

# 1 Introduction

The motivation for developing an optimized Java based jet clustering algorithm, is to provide a platform independent implementation for use in online validation scripts on HepSim[1] repository with Monte Carlo predictions for HEP experiments.

Currently, the most widely used implementation of jet clustering algorithms in high energy physics is FastJet[2]. Is it written in C++ and provides a highly optimized implementation of (anti)kt and Cambridge-Aachen jet finding algorithms with selectable  $O(N^2)$  and  $O(N \log N)$  complexities, which significantly reduce runtime in comparison to naive  $O(N^3)$  algorithms[3].

Unfortunately, platform dependence of C++ is prohibitive for use of FastJet in client-side web application scripts. Therefore, a Java implementation was necessary.

# 2 Implementation

It turns out, that for reconstruction of jets obtained in pp collisions, with at most a few thousand particles per event, the most efficient algorithms are those with  $O(N^2)$  complexity. The  $O(N \log N)$  algorithms provide an advantage only in events with more then 10,000 particles, which only arise in experiments with heavy ion collisions[3, 4]. While implementation of  $O(N \log N)$  algorithms requires use of sophisticated techniques, like Voronoi diagrams[5],  $O(N^2)$  complexity can be achieved with relatively simple approaches described below.

## 2.1 Generalizaed kt algorithm

## 2.2 Geometric Factorization

This is the most significant optimization, reducing complexity from  $O(N^2)$  to  $O(N^3)$ . It is explained by the FastJet Lemma[3].

**FastJet Lemma 1:** If particles  $i, j$  form the smallest  $d_{ij}$ , and  $p_t$

**Motivation:**

**Proof:**

## 2.3 Tiling

**FastJet Lemma 2:**

**Motivation:**

**Proof:**

## 2.4 Linked List

# 3 Benchmark

Make plots to compare to FastJet performarmance.

## References

- [1] S. V. Chekanov, “HepSim: a repository with predictions for high-energy physics experiments,” [arXiv:1403.1886 \[hep-ph\]](#).
- [2] M. Cacciari, G. P. Salam and G. Soyez, “FastJet user manual,” Eur. Phys. J. C **72** (2012) 1896 [[arXiv:1111.6097 \[hep-ph\]](#)].
- [3] M. Cacciari and G. P. Salam, “Dispelling the  $N^3$  myth for the  $k_t$  jet-finder,” Phys. Lett. B **641** (2006) 57 [[hep-ph/0512210](#)].
- [4] G. P. Salam and M. Cacciari, “Jet clustering in particle physics, via a dynamic nearest neighbour graph implemented with CGAL,” [LP THE-06-02](#), unpublished note.
- [5] F. Aurenhammer, “Voronoi diagrams: a survey of a fundamental data structure,” ACM Computing Surveys 23 (1991) 345.