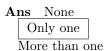
Constructing triangles

October 20, 2013

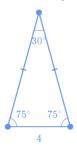
$1 \quad x0a2c8d4a7e3a85b9$

How many triangles can be drawn where the side length is known between two known angles?



Hint 1 Let's draw an example of a triangle where the side length is known between 2 angles. Let's look at when a side of length 5-4 is between a pair of 75° angles.

Hint 2 The other two sides can be drawn at 75° angles and are equal in length. The sides meet at a 30° angle to complete the triangle.



This triangle is unique, meaning no other triangle exists with exact same shape or size that satisfies these conditions.

Hint 3 #-When the side length is known between two known angles, only one triangle can be drawn.

Tags: Constructing triangles, CC.7.G.A.2

Version: 549fc212.. 2013-10-18-e08d4e9d.. 2013-10-20

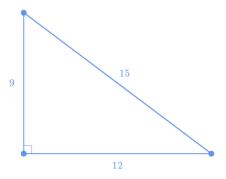
2 x18341f6f8d24d96e

How many triangles can be drawn with side lengths 9, 12 and 15?

Ans None
Only one
More than one

Hint 1 A triangle is a plane figure with 3 straight sides and 3 angles. Can we satisfy the definition given the conditions? Let's try to draw a triangle given the conditions.

Hint 2 In general, the longest side of a triangle must be shorter than the sum of the two other sides. Because 9+12=21, the two sides 9 and 12 meet to form 2 angles with the side of length 15. We can create 3 angles with the 3 Thus, we can create a triangle whose sides satisfy the definition of a triangle given conditions.



Hint 3 Given the conditions, only one triangle can be drawn.

Tags: Constructing triangles, CC.7.G.A.2

Version: 4c858421.. 2013-10-18 d17e39e1.. 2013-10-20

3 x1afa3df30210708e

Draw a triangle with side lengths 5a, 12a and 13a where a > 0, where a is any positive number.

Given these criteria, is the triangle unique? [[? interactive-graph 1]]

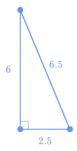
Ans Yes

Hint 1 Lets start by choosing a value for a where a > 0, then we can draw a triangle with side lengths 5a, 12a and 13a.

Hint 2 If a = 1, then Choosing a = 1, we can draw a triangle with side lengths 5, 12 and 13. This is a right triangle.

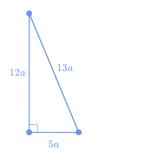


Hint 3 If a = 0.5, then Choosing a = 0.5, we can draw a right triangle with side lengths 2.5, 6 and 6.5.



Hint 4 The triangle is not unique. We can let a be any nonzero positive number and draw many triangles of with the same shape but different sizes.

Hint 4 The triangle is not unique.



Tags: Constructing triangles, CC.7.G.A.2

Version: 5e8d2d2a.. 2013-10-18 e7274d62.. 2013-10-20

4 x1c875467bbf94500

Draw a triangle with side length 4 between two 70° angles.

Given these criteria is the triangle unique? [[? interactive-graph 1]]



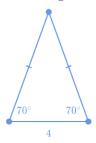
Hint 1 Lets start by drawing the length of 1 side, which we know is 4 side whose length is 4.

Hint 2 From the side 4, lets draw $2 70^{\circ}$ angles. Since we have 2 equal angles, we have an isosceles triangle. An isosceles triangle has at least 2 sides equal in length.

Since we have 270° angles, the third angle must be 40° . The sum of 3 angles in a triangle will always be 180° .

Hint 3 We know the measure of 2 angles and the length of the side between the angles, so we can draw only 1 triangle.

Hint 4 The triangle is unique.



Tags: Constructing triangles, CC.7.G.A.2

Version: 7ec6851f.. 2013-10-17-dd847b40.. 2013-10-20

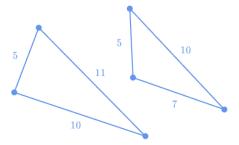
5 x1da87b180aca0e3d

How many triangles can be drawn which have side lengths of 5 and 10?

Ans None
Only one
More than one

Hint 1 We do not know the measure of at least 1 angle or length of the third side. We so we are free to choose any length. Thus, we cannot create a unique triangle with only one shape and size two side lengths.

Hint 2 We can draw many triangles with side lengths 5 and 10.



Hint 3 If we only know 2 side lengths, more than one triangle can be drawn.

