



**Universidad Nacional del Altiplano**  
Escuela de Posgrado  
Doctorado en Ciencias de la Computación

## Data Mining

### Unit 4. Data Mining with Complex Networks

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2025 - I

## Contenido

- Complex Networks
- Networks Modeling
- Network Measurements
- Community Detection
- Applications

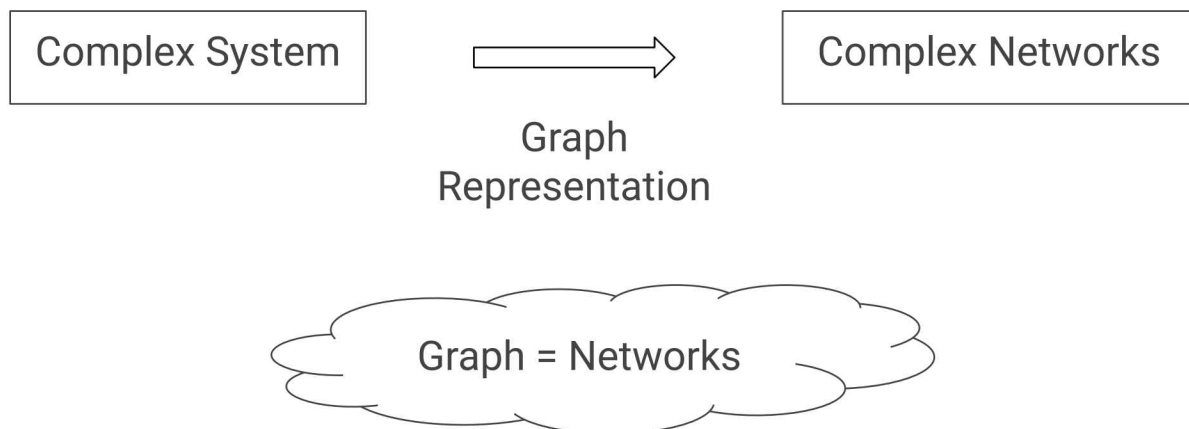
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- Complex Networks
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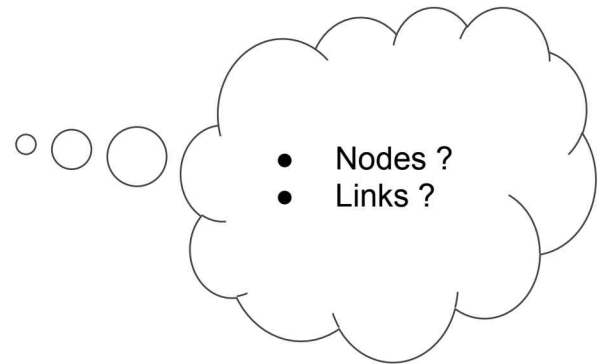
## Complex Networks

- They are the graph representation of a complex system



# Complex Networks

- Social Networks
- Communication
- Computer Science
  - Circuits
  - Image Processing and Analysis
- Internet
- Citations
- Electric power transmission systems
- Biomolecular Networks
- Epidemic spreading
- etc.



