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CSCI 190 GROUP ASSIGNMENT
WEEK 10
Ch. 8.3 Q's 1, 7

1. How many comparisons are needed for a binary search in a set of 64 elements?

Let $f(n)$ = number of comparisons needed in a binary search of a list of n elements.

$$f(n) = f(n/2) + 2$$

$$f(1) = 2$$

$$f(64) = f(64/2) + 2 = f(32) + 2 = f(16) + 4 = f(8) + 6 = f(4) + 8 = f(2) + 10 = f(1) + 12 = 2 + 12 = 14$$

7. $f(n) = f(n/3) + 1$ when n is a positive integer divisible by 3, $f(1) = 1$

a) $f(3) = f(1) + 1 = 1 + 1 = 2$

**b) $f(9) = f(3) + 1 = 2 + 1 = 3$;
 $f(27) = f(9) + 1 = 3 + 1 = 4$**

**c) $f(81) = f(27) + 1 = 4 + 1 = 5$;
 $f(243) = f(81) + 1 = 5 + 1 = 6$;
 $f(729) = f(243) + 1 = 6 + 1 = 7$**