Tags: Constructing triangles, CC.7.G.A.2

Version: f333944c.. 2013-10-18 cd0bdb35.. 2013-10-20

6 x25470998d7b41ee4

How many triangles can be drawn where side length 2 is not between which have two 45° angles and two sides of length 2?

Ans None
Only one
More than one

Hint 1 A triangle is a plane figure with 3 straight sides and 3 angles. The 3 angles always add up to 180°.

We have 2-two 45° angles. The third angle x is 90° :

$$\frac{180^{\circ}}{180^{\circ}} = \frac{2 \cdot 45^{\circ} + x}{2}$$

$$\frac{180^{\circ}}{x} = \frac{180^{\circ} - 90^{\circ}}{2}$$

$$\frac{180^{\circ}}{x} = \frac{45^{\circ} + 45^{\circ} + x}{2}$$

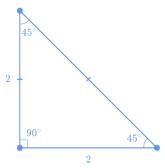
$$\frac{180^{\circ}}{x} = \frac{90^{\circ} + x}{2}$$

$$\frac{180^{\circ}}{x} = \frac{90^{\circ} + x}{2}$$

$$\frac{180^{\circ}}{x} = \frac{90^{\circ} + x}{2}$$

Let The third angle x is 90° so let's draw a right triangle.

Hint 2 We can draw a triangle given the side length 2 is not between the 2 45° angles. The side length 2 is right triangle and make two of its sides of length 2. The sides with length 2 are in between the 45° and 90° angles.



This triangle is unique, meaning no other triangle exists with exact same shape or exactly the same shape and size.

Hint 3 Given the conditions, only one triangle can be drawn.

Tags: Constructing triangles, CC.7.G.A.2

Version: dc27c435.. 2013-10-18-5c0563e0.. 2013-10-20

7 x2bce84b97313fd2b

Draw a triangle where the side length 3 is not between two angles 31° and 90° .

Given these criteria is the triangle unique? [[? interactive-graph 1]]

Ans Yes

Hint 1 Lets start by drawing a right angle which is 90°. Then, let's draw the side of length 3 next to the right angle, so our base is length 3.

Hint 2 The length of 3 is not between 2 angles 31° and 90° .

Since we drew the side of length 3 next to the right angle, the 31° angle must be *opposite* the side of length 3.

Hint 3 We know the measure of 2 angles and the length of 1 side not between the angles, so we can draw only 1 triangle.

Hint 4 The triangle is unique.



Tags: Constructing triangles, CC.7.G.A.2 Version: 1215aaf1.. 2013-10-17

8 x31c216ff88dad8e7

How many triangles can be drawn we draw with side lengths 4, 4 and 7?

Ans None
Only one
More than one

Hint 1 A triangle is a plane figure with 3 straight sides and 3 angles. Can we satisfy the definition given the conditions? Let's try to draw a triangle given the conditions.

Hint 2 In general, the longest side of a triangle must be shorter than the sum of the two other sides. Because 4+4=8, the two sides 4 and 4 meet to form 2 angles with the side of length 7. We can create 3 angles with the 3 sides satisfy the definition of a triangle.



Hint 3 Given the conditions, only one triangle can be drawn.

Tags: Constructing triangles, CC.7.G.A.2

Version: 13a63a31. . 2013-10-18-33683619.. 2013-10-20

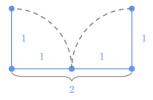
9 x38cc51ab93842600

How many triangles can be drawn with side lengths 1, 1 and 2?

Ans None Only one More than one

Hint 1 A triangle is a plane figure with 3 straight sides and 3 angles. Can we satisfy the definition given the conditions? Let's try to draw a triangle given the conditions.

Hint 2 In general, the longest side of a triangle must be shorter than the sum of the two other sides. Because 1+1=2, the two side lengths 1 and 1 cannot meet to form a third angle. We cannot create 3 angles to satisfy the definition of a triangle.



Hint 3 Given the conditions, no triangles can be drawn.

Tags: Constructing triangles, CC.7.G.A.2

Version: aeb719e4.. 2013-10-18

10 x4c335bfbee0cba92

Draw a right triangle with at least 2 side lengths equal sides of equal length.

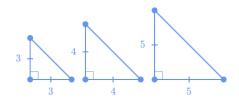
Given these criteria is the triangle unique? [[? interactive-graph 1]]

Ans Yes No

Hint 1 Lets start by drawing. A right triangle has one 90° angle.

A triangle with at least 2 side lengths equal is isosceles equal side lengths is called an isosceles triangle. We do not know the side lengths.

