mathbf{X}_{\mathbf{n}_0}$ .
  3. Initialize  $\mathbf{T} = \mathbf{X}_{\mathbf{n}_0}$ .
  4. For  $\mathbf{i} = (M+1)$  to  $(N(2M+1)-M)$  in steps of  $2M+1$ 
    - a. Let  $\mathbf{X}_{\mathbf{n}_0+\mathbf{i}(c)}$  be the correlation Toeplitz matrix of  $\mathbf{X}_{\mathbf{n}_0+\mathbf{i}}$
    - b. Let  $\mathbf{k} = \text{argmax}_j [|\mathbf{T} \cdot \mathbf{X}_{\mathbf{n}_0+\mathbf{i}(c)}^{(j)}|]$
    - c. If  $\mathbf{k} \approx \mathbf{n}_0$ 

$$\mathbf{T} = \mathbf{T} + \mathbf{X}_{\mathbf{n}_0+\mathbf{i}}^{(k)}$$
- End**
- End**
5. Normalize  $\mathbf{T}$  based on number of times condition 4.c was satisfied.

# Methodology - Template Generation



- Window of length  $2M+1$
- Centered at say  $n_0$



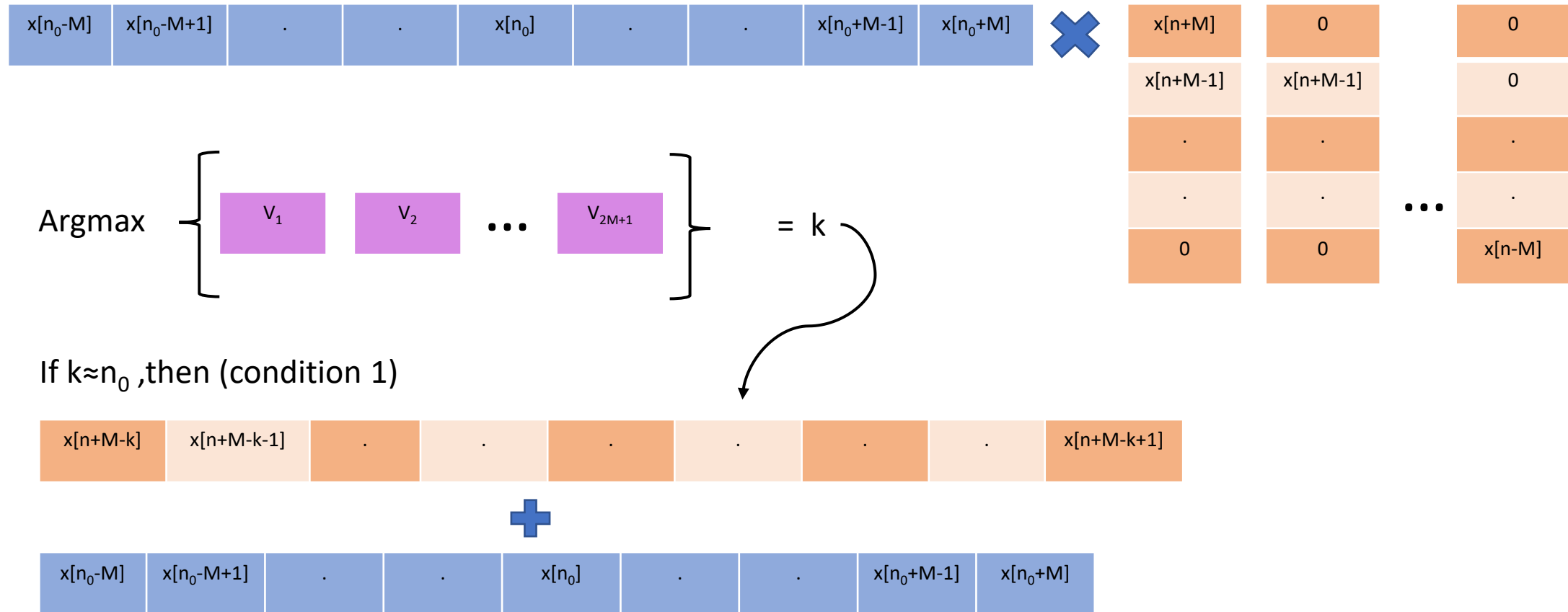


# Methodology - Template Generation

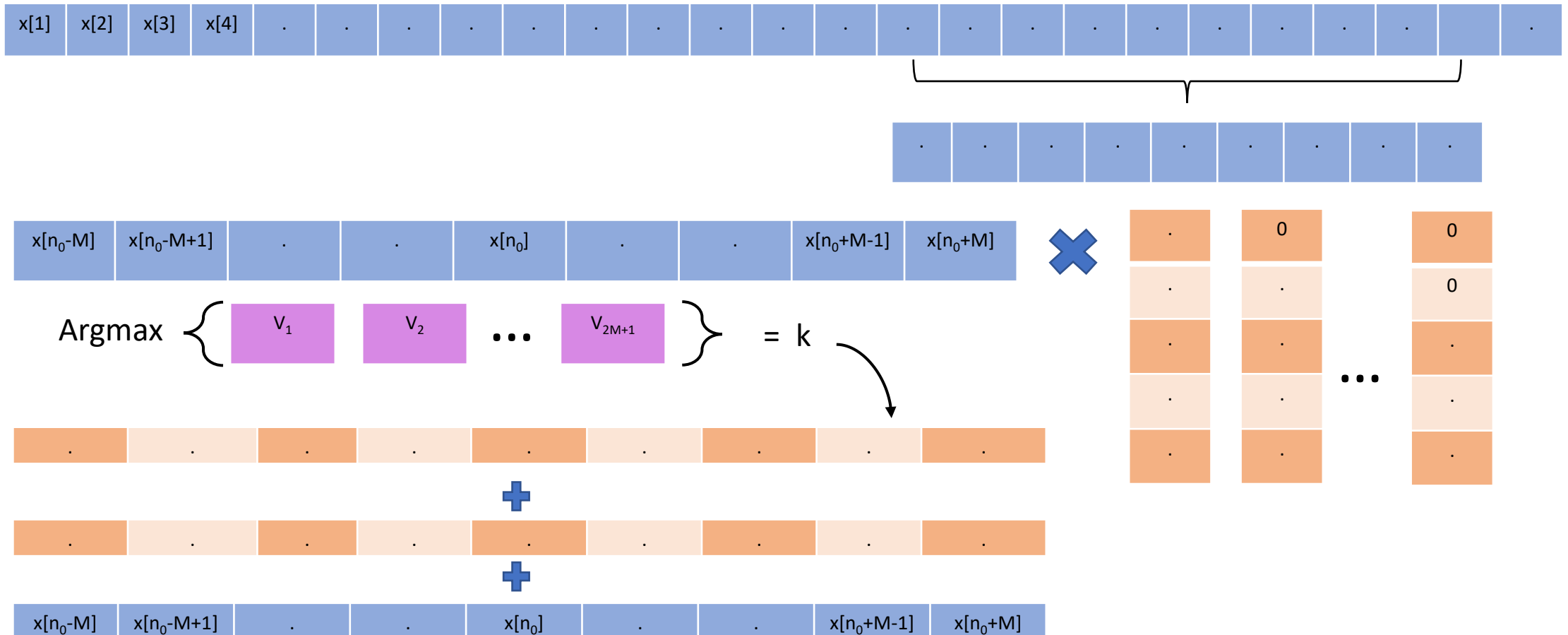
$x[n-M]$	$x[n-M+1]$	.	.	$x[n]$	.	.	$x[n+M-1]$	$x[n+M]$
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$x[n+M]$	$x[n+M-1]$	.	.	$X[n]$	$x[n-1]$	.	.	$x[n-M+1]$	$x[n-M]$	0	.	.	0
0	$x[n+M]$	$x[n+M-1]$	.	.	$x[n]$	$x[n-1]$	.	.	$x[n-M+1]$	$x[n-M]$	0	.	0
.	.	.	.	.	.	.	.	.	.	.	.	.	.
.	.	.	.	.	.	.	.	.	.	.	.	.	.
0	0	.	0	0	.	.	.	0	0	$x[n+M]$	.	$x[n-M+1]$	$x[n-M]$

