# IMPLEMENTATION OF BOX STENCIL **KERNEL**

## Algorithm 1 Box stencil kernel in TCstencil

- 1: Input: mesh A, para\_box1, para\_box2, para\_box3
- Output: the updated mesh
- 3: Shared Memory: sinput, soutput1,soutput2,soutput3
- 4: Fragment: a\_frag,b\_frag,c\_frag
- 5: p=[para\_box1, para\_box2, para\_box3]
- 6: sout=[soutput1,soutput2,soutput3]
- load A' of A to sinput
- 8: **for** i from 0 to 2 **do**
- wmma::fill fragment(c frag, 0.0f)
- wmma::load\_matrix\_sync(a\_frag, p[i], 16)
- wmma::load\_matrix\_sync(b\_frag, sinput, 16) wmma::mma\_sync(c\_frag, a\_frag, b\_frag, c\_frag) 11:
- wmma::store\_matrix\_sync(sout[i], c\_frag, 16, wmma::mem\_row\_major)
- 14: calculate result by soutput1,soutput2,soutput3 and store it to global memory

#### 2 **ROOFLINE ANALYSIS**

We adopt the roofline model [2] to analyze the effectiveness of stencil computation by Artemis, TCstencil, and TC-w/o tc. Since Nsight profiler do not supprot collect FLOP in half, so we give the theoretical value. Table 1 shows the the maximum operational intensity  $I_{max} = \pi/\beta$  (FLOP/Byte) in FP16 precision of A100 and V100, where  $\pi$  (TFLOPS) is the maximum attainable performance the  $\beta$  (GB/s) is maximum memory bandwidth. We are only considering the multiplication-and-add for stencil as FLOP and the access to global memory. For updating the inner points in 16×16 mesh with 9pt stencil, the Arithmetic Intensity (AI, FLOP/Byte) of Artemis/TC-w/o tc/TCstencil is 0.50/2.53/5.33. As for 25pt stencil, the AI of Artemis/*TC-w/o tc/TCstencil* is 0.50/7.03/6.00 All the above implementations are memory bound since their AI are lower than *I<sub>max</sub>* in Table 1. In A100, the highest TFLOPS of Artemis/*TC-w/o* tc/TCstencil is 0.65/1.06/7.52 for 9pt stencil and 0.88/1.55/8.00 for 25pt stencil. The computation details are in the appendix. In V100, the highest GFLOPS of Artemis/TC-w/o tc/TCstencil is 0.60/0.89/5.89 for 9pt stencil and 0.94/1.73/7.84 for 25pt stencil.

Table 1: The performance information of A100 and V100 in FP16 precision [1].

Item	A100 FMA	A100 TC	V100 FMA	V100 TC
π	78	312	31.4	125
β	1555		900	
$I_{max}$	50.1	200.64	34.88	128.8

### 3 APPENDIX

#### The AI computation detail:

- Artemis 9pt: 9 FLOP/(9\*2) Byte. update every point, read 9 points in half and perfrom 9 FLOP.
- Artemis 25pt: 25 FLOP/(25\*2) Byte.
- TC-w/o tc 9pt: (12\*12\*9) FLOP / (16\*16\*2) Byte. update every 12\*12 points, load 16\*16 points in global memory, perfrom 12\*12\*9 FLOP.
- TC-w/o tc 25pt: (12\*12\*25) FLOP / (16\*16\*2) Byte.

- TCstencil 9pt: (16\*16\*16\*2) FLOP/ (3\*16\*16)\*2 Byte. update every 12\*12 point, load 16\*16 points and 2\*16\*16 elements in parameter matrices. perform twice Tensor Core MMA, each MMA perform 16\*16\*16 FLOP.
- TCstencil 25pt: (16\*16\*16\*3) FLOP/ (4\*16\*16)\*2 Byte.

### The FLOPS computation detail:

- Artemis 9pt: ((N-r)\*(N-r))\*9 FLOP/ (time) s. every point in mesh need 9 FLOP to be updated.
- Artemis 25pt: ((N-r)\*(N-r))\*25 FLOP/ (time) s.
- TC-w/o tc 9pt: ((N-r)\*(N-r))\*9 FLOP/ (time) s.
- TC-w/o tc 25pt: ((N-r)\*(N-r))\*25 FLOP/ (time) s.
- TCstencil 9pt: [(N-r)\*(N-r)/(12\*12)\*(16\*16\*16\*2) ] FLOP/ (time) s. The needed FLOP is same with that of AI.
- TCstencil 25pt: [(N-r)\*(N-r)/(12\*12)\*(16\*16\*16\*3)] FLOP/ (time) s.

#### REFERENCES

- [1] NVIDIA. 2021-1-30. NVIDIA Turing Architecture Whitepaper. online. https: //www.nvidia.com/en-us/data-center/a100/ Accessed March 30, 2021.
- [2] Samuel Williams, Andrew Waterman, and David Patterson. 2009. Roofline: an insightful visual performance model for multicore architectures. Commun. ACM 52, 4 (2009), 65-76,