## **Cover Sheet for Submission of Maths Examinations Summer 2020**

We would advise preparing your coversheets with your CID, Module Name and Code and Date, before the exams are due to take place.

CID: 01738166

**Module Name: Calculus and Applications** 

**Module Code: MATH40004** 

Date: 12/05/2020

## **Questions Answered (in the file):**

Please tick next to the question or questions you have answered in this file.

Q1	
Q2	
Q3	<b>√</b>
Q4	
Q5	
Q6	

(Note: this is a coversheet for all students - not all students will have exams with 6 questions. Please tick the boxes which are appropriate for your exam and/or the file you are submitting).

## (Optional) Page Numbers for each question;

Page Number	Question Answered
- Trainiboi	7410470104

If handwritten, please complete in CAPITAL Letters, in Blue or Black Ink, ensuring the cover sheet is legible.

(i) 
$$f(x) = f(0) + f'(0) \cdot x + f''(0) \cdot (x^{2}) + \dots + \frac{f''(0) \cdot x^{2}}{n!} + \dots + \frac{f''(0) \cdot x^{2}}{n!} + Rn$$

$$R_{n} = \int_{0}^{x} \frac{(x-t)^{n}}{n!} f'''(t) dt$$

$$\int_{0}^{\infty} \frac{(x-t)}{n!} f(t) dt$$

$$f(x) = e^{x}$$
  $f'(x) = e^{x}$   $f(x) = 1$   
Using Taylors than we get

$$e^{\frac{1}{2}} = \sqrt{e} \approx 1 + \frac{1}{2} + \frac{1}{4 \cdot 2!} + \frac{1}{8 \cdot 3!} + \frac{1}{4000} + \frac{1}{4000} + \frac{1}{4000} + \frac{1}{2} + \frac{1}{8} + \frac{1}{98}$$

$$= \boxed{\frac{79}{2}}$$

$$\lim_{x\to 0} \frac{e^{\sin x} - x - 1}{1 - (\cos x)} = \lim_{x\to 0} \frac{\left(e^{\sin x} - x - 1\right)}{\left(1 - (\cos x)^{\frac{1}{2}}\right)} = \lim_{x\to 0} \frac{\left(e^{\sin x} - x - 1\right)}{\sin x} = \lim_{x\to 0} \frac{\left(e^{\sin x} - x - 1\right)}{\sin$$

$$\lim_{x \to 0} \frac{\left(e^{\sin x} \cdot (\cos x - 1)\right)^{1}}{\left(\sin(x)\right)^{1}} = \lim_{x \to 0} \frac{-e^{\sin(x)} \left(\sin(x) - \cos^{2}(x)\right)}{\cos(x)} = \frac{-e^{0} \left(0 - 1\right)}{1} = \frac{-1(-1)}{1}$$

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$$\frac{1}{2\eta} = \frac{1}{2\eta} = \frac{1}{2\eta} = \frac{1}{3\eta}$$

(fi) Notice 
$$f(x) = -1(-x) = 1$$
 denotion is odd = 1  $a_n = 0$ 

$$b_n = 2 \int_0^\infty f(x) \sin(nx) dx$$

$$f(x) = \int_0^\infty f(x) \sin(nx) dx$$

$$6n = \frac{2}{\pi} \int_{0}^{\infty} \sin(nx) dx = \frac{2}{\pi} \left[ -\frac{\cos(nx)}{n} \right]_{0}^{\pi} = \frac{2}{\pi} \left( \frac{1 - \cos(n\pi t)}{n} \right) = \begin{cases} 0 & n \text{ even} \\ \frac{4}{n\pi t} & n \text{ odd} \end{cases}$$

$$27 J(x) = \frac{4}{31} \left( \sin(x) + \sin(3x) + \dots \right)$$

(iii) 
$$J(\frac{11}{2}) = 1 = \frac{4}{3} \left( \frac{\sin(\frac{11}{2})}{3} + \frac{\sin(\frac{3n}{2})}{3} + \frac{\sin(\frac{5n}{2})}{5} \right)$$
  
=)  $\frac{1}{3} = 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots = \frac{2}{2} \frac{[-1]^n}{(2\mu + 1)}$ 

$$=)\frac{1}{u}=1-\frac{1}{3}+\frac{1}{5}-\frac{1}{7}+\ldots=\frac{2}{\kappa_{=0}}\frac{[-1)^{\kappa}}{(2\kappa_{1})}$$