

# Software quality and formal methods: Hoare/Dijkstra approach

Dr. Ivan S. Zapreev

Neat Software Designs

2020-01-20

## Global Outline:

- Software Quality
- Programming Languages
- Formal Methods
- Frama - C
- Verification in practice
- Concluding remarks

Software  
quality and  
formal  
methods:  
Hoare/Dijkstra  
approach

Dr. Ivan S.  
Zapreev

Software  
Quality

Programming  
Languages

Formal  
Methods

Frama - C

Verification in  
practice

Concluding  
remarks

# Software Quality

# Software Quality: Outline

Software  
quality and  
formal  
methods:  
Hoare/Dijkstra  
approach

Dr. Ivan S.  
Zapreev

Software  
Quality

Programming  
Languages

Formal  
Methods

Frama - C

Verification in  
practice

Concluding  
remarks

- Our Motivation
- Software Development
- Software Verification

# Our Motivation: Therac-25

- Years 1985–1987:
  - Radiation therapy overdose
  - Control software flaw:
    - Race conditions
  - Death of 6 (six) cancer patients



Figure 1: Radiation therapy

## Our Motivation: Ariane-5

- Year 1996:
  - Missile crash
  - Control software flaw:
    - 64-bit float to 16-bit int
  - \$7 billion development program
  - \$500 million cargo



# Our Motivation: Toyota Camry

- Year 2005
  - Sudden unintended acceleration:
  - Control software flaw:
    - Recursion causing stack overflow
  - 89 deaths and 57 injuries
  - \$1.2 billion compensations



Figure 3: Automobiles

# Our Motivation: Plenty More

The 12 Software Bugs That Caused Epic Failures: [<link>](#)

# BUGS



# BUGS EVERYWHERE



# Software Development: V-model

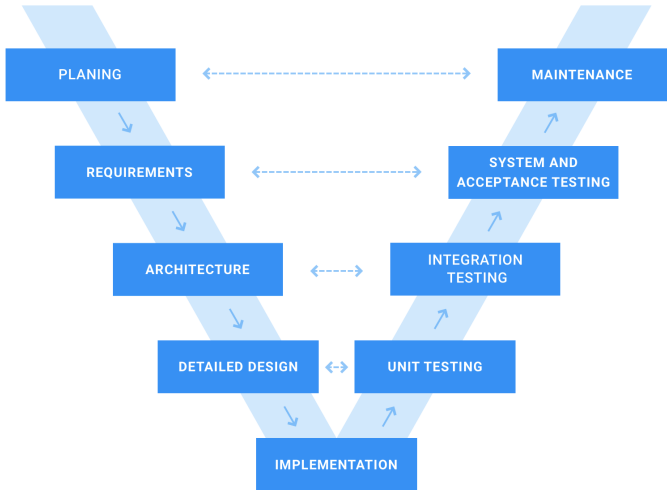


Figure 4: Software development process

Software  
quality and  
formal  
methods:  
Hoare/Dijkstra  
approach

Dr. Ivan S.  
Zapreev

Software  
Quality

Programming  
Languages

Formal  
Methods

Frama - C

Verification in  
practice

Concluding  
remarks

# Software Development: V & V

Software  
quality and  
formal  
methods:  
Hoare/Dijkstra  
approach

Dr. Ivan S.  
Zapreev

Software  
Quality

Programming  
Languages

Formal  
Methods

Frama - C

Verification in  
practice

Concluding  
remarks

Is formally defined in, e.g.: ISO-9000:2015:

- **Verification** – *“Confirmation, through the provision of objective evidence, that specified requirements have been fulfilled.”*
- **Validation** – *“Confirmation, through the provision of objective evidence, that the requirements for a specific intended use or application have been fulfilled.”*

# Software Development: Testing

- **Verification:**
  - Are we building the product right?
  - Does the system comply with its specification?
- **Validation:**
  - Are we building the right product?
  - Does the system meet the needs of the customer?

