

# Discrete Math facts:

Topic	Discrete Math Result
Sums	$1 + 2 + \dots + n = \frac{n(n+1)}{2}$
Log rule	$\log(n^a) = a \log(n)$
Log rule	$\log(a \cdot b) = \log(a) + \log(b)$
Log rule	$\log(\frac{a}{b}) = \log(a) - \log(b)$
Log rule	$\log(1) = 0$
Log rule	$a^{\log_a n} = n$ Note that the cancellation applies because the bases 'a' match up.
Log rule	$\log_a(a^k) = k$
Log rule	$a^{\log_b n} = n^{\log_b a}$ The exponent on the n is $\log_b a$ , which you can enter in your calculator.
Sum rule	$\sum_{k=0}^L a^k = \frac{a^{L+1} - 1}{a - 1}$
Sum Rule	$\sum_{k=0}^{\text{infinity}} a^k = \frac{1}{1-a}$ as long as $ a  < 1$
Sum Rule	$\sum_{k=0}^L a^k \leq c$ as long as $ a  < 1$
Sum Rule (from Week 3 bottom-up heap-building)	$\sum_{k=0}^L k(a)^k = \frac{a}{(1-a)^2}$ as long as $ a  < 1$

[illegible]