# Algorithm Complexity I DCA 0209

ivanovitch.silva@ufrn.br @ivanovitchm







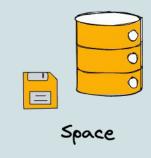
How to compare different algorithms and find the one that will perform the best?

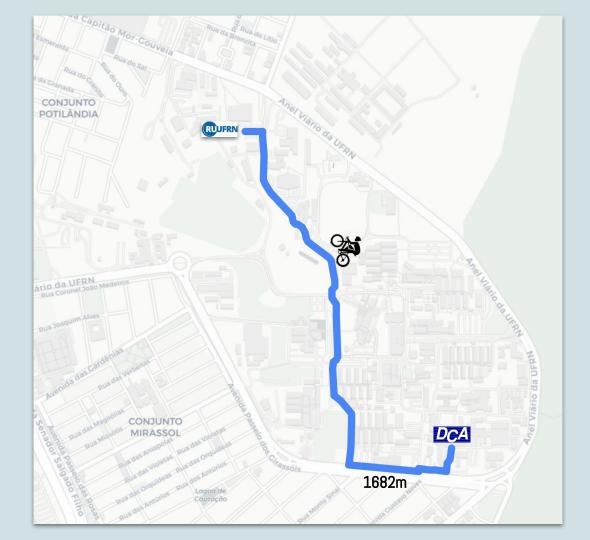


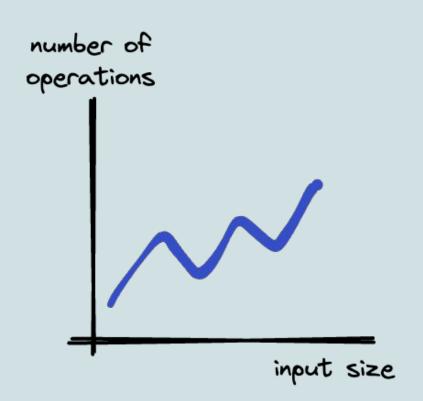
Time

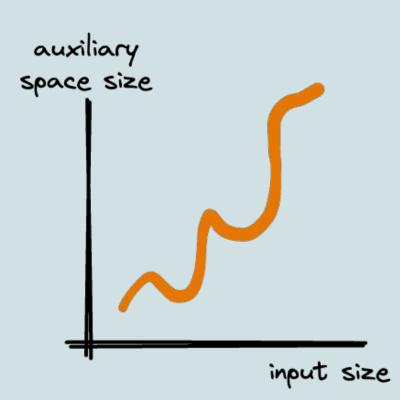








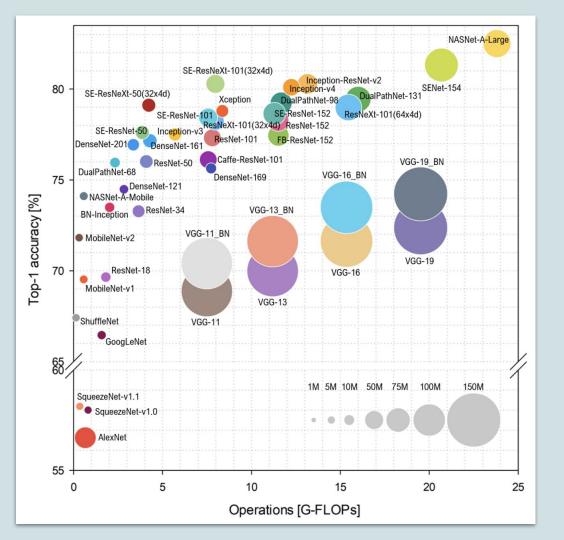




14,197,122 images, 21841 synsets indexed



https://www.image-net.org/



# Algorithm Complexity

## ML Model Evolution ImageNet

Source: S. Bianco, R. Cadene, L. Celona, and P. Napoletano, "Benchmark analysis of representative deep neural network architectures". IEEE Access, vol. 6, 2018.

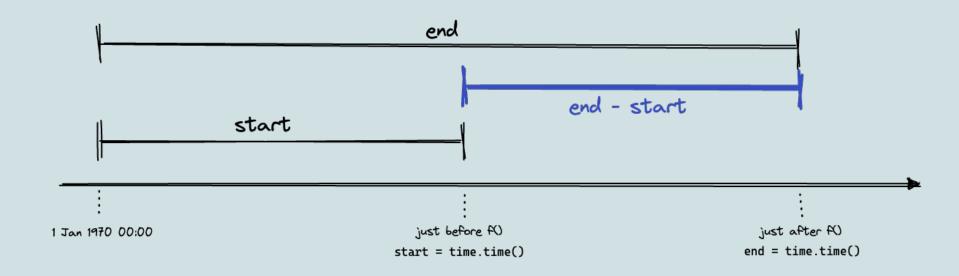
# 3 2 2 7 1 0 6 9 1 3

```
def maximum(values):
    answer = None
    for value in values:
        if answer == None or answer < value:
            answer = value
    return answer</pre>
```

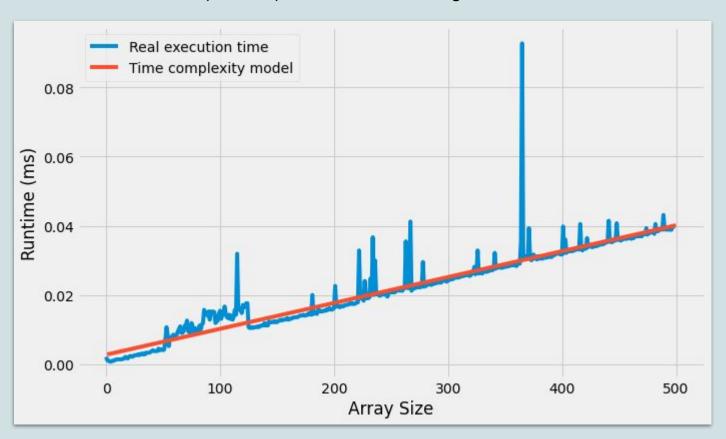
If we double the input, do we double the execution time, do we quadruple it, or something else entirely?

```
import time
start = time.time()
f()
end = time.time()
runtime = end - start
```

How to measure the execution times?