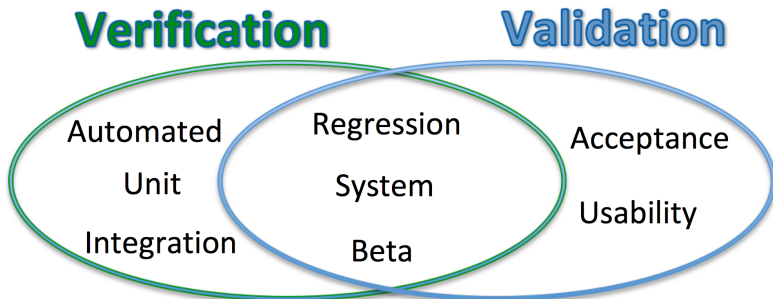


Figure 5: Devision of testing types

# Formal Verification

## Facts:

- No globally recognized definition of Formal Methods<sup>1</sup>.
- Local attempts to have one<sup>2</sup>, e.g.:

*“Formal methods are techniques used to model complex systems as mathematical entities.”*

*“By building a rigorous model of a complex system, it is possible to verify the system’s properties in a more thorough fashion than empirical testing.”*

## Conclusion:

Formal methods are techniques suitable for Verification.

---

<sup>1</sup>“Formal Methods for Industrial Critical Systems”, S. Gnesi, T. Margaria

<sup>2</sup>“Formal Methods”, Michael Collins, CMU

# Software Verification

## Goal:

A program shall satisfy a formal specification of its behavior.

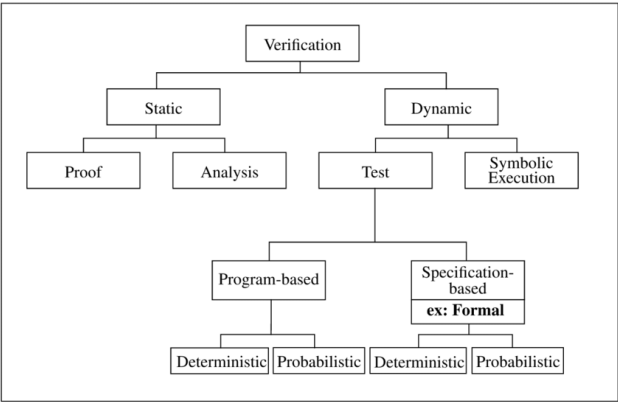


Figure 6: Verification methods

Software  
quality and  
formal  
methods:  
Hoare/Dijkstra  
approach

Dr. Ivan S.  
Zapreev

Software  
Quality

Programming  
Languages

Formal  
Methods

Frama - C

Verification in  
practice

Concluding  
remarks

# Programming Languages

# Programming Languages: Outline

Software  
quality and  
formal  
methods:  
Hoare/Dijkstra  
approach

Dr. Ivan S.  
Zapreev

Software  
Quality

Programming  
Languages

Formal  
Methods

Frama - C

Verification in  
practice

Concluding  
remarks

- Language generations
- Declarative vs. Imperative
- What is ANSI-C?

