First of all, I converted the lena.bmp to binary format by implementing *ConvertToBinary function* with threshold equal to 128, and this function is defined as followed:

```
def ConvertToBinary(originImg):
    binaryImage = Image.new('1', originImg.size)

for c in range(originImg.size[0]):
    for r in range(originImg.size[1]):
        originalPixel = originImg.getpixel((c, r))
        if (originalPixel >= 128):
            binaryImage.putpixel((c, r), 1)
        else:
            binaryImage.putpixel((c, r), 0)
    return binaryImage
```



Afterwards, a *downsampling function* is used to down sample the binary image to size = (64,64), by using 8x8 blocks as a unit, and take the topmost-left pixel as the downsampled data. The detailed of this function is defined as follow:

```
def downsampling(originImg, factor):
    downsamplingImage = Image.new('1', (64,64))
    for c in range(0, originImg.size[0], factor):
        for r in range(0, originImg.size[1], factor):
            # take the topmost-left pixel as the downsampled data
            downsamplingImage.putpixel((int(c/factor), int(r/factor)), orig
inImg.getpixel((c, r)))
    return downsamplingImage
```



Then after the preprocessing of binary image, I defined a *neighborhoodPixels function* to get set of neighborhood pixels which correspond to each position in the downsampling image:

```
def neighborhoodPixels(originImg, curPos):
    #define the neighborhood array size
    nbPixs = np.zeros(9)
    #current position in the image
    x, y = curPos

for dx in range(3):
        for dy in range(3):
        #calculating the position x,y in the image
        posX = x + (dx - 1)
        posY = y + (dy - 1)
        # Check if the pixel is out of boundary
        if ((0 <= posX < originImg.size[0]) and (0 <= posY < originImg.size[1])):

        # store the position in neighborhood array
            nbPixs[3 * dy + dx] = originImg.getpixel((posX, posY))
        else:
            nbPixs[3 * dy + dx] = 0
    return nbPixs</pre>
```

Then I defined *hFunc function* to classify every 2x2 region in 3x3 neighborhood pixels into types "q", "r" or "s":

```
def hFunc(b, c, d, e):
    if ((b == c) and (b != d or b != e)):
        return 'q'
    if ((b == c) and (b == d and b == e)):
        return 'r'
    if (b != c):
```

and fFunc is used to determine whether this 3x3 neighborhood pixels is 5,4,3,2,1 or 0.

```
def fFunc(a1, a2, a3, a4):
    if ([a1, a2, a3, a4].count('r') == 4):
        # Return label 5 (interior)
        return 5
    else:
        # Return count of 'q'
        return [a1, a2, a3, a4].count('q')
```

Below is the implementation of Yokoi connectivity number, which covers the whole process that I addressed above, and then it saves the result as a 2D array *Yokoi arr*:

```
def YokoiConnectivityNumber(originImg):
    Yokoi_init_list = [[ " " for x in range(originImg.size[0])] for y in ra
nge(originImg.size[1])]
    Yokoi_arr = np.array(Yokoi_init_list) #defined a 2d array to store the
result
    for c in range(originImg.size[0]):
        for r in range(originImg.size[1]):
            if (originImg.getpixel((c, r)) != 0):
                nbPixs = neighborhoodPixels(originImg, (c, r))
                Yokoi_arr[r, c] = fFunc(
                    hFunc(nbPixs[4], nbPixs[5], nbPixs[2], nbPixs[1]),
                    hFunc(nbPixs[4], nbPixs[1], nbPixs[0], nbPixs[3]),
                    hFunc(nbPixs[4], nbPixs[3], nbPixs[6], nbPixs[7]),
                    hFunc(nbPixs[4], nbPixs[7], nbPixs[8], nbPixs[5]))
            else:
                Yokoi_arr[r, c] = ' '
    return Yokoi_arr
```

Implementation of main:

```
if __name__ == '__main__':
    originImg = Image.open('lena.bmp')
    # Get binary image.
    binaryImg = ConvertToBinary(originImg)
```

```
binaryImg.save('binary.bmp')

# Get downsampling image.
dsaImg = downsampling(binaryImg, 8)
dsaImg.save('downsampling.bmp')

# Get Yokoi Connectivity Number
Yokoi_arr = YokoiConnectivityNumber(dsaImg)

with open('Yokoi.txt', "w") as txt_file:
    for line in Yokoi_arr:
        txt_file.write("".join(line) + "\n") # works with any number of elements in a line
```

