

## APPENDIX I

### TIME COMPLEXITY ANALYSES OF ALL CONSIDERED METHODS

For easy exposition, we analyze the complexity of the methods in the following order: HM, MHM, IMIHM, AGL, GP, JBI, AJBI, CMCC, our algorithm, and its modified version.

#### A. For HM, MHM and IMIHM

For the HM and MHM methods, once the HE mapping function has been constructed in  $O(|\Omega_t|)$  time using all target pixels in  $\Omega_t$  and all source pixels in  $\Omega_s$ , it can be reused for all target pixels in  $I_t$ . For the HM method, it takes  $O(|I_t|)$  time to complete the overall color correction task because the color of each target pixel can be corrected in  $O(1)$  time using the precomputed HE mapping function.

As mentioned before, the main difference between HM and MHM is that for the MHM method, when the color of each target pixel  $p_t$  corresponds to a nearly vertical or horizontal segment in the HM mapping function, the color of  $p_t$  is corrected by randomly sampling from a segment defined by a uniform distribution. Therefore, for MHM, it also takes  $O(|I_t|)$  time to complete the overall color correction task.

In the IMIHM method, the number of iterations and the overlapping rate between two consecutive sliding windows are set to 9 and 0.8, respectively. At the first iteration, using the sliding window approach and the HM mapping function, it takes  $O(|\Omega_t|)$  time to perform color correction on the target pixels within the window. At the second iteration, using the sliding window approach with overlapping rate 0.8 to build up a new HE mapping function, it takes  $O(|\Omega_t|)$  time to correct color for the target pixels in the newly moved window. In terms of the worst case consideration, for IMIHM, it also takes  $O(|I_t|)$  time to complete the overall color correction task.

#### B. For AGL

The AGL method consists of a global least squares optimization stage and a local compensation stage. In the global stage, the mean and standard deviation of the overlapping area are computed in  $O(|\Omega_t|)$  time. A set of linear equations is then constructed and solved via a least squares approach, which requires  $O(n^3)$  time, where  $n$  denotes the number of variables associated with all image pairs. For instance, for a set of 10 images,  $n$  equals 18 ( $= 2 \times 9$ ). In the local stage, each target image  $I_t$  is divided into a set of grids, and the color statistics within each grid are computed in  $O(|I_t|)$  time. Each target pixel is then adjusted using bilinear interpolation and adaptive gamma correction, both of which operate in  $O(1)$  time, resulting in an overall complexity of  $O(|I_t|)$  to refine the color of each target image  $I_t$  in the local stage. Therefore, the total time complexity of AGL is bounded by  $O(|I_t|)$  to complete the color correct task for  $I_t$ .

#### C. For GP

In the GP method, first, it takes  $O(|\Omega_t|)$  time to construct the HE mapping function using the source and target pixels in  $\Omega_t$ . Next, six equidistant anchor points are selected from

the mapping function. Then, it takes  $O(|\Omega_t|)$  time to calculate the gradient statistics of the target image. Based on the six anchor points and the constraints along with the calculated gradient statistics, a spline function is determined in  $O(1)$  time using the convex quadratic programming technique in practice. Finally, using the spline function, the color correction of all target pixels in  $I_t$  can be completed in  $O(|I_t|)$  time. Therefore, for GP, its time complexity is bounded by  $O(|I_t|)$ .

#### D. For JBI and AJBI

In the JBI method, the color differences along the stitching line  $L$  in the overlapping area  $\{\Omega_s, \Omega_t\}$  are fully utilized to correct the color of each target pixel in  $I_t$ . Using the JBI technique, it takes  $O(|L|)$  time to correct color for each target pixel in  $I_t$ . Overall, for JBI, it takes  $O(|L||I_t|)$  time to complete the color correction task for  $I_t$ . In the AJBI method, considering the color differences of an appropriate stitching line interval, it takes  $O(|L|)$  time to correct color for each target pixel. Overall, for AJBI, its time complexity is bounded by  $O(|L||I_t|)$  time to complete the color correction task.