[3] <https://doi.org/10.1080/00018732.2011.572452>

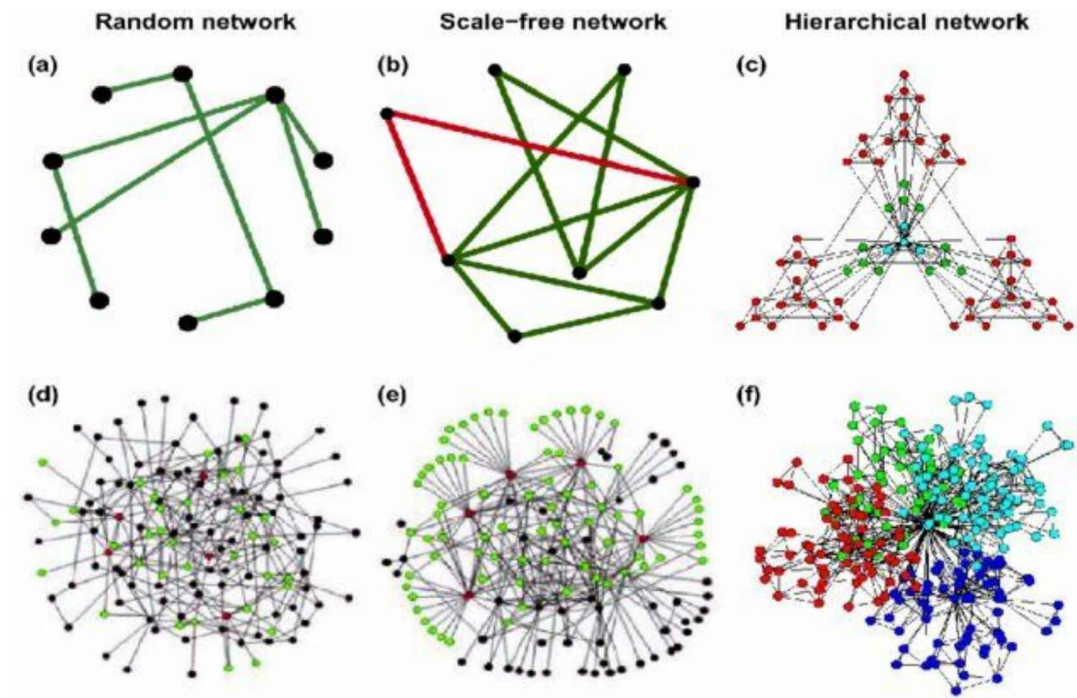
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- Complex Networks
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[32] [https://doi.org/10.1142/9789812772367\\_0001](https://doi.org/10.1142/9789812772367_0001)

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## Networks Modeling

- Make an approximation to the real representation of the complex system.

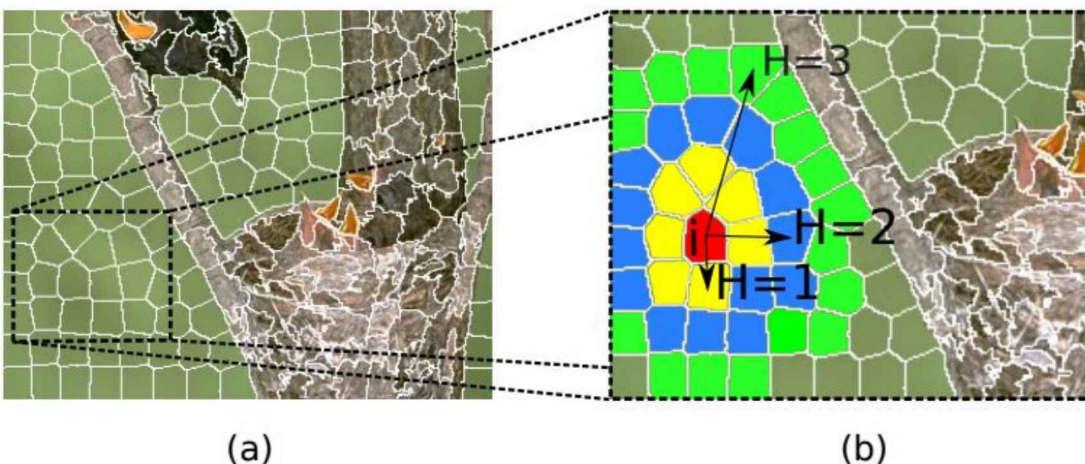


Figura 12 – Estratégia de criação de arestas em vários níveis. (a) Um subconjunto de superpixels; (b) Criação de arestas para o vértice  $i$  (superpixel vermelho) e seus  $j$  vizinhos para o primeiros níveis ( $H=3$ ) denotados com cores amarelo, azul, e verde.

[33] <https://doi.org/10.11606/T.55.2021.tde-09032021-123250>

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# Networks Modeling

- Make an approximation to the real representation of the complex system.