# Language generations

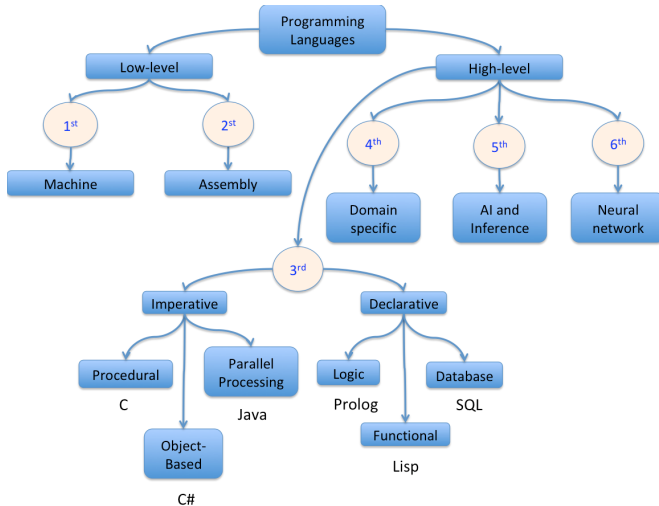


Figure 7: Generations of Programming languages



# Declarative vs. Imperative: Main

- *Declarative* – Expresses what to accomplish without specifying concrete steps.

```
//Declarative `JavaScript`  
var arr_dbl = arr.map((x) => x * 2)
```

- *Imperative* – Describes computation in terms of statements that change a program state.

```
//Imperative `JavaScript`  
var arr_dbl = []  
for (let i = 0; i < arr.length; i++) {  
    arr_dbl.push(arr[i] * 2)  
}
```

# Declarative vs. Imperative: Test

Software  
quality and  
formal  
methods:  
Hoare/Dijkstra  
approach

Dr. Ivan S.  
Zapreev

Software  
Quality

Programming  
Languages

Formal  
Methods

Frama - C

Verification in  
practice

Concluding  
remarks

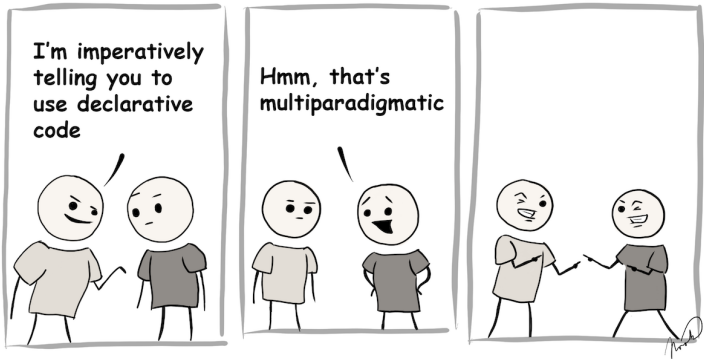


Figure 8: If you laugh, it means you've passed

# What is ANSI-C: Old C

## Procedural language:

Is an imperative language in which the program is built from one or more subroutines commonly known as `functions`.

## C language:

C is an *imperative procedural* language.

## Defining ANSI-C:

ANSI-C is a common name for two equivalent language specs:

- C89 by American National Standards Institute (ANSI)
- C90 by International Organization for Standardization (ISO)

Software  
quality and  
formal  
methods:  
Hoare/Dijkstra  
approach

Dr. Ivan S.  
Zapreev

Software  
Quality

Programming  
Languages

Formal  
Methods

Frama - C

Verification in  
practice

Concluding  
remarks

# Formal Methods

# Formal Methods: Outline

Software  
quality and  
formal  
methods:  
Hoare/Dijkstra  
approach

Dr. Ivan S.  
Zapreev

Software  
Quality

Programming  
Languages

Formal  
Methods

Frama - C

Verification in  
practice

Concluding  
remarks

- Formal Verification
- Hoare Approach
- Dijkstra Extension

# Formal verification

**Question:** Does formal *validation* exist?

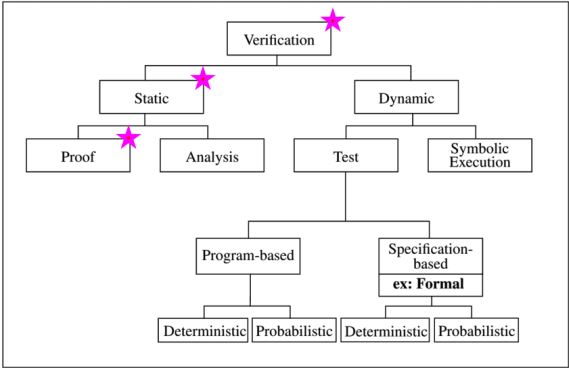


Figure 9: Formal correctness proving

*Prove* conformance to specifications for *imperative programs*.

