

# CSC411H1S Project 4

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1. The board is represented by a flat 9-element NumPy tuple. Turn denotes whose turn it is (1 for X, 2 for O). Done denotes whether the game is done (True if game is over, False otherwise.)

Below is an example of a sample game played against myself.

```
Python 2.7.14 |Anaconda custom (64-bit)| (default, Oct 5 2017, 02:28:52)
[GCC 4.2.1 Compatible Clang 4.0.1 (tags/RELEASE_401/final)] on darwin
env.render()
====
env.step(0)
Out[3]: (array([1, 0, 0, 0, 0, 0, 0, 0, 0]), 'valid', False)
env.render()
x..
====
env.step(4)
Out[5]: (array([1, 0, 0, 0, 2, 0, 0, 0, 0]), 'valid', False)
env.render()
x..
.o.
====
env.step(8)
Out[7]: (array([1, 0, 0, 0, 2, 0, 0, 0, 1]), 'valid', False)
env.render()
x..
.o.
..x
====
env.step(2)
Out[9]: (array([1, 0, 2, 0, 2, 0, 0, 0, 1]), 'valid', False)
env.render()
x.o
.o.
..x
====
env.step(6)
Out[11]: (array([1, 0, 2, 0, 2, 0, 1, 0, 1]), 'valid', False)
env.render()
x.o
.o.
x.x
====
env.step(3)
Out[13]: (array([1, 0, 2, 2, 2, 0, 1, 0, 1]), 'valid', False)
env.render()
x.o
oo.
x.x
====
env.step(7)
Out[15]: (array([1, 0, 2, 2, 2, 0, 1, 1, 1]), 'win', True)
env.render()
x.o
oo.
xxx
=====
```

```

env.done
Out[17]: True
env.step(1)
Out[18]: (array([1, 0, 2, 2, 2, 0, 1, 1, 1]), 'done', True)

```

2. (a) The following is the new implemented policy

Listing 1:

```

1  class Policy(nn.Module):
2      """
3      The Tic-Tac-Toe Policy
4      """
5      def __init__(self, input_size=27, hidden_size=64, output_size=9):
6          super(Policy, self).__init__()
7
8          self.linear1 = nn.Linear(input_size, hidden_size)
9          self.linear2 = nn.Linear(hidden_size, output_size)
10
11     def forward(self, x):
12         x = F.relu(self.linear1(x))
13         x = self.linear2(x)
14         return F.log_softmax(x)

```

- (b) The 27 dimensions are a flattened encoding of a one-hot encoding of the state of the board. If `.view(3,9)` is applied to the array, the columns would be the one-hot encoding of each cell in the board (starting from the top left, going across each row, and ending in the bottom right).  
 If a column contains “1 0 0,” the cell is empty.  
 If a column contains “0 1 0,” the cell is occupied by an X.  
 If a column contains “0 0 1,” the cell is occupied by an O.
- (c) The value in each dimension means the chance that making the move (e.g. adding an X into that cell) would result in winning the game. This policy is stochastic because it samples the next move from a distribution, rather than following a deterministic algorithm.
3. (a) The implementation of **compute\_returns** is shown below.

Listing 2:

```

1  def compute_returns(rewards, gamma=1.0):
2      """
3      Compute returns for each time step, given the rewards
4      @param rewards: list of floats, where rewards[t] is the reward
5                      obtained at time step t
6      @param gamma: the discount factor
7      @returns list of floats representing the episode's returns
8          G_t = r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + ...
9
10     >>> compute_returns([0,0,0,1], 1.0)
11     [1.0, 1.0, 1.0, 1.0]
12     >>> compute_returns([0,0,0,1], 0.9)
13     [0.7290000000000001, 0.81, 0.9, 1.0]
14     >>> compute_returns([0,-0.5,5,0.5,-10], 0.9)
15     [-2.5965000000000003, -2.8850000000000002, -2.6500000000000004,
16         -8.5, -10.0]
17     """
18     # TODO

```

```

18     result = []
19     for index in range(len(rewards)):
20         sum_returns = 0
21         power = 0
22         for i in range(index, len(rewards)):
23             sum_returns = sum_returns + ((gamma ** power) * rewards[i
24             ])
25             power = power + 1
26         result.append(sum_returns)
27     return result

```

- (b) If we update the weights in the middle of an episode, it would lead to erroneous results since the algorithm does not know the terminal state of the episode when it's updating the weights. For instance, if the terminal state for an agent is "loss", then this will cancel out all the rewards that are associating with the agent's previous actions in the episode. Therefore, we should not update the weights in the middle of an episode.