$$w(i, j) = \begin{cases} e^{-\left(\frac{F^2}{\sigma^2}\right)}, & \text{si } j \in r, \\ 0, & \text{caso contrario} \end{cases}$$

$$w_{gEU}(i, j) = e^{-\left(\frac{\text{Euclidean}(i, j)^2}{\sigma^2}\right)}$$

$$w_{gMH}(i, j) = e^{-\left(\frac{\text{Manhattan}(i, j)^2}{\sigma^2}\right)}$$

$$w_{gCH}(i, j) = e^{-\left(\frac{\text{Chebyshev}(i, j)^2}{\sigma^2}\right)}$$

$$w_{gCO}(i, j) = e^{-\left(\frac{1 - \text{Cosine}(i, j)^2}{\sigma^2}\right)}$$

$$w_{gTA}(i, j) = e^{-\left(\frac{1 - \text{Tanimoto}(i, j)^2}{\sigma^2}\right)}$$

$$w_{gFU}(i, j) = e^{-\left(\frac{1 - \text{Fu}(i, j)^2}{\sigma^2}\right)}$$

$$w_{gMB}(i, j) = e^{-\left(\frac{\text{Mahalanobis}(i, j)^2}{\sigma^2}\right)}$$

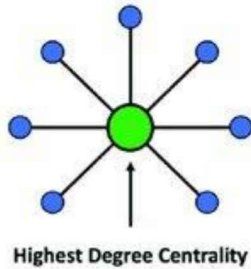


Shi and Malik (2000)

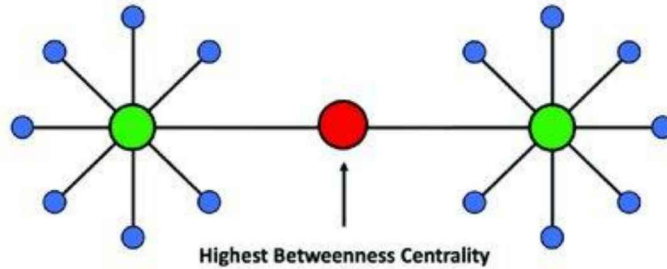
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A Degree Centrality



B Betweenness Centrality



[34] <https://doi.org/10.3390/tomography8030116>

[35] <https://doi.org/10.1080/00018730601170527>

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# Community Detection

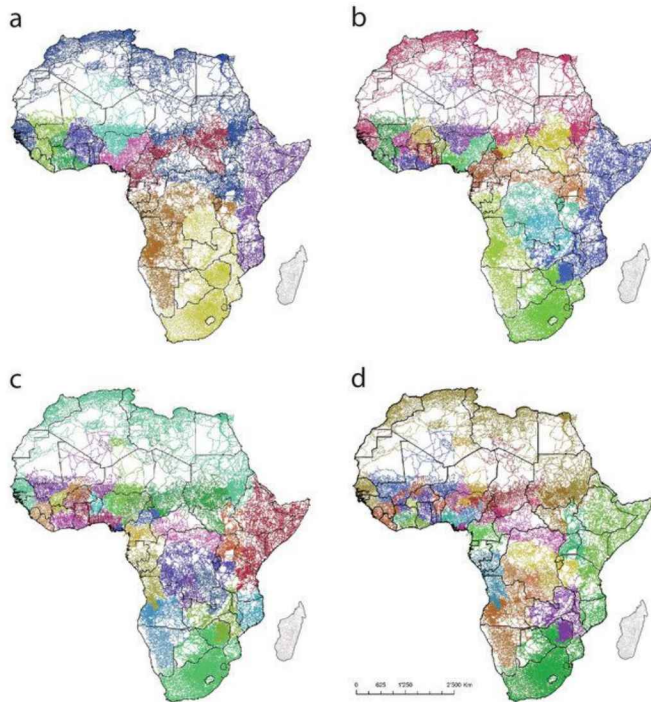


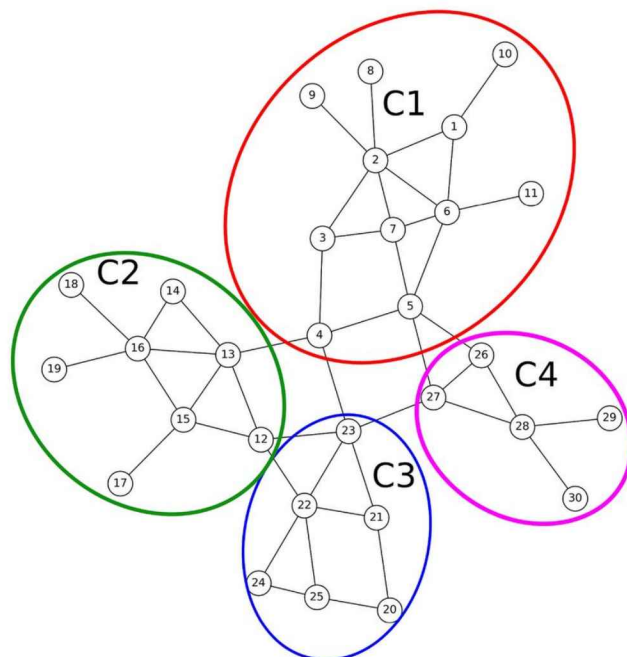
Fig. Example outputs of community detection on the unweighted Africa road network, constrained to (a) 10 communities; (b) 20 communities; (c) 30 communities and (d) 40 communities. Figure produced using ArcGIS v10.5 ([www.arcgis.com](http://www.arcgis.com)).