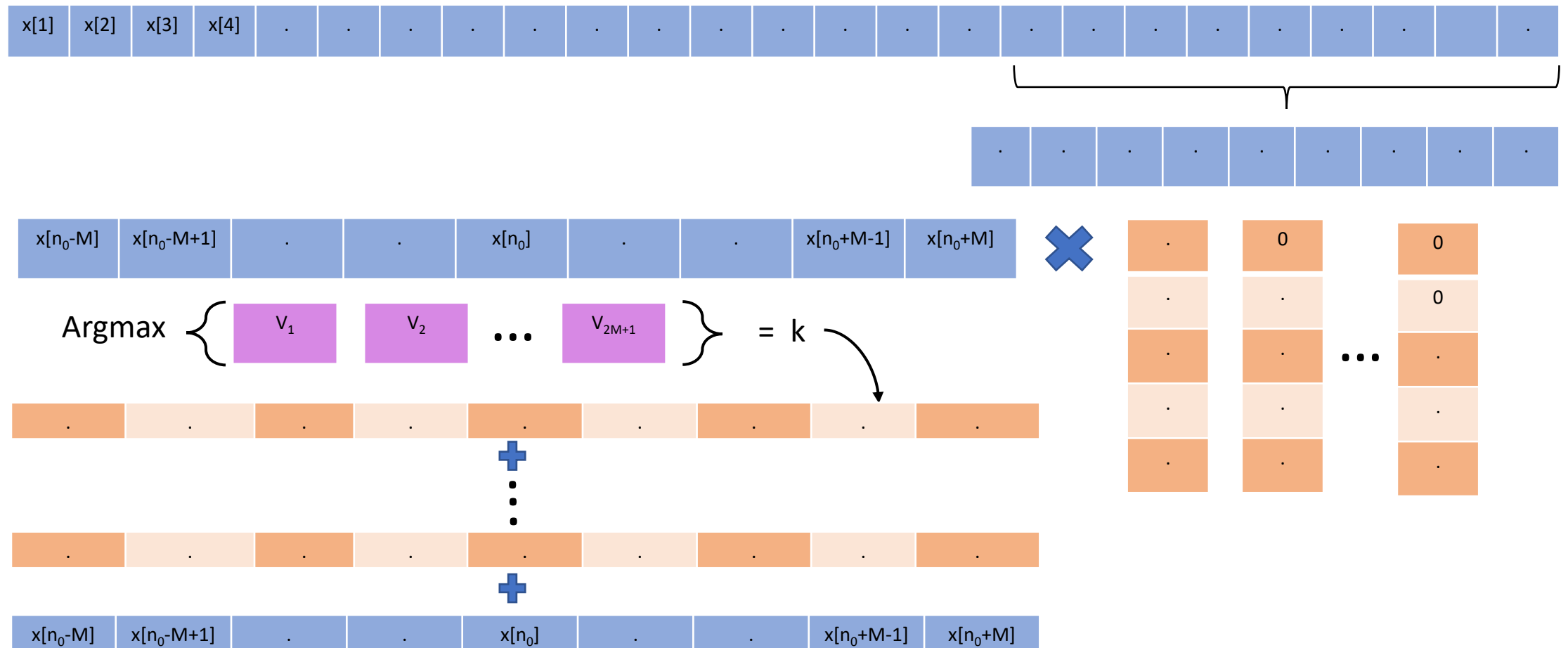
# Methodology - Template Generation



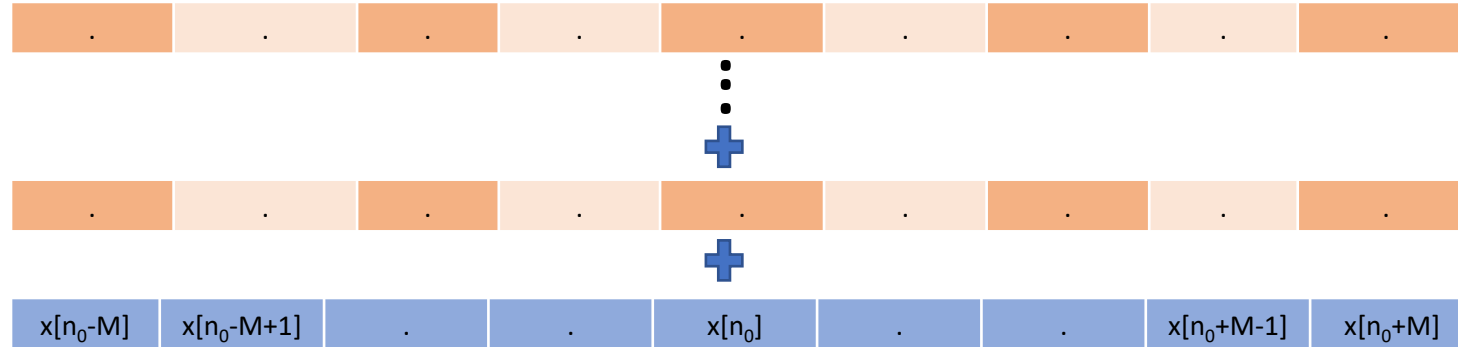
# Methodology - Template Generation



# Methodology - Template Generation



# Methodology - Template Generation

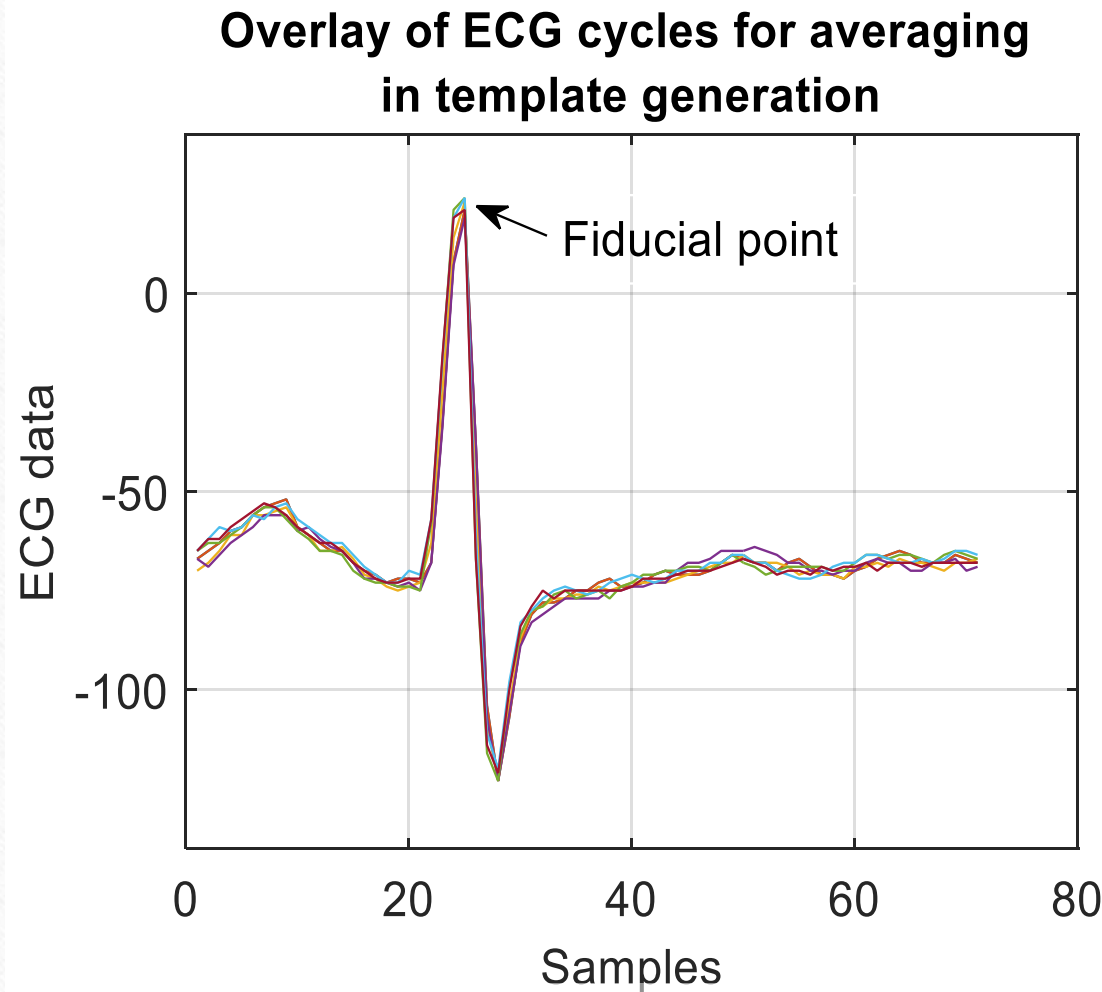


No of times condition  
1 was satisfied

Is the template  $T$







*Fig. 1*

## Methodology - Template Generation

- 10 cycles.
- template length- 70% of the average time period.
- missed fiducial point- segment discarded (condition 1).
- ECG- Q wave

# Methodology- cSQI calculation

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- Assigns quality value for each signal sample.
- Signal window centered at that sampled.
- cSQI [ $t_0$ ]  $\rightarrow$  inverse of the variance of the difference between the template and signal window centered at  $t_0$  at the point of maximum correlation with the template.
- cSQI [ $t_1$ ]  $\rightarrow$  shifting the window.



# Methodology- cSQI calculation

**Table 2: Algorithm for cSQI calculation**

**Initialize and calculate  $c[0]$ :**

- A. Let  $T_{(c)}$  be the Toeplitz correlation matrix of the template  $T$ .  $T_{(c)}[u]$  indicates  $u^{\text{th}}$  row of the matrix with  $u \in [0, 2M]$
- B. Signal vector  $S_0$  of length  $2M+1 \triangleq [s[-M], \dots, s[0], \dots, s[M]]$  where  $M$  has been decided based on the time period, centered at  $s[0]$ .
- C. Lag sequence  $L = [-M \ -M+1 \ \dots 0 \ \dots M-1 \ M]$