#### E. For CMCC

For the CMCC method, using the 4:2:0(L) downsampling scheme, and noting that  $|I_t| = |I_s|$  as stated in Table I, it takes  $O(|I_t|)$  time to downsample  $I_t$  and  $I_s$ , obtaining the downsampled target and source images,  $I_t^d$  and  $I_s^d$ , respectively. Using the dehazing method [??], it takes  $O(|I_t^d|)$  time to obtain the enhanced version of  $I_t^d$ , denoted by  $I_t'^d$ . Then, the low frequency component of  $I_t'^d$  is replaced by that of  $I_s^d$ , denoted by  $I_t''^d$ . Furthermore, it takes  $O(|I_t|)$  time to upsample  $I_t''^d$  to obtain the upsampled image  $I_t''$ . Based on a grid approach, using the mean compensation technique between  $I_t''$  and  $I_t$ , the color of  $I_t$  can be corrected in  $O(|I_t|)$  time. Overall, for CMCC, it takes  $O(|I_t|)$  time to complete the color correction task.

#### F. For Our Algorithm and Our Modified Algorithm

According to Theorem 1, the time complexity of our algorithm is  $O(|I_t||\Omega_t|)$ . Using our modified algorithm, we show that the time complexity can be reduced to  $O(|I_t|)$  time, while preserving the color correction quality of the original version.

As described in Subsection III-A, the inlier correspondence set between  $\Omega_s$  and  $\Omega_t$  is defined as  $C = \{c_1, c_2, \dots, c_m\}$  with  $m \leq |\Omega_t|$ . Each inlier correspondence  $c_i$  is transformed into a single point  $p_i$  by aligning the source and target feature points. Next, based on the  $m$  points  $p_1, p_2, \dots, p_m$ , the Delaunay triangulation subroutine “getTriangleList” [??] is applied to produce a set of triangles in  $O(|\Omega_t|)$  time due to  $m \leq |\Omega_t|$ . To correct each target pixel  $p_t$  in  $\Omega_t$ , we first identify the triangle that contains  $p_t$ , which can be done in  $O(1)$  time. For  $p_t$ , let the three corner points of the searched triangle be denoted by  $p'_1, p'_2$ , and  $p'_3$  corresponding to the three correspondences  $c'_1, c'_2$ , and  $c'_3$ , respectively. Based on the color differences of  $c'_1, c'_2$ , and  $c'_3$ , by Eqs. (2)–(3), the JBI-based color correction term for  $p_t$  in  $\Omega_t$  can be derived in  $O(1)$  time. Therefore, the EC-based fusion method can correct

the color of  $p_t$  in  $O(1)$  time. As a result, correcting color for all target pixels in  $\Omega_t$  can be done in  $O(|\Omega_t|)$  time.

After using our modified method to correct color for target pixels in  $\Omega_t$ , we further present the modified BRI-based fusion method to correct color for target pixels in  $I_t \setminus \Omega_t$ . As an initial ripple point, each target pixel  $p_i$  on the boundary  $B$  propagates its color difference  $D(p_i)$  (see Eq. (12)) and its position  $(x, y)$  forward to the neighboring target pixels in  $I_t \setminus \Omega_t$  until all propagated ripples of  $p_i(x, y)$  touch the fifth ripple instead of touching the boundary of the non-overlapping area. For all target points in the propagated five ripples, the BRI-based fusion method (see Eq. (17)) is applied to correct color for these target pixels, and it takes  $O(|B|)$  time. Otherwise, for the remaining target points, the HE method is applied to correct color for these target pixels directly, and it takes  $O(|I_t| - |\Omega_t| - 5|B|)$  time. As a result, the color correction task for target pixels in  $I_t \setminus \Omega_t$  can be done in  $O(|I_t|)$  time. Combining the time complexities spent in correcting color for target pixels in  $\Omega_t$  and  $I_t \setminus \Omega_t$ , the total time complexity of our modified algorithm is  $O(|I_t|)$  ( $= O(|\Omega_t| + |I_t|)$ ) time.