Listing 3:

```

4. (a) def get_reward(status):
2     """Returns a numeric given an environment status."""
3     return {
4         Environment.STATUS.VALID_MOVE : 0,
5         Environment.STATUS.INVALID_MOVE: -99,
6         Environment.STATUS.WIN : 1,
7         Environment.STATUS.TIE : 0,
8         Environment.STATUS.LOSE : -1
9     }[status]

```

- (b) The reward for a valid move is 0, since a single valid move doesn't directly contribute to a win or a loss. The reward for an invalid move is -99, since we really don't want our neural network to try invalid moves. Making invalid moves is worse than losing the game. The reward for a win is 2, and that's because we want to encourage our neural network to optimize for wins. The reward for a tie is 1, and that is because we want to encourage the neural network to finish the game, but we don't want the neural network to choose this option over a win. The reward for a loss is -1, since we want to discourage losses. The magnitude of these rewards are mostly close to zero, except for invalid moves. This is because all of the regular states are states that could occur in regular play, and since we really want to discourage invalid moves, having the rest of the rewards close together makes the -99 penalty more meaningful.
5. (a) The hyperparameter we tweaked was the  $\gamma$  value (discount factor) in order to improve the performance of the model, since a lower  $\gamma$  value would help the model prioritize shorter paths to win, which is a strong strategy when it comes to playing tic tac toe. Longer strategies would give the opponent more of an opportunity to disrupt the strategy, or even win in the shorter term before the strategy can complete.
- The learning curve given the above rewards and the tweaked  $\gamma$  value is in Figure 1

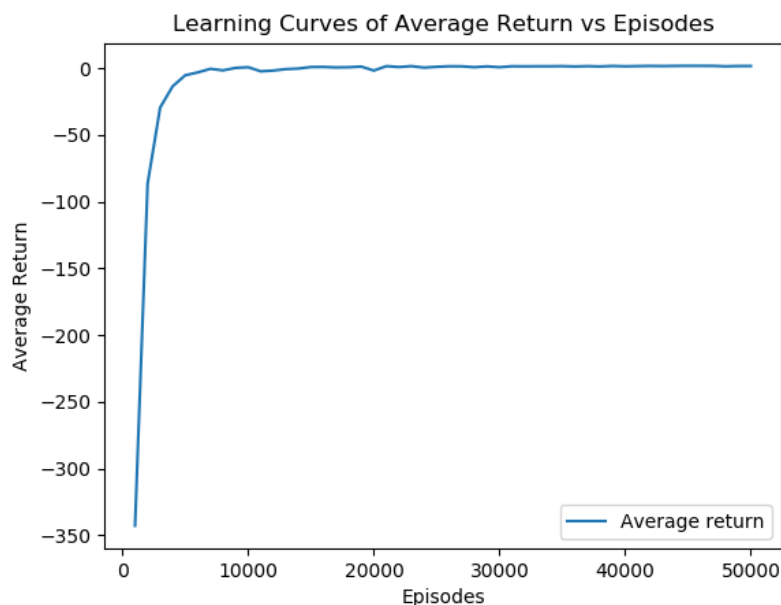


Figure 1: Initial Learning Curve

- (b) I have tuned the hyper-parameter number of hidden units by the following 3 values: 128, 32, 80. I have used the average return value at the last episode for performance metrics because this value reflects how well the trained model performs when it is being used to play against AI or human players. The learning curves of the 3 tests are shown below. **Note:** We have commented out the function call `part5b()` in the main function of the code. To reproduce the graphs and the stats below, please uncomment the line that says `part5b()`

