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# Software quality and formal methods: Hoare/Dijkstra approach

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Neat Software Designs

2020-01-24

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#### **Global Outline:**

- Software Quality
- Programming Languages
- Formal Verification
- Frama-C Framework
- Verification Practice
- Concluding Remarks

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# Software Quality

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# Software Quality: Outline

- Motivating examples
- Software Development
- Software Verification

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## Motivating examples: Therac-25

Years 1985-1987: Radiation overdose

- Control software flaw:
  - Race conditions
- Death of 6 (six) cancer patients



Figure 1: Radiation therapy

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## Motivating examples: Ariane-5

Year 1996: Missile crash

- Control software flaw:
  - 64-bit float to 16-bit integer conversion
- \$137 million Rocket + \$500 million cargo



Figure 2: Space flights

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# Motivating examples: Toyota

Year 2005: Sudden unintended acceleration

- Control software flaw:
  - Recursion causing stack overflow
- 89 deaths and 57 injuries
- \$1.2 billion compensations



Figure 3: Toyota Camry

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## Motivating examples: Plenty More



# **BUGS EVERYWHERE**

The 12 Software Bugs That Caused Epic Failures: <a href="mailto:link"><a href="mailto:li

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# Software Development: V-model

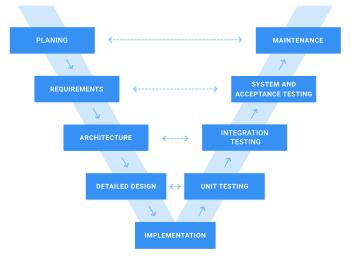


Figure 4: Software development process

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# Software Development: V & V

Software Validation and Verification.

Formally defined by the International Organization for Standardization, see ISO-9000:2015:

- Verification "Confirmation, through the provision of objective evidence, that <u>specified requirements</u> have been fulfilled."
- Validation "Confirmation, through the provision of objective evidence, that the requirements for a specific intended use or application have been fulfilled."

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# Software Development: Testing

#### Verification:

- Are we building the product right?
- Does the system comply with its specification?

#### Validation:

- Are we building the right product?
- Does the system meet the needs of the customer?

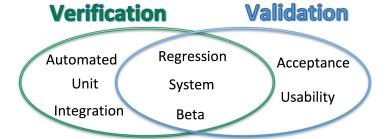


Figure 5: Types of testing

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### Software Verification: Formal

#### Formal verification<sup>1</sup>:

"Is the act of proving or disproving the correctness of intended algorithms underlying a system with respect to a certain formal specification or property, using formal methods of mathematics."

#### Formal methods<sup>2</sup>:

"Formal methods are techniques used to model complex systems as mathematical entities."

"By building a rigorous model of a complex system, it is possible to verify the system's properties in a more thorough fashion than empirical testing."

<sup>&</sup>lt;sup>1</sup> "Formal Verification" on Wikipedia

<sup>&</sup>lt;sup>2</sup>"Formal Methods", Michael Collins, CMU

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# Programming Languages

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# Programming Languages: Outline

- Language Generations
- Declarative vs. Imperative
- What is ANSI-C?

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## Language Generations

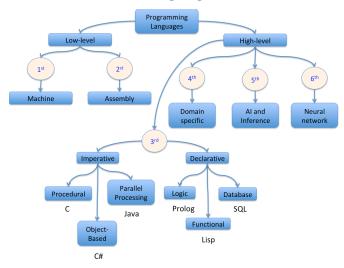


Figure 6: Generations of Programming languages

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# Declarative vs. Imperative: Main

Consider a problem of multiplying all array elements by 2:

Declarative – Specifies what to achieve:

```
//Declarative `JavaScript`
var arr_dbl = arr.map((x) => x * 2)
```

• Imperative – Defines the how steps:

```
//Imperative `JavaScript`
var arr_dbl = []
for (let i = 0; i < arr.length; i++) {
   arr_dbl.push(arr[i] * 2)
}</pre>
```

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## Declarative vs. Imperative: Test

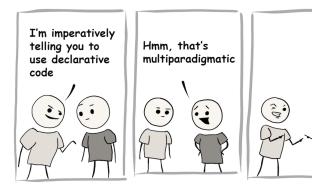


Figure 7: If you laugh, it means you've passed

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### What is ANSI-C: An old C

#### C language:

C is an *imperative procedural* language.