## Hoare Approach<sup>3</sup>

**Hoare triples:**  $\{P\} C \{Q\}$

$C$  - code;  $P$  - pre-condition;  $Q$  - post-condition;

**Axioms**, e.g. *Skip* and *Assign*:

$$\overline{\{P\} \text{skip} \{P\}} \text{ and } \overline{\{P[E/V]\} V := E \{P\}}$$

Where  $E$  is any expression and  $V$  is any variable.

**Inference rules**, e.g. *Composition* and *Conditional*:

$$\frac{\{P\} S_1 \{R\}, \{R\} S_2 \{Q\}}{\{P\} S_1; S_2 \{Q\}} \text{ and } \frac{\{B \wedge P\} S \{Q\}, \{\neg B \wedge P\} T \{Q\}}{\{P\} \text{ if } B \text{ then } S \text{ else } T \text{ elseif } \{Q\}}$$

**Partial correctness:** If  $P$  holds before executing  $C$  then  $Q$  holds afterwards, **ONLY** if  $C$  terminates.

---

<sup>3</sup>"An Axiomatic Basis for Computer Programming", Tony Hoare, 1969.

## Dijkstra Extension<sup>4</sup>

The *weakest precondition calculus* for

- A predicate transform semantics to mechanize the proofs.
- Explains how  $C$  transforms  $P$  into  $Q$ .

### Backward reasoning:

- Based on  $Q$  and  $C$  calculate the *weakest pre-condition*  $\hat{P}$
- If  $P \implies \hat{P}$ , then the proof is complete

### Forward reasoning:

- Based on  $P$  and  $C$  calculate the *strongest post-condition*  $\hat{Q}$
- If  $\hat{Q} \implies Q$ , then the proof is complete

---

<sup>4</sup>“Guarded commands, non-determinacy and formal derivation of programs”, Edsger Dijkstra, 1975



Software  
quality and  
formal  
methods:  
Hoare/Dijkstra  
approach

Dr. Ivan S.  
Zapreev

Software  
Quality

Programming  
Languages

Formal  
Methods

**Frama - C**

Verification in  
practice

Concluding  
remarks

# Frama - C

# Frama - C: Outline

- Platform description
- Plugins overview
- What is ACSL?

# Platform description

A plug-in-based open-source cross-platform framework for ANSI-C source-code analysis:

- Browsing unfamiliar code
- Static code analysis
- Dynamic code analysis
- Code transformations
- Certification of critical software

You can easily build upon the existing plug-ins to implement your own analysis.

# Plugins overview: Main

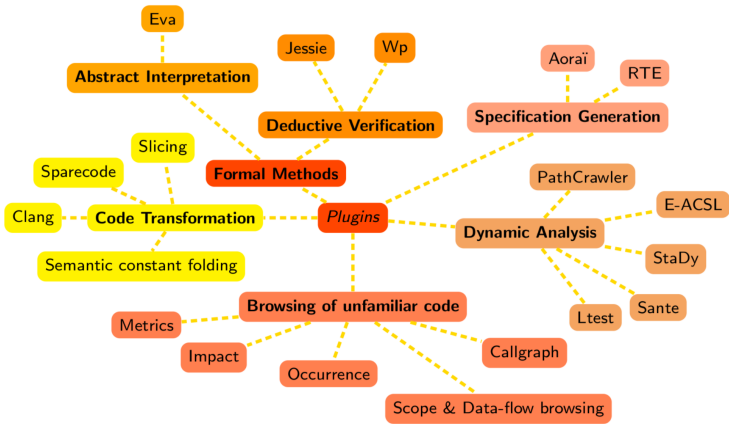


Figure 10: Frama-C plugins

# Plugins overview: WP

WP – *weakest precondition* for ACSL specs of ANSI-C programs.