- D. Calculate  $A' = S_0 \times T$  where  $A'$  is the L-R flipped result of the correlation sequence
- E. Lag  $t = L[\text{argmax}(A)]$
- F.  $c[0] = (\text{var}(S_0 - T^{(t)}))^{-1}$  and  $b = s[-M]$

**Loop till no signal is read:**

For  $i=1$  to  $Z$  in steps of 1

- a. Window centered at  $s[i]$ ,  $S_i$  of length  $2M+1$ .
- b.  $NR = s[i+M]$ .  $T_{(c)}[2M]$  and  $FR = b$ .  $T_{(c)}[0]$
- c. Calculate L-R flipped correlation sequence  $A' = (A' - FR)^{(1)} + NR$
- d. Lag  $t = L[\text{argmax}(A)]$
- e.  $c[i] = (\text{var}(S_k - T^{(t)}))^{-1}$  and  $b = s[i-M]$

**End**

$cSQI = \text{LPF}(c)$ , where the low pass filter could be a moving average filter to avoid rapid variations that can be attributed to edge effects of windowing. The block diagram of the algorithm for a circuit implementation is shown in Fig 1.

# cSQI calculation

$T[-M]$	$T[-M+1]$	.	.	.	.	.	$T[M-1]$	$T[M]$
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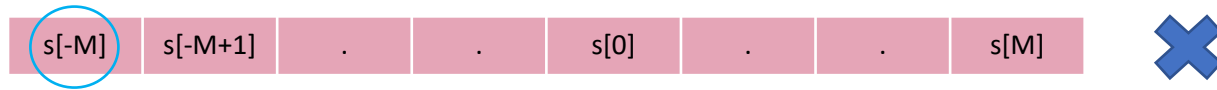
$T[n+M]$	$T[n+M-1]$	.	.	$T[n]$	$T[n-1]$	.	.	$T[n-M+1]$	$T[n-M]$	0	.	.	0
0	$T[n+M]$	$T[n+M-1]$	.	.	$T[n]$	$T[n-1]$	.	.	$T[n-M+1]$	$T[n-M]$	0	.	0
.	.	.	.	.	.	.	.	.	.	.	.	.	.
.	.	.	.	.	.	.	.	.	.	.	.	.	.
0	0	.	0	0	.	.	.	0	0	$T[n+M]$	.	$T[n-M+1]$	$T[n-M]$

.	.	.	$s[3]$	$s[2]$	$s[1]$	$s[0]$	$s[1]$	$s[2]$	$s[3]$	.	.	.	.	.	.	.	.	.	.
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$s[-M]$	$s[-M+1]$	.	.	$s[0]$	.	.	$s[M]$
---------	-----------	---	---	--------	---	---	--------

