Intérprete con estrategia Call By Name (CBN)



$$\frac{\Gamma' \vdash M \hookrightarrow V}{\Gamma, x = \langle M, \Gamma' \rangle, \Delta \vdash x \hookrightarrow V} \ x \not\in \mathsf{D}(\Delta)$$

$$\frac{\Gamma \vdash M \hookrightarrow \langle x, M', \Gamma' \rangle \quad \Gamma', x = \langle N, \Gamma \rangle \vdash M' \hookrightarrow V}{\Gamma \vdash MN \hookrightarrow V}$$

$$\frac{\Gamma \vdash M \hookrightarrow \mathsf{True} \hookrightarrow \mathsf{True}}{\Gamma \vdash \mathsf{if} \ M \ \mathsf{then} \ N_1 \ \mathsf{else} \ N_2 \hookrightarrow V} \qquad \frac{\Gamma \vdash M \hookrightarrow \mathsf{False} \hookrightarrow \mathsf{False}}{\Gamma \vdash \mathsf{if} \ M \ \mathsf{then} \ N_1 \ \mathsf{else} \ N_2 \hookrightarrow V}$$

$$\frac{\Gamma, x = \langle \mu x. M, \Gamma \rangle \vdash M \hookrightarrow V}{\Gamma \vdash \mu x. M \hookrightarrow V}$$

Intérprete con estrategia Call By Value (CBV)



$$\frac{\Gamma' \vdash \mu y.M \to V}{\Gamma, x = V, \Delta \vdash x \hookrightarrow V} \ x \notin \mathsf{D}(\Delta) \qquad \frac{\Gamma' \vdash \mu y.M \to V}{\Gamma, x = \langle \mu y.M, \Gamma' \rangle, \Delta \vdash x \hookrightarrow V} \ x \notin \mathsf{D}(\Delta)$$

$$\frac{\Gamma \vdash N \hookrightarrow W \quad \Gamma \vdash M \hookrightarrow \langle x, M', \Gamma' \rangle \quad \Gamma', x = W \vdash M' \hookrightarrow V}{\Gamma \vdash \mathsf{M} S \hookrightarrow \mathsf{V}} \qquad \frac{\Gamma \vdash MN \hookrightarrow V}{\Gamma \vdash \mathsf{False} \hookrightarrow \mathsf{False}}$$

$$\frac{\Gamma \vdash M \hookrightarrow \mathsf{True} \quad \Gamma \vdash N_1 \hookrightarrow V}{\Gamma \vdash \mathsf{if} \ M \ \mathsf{then} \ N_1 \ \mathsf{else} \ N_2 \hookrightarrow V} \qquad \frac{\Gamma \vdash M \hookrightarrow \mathsf{False} \ \Gamma \vdash N_2 \hookrightarrow V}{\Gamma \vdash \mathsf{if} \ M \ \mathsf{then} \ N_1 \ \mathsf{else} \ N_2 \hookrightarrow V}$$

$$\frac{\Gamma, x = \langle \mu x.M, \Gamma \rangle \vdash M \hookrightarrow V}{\Gamma \vdash \mu x.M \hookrightarrow V}$$

Extensión de los intérpretes con números naturales



CBN y CBV

Semántica denotacional del Cálculo Lambda (sin error)