Hint 2 Since we are given the measures of 3 angles and do not know any side lengths, we We can draw many triangles with at least right triangles with 2 side lengths equal sides of equal length.



Hint 3 The triangle is not unique.

Tags: Constructing triangles, CC.7.G.A.2

Version: 0abcb8e1.. 2013-10-18-5f71c91d.. 2013-10-20

x531e157ba7c498eb 11

How many triangles can be drawn where the measures of all 3 angles are known the same?

Ans None Only one More than one

Hint 1 A triangle is a plane figure with 3 straight sides and 3 angles. Can we satisfy the definition given the conditions? What triangle or triangles would satisfy the conditions?

Let's try to draw a triangle where we known the measures of all 3 angles. For example, let's look at when is the same.

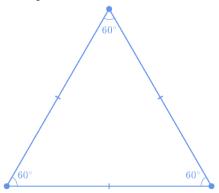
Hint 2 The 3 angle measures in a triangle must sum to 180°. Because we know the measure of all 3 angles must be the same, we know all 3 angles are 60° have measure $=60^{\circ}$



This is an equilateral triangle.

Hint 23 Is this triangle unique , meaning do no other or do other equilateral triangles exist with exact same shape or a different size?

Hint 3 We can draw many equilateral triangles with the same shape but different sizes.



Hint 4 If the measures of all 3 angles are known, more More than one triangle can be drawn with all 3 angles measures equal.

Tags: Constructing triangles, CC.7.G.A.2

Version: 30ec1d68.. 2013-10-18-47228a28.. 2013-10-20

12 x572fecbc70b353aa

Draw an isosceles right triangle with two side lengths a right triangle that is also an isosceles triangle and has two sides of length 3.

Given these criteria is the triangle unique? [[? interactive-graph 1]]

Ans Yes

Hint 1 Lets start by drawing. A right triangle has one $90^{\circ}90^{\circ}$ angle.

An isosceles triangle has at least 2 side lengths equal. We are given 2 side lengths both equal to 3.

Hint 2 Let's draw 1 side length 3 as the height vertically (up and down) from the 90° angle. Let's draw the other side length 3 as the base horizontally (left and right) from the $90^{\circ}90^{\circ}$ angle.

Hint 3 Since we are given the measures of 2 sides and the angle between them, we can draw only 1 triangle.

Hint 4 The triangle is unique.



Tags: Constructing triangles, CC.7.G.A.2

Version: 2e87ab50.. 2013-10-17-b8c14c25.. 2013-10-20

13 x651844ecfaac48e9

Draw a right triangle with two 45° angles.

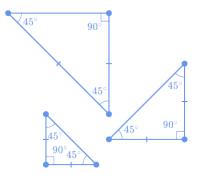
Given these criteria is the triangle unique? [[? interactive-graph 1]]

Ans Yes No

Hint 1 Lets start by drawing. A right triangle has one 90° angle.

We have The triangle we want is an isosceles right triangle. An isosceles right triangle has at least 2 side lengths equal and 2 45° two 45° angles.

Hint 2 We know the measure of all 3 angles but not the length of any side. We Therefore, we can draw many triangles of various sizes all with a pair of 45° 45° angles.



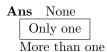
Hint 3 The triangle is not unique.

Tags: Constructing triangles, CC.7.G.A.2

Version: 85d97ee1.. 2013-10-17-525a66e3.. 2013-10-20

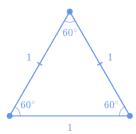
14 x6763ceb1ec0ceb41

How many triangles can be drawn where the lengths of all 3 sides are knownegual to 1?



Hint 1 A triangle is a plane figure with 3 straight sides and 3 angles. Can we satisfy the definition given the Is there a triangle or triangles that satisfy the conditions? Let's try to draw a triangle where we known the lengths of all 3 sides. with all side lengths equal to 1.

Hint 2 For example, let's look at when all side lengths are 1. We have The result is an equilateral triangle with equal sides side lengths and equal angles measures:



This triangle is unique, meaning no other triangle exists with exact same shape or size that has all sides equal to 1.

Hint 3 H—In general, if the lengths of all 3 sides are known, only one triangle can be drawn.

Tags: Constructing triangles, CC.7.G.A.2

Version: def3450f.. 2013-10-18 ca634aaf.. 2013-10-20

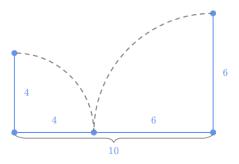
15 x67ee6010588311f2

How many triangles can be drawn with side lengths 4, 6 and 10?