# cSQI calculation



$T[n+M]$	$T[n+M-1]$	.	.	$T[n]$	$T[n-1]$	.	.	$T[n-M+1]$	$T[n-M]$	0	.	.	0
0	$T[n+M]$	$T[n+M-1]$	.	.	$T[n]$	$T[n-1]$	.	.	$T[n-M+1]$	$T[n-M]$	0	.	0
.	.	.	.	.	.	.	.	.	.	.	.	.	.
.	.	.	.	.	.	.	.	.	.	.	.	.	.
0	0	.	0	0	.	.	.	0	0	$T[n+M]$	.	$T[n-M+1]$	$T[n-M]$

$$= A_0' = \begin{array}{|c|c|c|c|c|c|c|c|c|c|} \hline A[M] & A[M-1] & . & . & A[0] & . & . & A[-M+1] & A[-M] \\ \hline \end{array}$$

$$\Rightarrow A_0 = \begin{array}{|c|c|c|c|c|c|c|c|c|c|} \hline A[-M] & A[-M+1] & . & . & A[0] & . & . & A[M-1] & A[M] \\ \hline \end{array}$$



# cSQI calculation

Lag Matrix, L=

-M	-M+1	.	.	0	.	.	M-1	M
----	------	---	---	---	---	---	-----	---

Argmax {

A[-M]	A[-M+1]	.	.	A[0]	.	.	A[M-1]	A[M]
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} = arg

1	2	3	.	.	arg	.	.	2M+1
-M	-M+1	.	.	0	.	.	M-1	M

Lag t

$c[0] =$

1

Var

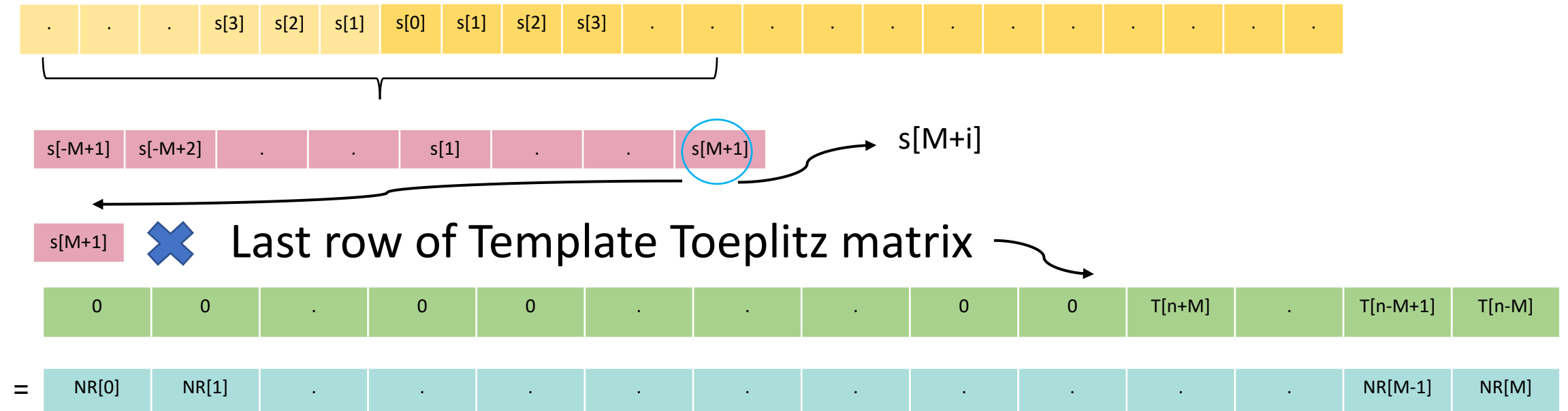
$T^{(t)} =$

A[-M]	A[-M+1]	.	.	A[0]	.	.	A[M-1]	A[M]
T[-M+t]	T[-M+1+t]	.	.	.	.	.	T[-M+t-2]	T[-M+t-1]


# cSQI calculation

For every subsequent  $c[i]$ :

To calculate,  $c[1] =$



# cSQI calculation

$s[-M]$   First row of Template Toeplitz matrix

$s[-M-(i-1)]$

$T[n+M]$	$T[n+M-1]$	.	.	$T[n]$	$T[n-1]$	.	.	$T[n-M+1]$	$T[n-M]$	0	.	.	0
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$=$ 

$FR[-M]$	$FR[-M+1]$	.	.	.	$FR[0]$	.	.	.	.	.	.	$FR[M-1]$	$FR[M]$
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$A_{i-1}' - FR =$ 

$A[M]-FR[-M]$	$A[M-1]-FR[-M+1]$	.	.	$A[0]-FR[0]$	.	.	$A[-M+1]-FR[M-1]$	$A[-M]-FR[M]$
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$(A_0' - FR)^{(1)} =$ 

$A[M-1]-FR[-M+1]$	.	.	$A[0]-FR[0]$	.	.	$A[-M+1]-FR[M-1]$	$A[-M]-FR[M]$	$A[M]-FR[-M]$
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$A_i' = A_1' =$ 

$A[M-1]-FR[-M+1]$	.	.	$A[0]-FR[0]$	.	.	$A[-M+1]-FR[M-1]$	$A[-M]-FR[M]$	$A[M]-FR[-M]$
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 $+$ 

