

## INCOME VARIANCE DYNAMICS AND HETEROGENEITY

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Recent theoretical work has shown the importance of measuring microeconomic uncertainty for models of both general and partial equilibrium under imperfect insurance. In this paper the assumption of i.i.d. income innovations used in previous empirical studies is removed and the focus of the analysis is placed on models for the conditional variance of income shocks, which is related to the measure of risk emphasized by the theory. We first discriminate amongst various models of earnings determination that separate income shocks into idiosyncratic transitory and permanent components. We allow for education- and time-specific differences in the stochastic process for earnings and for measurement error. The conditional variance of the income shocks is modelled as a parsimonious ARCH process with both observable and unobserved heterogeneity. The empirical analysis is conducted on data drawn from the 1967–1992 Panel Study of Income Dynamics. We find strong evidence of sizeable ARCH effects as well as evidence of unobserved heterogeneity in the variances.

KEYWORDS: Microeconomic uncertainty, earnings, consumption, savings, income mobility, ARCH.

### 1. INTRODUCTION

WHILE A NUMBER OF PAPERS have focused on modelling the time series properties of the mean of earnings, the modelling of the variance has been neglected. Seminal papers in this area have been Lillard and Willis (1978), MaCurdy (1982), Abowd and Card (1989) who fit ARMA type processes, using panel data. However, the properties of the variance of income are also important for our understanding of behavior. For example, results reported in Deaton (1992) relating to consumption and savings rely on the assumption that income shocks are independently and identically distributed, while Caballero (1990) discusses the potential importance of relaxing the i.i.d. assumption. Some recent studies allow for heterogeneity when measuring the variance of income (Carroll and Samwick (1997), Hubbard, Skinner, and Zeldes (1994)), while Alvarez, Browning, and Ejrnaes (2002) emphasize heterogeneity in many aspects of the income process including the mean and the variance.<sup>2</sup>

The assumption of i.i.d. income innovations has probably been used for its convenience since it simplifies the analysis and search for the numerical solutions in simulations of say the consumption plan. Nevertheless, it can lead

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<sup>2</sup>Other authors rely on subjective expectation data (Guiso, Jappelli, and Pistaferrri (2002)). See also Zeldes (1992) for a discussion of these issues.

to wrong conclusions about individual behavior. In particular, the presence of ARCH effects or stochastic volatility has implications for the study of life-cycle consumption and savings, for the welfare effects of uncertainty, as well as for income mobility and poverty, among other issues. The importance of considering the evolution of the variance of earnings over the business cycle, as well as acknowledging differences across individuals (under imperfect insurance) has been emphasized recently by Browning, Hansen, and Heckman (2000).

In this paper we address some of these issues and model earnings as the sum of a martingale component and a (possibly persistent) transitory disturbance. Since the presence of permanent shocks is central for a number of economic questions, we investigate the validity of this representation by testing whether the variance of the permanent shock is zero and consider the implications of some alternative specifications. Since part of the transitory fluctuation is in reality measurement error, we tackle explicitly the issue of reporting errors in earnings data. We allow for the possibility that individuals with different education levels face different income processes, both at the mean and at the variance level, thus allowing for the changing returns to observable skills (see Juhn, Murphy, and Pierce (1993) for the U.S. and Gosling, Machin, and Meghir (2000) for the UK).

In a second step, we model the conditional variance of the earnings shocks as an ARCH process with observed and unobserved heterogeneity.<sup>3</sup> Our task is complicated by the fact that in the context of a model with permanent and transitory income shocks, these are not separately observable. We show how moment conditions can be derived to estimate the dynamic properties of the conditional variance of income and to test for permanent unobserved heterogeneity in the variance of both the transitory and the permanent innovation.<sup>4</sup> Our data draw from the Panel Study of Income Dynamics (PSID) for the years 1967–92.

We find that permanent and transitory shocks are important components of income shocks. We also find strong evidence of state dependence in the variance of both permanent and transitory components. Finally we find that earnings variances are heterogeneous across individuals. Thus the i.i.d. nature of income innovations is rejected by our data, which points to both heteroskedasticity and stochastic earnings risk as important facts.

<sup>3</sup>See among others Engle (1982).

<sup>4</sup>Banks, Blundell, and Brugiavini (2001) is the only attempt we know of to estimate the conditional variance of income shocks according to an ARCH process. However, the authors do not allow for the distinction between transitory and permanent disturbances and do not present ARCH estimates. Moreover, their analysis is based on cohort data and misses truly idiosyncratic uncertainty. Meghir and Windemeijer (1999) recover orthogonality conditions for the estimation of an ARCH process but do not allow for a distinction between transitory shocks and permanent shocks. Chamberlain and Hirano (1999) estimate earnings dynamics allowing for volatility heterogeneity.