#### Procedural language:

Is an imperative language in which the program is built from one or more subroutines commonly known as functions.

#### **Defining ANSI-C:**

ANSI-C is a common name for two equivalent standards:

- C89 American National Standards Institute (ANSI)
- C90 International Organization for Standardization (ISO)

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## Formal Verification: Outline

- Verification Goal
- Hoare Approach
- Dijkstra Extension

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## Verification Goal: Global

A program shall satisfy a formal specification of its behavior.

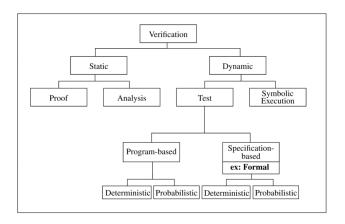


Figure 8: Verification methods

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# Verification Goal: Proving

Mathematically prove conformance to formal specifications.

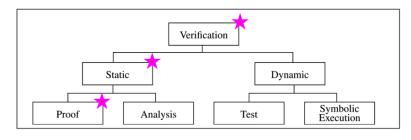


Figure 9: Formal correctness proving

#### Consider:

The Hoare/Dijkstra approach for proving correctness of *imperative programs*.

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# Hoare Approach<sup>3</sup>

Hoare triples:  $\{P\} C \{Q\}$ 

 ${\cal C}$  - code;  ${\cal P}$  - pre-condition;  ${\cal Q}$  - post-condition;

Axioms, e.g. Skip and Assign:

$$\frac{-}{\{P\}skip\{P\}}$$
 and  $\frac{-}{\{P[E/V]\}V:=E\{P\}}$ 

Where E is any expression and V is any variable.

Inference rules, e.g. Composition and Conditional:

$$\frac{\{P\}S_1\{R\},\{R\}S_2\{Q\}}{\{P\}S_1;S_2\{Q\}} \text{ and } \frac{\{B\land P\}S\{Q\},\{\neg B\land P\}T\{Q\}}{\{P\} \text{ if } B \text{ then } S \text{ else } T \text{ elseif } \{Q\}}$$

**Partial correctness:** If P holds before executing C then Q holds afterwards, ONLY if C terminates.

<sup>&</sup>lt;sup>3</sup>"An Axiomatic Basis for Computer Programming", Tony Hoare, 1969.

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# Dijkstra Extension<sup>4</sup>

The weakest pre-condition calculus for  $\{P\} C \{Q\}$ 

- Explains how C transforms P into Q;
- Gives a predicate transform semantics for proofs;

Backward reasoning: (W.P.)

- Based on Q and C calculate the weakest pre-condition  $\widehat{P}$
- If  $P \implies \widehat{P}$ , then  $\{P\} C \{Q\}$  holds

Forward reasoning: (S.P.)

- Based on P and C calculate the strongest post-condition  $\widehat{Q}$
- If  $\widehat{Q} \implies Q$ , then  $\{P\} C \{Q\}$  holds

<sup>&</sup>lt;sup>4</sup>"Guarded commands, non-determinacy and formal derivation of programs", Edsger Dijkstra, 1975

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# Frama-C Framework

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## Frama-C Framework: Outline

- Framework Description
- Plugins Overview
- What is ACSL?

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# Framework Description

#### Frama-C is a:

- Plug-in-based
- Open-source
- Cross-platform

### framework for ANSI-C source-code analysis:

- Browse unfamiliar code
- Static code analysis
- Dynamic code analysis
- Code transformations
- Certification of critical software

You can easily build upon the existing plug-ins to implement your own analysis.

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## Plugins Overview: Main

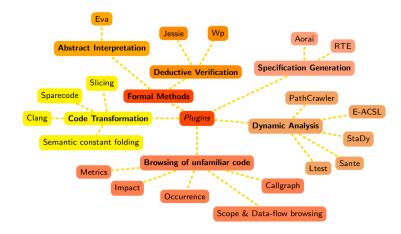


Figure 10: Frama-C plugins

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# Plugins Overview: WP

WP - weakest precondition for ACSL specs of ANSI-C programs.