Ans None Only one More than one

Hint 1 A triangle is a plane figure with 3 straight sides and 3 angles. Can we satisfy the definition given the conditions? Let's try to draw a triangle given the conditions.

Hint 2 In general, the longest side of a triangle must be shorter than the sum of the two other sides. Because 4+6=10, the two sides 4 and 6 cannot meet to form a third angle. We cannot create 3 angles to satisfy the definition of a triangle.



Hint 3 Given the conditions, no triangles can be drawn.

Tags: Constructing triangles, CC.7.G.A.2 Version: 9421cd19.. 2013-10-18

16 x67fd10caf4f54df2

Draw a triangle with side lengths 3a, 4a and 5a where a > 0, where a is any positive number.

Given these criteria is the triangle unique? [[? interactive-graph 1]]

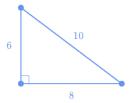
Ans Yes No

Hint 1 Lets start by choosing a value for a where a > 0, then we can draw a triangle with side lengths 3a, 4a and 5a.

Hint 2 If a = 1, then we can draw a triangle with side lengths 3, 4 and 5. This is a right triangle.

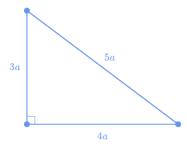


Hint 3 If a = 2, then we can draw a right triangle with side lengths 6, 8 and 10.



We can let a be any nonzero positive number and draw many triangles of same shape but different sizes.

Hint 4 The triangle is not unique. Multiple triangles satisfy the conditions.



Tags: Constructing triangles, CC.7.G.A.2

Version: 196bcc1a.. 2013-10-18-95e0a049.. 2013-10-20

17 x6d7be6276bcb5815

Draw a right triangle with a height of 4 and base of 5.

Given these criteria is the triangle unique? [[? interactive-graph 1]]

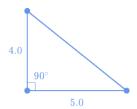
Ans Yes

Hint 1 Lets start by drawing. A right triangle has a $90^{\circ}90^{\circ}$ angle.

The height of length 4 is drawn vertically (up and down) from the $90^{\circ}90^{\circ}$ angle. The base of length 5 is drawn horizontally (left and right) from the $90^{\circ}90^{\circ}$ angle.

Hint 2 Since we are given the measures of 2 sides and the angle between them, we can draw only 1 triangle.

Hint 3 The triangle is unique.



Tags: Constructing triangles, CC.7.G.A.2

Version: ef653e34. . 2013-10-17-41522448.. 2013-10-20

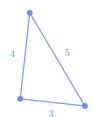
$18 ext{ } ext{x}72d893d1e3229dfd$

How many triangles can be drawn side lengths of we draw with side lengths 3 and 4?

Ans None
Only one
More than one

Hint 1 We can draw many triangles with side lengths 3 and 4.





Hint 2 Without knowing at least 1 angle measure, we cannot create a unique triangle with only one shape and size.

Hint 2 We can draw many triangles with side lengths 3 and 4side lengths 3 and 4.

Hint 3 If we only know 1 angle and 1 side length2 side lengths, more than one triangle can be drawn.

Tags: Constructing triangles, CC.7.G.A.2

Version: 58c104bc.. 2013-10-18-af92749c.. 2013-10-20

19 x892857b71e427c39

How many triangles can be drawn with angles 60° , 60° and 70° ?

Ans None

Only one

More than one

Hint 1 A triangle is a plane figure with 3 straight sides and 3 angles. The 3 angles always add up to In a triangle, the sum of the three angle measures is 180°.

Hint 2 Let's add together the angles angles measures 60°, 60° and 70°:

sum of angle measures = $60^{\circ} + 60^{\circ} + 70^{\circ}$ = $120^{\circ} + 70^{\circ}$ = 190° > 180°

The sum of the 3 angles sum up to a value angle measures is greater than 180° .

Hint 3 Given the conditions, no triangles No triangle can be drawn that satisfies the given conditions.

Tags: Constructing triangles, CC.7.G.A.2

Version: bc3efef4.. 2013-10-18-88ce2f2f.. 2013-10-20

20 xb9aa47b3de982d55

Draw an isosceles triangle with two 70° angles.

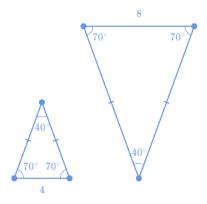
Given these criteria is the triangle unique? [[? interactive-graph 1]]

Ans Yes

Hint 1 Lets start by drawing an isosceles triangle with 270° angles. An isosceles triangle has at least 2 side lengths equal and 2 angles equal.