[36] <https://www.nature.com/articles/s41598-018-22969-4>

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# Community Detection



[37] <http://dx.doi.org/10.1038/s41598-023-41460-3>

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# Community Detection

## Finding community structure in very large networks

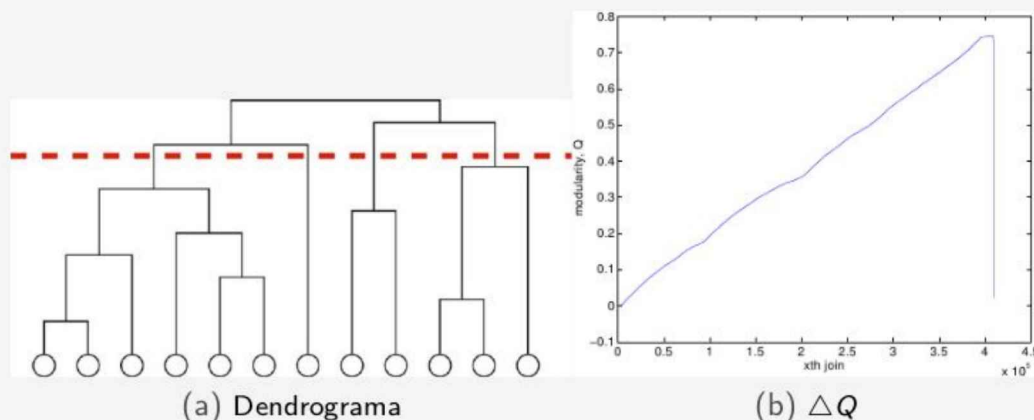


Figura: (a) Representação do dendrograma, para o algoritmo *fast greedy*, a **linha vermelha** representa o corte do dendrograma empregando o máximo valor de  $\Delta Q$ . (b) No eixo x é mostrado o número de uniões realizadas entre duas comunidades ao longo do algoritmo, nela é mostrada o acrescentamento de  $\Delta Q$ , onde  $\Delta Q$  apresenta um único valor máximo.

[38] <http://dx.doi.org/10.1103/PhysRevE.70.066111>

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# Community Detection

## Near Linear Time Algorithm to Detect Community Structures in Large-Scale Networks

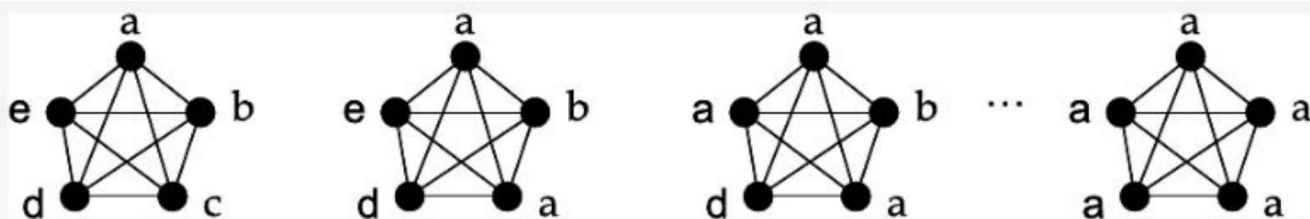


Figura: Atualização de rótulos no *label propagation*: na figura de esquerda a direita, os vértices são atualizados um por um. Neste caso existe uma grande densidade de arestas, isto faz possível que todos os vértices adquiram o mesmo rótulo.