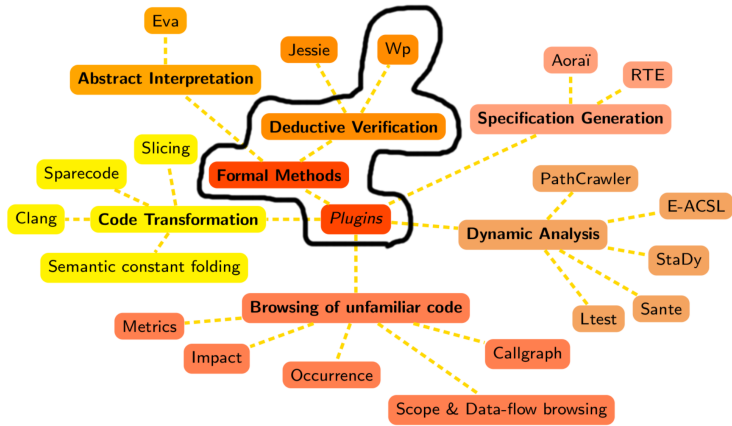


Figure 11: Frama-C WP plugin

# What is ACSL: General

In short:

- ACSL – ANSI/ISO C Specification Language
- Allows to formally specify properties of a C program

It is all about function contracts:

```
/*@ ensures \result >= x && \result >= y;  
    ensures \result == x || \result == y;  
*/  
int max (int x, int y) {  
    return(x > y) ? x : y;  
}
```

A function contract is a combination of:

- post-conditions - ensures
- pre-conditions - requires

# What is ACSL: Pointers

ACSL allows to reason about, e.g.:

- Pointers
- Arrays
- Termination

Consider pointers:

```
/*@ requires \valid(p) && \valid(q);  
    ensures *p <= *q;  
    */  
void max_ptr (int *x, int *y) {  
    if(*x > *y) {  
        int tmp = *x;  
        *x = *y;  
        *y = tmp;  
    }  
}
```

# What is ACSL: Completeness

Is the following `max_ptr` implementation correct?

```
/*@ requires \valid(p) && \valid(q);
    ensures *p <= *q;
*/
void max_ptr (int *x, int *y) {
    *p = *q = 0;
}
```

Is the following specification *complete*?

```
/*@ requires \valid(p) && \valid(q);
    ensures *p <= *q;
    ensures (*p == \old(*p) && *q == \old(*q)) ||
           (*p == \old(*q) && *q == \old(*p));
*/
void max_ptr(int*p, int*q);
```



# What is ACSL: The whole spec.

The complete specification v1.4 has 93 pages:

[https://frama-c.com/download/acsl\\_1.4.pdf](https://frama-c.com/download/acsl_1.4.pdf)



Figure 12: Feel free to explore

Software  
quality and  
formal  
methods:  
Hoare/Dijkstra  
approach

Dr. Ivan S.  
Zapreev

Software  
Quality  
  
Programming  
Languages

Formal  
Methods

Frama - C

Verification in  
practice

Concluding  
remarks

# Verification in practice

# Verification in practice: Outline

Software  
quality and  
formal  
methods:  
Hoare/Dijkstra  
approach

Dr. Ivan S.  
Zapreev

Software  
Quality  
  
Programming  
Languages  
  
Formal  
Methods  
  
Frama - C  
  
Verification in  
practice  
  
Concluding  
remarks

- Verification Examples
- Verification Outcomes
- The morale

# Verification Examples: abs(.)

Software  
quality and  
formal  
methods:  
Hoare/Dijkstra  
approach

Dr. Ivan S.  
Zapreev

Software  
Quality  
Programming  
Languages

Formal  
Methods

Frama - C

Verification in  
practice

Concluding  
remarks

Consider a primitive integer absolute value computation:

```
/*@  
    ensures \result >= 0;  
*/  
int abs(int val) {  
    if(val < 0) return -val;  
    return val;  
}
```

The verification shall return **OK**, right?

