

Problem 1.1 (L1)

a)

b)

c)

Problem 1.2 (L1)

a)

b)

c)

Problem 2 (L.2)

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My mistake was that I used conditional identity on $p \vee r$ when I should apply double negation law first because without a negation preceding p , I cannot apply conditional identity.

$((\neg \bar{i} \rightarrow \bar{j}) \vee K) \wedge ((\neg K \rightarrow \bar{j}) \vee (\bar{j} \rightarrow K))$	start
$((\neg \bar{i} \vee \bar{j}) \vee K) \wedge ((\neg K \rightarrow \bar{j}) \vee (\bar{j} \rightarrow K))$	conditional identity
$((\neg \bar{i} \vee \bar{j}) \vee K) \wedge ((\neg \neg K \vee \bar{j}) \vee (\bar{j} \rightarrow K))$	conditional identity
$((\neg \bar{i} \vee \bar{j}) \vee K) \wedge ((\neg \neg K \vee \bar{j}) \vee (\neg \bar{j} \vee K))$	conditional identity
$((\neg \bar{i} \vee \bar{j}) \vee K) \wedge ((K \vee \bar{j}) \vee (\neg \bar{j} \vee K))$	double negation law
$((\neg \bar{i} \vee \bar{j}) \vee K) \wedge (K \vee \bar{j} \vee (\neg \bar{j} \vee K))$	associative law
$((\neg \bar{i} \vee \bar{j}) \vee K) \wedge (K \vee \bar{j} \vee \neg \bar{j} \vee K)$	associative law
$((\neg \bar{i} \vee \bar{j}) \vee K) \wedge (K \vee (\bar{j} \vee \neg \bar{j}) \vee K)$	associative law
$((\neg \bar{i} \vee \bar{j}) \vee K) \wedge (K \vee T \vee K)$	complement law
$((\neg \bar{i} \vee \bar{j}) \vee K) \wedge (K \vee K \vee T)$	commutative law
$((\neg \bar{i} \vee \bar{j}) \vee K) \wedge ((K \vee K) \vee T)$	associative law
$((\neg \bar{i} \vee \bar{j}) \vee K) \wedge (K \vee T)$	idempotent law
$((\neg \bar{i} \vee \bar{j}) \vee K) \wedge T$	domination law
$(\neg \bar{i} \vee \bar{j}) \vee K$	identity law
$\neg \bar{i} \vee \bar{j} \vee K$	associative law
$\bar{j} \vee \neg \bar{i} \vee K$	commutative law
$\bar{j} \vee K \vee \neg \bar{i}$	commutative law
$K \vee \bar{j} \vee \neg \bar{i}$	commutative law
$(K \vee \bar{j}) \vee \neg \bar{i}$	associative law
$(\neg \neg K \vee \bar{j}) \vee \neg \bar{i}$	double negation law
$(\neg K \rightarrow \bar{j}) \vee \neg \bar{i}$	conditional identity

The two expressions are logically equivalent

Problem 3 (L.3)

a)

Row #	p	q	$p \rightarrow q$	$p \vee q$	$\neg p \rightarrow q$	$(p \rightarrow q) \vee (\neg p \rightarrow q)$	$\neg p \rightarrow \neg q$	$(p \vee q) \rightarrow (\neg p \rightarrow \neg q)$
1	T	T						
2	T	F						
3	F	T						
4	F	F						

b)

Problem 4.1 (L.4)

☐ tautology ☐ not a tautology

Problem 4.2 (L.4)

a)

☐ equivalent ☐ not equivalent

b)

☐ equivalent ☐ not equivalent