

Academic Integrity: I certify that this is my own work.

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Read problems carefully (>twice!), write only on this sheet, show all work, and box your final answers.

- 1) The wave function for a traveling wave on a taut string is (in SI units)

$$y(x, t) = 0.35\text{m} \sin \left[ -(10\pi \text{ s}^{-1})t - (3\pi \text{ m}^{-1})x + \frac{\pi}{4} \right]$$

- a) What is the direction of travel of the wave? Explain. [4 points]

This wave is traveling in the -x direction.

consider:  $[-(10\pi \text{ s}^{-1})t - (3\pi \text{ m}^{-1})x + \frac{\pi}{4}] = \text{constant}$  SAT!

As time increases, the value of  $kx$  must increase to compensate, thus,  $x$  must be a negative value, hence,

$\leftarrow (-) x$   
 $- \hat{i}$

(Alternate solution is take derivative.)

- b) What is the wave propagation speed of the wave? [4 points]

$V = \frac{\omega}{k}$  ✓ Note:  $y(x, t) = y_{\text{max}} \sin(\underbrace{\omega t}_{10\pi} - \underbrace{kx}_{3\pi} + \phi)$

$V = \frac{10\pi (\text{s}^{-1})}{3\pi (\text{m}^{-1})} = \boxed{3.33 \text{ m/s}}$

$\omega = 2\pi f \rightarrow f = \frac{\omega}{2\pi}$   
 $k = \frac{2\pi}{\lambda} \rightarrow \lambda = \frac{2\pi}{k}$

$V = \lambda f \rightarrow V = \frac{\omega}{k} \frac{2\pi}{2\pi}$

- c) What is the wavelength? [4 points]

$\lambda = ?$  ✓

$k = \frac{2\pi}{\lambda} \rightarrow \lambda = \frac{2\pi}{k} = \frac{2\pi}{3\pi (\text{m}^{-1})} = \boxed{0.667 \text{ m}}$

$y(x, t) = y_{\text{max}} \sin(kx - \omega t + \phi) \quad k = \frac{2\pi}{\lambda}$

$\omega = 2\pi f = \frac{2\pi}{T}$

$v = \lambda f$

$v = \sqrt{\frac{T}{\mu}}$

Reproduced for convenience:  $y(x, t) = 0.35\text{m} \sin \left[ -(10\pi \text{ s}^{-1})t - (3\pi \text{ m}^{-1})x + \frac{\pi}{4} \right]$

d) What is the maximum transverse acceleration of an element of the string? [4 points]

$$a_{y\text{max}} = ?$$

$$y(x, t) = \underbrace{0.35\text{m}}_{\text{consider constant } y_{\text{max}}} \sin(\underbrace{-10\pi \text{ s}^{-1}}_{\omega} t - \underbrace{3\pi \text{ m}^{-1}}_K x + \underbrace{\frac{\pi}{4}}_{\phi})$$

$$y(x, t) = y_{\text{max}} \sin(-\omega t - kt + \phi)$$

$$v_y = \frac{\partial y}{\partial t} = (y_{\text{max}})(-\omega) \cos(-\omega t - kt + \phi)$$

$$a_y = \frac{\partial^2 y}{\partial t^2} = -(y_{\text{max}})(\omega^2) \sin(-\omega t - kt + \phi)$$

$$a_{y\text{max}} = (y_{\text{max}})\omega^2 = (0.35\text{m})(10\pi \text{ s}^{-1})^2$$

e) What is the vertical position of an element of the string at  $t = 0$ ,  $x = 0.2\text{m}$ ? [4 points]

$$y(0.2, 0) = 0.35\text{m} \sin(\underbrace{-1}_{\text{BET}} \underbrace{3\pi \text{ m}^{-1}}_K (0.2) + \frac{\pi}{4})$$

$$= \boxed{0.891\text{m}}$$

$$= \boxed{345\text{m/s}^2}$$

$$y(x, t) = y_{\text{max}} \sin(kx - \omega t + \phi) \quad k = \frac{2\pi}{\lambda}$$

$$\omega = 2\pi f = \frac{2\pi}{T}$$

$$v = \lambda f$$

$$v = \sqrt{\frac{T}{\mu}}$$