Hint 2 We do not know the side lengths, so we can draw many triangles.

Hint 3 The triangle is not unique.



Tags: Constructing triangles, CC.7.G.A.2 Version: 3bc9edc0.. 2013-10-18

$21 ext{ xbd}061a8700fced6c$

How many right triangles can be drawn with angles 40° and $60^{\circ}?^{}$

Ans None Only one More than one

Hint 1 A triangle is a plane figure with 3 straight sides and 3 angles. The 3 angles always add up to In a triangle, the sum of the three angle measures is 180°.

A right triangle has a 90° angle.

Hint 2 Let's add together the angles angles measures 40°, 60° and 90°:

$$. = 40^{\circ} + 60^{\circ} + 90^{\circ}$$

$$= 190^{\circ}$$

$$> 180^{\circ}$$
sum of angle measures= $40^{\circ} + 60^{\circ} + 90^{\circ}$

$$= 190^{\circ}$$

$$> 180^{\circ}$$

$$> 180^{\circ}$$

The sum of the 3 angles sum up to a value is greater than 180° .

Hint 3 Given the conditions, no triangles No triangle can be drawn that satisfies the given conditions.

Tags: Constructing triangles, CC.7.G.A.2

Version: aabc8c4a.. 2013-10-18-69a54880.. 2013-10-20

$22 ext{ } ext{xc} 001c788d01d9e5f$

Draw a triangle where side length 4 is not between two angles 58° and 90° .

Given these criteria is the triangle unique? [[? interactive-graph 1]]

Ans Yes

Hint 1 Lets start by drawing a right angle which is 90°. Then, let's draw the side of length 4 next to the right angle, so our base has a length of 4.

Hint 2 The side of length 4 is **not** between 2 angles 58° and 90° .

Since we drew the side of length 4 next to the right angle, the 58° angle must be *opposite* the side of length 4 .

Hint 3 We know the measure of 2 angles and the length of 1 side not between the angles, so we can draw only 1 triangle.

Hint 4 The triangle is unique.



Tags: Constructing triangles, CC.7.G.A.2 **Version:** 9534c031.. 2013-10-17

23 xc256611ab7d92e83

Draw a triangle with side length 5 between two 58° angles.

Given these criteria is the triangle unique? [[? interactive-graph 1]]

Ans Yes No

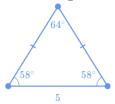
Hint 1 Lets start by drawing the length of 1 side, which we know is 5.

Hint 2 From the side 5, lets draw 2 58° angles. Since we have 2 equal angles, we have an isosceles triangle. An isosceles triangle has at least 2 sides equal in length.

Since we have 2.58° angles, the third angle must be 64° . The sum of 3 angles in a triangle will always be 180° .

Hint 3 We know the measure of 2 angles and the length of the side between the angles, so we can draw only 1 triangle.

Hint 4 The triangle is unique.



Tags: Constructing triangles, CC.7.G.A.2 Version: 5ba2ed08.. 2013-10-17

$24 \times c40b1278855716df$

Draw a triangle with side lengths 3, 4 and 5.

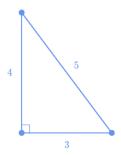
Given these criteria is the triangle unique? [[? interactive-graph 1]]



Hint 1 Lets start by drawing. We know the lengths of all 3 sides. How many triangles can we draw?

Hint 2 The triangle with side lengths 3, 4 and 5 is a right triangle. Since we are given the measures of 3 sides, we can draw only 1 triangle.

Hint 3 The triangle is unique.



Tags: Constructing triangles, CC.7.G.A.2 Version: b5262e6e.. 2013-10-17

25 xcfae18d2af4efa34

Draw an obtuse triangle with angles 45°, 35° and 100°.

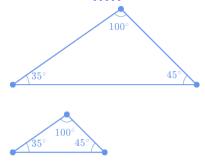
Given these criteria is the triangle unique? [[? interactive-graph 1]]



Hint 1 Lets start by drawing. While keeping 1 angle one angle constant, we can change the side lengths to create 1 one of the other 2 two angles.

For example, while keeping a 45° angle, we can change the side lengths to create the 35° angle. The final angle will be third angle will have measure 100°.

Hint 2 We know the measure of 3 angles but not the length of any side. We can therefore draw many triangles of the same shape but with different sizes.



