Chomsky Normal Form (CNF)

Chomsky Normal Form (CNF) is a very common form for context-free grammars (CFGs), and worth learning. As noted on Wikipedia, CNF is used in the CYK algorithm. The CYK algorithm will, given a CNF grammar and a string, decide whether the string is recognized by the grammar. And it does so quite efficiently! CYK can be modified easily to also generate a parse tree (automatically).

CNF is a grammar having the following general forms:

 $A \rightarrow BC$ // two variables on the right $A \rightarrow b$ // a single symbol on the right $S \rightarrow \varepsilon$ // the empty string

Every CFG can be converted to an equivalent one in CNF. There are a few variations on the conversion procedure into CNF. The one we covered in class has four steps:

- 1. Start with a new S_0 (a.k.a., eliminate start symbols on the right-hand side),
- 2. Eliminate ϵ rules of the form $A \rightarrow \epsilon$,
- 3. Eliminate unit rules of the form $A \rightarrow B$, and
- 4. Final clean-up into CNF formatting.

 $\label{thm:continuity} The following YouTube\ video\ does\ a\ nice\ job\ walking\ through\ the\ procedure\ using\ this\ specific\ method:$

CNF Conversion Video