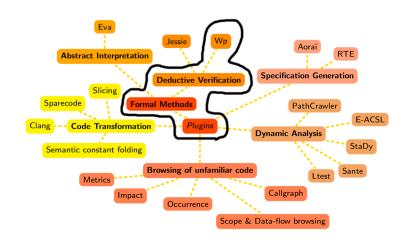


Figure 11: Frama-C WP plugin

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### What is ACSL: General

#### In short:

- ACSL ANSI/ISO C Specification Language
- Allows to formally specify properties of C programs

It is all about function contracts:

```
/*@ ensures \result >= x & \result >= y;
    ensures \result == x // \result == y;
    */
int max (int x, int y) {
    return(x > y) ? x : y;
}
```

A function contract is a combination of:

- post-conditions ensures
- pre-conditions requires

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## What is ACSL: Pointers

ACSL allows to reason about, e.g.:

- Pointers
- Arrays
- Termination

#### Consider pointers:

```
/*@ requires \valid(x) & \valid(y);
    ensures *x <= *y;
*/
void max_ptr (int *x, int *y) {
    if(*x > *y) {
        int tmp = *x;
        *x = *y;
        *y = tmp;
    }
}
```

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# What is ACSL: Completeness

Is the following max\_ptr implementation correct?

```
/*0 requires \valid(x) & \valid(y);
    ensures *x <= *y;
    */
void max_ptr (int *x, int *y) {
    *x = *y = 0;
}</pre>
```

We need to make our specification **complete**:

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# What is ACSL: The whole spec.

The complete ACSL specification v1.4 has 93 pages: https://frama-c.com/download/acsl\_1.4.pdf



Figure 12: Feel free to explore

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# Verification Practice

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## Verification Practice: Outline

- Verification Examples
- Verification Outcomes
- Experience Summary

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# Verification Examples: abs(.)

Consider a primitive integer absolute value computation:

```
/*@
    ensures \result >= 0;
*/
int abs(int val) {
    if(val < 0) return -val;
    return val;
}</pre>
```

The verification shall return **OK**, right?

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### Verification Examples: Issue #1

**NOP** - the verification results are inconclusive:

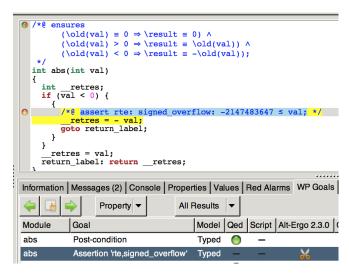


Figure 13: WP detects a possible overflow

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## Verification Examples: Issue #2

Extend the specification with a pre-condition:

```
/*@ requires INT_MIN < val;
    ensures \result >= 0;
    */
int abs(int val) {
    if(val < 0) return -val;
    return val;
}</pre>
```

The verification is OK, but the spec is NOT complete:

```
/*@ requires INT_MIN < val;
    ensures \result >= 0;

*/
int abs(int val) {
    return 1;
}
```

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## Verification Examples: Final?

An explicit \result value specification makes it complete:

What if the implementation was wrong?

Would we be able to identify the root-cause?

```
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formal
methods:
Hoare/Dijkstra
approach
```

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## Verification Examples: Faulty

Consider a lengthy and potentially buggy implementation:

```
/*@ requires INT MIN < val;
    ensures (val == 0 ==> \result == 0) &&
             (val > 0 ==> \result == val)
            (val < 0 \Longrightarrow \ \ \ ):
 */
int abs(int val) {
  if(val == 0) {
    return 0:
  } else {
    if(val < 0) {
      return val;
    } else {
      return -val;
```

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## Verification Examples: Issue #3

The verification is inconclusive, the prover has failed!

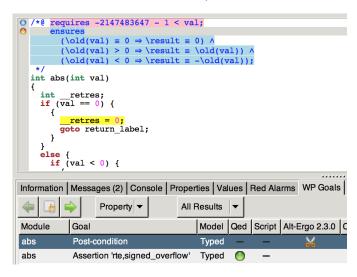


Figure 14: What is the actual reason?

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## Verification Examples: Split

What if we split the post-condition from:

```
/*@ requires INT_MIN < val;
ensures (val == 0 ==> \result == 0) &&
(val > 0 ==> \result == val) &&
(val < 0 ==> \result == -val);
*/
```

#### into separate statements:

```
/*@ requires INT_MIN < val;
  ensures (val == 0 ==> \result == 0);
  ensures (val > 0 ==> \result == val);
  ensures (val < 0 ==> \result == -val);
*/
```

and then run verification again.