The paper has five more sections. In Section 2 we introduce the data used in the empirical application. In Sections 3 and 4 we discuss and motivate our approach for modelling the conditional mean and the conditional variance of earnings, respectively, and present and discuss our empirical findings. Section 5 analyzes some implications of the empirical results. Section 6 concludes.

## 2. THE DATA

The data used in this study are drawn from the 1968–1993 family and individual-merged files of the PSID (waves I through XXVI).<sup>5</sup>

The PSID started in 1968 collecting information on a sample of roughly 5,000 households. Of these, about 3,000 were representative of the U.S. population as a whole (the core sample), and about 2,000 were low-income families (the Census Bureau's SEO sample). Thereafter, both the original families and their split-offs (children of the original family forming a family of their own) have been followed. In the empirical analysis we use both the core sample and the SEO sample. Some authors (Lillard and Willis (1978)) suggest dropping the SEO low-income sample because of endogenous selection. In other words, an initial condition problem arises. However, given linearity, the initial condition problem is taken care of by the presence of the permanent component. **To put it differently, we deal with the problem by estimating models for the growth rate rather than specifications in levels.** This is also true for the model of the variance where we include fixed effects.

Questions referring to labor income are retrospective; thus, those asked in 1968, say, refer to the 1967 calendar year. The earnings variable is the labor portion of money income from all sources; the variable name in the PSID tapes is "head's money income from labor" and includes the labor part of farm income and business income, wages, bonuses, overtime, commissions, professional practice, labor part of income from roomers and boarders or business income.<sup>6</sup> We deflate the nominal measure of earnings by the GNP personal consumption expenditure deflator (using 1992 as the base year). We use information on the highest grade completed to allocate individuals in our sample to three education groups: High School dropouts (those with less than 12 grades of schooling), High School graduates (those with at least a High School diploma, but no College degree), and College graduates (those with a College degree or more).

Step-by-step details on sample selection are reported in the Appendix. Briefly, we select male heads aged 25 to 55 with at least nine years of usable earnings data. The selection process leads to a sample of 2,069 individuals and

<sup>5</sup>See Hill (1992) for more details about the PSID.

<sup>6</sup>As noted by Gottschalk and Moffitt (1993), the measure of labor income available in the PSID has sources that may reflect capital income, such as the labor part of farm income and roomers and boarders. We do not account for this problem.

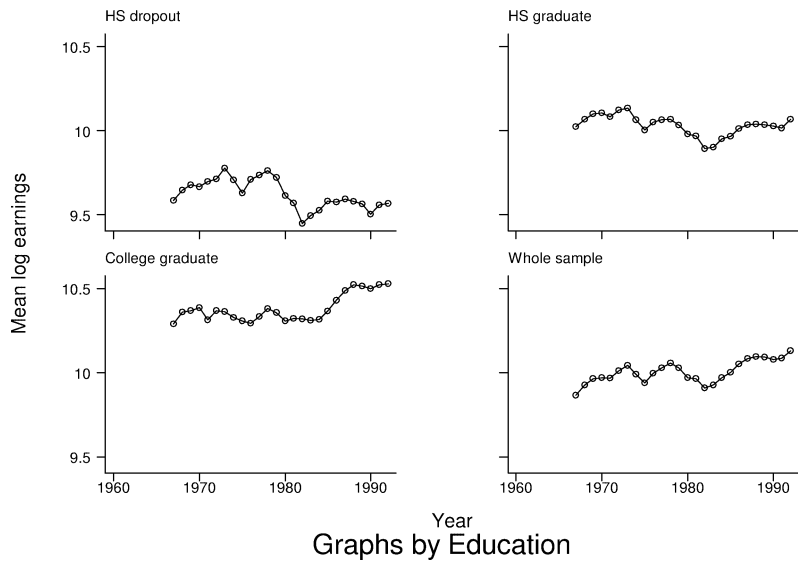


FIGURE 1.—The mean of log real earnings.

31,631 individual-year observations. Relevant sample statistics are presented in Tables A1–A3 (sample composition by year and by education, and demographic characteristics) in the Appendix. Figures 1 and 2 plot the mean and