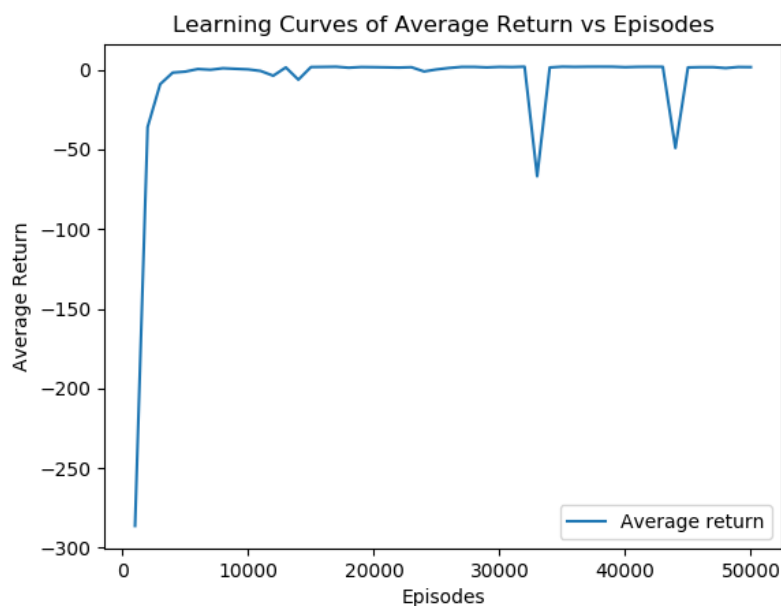


Figure 2: Learning Curve with 128 hidden units

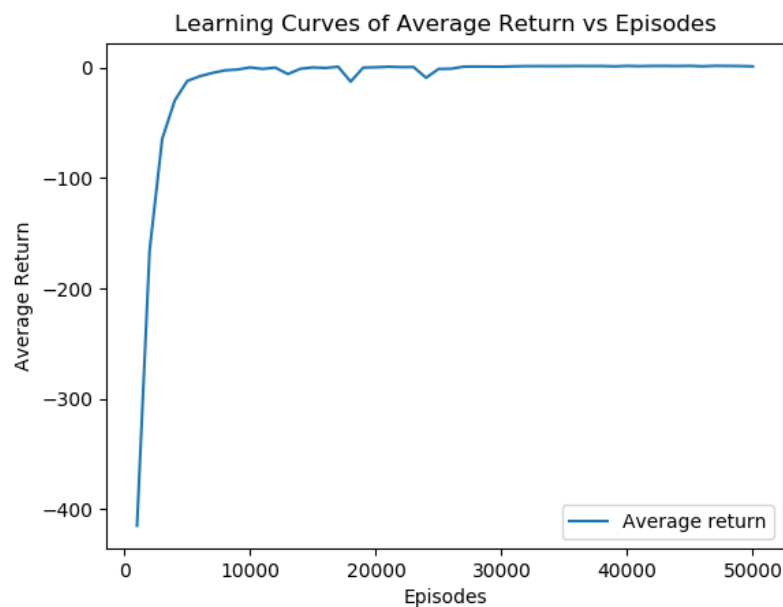


Figure 3: Learning Curve with 32 hidden units

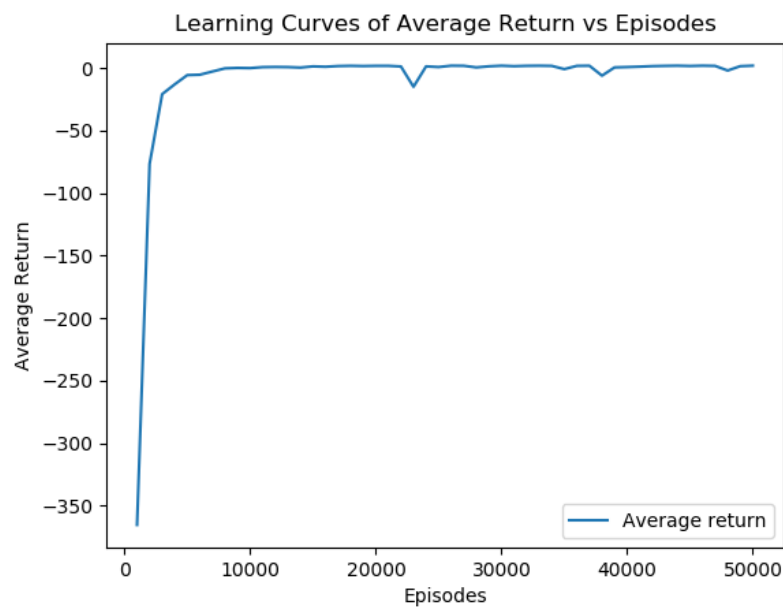


Figure 4: Learning Curve with 80 hidden units

The average return values for the 3 tests are as follows:

**128 Hidden Units:** 1.62

**32 Hidden Units:** 1.41

**80 Hidden Units:** 1.91

From testing, the algorithm with 80 hidden units has the best performance.

- (c) The policy learned to stop playing invalid moves between 13000 and 14000 episodes. This was determined by recording the number of invalid moves during training, and aggregating them into 1000-episode chunks. When the average number of invalid moves per episode falls below 30% (30 per 1000), that's when we know the policy has learned to stop playing invalid moves.
- (d)

Wins : 94

Ties : 2

Losses : 4

Included are 5 games that were played.

Game #1:

```
...
..x
.O.
====
...
x.x
oo.
====
...
xxx
oo.
====
Win!
```

Game #21:

```
...
..x
.O.
====
.O.
x.x
.O.
====
.O.
xxx
.O.
====
Win!
```

Game #41:

```
...
..x
.O.
====
...
x.x
.oo
====
...
xxx
```

```
.oo
====
Win!
```

Game #61:

```
...
..x
..o
====
o..
x.x
..o
====
o..
xxx
..o
====
Win!
```

Game #81:

```
..o
..x
...
====
.oo
x.x
...
====
.oo
xxx
...
====
Win!
```

The main strategy of the agent seems to be to prioritize building the longest chain of X's as possible. It will ignore any O's unless the O blocks its way. In that case, it will place an X in a place where a 3-X chain is possible. It will even ignore a 2-O chain if extending an X chain won't block it. This is the main way it loses the game. The agent probably learned this behaviour because it is relatively unlikely that the random agent will play the cell that blocks the AI from building a 3-X chain. Also, the random agent doesn't actively attack the AI's X-chains, so it has no reason to counter that.

The agent also prefers to put its starting move in the right column of the centre row, and then either plays the left column of the centre row if not blocked, otherwise it plays the bottom-right cell. In essence, it avoids taking the centre cell. This is strange, since conventional wisdom would recommend either controlling the centre or a corner, to allow for setting up a guaranteed win state. The agent probably chose this state because it chose this cell initially, and since a greedy strategy of building 3-X chains seemed to be sufficient to win, it had no reason to learn any other initial moves. Also, since its lookahead isn't the entire game tree, it cannot determine whether an endgame state is a guaranteed win state if the board is relatively full.