[39] <http://dx.doi.org/10.1103/PhysRevE.76.036106>

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## Applications

### Segmentation of Large Images with Complex Networks

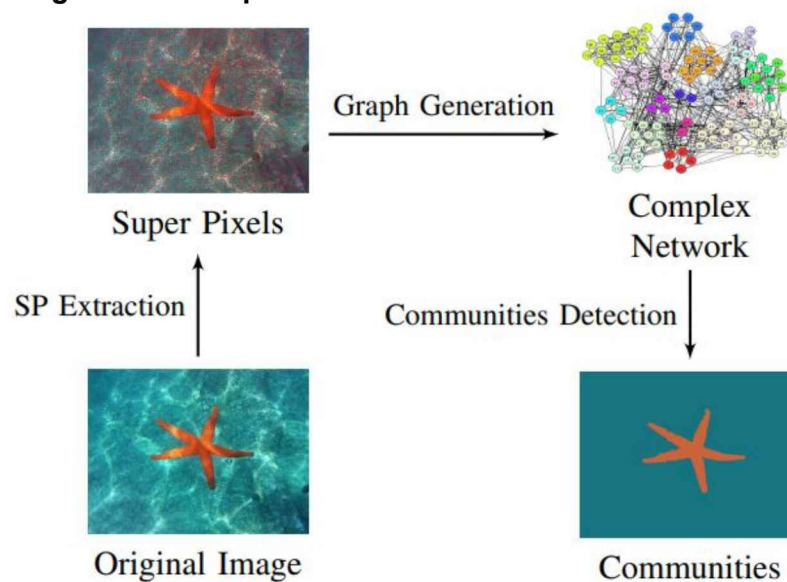


Fig. 4. Image segmentation approach based on complex network combined with super pixels. In the figure, SP = Super Pixel.

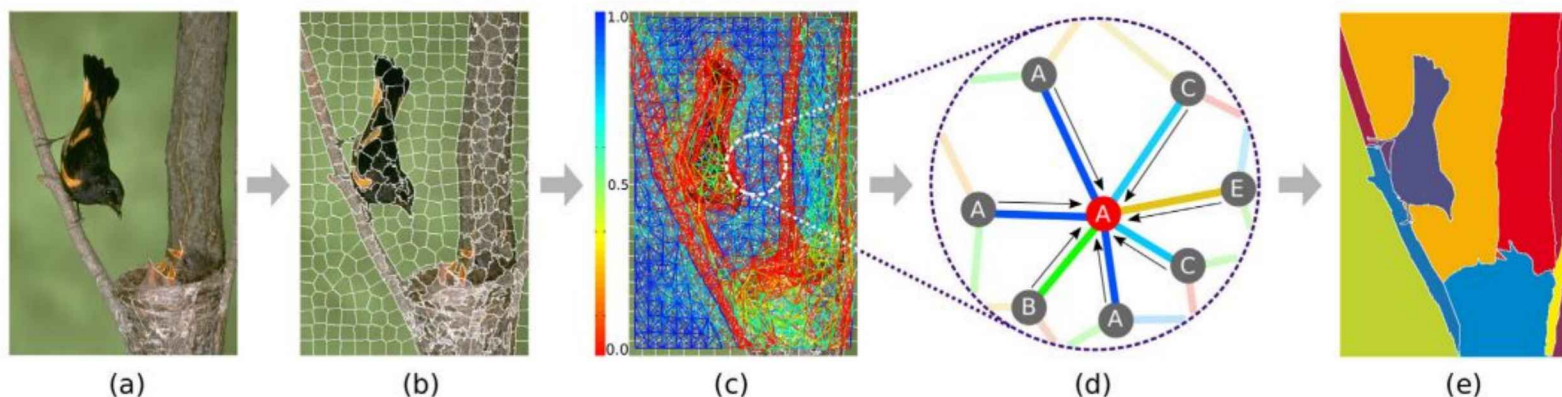
[40] <https://doi.org/10.1109/SIBGRAP.2012.13>

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# Applications

## Automatic image segmentation based on label propagation



**FIGURE 1** Illustration of our method. (a) Input image; (b) super-pixel extraction; (c) graph building. Blue edges indicate high similarity among vertices, whereas red edges represent low similarity; (d) label propagation. The red vertex is assigned the most frequent label in its neighbourhood, (e) segmentation result, that is, regions containing super-pixels with the same label