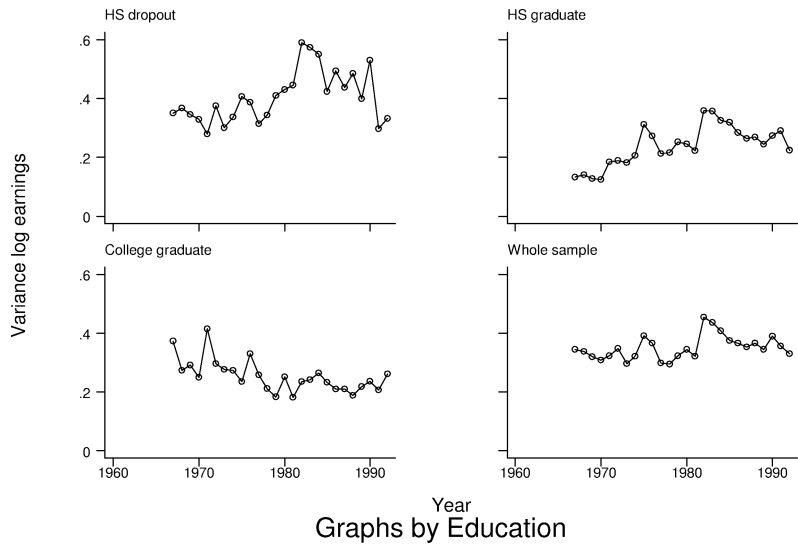


FIGURE 2.—The variance of log real earnings.

the variance of log real earnings against time for each education group and for the whole sample. These figures reproduce well known facts about the distribution of male earnings in the U.S. (see Levy and Murnane (1992)).

### 3. THE CONDITIONAL MEAN OF EARNINGS

As in previous empirical work, we posit the following model for the conditional mean of log earnings:

$$(1) \quad y_{it} = m_t^e + \beta^{e'} Z_{it} + u_{it},$$

where  $y_{it}$  is the logarithm of real annual measured earnings, the superscript “ $e$ ” stands for education,  $m_t^e$  is a calendar year effect,  $Z_{it}$  a vector of observable characteristics, and  $u_{it}$  the stochastic component of earnings. **Aggregate shocks specific to an education group are captured by  $m_t^e$  (aggregate risk).** The return to education varies with calendar time while the returns to observable attributes vary with education in a very general way.<sup>7</sup>

We assume that the unexplained component of income can be decomposed into a measurement error, a transitory innovation with low persistence and a martingale permanent component. Therefore,

$$(2) \quad u_{it} = r_{it} + e_{it} + p_{it}$$

with  $r_{it}$  being a classical i.i.d. measurement error,  $e_{it}$  the transitory shock, and  $p_{it}$  the permanent component of income, which follows the process

$$(3) \quad p_{it} = p_{it-1} + \zeta_{it}.$$

We assume that the transitory shock follows an MA( $q$ ) process (i.e.  $e_{it} = \Theta^e(L, q)\varepsilon_{it} = \varepsilon_{it} - \sum_{j=1}^q \theta_j^e \varepsilon_{it-j}$ ), with the order  $q$  of the process to be determined empirically, and assume that the permanent and the transitory shocks are uncorrelated at all leads and lags.<sup>8</sup>

<sup>7</sup>We test the hypothesis that the coefficients on the conditioning variables other than education, (i.e. age, race, region of residence, and residence in a SMSA) vary only with education and not with time (as in Card and Lemieux (2001)). The  $p$ -values of the tests are 99% in the High School dropout sample, 3% in the High School graduate sample, and 24% in the College graduate sample. We also considered whether for the marginal case of the High School graduate sample the dynamics of the variance that we consider later is affected by relaxing this restriction; one of the coefficients we report later changes from 0.6672 to 0.6715 and the other from 0.8912 to 0.8536. See Table V. Since these differences are negligible, we keep the restriction, which can improve the precision.

<sup>8</sup>Some examples of permanent innovations are associated to job mobility, long-term unemployment, health shocks, promotions, and even demotions. Transitory shocks to individual earnings include overtime labor supply, piece-rate compensation, bonuses and premia, etc.; in general, such shocks are mean reverting and their effect does not last long.

We define the unexplained component of the rate of growth of earnings as

$$(4) \quad g_{it} = \Delta u_{it} = \Delta r_{it} + \Theta^e(L, q) \Delta \varepsilon_{it} + \zeta_{it}.$$

This is a composite MA( $q + 1$ ) process. Equation (4) implies that  $g_{it}$  will be orthogonal to variables dated  $t - q - 2$  or earlier.

We recover the order of the MA process for the transitory shock from the estimated autocovariances of  $g_{it}$ . For instance, if transitory shocks are not serially correlated (i.e., if  $q = 0$ ) one should find  $E(g_{it}g_{it-j}) = 0$  for  $j > 1$ .<sup>9</sup>

Since we use estimated residuals we need to assume that the underlying processes, including the measurement error, have distributions such that the cross-sectional moments of  $g_{it}$  exist up to the fourth order. However, since we are dealing with finite lived individuals we do not necessarily require that these moments exist as the time dimension goes to infinity.