$NR[0]$	$NR[1]$	.	.	.	.	.	$NR[M-1]$	$NR[M]$
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# cSQI calculation

$$A_1 = A_i = \begin{array}{|c|c|c|c|c|c|c|c|c|} \hline A[-M+1] & A[-M+2] & . & . & A[1] & . & . & A[M] & A[M+1] \\ \hline \end{array}$$

$$\text{Argmax} \left\{ \begin{array}{|c|c|c|c|c|c|c|c|c|} \hline A[-M+1] & A[-M+2] & . & . & A[1] & . & . & A[M] & A[M+1] \\ \hline \end{array} \right\} = \arg$$

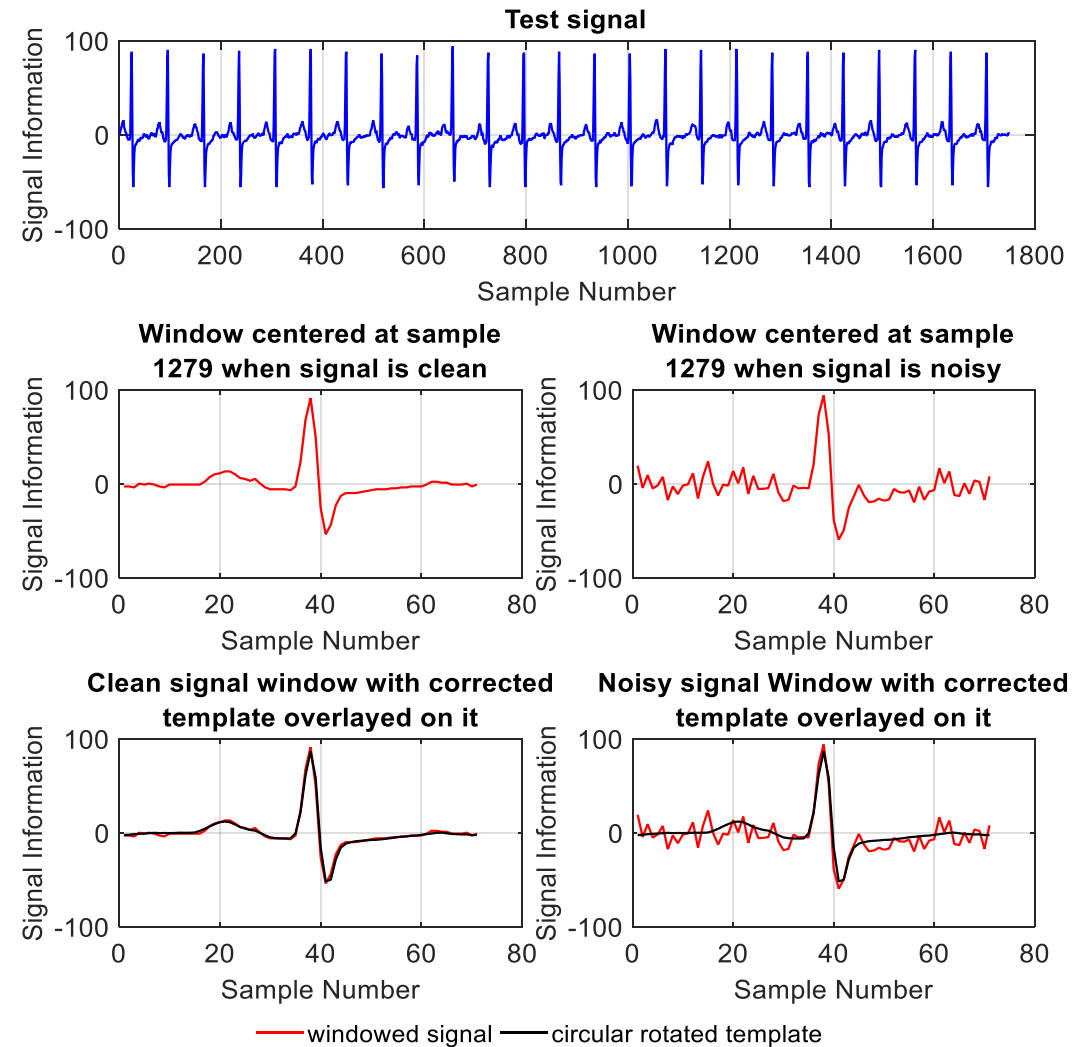
$$\begin{array}{cccccccccc} 1 & 2 & 3 & . & \arg & . & . & . & 2M+1 \\ -M & -M+1 & . & . & . & . & . & M-1 & M \end{array}$$

Lag t

$$c[1] = \frac{1}{\text{Var}} \left( \begin{array}{|c|c|c|c|c|c|c|c|c|} \hline A[-M+1] & A[-M+2] & . & . & A[1] & . & . & A[M] & A[M+1] \\ \hline T^{(t)} = T[-M+t] & T[-M+1+t] & . & . & . & . & . & T[-M+t-2] & T[-M+t-1] \\ \hline \end{array} \right)$$

# Methodology- cSQI calculation

- cSQI - corrupted by 5 dB Gaussian noise and when clean.
- The template generated (Fig. 1) is circularly rotated – align with fiducial feature.
- Difference - would correspond to noise.