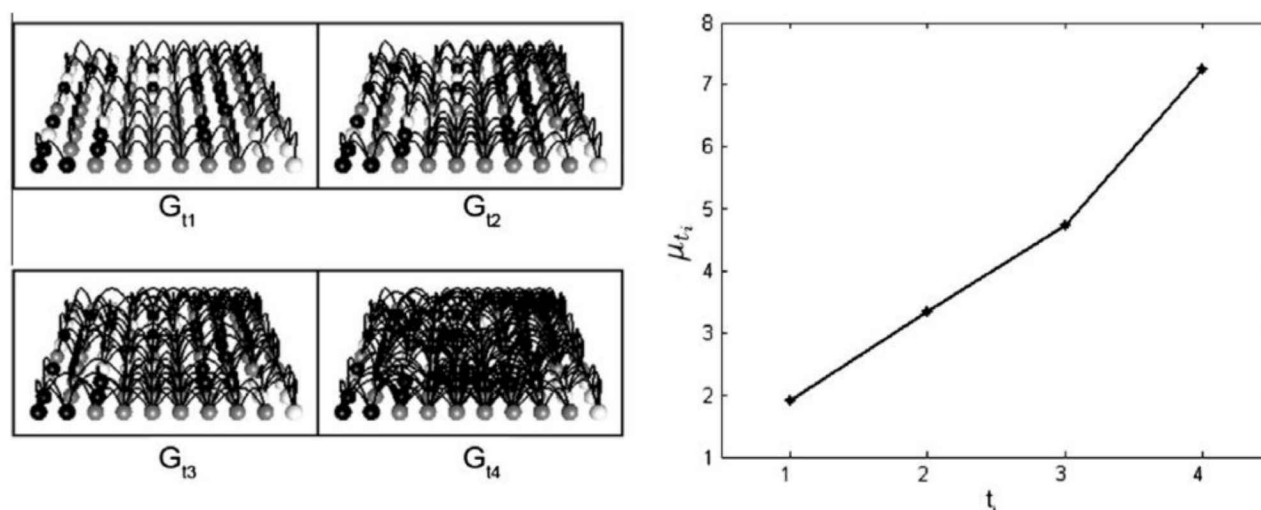
[41] <https://doi.org/10.1049/ipr2.12242>

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# Applications

## Texture analysis and classification: A complex network-based approach



**Fig. 2.** Left: a texture example modeled as a Complex network, different threshold values ( $t_1 \dots t_4$ ) make different topological features. Right: complex network characterization by its evolution (mean degree at each threshold  $t_i$ ).

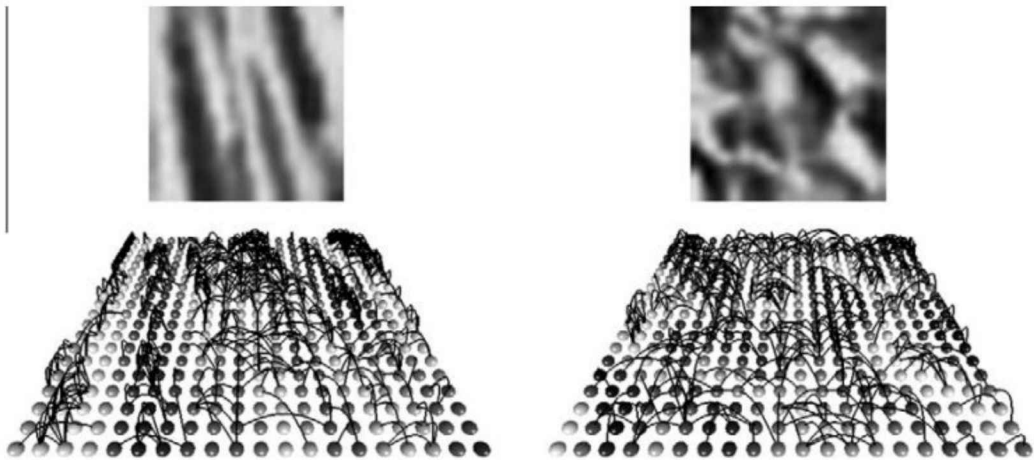
[42] <https://doi.org/10.1016/j.ins.2012.07.003>

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# Applications

## Texture analysis and classification: A complex network-based approach



**Fig. 3.** Two complex networks, at same threshold value, for two different texture samples. The differences in their topological features results in measurements which can be used as texture descriptors.