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### Verification Examples: Insights

This gives us insights into what could be wrong:

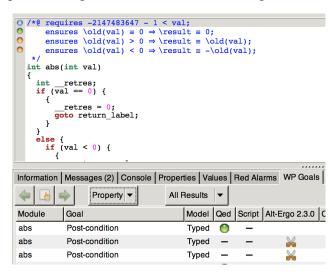


Figure 15: Finding the root-causes

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## Verification Examples: Bugs

Now we can now look into the code and identify bugs:

```
/*@ requires INT MIN < val;
    ensures (val == 0 ==> \text{result} == 0):
    ensures (val > 0 ==> \result == val):
    ensures (val < 0 ==> \result == -val):
 */
int abs(int val) {
  if(val == 0) {
    return 0; //OK
  } else {
    if(val < 0) {
      return val; //BUG #1, should return -val
    } else {
      return -val; //BUG #2, should return val
```

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## Verification Examples: Issue #4

Fixing BUG #1 turns the corresponding post-conditions green!

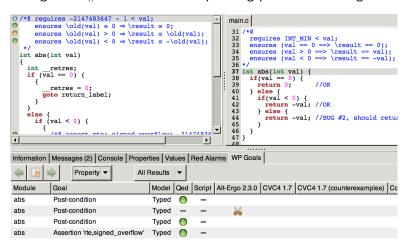


Figure 16: Sequential issue resolution

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## Verification Examples: Issue #5

#### Fixing BUG #2 yields an **OK** verification result!

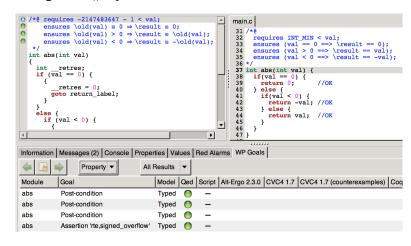


Figure 17: Now we are all fine

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### Verification Outcomes

#### If the verification result is **OK**:

- The program satisfies the specification, BUT
- Is the specification correct/complete?

### If the verification result is **NOK**<sup>5</sup>:

- An incorrect implementation:
  - Find counter-example via test generation;
- A wrong specification:
  - Complete spec. and proof analysis;
  - Change/extend the specification;
- A prover's failure:
  - Alternative provers;
  - Interactive proof assistants;

<sup>&</sup>lt;sup>5</sup>This includes a failed verification attempt, e.g. a time out

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## **Experience Summary**

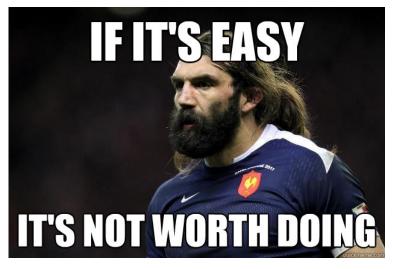


Figure 18: It is not so easy but it helps!

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# Concluding Remarks

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## **Concluding Remarks**

#### We have looked into:

- Software quality and software engineering
- Programming language classification
- Formalization of software verification
- Hoare/Dijkstra approach to formal proving
- Frama-C a platform for ANSI-C code analysis
- Experienced practical program verification

#### We can conclude that:

- Formal software verification is useful
- It is not yet fully automated
- There is a lot more to learn about it!

Thank you and are there any questions?

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## I appreciate your time!



Figure 19: It was great to give you a talk!

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### More useful links:

- ACSL Mini-Tutorial:
  - https://frama-c.com/download/acsl-tutorial.pdf
- ACSL-tutorial:
  - https://frama-c.com/download/acsl-tutorial.pdf
- ACSL-by-Example:
  - https://www.cs.umd.edu/class/spring2016/cmsc838G/frama-c/ACSL-by-Example-12.1.0.pdf
- Frama-C website: https://frama-c.com/
- Frama-C v20.0 manual: https://framac.com/download/user-manual-20.0-Calcium.pdf
- Frama-C WP tutorial: https://allanblanchard.fr/publis/frama-c-wp-tutorial-en.pdf