Unless noted otherwise, in what follows we compute all the standard errors using the block **bootstrap procedure** (see Hall and Horowitz (1996), Horowitz (2002)). In this way we account for serial correlation of arbitrary form, heteroskedasticity, as well as for the fact that we use pre-estimated residuals.<sup>10</sup>

### 3.1. *The Conditional Mean and the Structure of the Error Term*

We first estimate the conditional mean process. For each education group separately, we regress log real earnings on year dummies, a quadratic in age, dummies for race (white), region of residence, and residence in a SMSA. This first stage allows the effects of all characteristics to be education specific. **More-over the returns to education also vary over time.** For the remaining analysis of the stochastic properties of income we use the residuals from these regressions, i.e.  $(\hat{g}_{it} = \Delta y_{it} - \Delta \hat{m}_t^e - \Delta \hat{\beta}' Z_{it})$  in the place of  $g_{it}$ , and replace theoretical moments with sample analogs.

The next step is to evaluate whether the data conform to our hypotheses concerning the stochastic structure of the error term. We estimate the autocovariances of  $g_{it}$  using standard methods (Abowd and Card (1989)).

The estimated unconditional autocovariances up to order four are presented in Table I for the pooled sample and separately for the three education groups on which we focus. For simplicity, we report values pooled over time.<sup>11</sup> In

<sup>9</sup>The restriction can be tested computing the  $\chi^2$  zero restrictions test described by Abowd and Card (1989).

<sup>10</sup>Later on we will be using GMM to estimate processes for the mean and the variance of income. Windmeijer (2000) provides a small sample correction for the standard errors of two step GMM procedures, whose asymptotic approximation is known to be heavily biased. However, in our case the bootstrap procedure of Hall and Horowitz (1996) not only corrects for this but also accounts for pre-estimated residuals, and hence we have preferred it.

<sup>11</sup>The estimated matrices of autocovariances and the associated standard errors are available on request for the whole sample and separately for each education group. Each matrix contains 325 unique elements.

TABLE I  
THE AUTOCOVARIANCES OF THE UNEXPLAINED GROWTH OF EARNINGS<sup>a</sup>

| Order | Pooled<br>Sample    | High<br>School<br>Dropout | High<br>School<br>Graduate | College<br>Graduate |
|-------|---------------------|---------------------------|----------------------------|---------------------|
| 0     | 0.109<br>(0.0051)   | 0.164<br>(0.014)          | 0.103<br>(0.0068)          | 0.065<br>(0.0058)   |
| 1     | -0.0303<br>(0.0021) | -0.0535<br>(0.0055)       | -0.028<br>(0.0027)         | -0.0105<br>(0.0018) |
| 2     | -0.0079<br>(0.0014) | -0.0134<br>(0.0046)       | -0.0077<br>(0.0015)        | -0.0025<br>(0.0013) |
| 3     | -0.0024<br>(0.0011) | -0.0018<br>(0.0034)       | -0.0026<br>(0.0014)        | -0.0024<br>(0.0011) |
| 4     | 0.0007<br>(0.0011)  | 0.0074<br>(0.0035)        | -0.0015<br>(0.0013)        | -0.0017<br>(0.0012) |

<sup>a</sup>Asymptotic standard errors are reported under the coefficient estimate. Values are pooled over all years and individuals.

Table II we report the test of zero restrictions for the null hypothesis that  $E(g_{it}g_{it-j}) = 0$  (with  $1 \leq j \leq 4$ ) allowing the estimated autocovariances to differ over time.

In the pooled sample, unexplained earnings growth rates appear correlated up to the second order. Autocovariances at the third order and beyond are small and statistically insignificant or of borderline significance. This is con-

TABLE II  
TESTS OF THE HYPOTHESIS OF ZERO AUTOCOVARIANCES IN EARNINGS GROWTH<sup>a</sup>

|                      | Order of Autocovariance |                         |                         |                         |
|----------------------|-------------------------|-------------------------|-------------------------|-------------------------|
|                      | 1                       | 2                       | 3                       | 4                       |
| Pooled Sample        | 320<br>df 24; $p=0$     | 61.2<br>df 23; $p=0$    | 27.7<br>df 22; $p=0.19$ | 20.2<br>df 21; $p=0.52$ |
| High School Dropout  | 159<br>df 24; $p=0$     | 38.0<br>df 23; $p=0.03$ | 31.7<br>df 22; $p=0.09$ | 23.9<br>df 21; $p=0.30$ |
| High School Graduate | 193<br>df 24; $p=0$     | 57.3<br>df 23; $p=0.00$ | 23.8<br>df 22; $p=0.36$ | 28.1<br>df 21; $p=0.14$ |
| College              | 73.7<br>df 24; $p=0$    | 28.3<br>df 23; $p=0.22$ | 22.7<br>df 22; $p=0.43$ | 27.3<br>df 21; $p=0.17$ |

<sup>a</sup>In this table we present tests for zero autocovariance of order 1–4. We provide the test statistic for the hypothesis that the respective autocovariance is zero in all time periods, the degrees of freedom of the test (df), which is determined by the number of time periods for which we can estimate the autocovariance, and the asymptotic  $p$ -value for the hypothesis that the autocovariances are zero. We have also tested the hypothesis that all autocovariances of order 3 or higher are jointly zero as in Abowd and Card (1989). The test statistic is 279.83 with 253 degrees of freedom and a  $p$ -value of 12%.

firmed also by the analysis conducted on different education groups (see Table I). In the pooled sample the test that  $E(g_{it}g_{it-3}) = 0$  has a  $p$ -value of 19 percent (see Table II). The null is similarly not rejected when we stratify the sample by schooling. The statistical implication is that  $q = 1$ .<sup>12</sup> We impose this restriction thereafter. The economic implication is that transitory shocks are somewhat persistent: it takes at least one period for the full impact of the transitory shock to be felt.