# Verification Examples: Issue #1

**NOP** - the verification results are inconclusive:

The screenshot displays the Frama-C WP (Wp) interface. The top pane shows a C code snippet for a function `abs`. The code includes an `/*@ ensures` block with three post-conditions: `(\old(val) == 0 => \result == 0) ^`, `(\old(val) > 0 => \result == \old(val)) ^`, and `(\old(val) < 0 => \result == -\old(val));`. The function body calculates `__retres` based on whether `val` is negative, and then returns it. A specific line is highlighted in yellow: `/*@ assert rte: signed_overflow: -2147483647 <= val; */` followed by `__retres = - val;`. The bottom pane shows the WP Goals table.

Module	Goal	Model	Qed	Script	Alt-Ergo 2.3.0
abs	Post-condition	Typed		—	
abs	Assertion 'rte,signed_overflow'	Typed	—	—	

Figure 13: WP detects a possible overflow

## Verification Examples: Issue #2

Extend the specification with a pre-condition:

```
/*@ requires INT_MIN < val;  
    ensures \result >= 0;  
    */  
int abs(int val) {  
    if(val < 0) return -val;  
    return val;  
}
```

The verification is **OK**, but are we complete (?), consider:

```
/*@ requires INT_MIN < val;  
    ensures \result >= 0;  
    */  
int abs(int val) {  
    return 1;  
}
```

# Verification Examples: Final?

An explicit `\result` value specification makes it complete:

```
/*@ requires INT_MIN < val;  
    ensures (val == 0 ==> \result == 0) &&  
           (val > 0 ==> \result == val) &&  
           (val < 0 ==> \result == -val);  
*/  
int abs(int val) {  
    if(val < 0) return -val;  
    return val;  
}
```

What if the implementation was wrong?

Would we be able to identify the root-cause?

## Verification Examples: Faulty

Consider a lengthy and potentially buggy implementation:

```
/*@ requires INT_MIN < val;  
    ensures (val == 0 ==> \result == 0) &&  
           (val > 0 ==> \result == val) &&  
           (val < 0 ==> \result == -val);  
*/  
int abs(int val) {  
    if(val == 0) {  
        return 0;  
    } else {  
        if(val < 0) {  
            return val;  
        } else {  
            return -val;  
        }  
    }  
}
```



## Verification Examples: Issue #3

The verification is inconclusive, the entire post condition failed!

The screenshot displays the Frama-C IDE interface. The top pane shows a C program with a post-condition. The bottom pane shows a table of verification results.

```
/*@ requires -2147483647 - 1 < val;
   ensures
      (\old(val) == 0 => \result == 0) ^
      (\old(val) > 0 => \result == \old(val)) ^
      (\old(val) < 0 => \result == -\old(val));
*/
int abs(int val)
{
    int __retres;
    if (val == 0) {
        __retres = 0;
        goto return_label;
    }
    else {
        if (val < 0) {
```

Module	Goal	Model	Qed	Script	Alt-Ergo 2.3.0
abs	Post-condition	Typed	—	—	✂
abs	Assertion 'rte,signed_overflow'	Typed	●	—	

Figure 14: What is the actual reason?

## Verification Examples: Split

What if we split the post-condition from:

```
/*@ requires INT_MIN < val;  
    ensures (val == 0 ==> \result == 0) &&  
           (val > 0 ==> \result == val) &&  
           (val < 0 ==> \result == -val);  
*/
```

into separate statements:

```
/*@ requires INT_MIN < val;  
    ensures (val == 0 ==> \result == 0);  
    ensures (val > 0 ==> \result == val);  
    ensures (val < 0 ==> \result == -val);  
*/
```

and then run verification again!

