

## Cover Sheet for Submission of Maths Examinations Summer 2020

We would advise preparing your coversheets with your CID, Module Name and Code and Date, before the exams are due to take place.

**CID: 01738166**

**Module Name: Probability and Statistics**

**Module Code: MATH40005**

**Date: 14/05/2020**

### Questions Answered (in the file):

Please tick next to the question or questions you have answered in this file.

<b>Q1</b>	<input checked="" type="checkbox"/>
<b>Q2</b>	<input type="checkbox"/>
<b>Q3</b>	<input type="checkbox"/>
<b>Q4</b>	<input type="checkbox"/>
<b>Q5</b>	<input type="checkbox"/>
<b>Q6</b>	<input type="checkbox"/>

(Note: this is a coversheet for all students - not all students will have exams with 6 questions. Please tick the boxes which are appropriate for your exam and/or the file you are submitting).

### (Optional) Page Numbers for each question;

<b>Page Number</b>	<b>Question Answered</b>

If handwritten, please complete in CAPITAL Letters, in Blue or Black Ink, ensuring the cover sheet is legible.

(a) A  $\sigma$ -algebra  $\mathcal{F}$  is a collection of subsets of  $\Omega$  denoted by  $\mathcal{F}$  that satisfy:

(i)  $\emptyset \in \mathcal{F}$

(ii)  $\mathcal{F}$  is closed under complements, i.e.  $A \in \mathcal{F} \Rightarrow A^c \in \mathcal{F}$ .

(iii)  $\mathcal{F}$  is closed under countable union, i.e.  $A_1, A_2, \dots \in \mathcal{F} \Rightarrow \bigcup_{i=1}^{\infty} A_i \in \mathcal{F}$ .

(b)  $P$  is a probability measure on  $(\Omega, \mathcal{F})$  id  $P: \mathcal{F} \rightarrow \mathbb{R}$  satisfies

(i)  $P(\Omega) = 1$

(ii)  $P\left(\bigcup_{i=1}^{\infty} A_i\right) = \sum_{i=1}^{\infty} P(A_i)$

(iii)  $P(A) \geq 0, \forall A \in \mathcal{F}$

(c)

(i)  $P(\text{positive test}) = P(\text{positive test} | \text{sufferer}) \cdot P(\text{sufferer}) + P(\text{positive test} | \text{healthy}) \cdot P(\text{healthy})$   
 $\uparrow$   
 by the law of total probability

$$= 0,9 \cdot \frac{1}{10} + 0,2 \cdot \frac{9}{10} = \frac{27}{100}$$

(ii)  $P(\text{sufferer} | +) = \frac{P(+ | \text{sufferer}) \cdot P(\text{sufferer})}{P(+)} - \text{Bayes Law.}$

$$= \frac{\frac{9}{10} \cdot \frac{1}{10}}{\frac{27}{100}} = \boxed{\frac{1}{3}}$$

(d) Out of 6 total, we chose 2 dividers. So we get

$$\binom{6}{2} = \frac{6!}{2!4!} = \frac{6 \cdot 5 \cdot 4}{2} = \boxed{15 \text{ ways}}$$

(e) So by similar methods, we get

$\binom{k-1}{n-1}$  with the convention that  $\binom{a}{b} = 0$  if  $a < b$ .