### 3.2. Testing for the Absence of Permanent Shocks

Whether permanent shocks are present, and the magnitude of their variance, are issues of great importance for a number of economic questions, such as consumption. This is established in a number of papers in the literature. Thus we next estimate the variance of the permanent shock and test the null hypothesis that it is zero.<sup>13</sup> To do this we use the sample autocovariances and impose the restriction that they are generated by (4). We use Equally Weighted Minimum Distance (EWMD) for reasons explained in Altonji and Segal (1996).

The key moment condition that identifies the variance of the permanent shock is

$$(5) \quad E \left[ g_{it} \left( \sum_{j=-(1+q)}^{(1+q)} g_{it+j} \right) \right] = E(\zeta_{it}^2),$$

where  $E(\zeta_{it}^2)$  is the unconditional variance of the permanent shock. This moment condition does not require constant autocovariances over time and exploits the structure of the MA process to cancel terms out, leaving us with the variance of the permanent shock in period  $t$ . In the Appendix we present EWMD estimates that allow for nonstationarity (see Table A4). We also present an estimate of  $E(\zeta_{it}^2)$  in Table III (along with its standard error) under the assumption that this is constant over time, which gives us a one degree of freedom test for the null of no permanent shock.

The test statistic, which is equal to the pooled estimate of the permanent shock divided by its standard error, is asymptotically (for large  $N$ ) distributed standard normal. The standard error is computed using the block bootstrap, allowing for pre-estimated residuals as well as for serial correlation and heteroskedasticity.

<sup>12</sup>For the College graduate  $q = 0$  cannot be rejected; we estimate the ARCH parameters below for both  $q = 0$  and  $q = 1$ .

<sup>13</sup>The null hypothesis encompasses two different assumptions concerning the structure of the error term: either that a permanent component is absent altogether, or that it is time invariant (e.g. a random growth model). The alternative hypothesis is that the permanent component follows a martingale process. We ignore the problem associated with the fact that  $q$  is pre-estimated rather than known.



TABLE III  
THE UNCONDITIONAL VARIANCE OF INCOME SHOCKS<sup>a</sup>

|  | Pooled<br>Sample    | High School<br>Dropout | High School<br>Graduate | College<br>Graduate |
|--|---------------------|------------------------|-------------------------|---------------------|
| <i>Conditioning on the Feasible Range of <math>\theta</math></i> |                     |                        |                         |                     |
| Transitory shock<br>(upper bound)                                | 0.0439<br>(0.0070)  | 0.0767<br>(0.0221)     | 0.0407<br>(0.0079)      | 0.0160<br>(0.0070)  |
| Transitory shock<br>(lower bound)                                | 0.0079<br>(0.0012)  | 0.0130<br>(0.0038)     | 0.0077<br>(0.0015)      | 0.0027<br>(0.0012)  |
| Measurement error<br>(upper bound)                               | 0.0303<br>(0.0021)  | 0.0530<br>(0.0055)     | 0.0278<br>(0.0030)      | 0.0114<br>(0.0018)  |
| $\theta$ (upper bound)   | -0.18               | -0.17                  | -0.19                   | -0.17               |
| <i>Using an External Estimate of <math>\sigma_r^2</math></i>     |                     |                        |                         |                     |
| Measurement error  | 0.0138              | 0.0206                 | 0.0129                  | 0.0081              |
| Transitory shock   | 0.0300<br>(0.0031)  | 0.0548<br>(0.0100)     | 0.0267<br>(0.0039)      | 0.0049<br>(0.0030)  |
| $\theta$   | -0.2566<br>(0.0339) | -0.2535<br>(0.0610)    | -0.2674<br>(0.0400)     | -0.5101<br>(0.2901) |
| Permanent shock <sup>b</sup>                                     | 0.0313<br>(0.0026)  | 0.0331<br>(0.0067)     | 0.0277<br>(0.0039)      | 0.0437<br>(0.0068)  |

<sup>a</sup>Equally weighted minimum distance estimates. Asymptotic standard errors are reported in parentheses.

<sup>b</sup>Bootstrap standard errors in parentheses.

