

1. The following regression output is for predicting annual murders per million from the percentage of citizens living in poverty in a random sample of 20 metropolitan areas.

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-29.901	7.789	-3.839	0.001
poverty%	2.559	0.390	6.562	0.000

$$s = 5.512$$

$$R^2 = 70.52\%$$

$$R^2_{adj} = 68.89\%$$

- (a) Write out the linear model.

$$\hat{y}_i = -29.901 + 2.559x_i$$

- (b) Interpret the slope.

For every percentage increase of citizens living in poverty, there is 2.559 increase in murders per million.

- (c) Interpret  $R^2$ .

There is good predictive power.  
70.52% of variation can be explained in annual murder per million can be explained by the percentage of citizens living in poverty.

- (d) Calculate the correlation coefficient.

$$r = \sqrt{R^2} = \sqrt{0.7052} = 0.8398$$

- (e) Interpret the correlation coefficient.

There is a strong positive linear relationship between the percentage of citizens living in poverty and the percentage of annual murders in million.

- (f) Predict the number of murders per million if one city has a 14% of its citizens living in poverty.

$$\hat{y}_i = -29.901 + 2.559(14) = 5.925$$

- (g) After a few months, the city with 14% of its citizens living in poverty reported the number of murders per million was 4.773. Calculate the residual for this city's reported murder rate.

$$e_i = y_i - \hat{y}_i = 4.773 - 5.925 = -1.152 \quad \text{overpredicted}$$

2. A regression line relating  $y$  = hours of sleep the previous day to  $x$  = hours studied the previous day is estimated using data from  $n = 10$  students. The estimated slope  $\beta_1 = -0.30$ . The standard error of the slope is 0.20.

- (a) What is the value of the test statistic for the following hypothesis test about , the population slope?

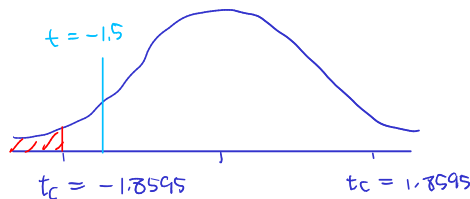
$$H_0: \beta_1 = 0$$

$$H_a: \beta_1 \neq 0$$

$$t = \frac{\hat{\beta}_1 - 0}{SE_{\hat{\beta}_1}} = \frac{-0.30}{0.20} = -1.5$$

- (b) At the  $\alpha = 0.10$  level, would you reject the null hypothesis? State your conclusion in terms of the problem.

$t_c = qt(\frac{\alpha}{2}, df = n - 2) = qt(0.05, 8) = \pm 1.8595$   
 Since the test statistic is NOT more extreme than the critical value, we FAIL to reject the null hypothesis and conclude the alternative is not true. There is not a linear relationship between hours studied the previous day, and the hours of sleep the previous day.



- (c) What is a 90% confidence interval for  $\beta_1$ , the population slope? Interpret the confidence interval you calculate.

$PE \pm t_c \cdot SE_{\hat{\beta}_1} = -0.3 \pm 1.8595(0.2) = (-0.6719, 0.0719)$   
 We are 90% confident that a one hour increase in hours studied the previous day is associated with somewhat between 0.6719 decrease and 0.0719 increase in hours of sleep the previous day.