Hint 3 The triangle is not unique.

Tags: Constructing triangles, CC.7.G.A.2

Version: 040283a2.. 2013-10-18-71b1e27f.. 2013-10-20

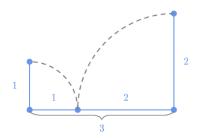
26 xdba9a2b900c8bbcd

How many triangles can be drawn with side lengths 1, 2 and 3?

Ans None Only one More than one

Hint 1 A triangle is a plane figure with 3 straight sides and 3 angles. Can we satisfy the definition given the conditions? Let's try to draw a triangle given the conditions.

Hint 2 In general, the longest side of a triangle must be shorter than the sum of the two other sides. Because 1+2=3, the two sides 1 and 2 cannot meet to form a third angle. We cannot create 3 angles to satisfy the definition of a triangle.



Hint 3 Given the conditions, no triangles can be drawn.

Tags: Constructing triangles, CC.7.G.A.2 Version: 2feadc91.. 2013-10-18

$27 ext{ xe}06107bc78ca0b3c$

How many triangles can be drawn we draw with angles 30° , 50° and 100° ?

Ans None
Only one
More than one

Hint 1 A triangle is a plane figure with 3 straight sides and 3 angles. The 3 angles always measures must add up to 180°. Let's add together the angles 30°, 50° and 100°:

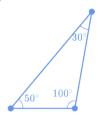
$$= 30^{\circ} + 50^{\circ} + 180^{\circ}$$

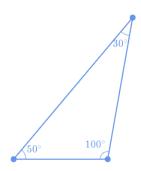
$$= 180^{\circ}$$
total angle measure= $30^{\circ} + 50^{\circ} + 180^{\circ}$

$$= 180^{\circ}$$

So, at least 1 triangle exists. Let's start by drawing draw it.

Hint 2 We know the measure of 3 angles but not the length of any side. We can draw many triangles with the same shape but different sizes.





Hint 3 If—When only the measures of all 3 angles are known, more than one triangle can be drawn.

Tags: Constructing triangles, CC.7.G.A.2

Version: 99af1276.. 2013-10-18-089fe1ab.. 2013-10-20

28 xe937d430ba8d75d8

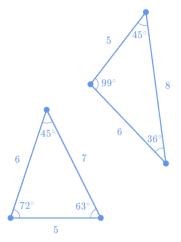
How many triangles can be drawn with one we draw that have one angle measure equal to 45° and a side length of one side of length 5?

Ans None
Only one
More than one

Hint 1 A triangle is a plane figure with 3 straight sides and 3 angles.

The 3 angles measures always add up to 180° . We only know 1 angle is 45° . We can't find the measures of the other 2 angles.

Hint 2 We know the length of only 1 side is 5. Depending if we place the side of length 5 next to or across from the 45° angle, we can draw many triangles with different shapes and different sizes.



Hint 3 If we only know 1 angle and 1 side length, more than one triangle can be drawn.

Tags: Constructing triangles, CC.7.G.A.2

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29 xf51994a651ca1d7f

Draw a triangle with angles 30°, 50° and 100°.

Given these criteria is the triangle unique? [[? interactive-graph 1]]

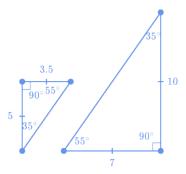
Ans Yes

Hint 1 Lets start by drawing. While keeping 1 angle, we can change the side lengths to create 1 of the other 2 angles.

While keeping a 100° angle, we can change the side lengths to create the 50° angle. The final angle will be 30° .

Hint 2 We know the measure of 3 angles but not the length of any side. We can draw many triangles of same shape but different sizes.

Hint 3 The triangle is not unique.



Tags: Constructing triangles, CC.7.G.A.2 **Version:** ac2e7f53.. 2013-10-18

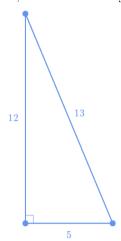
30 xf9872931929ac56c

Draw a triangle with side lengths 5, 12 and 13.

Given these criteria is the triangle unique? [[? interactive-graph 1]]

Hint 1 Lets start by drawing. We know the lengths of all 3 sides. How many triangles can we draw?

Hint 2 Since we are given the measures of lengths of all 3 sides, we can draw only 1 triangle. The one triangle.



Note the triangle with side lengths 5, 12 and 13 is a right triangle.

Hint 3 The triangle is unique.

Tags: Constructing triangles, CC.7.G.A.2

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