There are a number of advantages of the test we use. First, it does not hinge on the assumption of covariance stationarity. Stationarity is in fact often rejected with PSID data on earnings. Second, it can be generalized to any form of serial correlation (of the MA type) in the transitory component. Finally, it is robust to the presence of measurement error (either classical or with MA-type serial correlation).

### 3.2.1. Results

The pooled variances of the permanent shock are estimated to be 0.0313 (with a bootstrap standard error of 0.0026) in the whole sample, 0.0331 (0.0067) for the High School dropouts, 0.0277 (0.0039) for the High School graduates, and 0.0437 (0.0068) for the College graduates (the results are reported at the bottom of Table III). The hypothesis of no permanent shock is strongly rejected for all education groups with  $p$ -values well below 1 percent in all cases. Henceforth we assume that log earnings for each education group follows the mean process described in equations (1), (2), and (3) with the transitory shock following an MA(1) process.

Assuming this variance represents uninsurable risk, the high variance for the College graduates is consistent with the idea that the higher returns emanat-

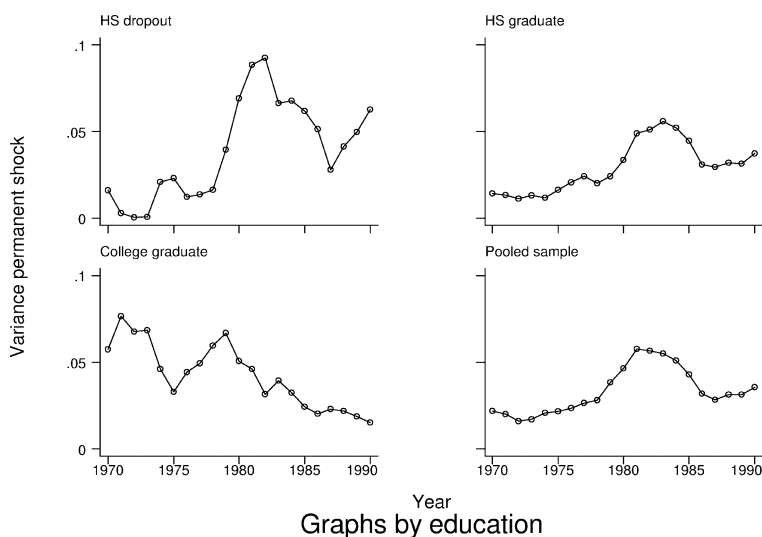


FIGURE 3.—The variance of the permanent shock to earnings.

ing from increased education come at the cost of higher earnings risk. Our estimates are close to those found elsewhere in the empirical literature (see Carroll and Samwick (1997)), although our focus is on earnings rather than family income. Given that family income may include some form of implicit or explicit insurance, our estimates are likely to be larger.

Figure 3 plots the estimates of the unconditional variance of the permanent shock against time, for the whole sample and by education (see Table A4 in the Appendix for the standard errors of these estimates). Overall the variance increases throughout the 1970's and in the early 1980's, it declines after 1984 with a slight tendency to increase at the end of the survey period. This evidence is very similar to that reported by Moffitt and Gottschalk (1994), who note that “the permanent variance grows, on average, through about 1982 or 1983, [while] it levels off or falls subsequently.”<sup>14</sup> A similar pattern holds for the least educated and for the High School graduates. Finally, for the College graduates there is not much evidence of a monotonic increase in permanent income variance in the 1970's; on the other hand, the decline in variance that occurs in the 1980's is much more pronounced than for the other two groups.<sup>15</sup>

<sup>14</sup>See Moffitt and Gottschalk (1994, p. 12).

<sup>15</sup>The counter-cyclical of income uncertainty has been advocated by those who propose a resolution of the equity premium puzzle based on the negative correlation between aggregate shocks and individual risk (Mankiw (1986)). We find mixed support for this. If we plot our estimates of the unconditional variance of the permanent shock against the U.S. male unemployment rate, we find that they are quite synchronized, especially in the 1970's and in the early 1980's. However, in the late 1980's the unconditional variance of the permanent shock displays a more erratic behavior than the unemployment rate.

### 3.3. *The Variance of the Transitory Shock, the Variance of Measurement Error, and the MA Coefficients*

Although we can identify the variance of the permanent shock, it is not possible to disentangle the unconditional variance of the transitory shock, the variance of the measurement error, and the MA coefficients. Earlier studies have ignored this point. However, this may be important to the extent that the transitory shock reflects uncertainty and induces economic responses, while measurement error is noise due to imperfect data.