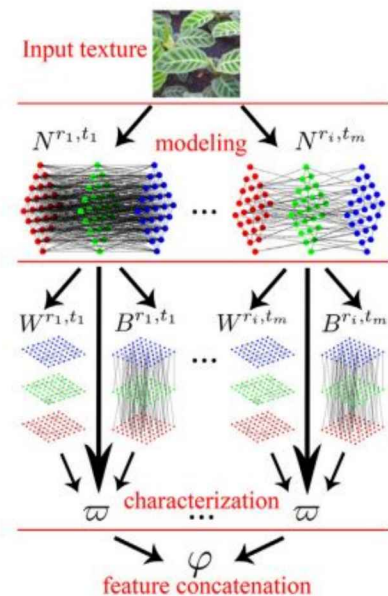
[42] <https://doi.org/10.1016/j.ins.2012.07.003>

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# Applications

## Multilayer complex network descriptors for color–texture characterization



**Fig. 6.** Step-by-step of the proposed method. The modeling step considers the network dynamic evolution, thus combining each parameter  $r$  and  $t$  results in a set of networks  $N$ . The characterization consists on first obtaining the subnets  $W$  and  $B$  and then quantify the structure of all networks ( $N$ ,  $W$  and  $B$ ) with degree ( $k$ ) and clustering ( $c$ ) statistics  $\omega$ . The final feature vector  $\varphi$  is the concatenation of statistics from all networks.

[43] <https://doi.org/10.1016/j.ins.2019.02.060>

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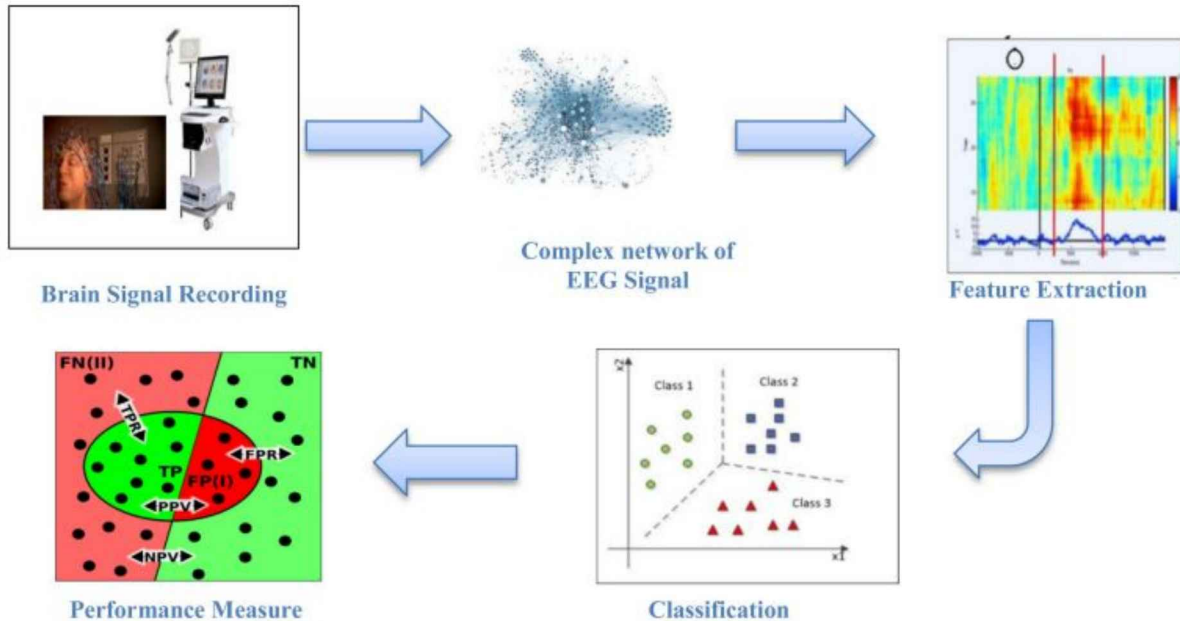


Fig. 2. Schematic representation of general sequence of steps followed by graph theory based approaches for epileptic seizure detection from brain EEG signals.

[44] <https://doi.org/10.1109/RBME.2021.3055956>

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**Gracias**

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