# Performance Evaluation

- cSQI
  - 50 Hz power line interference,
  - Baseline Wander,
  - Muscle Artifacts, and
  - Electrode Motion at -10 dB.
- For all noisy samples- cSQI lower than clean samples

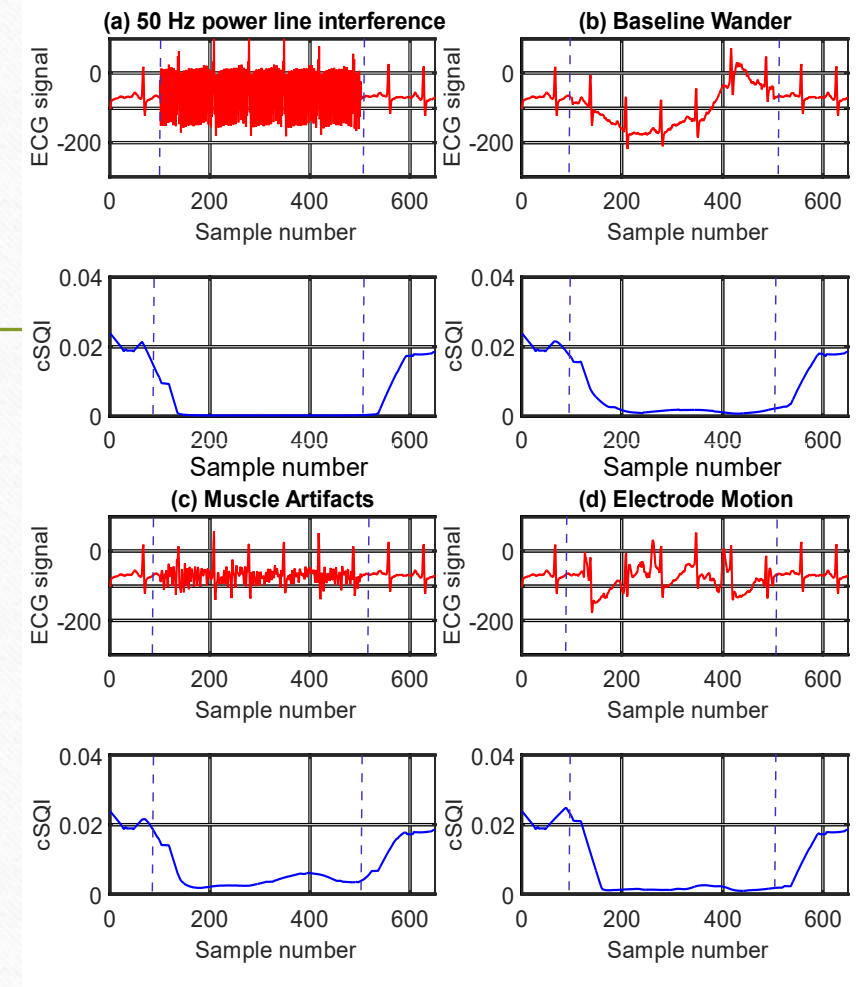


Fig. 3.

# Performance Evaluation

- The cSQI vs SNR plot
- SQI averaged over the entire signal
- cSQI- almost linear behavior in the medium SNR ranges