We follow two approaches to deal with this issue. The first strategy is to obtain bounds for the unidentified measures. The second is to use an external estimate of the measurement error in earnings.<sup>16</sup> Both approaches rely on the assumption that measurement error is classical—an assumption that is not universally accepted.<sup>17</sup>

For illustrative purposes take the case with an MA(1) transitory shock and assume invertibility of the MA process. Thus  $e_{it} = \varepsilon_{it} - \theta \varepsilon_{it-1}$  with  $|\theta| < 1$ . The autocovariances of earnings growth of order one and two can be used to derive the following two equations in three unknowns:

$$(6) \quad \begin{aligned} (i) \quad \sigma_\varepsilon^2 &= \frac{E(g_{it}g_{it-2})}{\theta}, \\ (ii) \quad \sigma_r^2 &= -E(g_{it}g_{it-1}) - \frac{(1+\theta)^2}{\theta}E(g_{it}g_{it-2}). \end{aligned}$$

The sign of  $E(g_{it}g_{it-2})$  defines the sign of  $\theta$ . In our case we can conclude that  $\theta < 0$  (see Table I). Taking the two variances as functions of the MA coefficient we note two points. First,  $\sigma_r^2(\theta)$  declines and  $\sigma_\varepsilon^2(\theta)$  increases when  $\theta$  declines in absolute value. Second, for sufficiently low values of  $|\theta|$  the estimated variance of the measurement error  $\sigma_r^2(\theta)$  may become negative. Given the sign of  $\theta$  (defined by (i) in equation (6)) this fact defines a bound for the MA coefficient. In our case, where  $\theta < 0$ , we have that  $\theta \in [-1, \tilde{\theta}]$  where  $\tilde{\theta}$  is the negative value of  $\theta$  that sets  $\sigma_r^2$  in (6) to zero. If  $\theta$  was found to be positive, the bounds would be in a positive range. The bounds on  $\theta$  in turn define bounds on  $\sigma_\varepsilon^2$  and  $\sigma_r^2$ .

An alternative empirical strategy is to rely on an external estimate of the variance of the measurement error,  $\overline{\sigma_r^2}$ . Define the moments, adjusted for measurement error, as

$$E[g_{it}^2 - 2\overline{\sigma_r^2}] = \sigma_\varepsilon^2 + 2(1 + \theta + \theta^2)\sigma_\varepsilon^2,$$

<sup>16</sup>A natural extension of our framework is a multiple indicator model that can be used to identify the sources of permanent and transitory earnings variation (e.g., wage changes, unemployment, etc.), and to distinguish between transitory shocks and measurement error. This strategy is pursued in [Altonji, Martins, and Siow \(2001\)](#).

<sup>17</sup>As we discuss below, other aspects of our approach, such as the identification of ARCH effects, do not depend on whether the measurement error is classical.

$$E(g_{it}g_{it-1} + \overline{\sigma_r^2}) = -(1 + \theta)^2 \sigma_\varepsilon^2,$$

$$E(g_{it}g_{it-2}) = \theta \sigma_\varepsilon^2,$$

where  $\overline{\sigma_r^2}$  is available externally. The three moments above depend only on  $\theta$ ,  $\sigma_\varepsilon^2$ , and  $\sigma_\zeta^2$ . We can then estimate these parameters using EWMD.

### 3.3.1. Results

Table III reports the results of the two approaches we follow to bound or point estimate the MA coefficient and the variances.

In the pooled sample we find that the lowest  $\theta$  (in absolute value) that satisfies  $\sigma_r^2 \geq 0$  is  $-0.18$ . The variance of the transitory shock is in the range  $\sigma_\varepsilon^2 \in [0.0079, 0.0439]$ , while  $\sigma_r^2 \in [0, 0.0303]$ . For the High School dropouts we find  $\sigma_\varepsilon^2 \in [0.0130, 0.0767]$ . The corresponding MA parameter is  $\theta \in [-1, -0.17]$ . For the High School graduates, we find  $\sigma_\varepsilon^2 \in [0.0077, 0.0407]$  corresponding to  $\theta \in [-1, -0.19]$ . Finally, for the College graduates,  $\sigma_\varepsilon^2 \in [0.0027, 0.0160]$  with  $\theta \in [-1, -0.17]$ . The upper bound of the variance of measurement error is 0.0530 for the High School dropouts, 0.0278 for the High School graduate, and 0.0114 for the College graduate.

Bound and Krueger (1994) conduct a validation study of the CPS data on earnings and conclude that measurement error explains 28 percent of the overall variance of the rate of growth of earnings in the CPS. Bound, Brown, Duncan, and Rodgers (1994) find a value of 22 percent using the PSID-Validation Study.<sup>18</sup> We assume an intermediate value of 25 percent. Since in our data the earnings growth variances are 0.1651, 0.1033, and 0.0650, respectively for the High School dropouts, the High School graduates, and the College graduates, we calculate (separately for the three education groups):  $\overline{\sigma_r^2} = 0.0206$ , 0.0129, and 0.0081.<sup>19</sup> We use EWMD to estimate  $\theta$ ,  $\sigma_\varepsilon^2$ , and  $\sigma_\zeta^2$  (conditioning on  $\overline{\sigma_r^2}$ ) and find that  $\theta$  ranges between  $-0.25$  (High School dropout) and  $-0.51$  (College graduate). The variance of the transitory shock is 0.0548 for the High School dropout, 0.0267 for the High School graduate, and 0.0049 for the College graduate.

