

Along the ~~normal~~ movement on the smooth inclined plane, the ball will receive  $g$  force. The  $g$  force NORMAL (perpendicular) to the ~~path~~ plane has no influence to the movement of the ball.

Only the  $g$  force parallel to the inclined plane

(~~perp~~ parallel to the plane) needs to be considered.

Let the velocity of the ball as the function of time,  $t$ , be  $v(t)$ .

So,  $v(t) = u - g \sin \alpha \cdot t$  . . . . .  $\rightarrow$  ①

Then, find time needed to travel  $\pm$  the distance  $L$ . That is,

$$L = ut - \frac{1}{2} g \sin \alpha t^2 \Rightarrow \frac{1}{2} g \sin \alpha t^2 - ut + L = 0$$

$$\Rightarrow t_{1,2} = \frac{u \pm \sqrt{u^2 - 2g \sin \alpha L}}{g \sin \alpha}$$

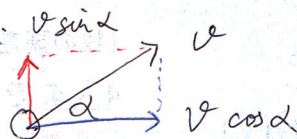
Using the above result, find the velocity of the ball at the end of  $L$ , that is  $v$  (using eqn ①)

$$v = u - g \sin \alpha \left( \frac{u \pm \sqrt{u^2 - 2g \sin \alpha L}}{g \sin \alpha} \right)$$

$$= u - u \mp \sqrt{u^2 - 2g \sin \alpha L}$$

$$v = \sqrt{u^2 - 2g \sin \alpha L}$$

~~At~~ At the end of the plane,  $L$ , the velocity of the ball is:



The ~~vertical~~ vertical part of  $v$  will receive the  $g$  force, so it will decrease to 0, then increased to more than 0 downward.

So the minimum speed of the ball is  $v \cos \alpha$ , i.e.,

$$\cos \alpha \sqrt{u^2 - 2g \sin \alpha L}$$

Note:  $u^2 - 2g \sin \alpha L > 0$  is the condition for the ball to be able to clear off the inclined plane.