# Verification Examples: Insights

This is enough hint to know where to look:

```
/*@ requires -2147483647 - 1 < val;
    ensures \old(val) == 0 => \result == 0;
    ensures \old(val) > 0 => \result == \old(val);
    ensures \old(val) < 0 => \result == -\old(val);
*/
int abs(int val)
{
    int __retres;
    if (val == 0) {
        {
            __retres = 0;
            goto return_label;
        }
    }
    else {
        if (val < 0) {
            {

```

\*\*\*\*\*

Information

Messages (2)

Console

Properties

Values

Red Alarms

WP Goals

Property ▾

All Results ▾

Module	Goal	Model	Qed	Script	Alt-Ergo 2.3.0	C
abs	Post-condition	Typed	<div></div>	—		
abs	Post-condition	Typed	—	—	<div></div>	
abs	Post-condition	Typed	—	—	<div></div>	

Figure 15: Finding the root-causes

# Verification Examples: Bugs

Now we can identify the actual bugs:

```
/*@ requires INT_MIN < val;
    ensures (val == 0 ==> \result == 0);
    ensures (val > 0 ==> \result == val);
    ensures (val < 0 ==> \result == -val);
*/
int abs(int val) {
    if(val == 0) {
        return 0;          //OK
    } else {
        if(val < 0) {
            return val;    //BUG #1, should return -val
        } else {
            return -val;   //BUG #2, should return val
        }
    }
}
```

# Verification Examples: Issue #4

Fixing BUG #1 turns the corresponding post-conditions green!

```

/*@ requires -2147483647 - 1 < val;
    ensures \old(val) == 0 => \result == 0;
    ensures \old(val) > 0 => \result == \old(val);
    ensures \old(val) < 0 => \result == -\old(val);
*/
int abs(int val)
{
    int retres;
    if (val == 0) {
        retres = 0;
        goto return_label;
    }
    else {
        if (val < 0) {
            /* assert that signed overflow: -2147483647 - 1 < val;
            */

```

```

main.c
31 /*@
32 requires INT_MIN < val;
33 ensures (val == 0 ==> \result == 0);
34 ensures (val > 0 ==> \result == val);
35 ensures (val < 0 ==> \result == -val);
36 */
37 int abs(int val) {
38     if(val == 0) {
39         return 0; //OK
40     } else {
41         if(val < 0) {
42             return -val; //OK
43         } else {
44             return -val; //BUG #2, should return val
45         }
46     }
47 }
48

```

Information		Messages (2)	Console	Properties	Values	Red Alarms	WP Goals	
		Property		All Results				
Module	Goal	Model	Qed	Script	Alt-Ergo 2.3.0	CVC4 1.7	CVC4 1.7 (counterexamples)	Coq 8.9.1
abs	Post-condition	Typed		—				
abs	Post-condition	Typed	—	—				
abs	Post-condition	Typed		—				
abs	Assertion 'rte,signed_overflow'	Typed		—				

Figure 16: Sequential issue resolution

# Verification Examples: Issue #5

Fixing BUG #2 yields an **OK** verification result!

```

/*@ requires -2147483647 - 1 < val;
  ensures \old(val) == 0 => \result == 0;
  ensures \old(val) > 0 => \result == \old(val);
  ensures \old(val) < 0 => \result == -\old(val);
*/
int abs(int val)
{
  int __retres;
  if (val == 0) {
    {
      __retres = 0;
      goto return_label;
    }
  }
  else {
    if (val < 0) {
      {

```

```

main.c
31 /*@
32 requires INT_MIN < val;
33 ensures (val == 0 ==> \result == 0);
34 ensures (val > 0 ==> \result == val);
35 ensures (val < 0 ==> \result == -val);
36 */
37 int abs(int val) {
38   if (val == 0) {
39     return 0; //OK
40   } else {
41     if (val < 0) {
42       return -val; //OK
43     } else {
44       return val; //OK
45     }
46   }
47 }

```

Information | Messages (2) | Console | Properties | Values | Red Alarms | WP Goals