6. The graph that illustrates the win/lose/tie rates is shown below:



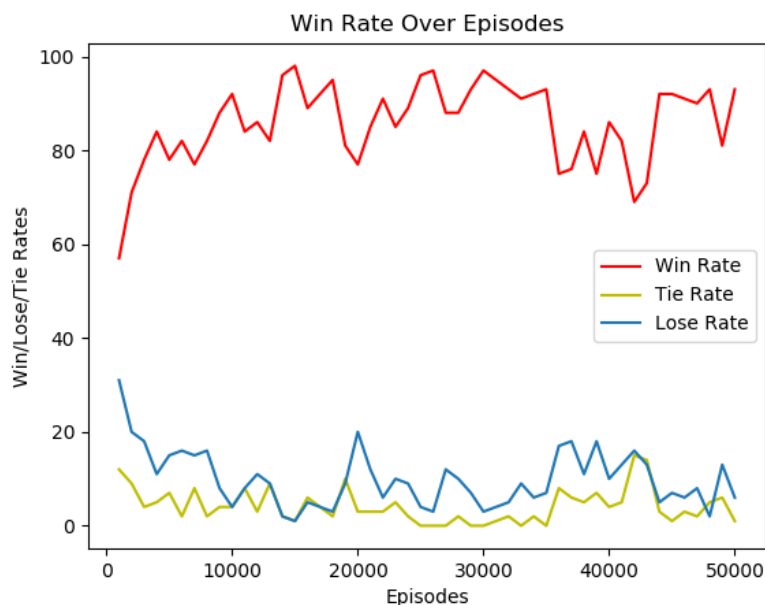


Figure 5: Win Rate Over the Episodes

From the figure above we can see the win rate generally goes up when the number of episodes increases and the lose/tie rate goes down. The result above shows the reward/punishment numbers that we come up with earlier in part 4 are reasonable and effective as the win rate is near 90% at the end.

7. For the final trained model, the first move distribution is the following:
  - Column 0:  $2.7633e-12$
  - Column 1:  $4.8411e-09$
  - Column 2:  $3.5970e-09$
  - Column 3:  $1.7473e-02$
  - Column 4:  $2.2157e-09$
  - Column 5:  $9.8252e-01$
  - Column 6:  $8.8324e-09$
  - Column 7:  $1.4350e-08$
  - Column 8:  $3.6817e-06$

From the data shown above, our final trained model would be most likely to place a move at column 5 as its first move. From a human standpoint, this is indeed quite odd for the opponent to make its first move there as it is quite easy and intuitive to tie the AI model or even outright win. However, since the model is trained against a player that makes random moves, it might be reasonable since it will just try to make the first three connected moves over the random opponent.

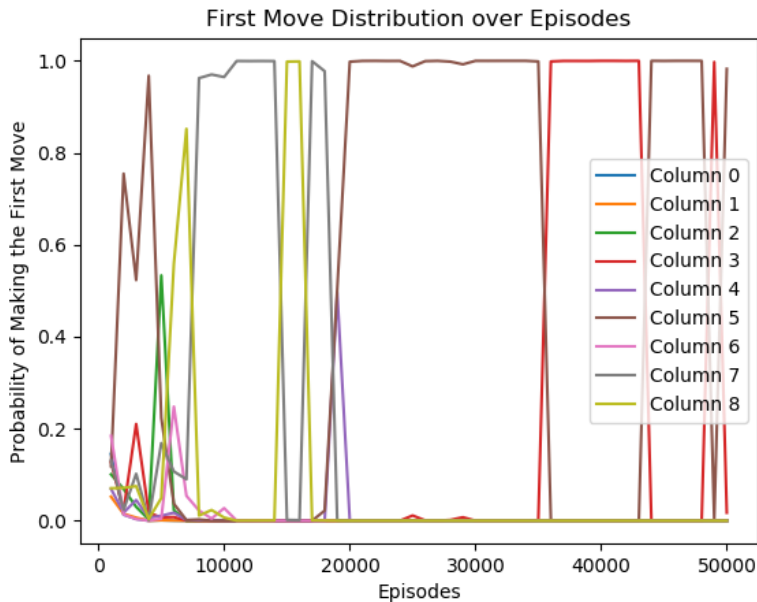


Figure 6: First Move Distribution over Episodes

As the above graph shows, the probabilities of making the first move at each column fluctuates a lot. We can conclude that it may be immaterial of what is the first move that the model makes in terms of winning the game.

8. The major mistake is to prioritize building 3-X chains over blocking the opponent's 3-O chains. If the random agent manages to build a state where a 3-O chain is possible in the next move, but that cell isn't needed for a 3-X chain, the AI will not block it, and may lose.

The agent also prefers to choose the rightmost column of the centre row as its opening move. However, this limits the agent to only being able to pursue two winning states from the initial move: taking the right-most column or taking the centre row. It could try pursuing other winning states, but it would give the opponent an advantage. A better strategy would to either take the centre (allowing for the pursuit of either diagonal, the centre row, or centre column), or one of the corners (allowing for the pursuit of one diagonal, one row, and one column). Furthermore, these strategies allow for forcing a state where the opponent cannot win.