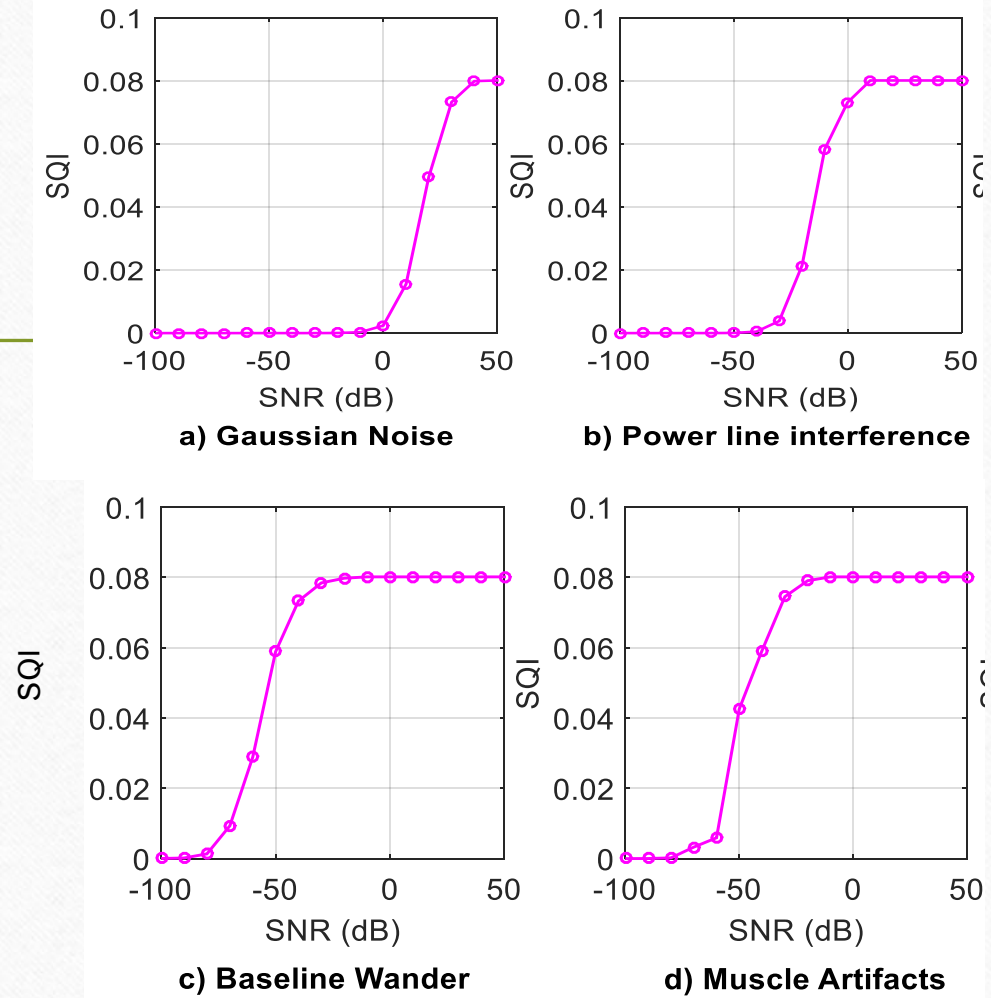


Fig. 4.

## Performance Evaluation

cSQI performance- records  
of CinC 2011 challenge.

Validation set score - 0.938.

Test set score - 0.904  
(Event 1)

# Circuit Diagram

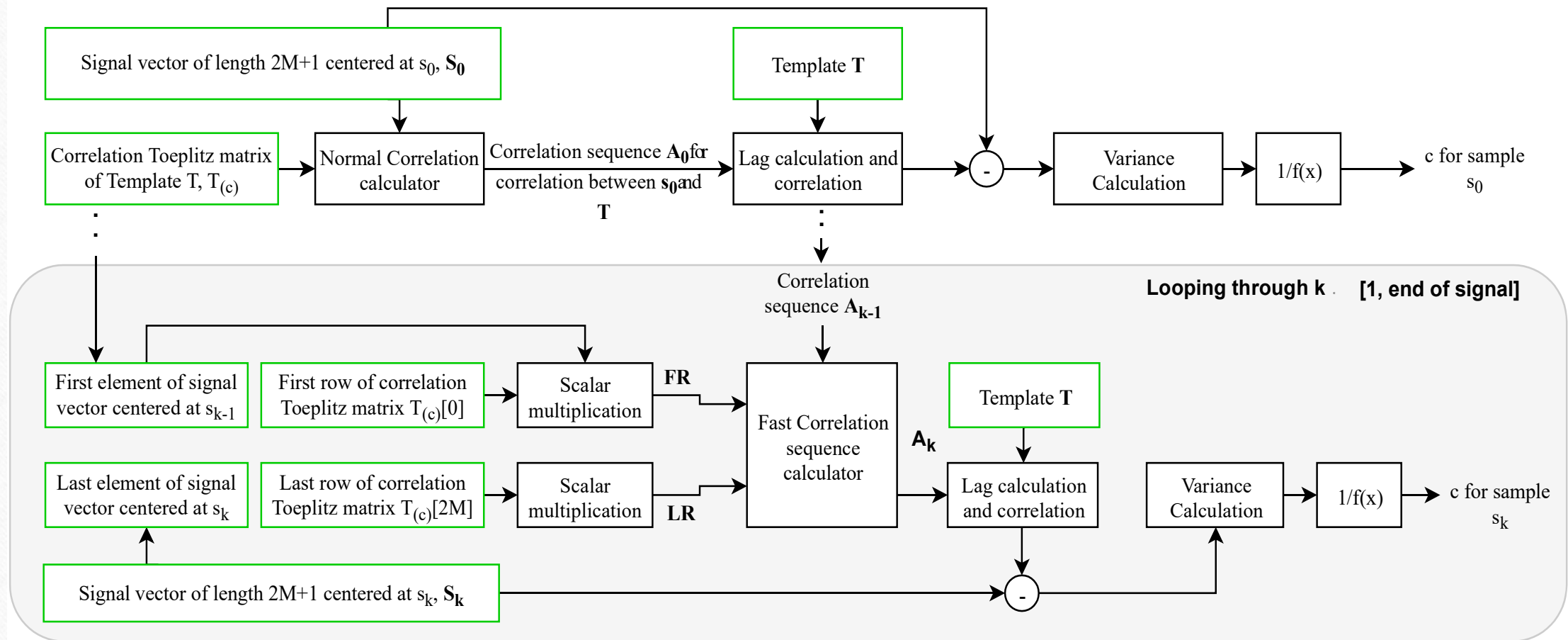


Fig. 4.



# Complexity Evaluation

Operation	Count	Count for N=10, M=35 for $F_s=125$
<b>Multiplication</b>	$N(8M^2+6M+1)$	100110
<b>Addition</b>	$N(8M^2+4M+1)$	99410

TABLE 3. Complexity of template generation

Operation	Count	Count for M=35 for $F_s=125$
<b>Multiplication</b>	$8M^2+8M+3$	10083
<b>Addition</b>	$8M^2+6M+1$	10011

TABLE 4. Complexity of cSQI calculation for the first  $c[0]$

- Low computational complexity.
- Smart Algorithm design.

Operation	Count	Count for M=35 for $F_s=125$
<b>Multiplication</b>	$10M+3$	353
<b>Addition</b>	$12M+3$	423

TABLE 5. Complexity of cSQI calculation for every subsequent sample after initialization



## Conclusions

Novel generalized signal quality indicator

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Any periodic or quasi-periodic signal- identifiable fiducial point.

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A monotonically increasing function of SNR.

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Low complexity- attractive option for edge IoT devices.



THANK YOU