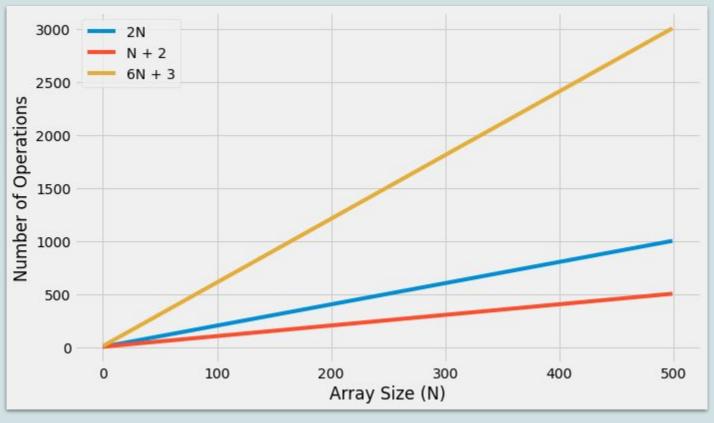
#### Exec maximum(values) 500 times change the values size



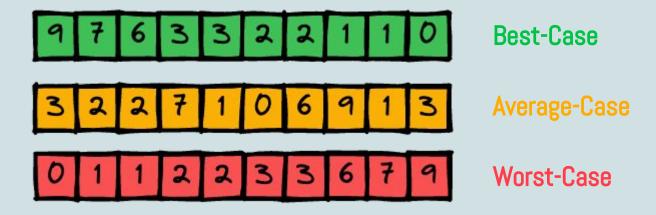


# Recall that we don't want to know the exact execution time, just how fast it is growing

$$egin{aligned} C_1 + C_2 imes N + C_3 imes N + C_4 imes N + C_5 \ (C_1 + C_5) + N(C_2 + C_3 + C_4) \ lpha + Neta \end{aligned}$$



Regardless of the values of  $\alpha$  and  $\beta$ , the function  $\alpha + N\beta$  is a straight line. We call an algorithm whose time complexity is a straight line a **linear time algorithm.** 



```
def maximum(values):
    answer = None
    for value in values:
        if answer == None or answer < value:
            answer = value
            return answer</pre>
```

How many times is this line executed?



### Two Number Sum

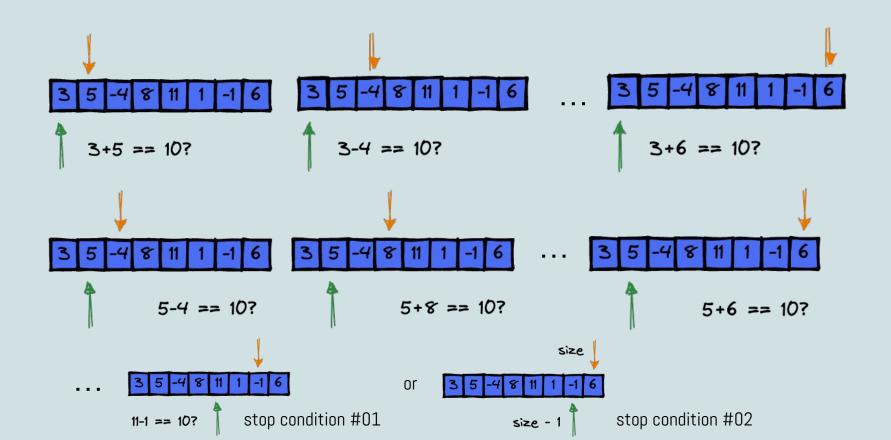
```
# sample input
array = [3,5,-4,8,11,1,-1,6]
targetSum = 10

# sample output
[-1,11] or [11,-1]
```

Write a function that take in a non-empty array of distinct integers and an integer representing a target sum. If any two numbers in the input array sum up to the target sum, the function should return then in an array, in any order. If no two numbers sum up to the target sum, the function should return an empty array.

Note that the target sum has to be obtained by summing two different integers in the array, you can't add a single integer to itself in order to obtain the target sum.

## Solution



## Solution

```
egin{split} &2(N-1)+3(N-1)^2+2\ &2(N-1)+2(N^2-2N+1)+2\ &2N^2-2N+2\gg N^2 \end{split}
```

```
def twoNumberSum(array, targetSum):
for i in range(len(array) - 1):
                                             #C1 N-1
   firstNum = array[i]
                                             #C2 N-1
                                             \#C3 (N-1)^2
   for j in range (i+1, len(array)):
     secondNum = array[j]
                                             \#C4 (N-1)^2
                                           \#C5 (N-1)^2
     if firstNum + secondNum == targetSum:
       return [firstNum, secondNum]
                                             #C6 1
 return []
                                             #C7 1
```