Result in Yokoi.txt: (shown in next page)

```
121111111111122322221
111111111
                                  1111111111111
15555551
             115555555511 2 11 11 1155555555511
15555551
             1 2115555112 21112221 155555555551
                                                  21
15555551
            1 2 155112 22221511
                                  1555555555511
                                                 1
             15555551
15555551
                            1321 15555555555511
15555551
               12 1 121111
15111551
               1322 1155551111
                                   15555555555551
111 1551
                1 121555555511
                                   15555555555511
11 1551
                    21155555511
                                  15511155555511
21 1551
                    2 15555555111
                                  1551 11555511
1 1551
                    2 155555555511 1551 115551
  1551
                  1121155555555555 1551 15511
   1551
                  15555555555555511 1551 1111
  1551
            1
                 22211555555555555511 1151 11
                                                 1151
            2 22 1 1555555555555511 151 11111
   1551
                                                 1551
   1551
             2
                 1 11555555555555551 151 115551
                                                 11551
   1551
             2
                    115555555555555555111511155511
                                               115551
   1551
             12
                   11555555555555555555555555555
                                               155551
   1551
           11
                1155551
  1551
           1555551
  1551
           1511 1 1251121111121115555555555111
                                              11555551
  1551
           15521 1 121 1 11 1 15555555111 0
                                             15555551
            1151 132 2
  1551
                             1155555111 0
                                            115555551
  1551
             151 0 322
                            115555111 121
                                             155555551
             1221 2
                            1555551 131
   1551
                                             1155555551
             2 0 1
                            115555511 1
   1551
                                            1155555551
                       0 1155555551 0
   1551
                                            1 155555551
   1551
             2
                          11555555551
                                            21155555551
                                           1555555551
   1551
                         115555555551
  1551
                        11511115555521 1
                                          115555555551
             1
                       11111 1155511 2
                                          15555555551
  1551
             1 1
  1551
                       111 15111 2
            131
                                          155555555551
                     1121 1 111 1 2 1155555555551
  1551
           121 0
          11
                      111 1 221 11 1 2 15555555555551
  1551
                      21 121 11 1111 2
22 1511111111551 2
   1551
          12 0
                                         155555555551
                 12
    1551
                                         11555555555551
   1551
         1
                     2
                         1555551115511
                                         1555555555551
                                     1 15555555555551
                    22 12555551 15551
   1551 2 0
                  0
                                      2 115555555555551
                    1 1555511 11511
   1551
           0 0
                        155551 1 151
                                      2 15555555555551
   1551
                   21
   1551
                  2
                        15555112 151
                                      2 155555555555551
  1551
             1 11
                        1155555511111
                                      2 155555555555551
             2 22
   1551
                        1115111111212
                                      21155555555555551
             1 12
   1551 0
                         151 2 1
                                      15555555111555551
                         1111 121
             0 0 0
   1551
                                       155555551 1555551
   1551
                0
                          111111111
                                       155555551 1555551
                          115551
                                      155555551 1555511
   1551
             Θ
                                      211111111 155511
    1551
                            15551
   11521
                                      2 11 115511
           1 12
                         122155511
   151 0
            1 1
                          155555111
                                      2111 15511
1
22 1511
                1
                           15555555111 155111 1511
22 1511
               1
                           15555555551 155551 1151
 2 151
                 0 1
                         111555555555511 155511 1511
                         155555555555511 15551 12151
 2 1521
           0
                1
 2 151
                         15555555555551 155511 1551
                121
  2 1511
                       0 155555555555551 115551 1511
                 11
                         155555555555551 111111151
  21 1511
  11 151
               Θ
                         1155555555555511
                                          111511
 11 151
                        1555555555555551
                                           151
 11 151
                        11555555555555555
 11 151
                        115555555555555511
  11 151
                       0 1555555555555555
 11 111
            Θ
                       1211111111111111111111
```