Property ▾ All Results ▾

Module	Goal	Model	Qed	Script	Alt-Ergo 2.3.0	CVC4 1.7	CVC4 1.7 (counterexamples)	Coc
abs	Post-condition	Typed		—				
abs	Post-condition	Typed		—				
abs	Post-condition	Typed		—				
abs	Assertion 'rte,signed_overflow'	Typed		—				

Figure 17: Now we are all fine

# Verification Outcomes

If the proof is **OK**:

- The program satisfies the specification
- *Is the specification correct/complete?*

If the proof is **NOK**:

- An *incorrect implementation*
  - Find counter-example via test generation;
- A *wrong specification*
  - Complete spec. and proof analysis;
  - Change/extend the specification;
- A *prover's failure*
  - Alternative provers;
  - Interactive proof assistants;

## The morale

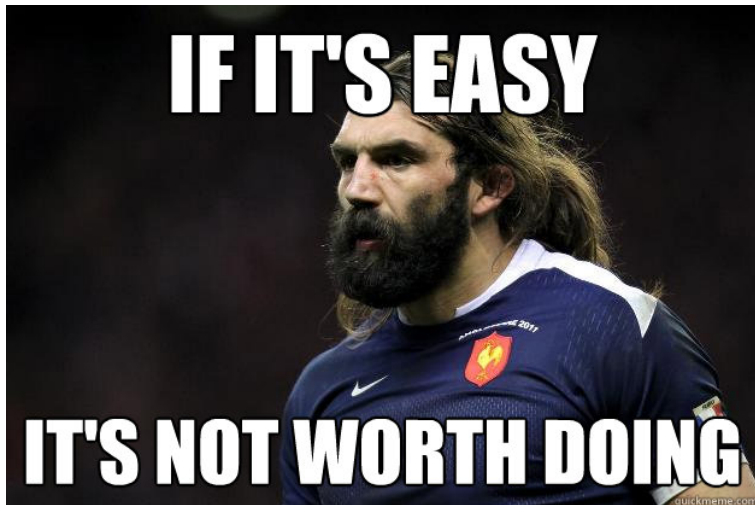


Figure 18: It is not so easy but ...



Software  
quality and  
formal  
methods:  
Hoare/Dijkstra  
approach

Dr. Ivan S.  
Zapreev

Software  
Quality

Programming  
Languages

Formal  
Methods

Frama - C

Verification in  
practice

Concluding  
remarks

## Concluding remarks

## Concluding remarks

We have looked into:

- Software quality and software engineering
- Programming language classification
- Formalization of software verification
- Hoare/Dijkstra approach to formal proving
- Frama-C a platform for ANSI-C code analysis
- Experienced practical program verification

We can conclude that:

- Formal software verification is useful
- It is not yet fully automated
- There is a lot more to learn about it!

Thank you and are there any questions?

I appreciate your time!

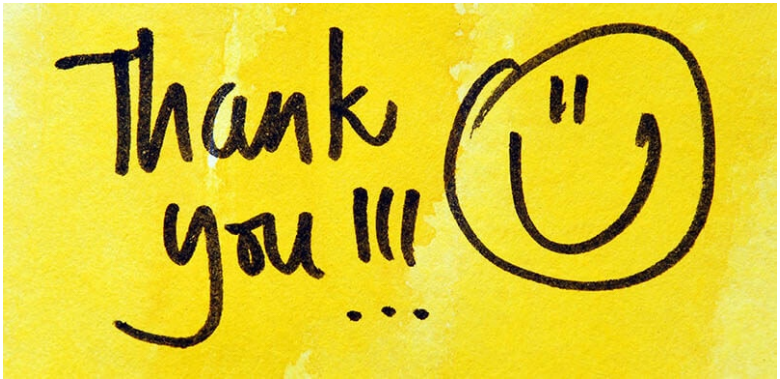


Figure 19: It was great to give you a talk!