

## Properties of Turing Machines

Turing machines have the following **closure properties**:

| <b>Turing-Decidable</b> | <b>Turing-Recognizable</b> |
|-------------------------|----------------------------|
| union                   | union                      |
| concatenation           | concatenation              |
| star                    | star                       |
| complementation         | --                         |
| intersection            | intersection               |

Turing-recognizable languages are NOT closed under complements! Why? Knowing that the Halting Problem is not decidable, if we assume  $L$  being recognizable forces  $L^C$  to be recognizable, then we can build a decider for  $L$  (reject when  $L^C$  accepts), which is not possible.

**This would make a great final exam question, wouldn't it?**