The above can be viewed as unconditional averages of the underlying (changing) variances and  $\theta$ . It is however possible to allow for nonstationarity and still be able to identify the parameters of interest. These are reported, for the pooled sample only, in Table A5 in the Appendix.

<sup>18</sup>See Bound, Brown, and Mathiowetz (2001) for a recent survey of the growing literature on measurement error in micro data.

<sup>19</sup>In the absence of better information, we assume that the fraction of earnings growth variance due to measurement error is the same across education groups (25 percent). Bound and Krueger (1994) provide evidence that measurement error is not correlated with education.

## 4. THE CONDITIONAL VARIANCE OF EARNINGS

We now specify the conditional variance of the transitory and the permanent shock, thus allowing for non-i.i.d. income innovations. In both cases we specify an ARCH(1) structure of the form

$$(7) \quad \begin{aligned} E_{t-1}(\varepsilon_{it}^2) &= \kappa_i^e + \gamma^e \varepsilon_{it-1}^2 + \lambda_i && \text{Transitory,} \\ E_{t-1}(\zeta_{it}^2) &= \phi_i^e + \varphi^e \zeta_{it-1}^2 + \eta_i && \text{Permanent,} \end{aligned}$$

where  $E_{t-1}(\cdot)$  denotes an expectation conditional on information available at time  $t - 1$ . The parameters are all education specific. We test whether they vary across education. The terms  $\kappa_i^e$  and  $\phi_i^e$  are year effects that capture the way that the variance of the transitory and permanent shocks change over time, respectively. In the empirical analysis we also allow for life-cycle effects. In this specification we can interpret the lagged shocks ( $\varepsilon_{it-1}$ ,  $\zeta_{it-1}$ ) as reflecting the way current information is used to form revisions in expected risk. Hence it is a natural specification when thinking of consumption models that emphasize the role of the *conditional* variance in determining savings and consumption decisions.

The terms  $\lambda_i$  and  $\eta_i$  are fixed effects that capture all those elements that are invariant over time and reflect long term occupational choices, etc. The latter reflects permanent variability of income due to factors unobserved by the econometrician. Such variability may in part have to do with the particular occupation or job that the individual has chosen. The nature and extent of this variability may be known by the individuals when they make their occupational choices and hence it may also reflect preferences. Whether this variability is partly predictable or whether it reflects genuine permanent risk or not is of course another issue that cannot be answered here and requires the use of consumption data.<sup>20</sup>

4.1. *The Conditional Variance of the Transitory Shock*

In the general MA( $q$ ) case the conditional autocovariance of the unexplained component of earnings growth of order  $q + 1$  identifies the conditional variance of the transitory shock up to the constant MA( $q$ ) parameter  $\theta_q^e$ :

$$(8) \quad E_{t-1}(g_{it+q+1}g_{it}) = \theta_q^e E_{t-1}(\varepsilon_{it}^2).$$

<sup>20</sup>An interesting possibility allowed in ARCH models for time-series data is that of asymmetry of response to shocks. In other words, the conditional variance function is allowed to respond asymmetrically to positive and negative past shocks. This could be interesting here as well, for a considerable amount of asymmetry in the distribution of earnings is related to unemployment. Caballero (1990) shows that asymmetric distributions enhance the need for precautionary savings. In our case, however, models embedding the notion of asymmetry are not identifiable. The reason is that we do not observe separately the transitory and permanent shock. Finally, our results are consistent with the presence, in addition to ARCH effects, of a stochastic volatility term. This would only be detectable if it is sufficiently serially correlated.

Taking the first lag of the transitory variance function in (7), pre-multiplying by the MA coefficient  $\theta_q^e$ , using (8), and then applying the law of iterated expectations, yields

$$(9) \quad E_{t-2}(g_{it+q+1}g_{it} - \theta_q^e \kappa_t^e - \gamma^e g_{it+q}g_{it-1} - \theta_q^e \lambda_i) = 0.$$

Two important points can be made about this result. First, identification of the ARCH coefficient requires only the knowledge of the *order* of the MA process, *not* the value of the parameters  $\theta_q^e$ . Second, the ARCH coefficients are identified in the presence of classical or even serially correlated measurement error (so long as that has no ARCH component).

One way to eliminate unobserved heterogeneity is to use first differences. However, this gives rise to weak instruments since it is hard to predict changes in the autocovariances using lagged ones; weak instruments can lead to substantial small sample biases (see Bound, Jaeger, and Baker (1995)). We use within groups combined with instrumental variables, which for a moderate to large time series dimension is likely to behave much better. Neglecting time effects for simplicity, the ex-post equivalent of (9) is

$$g_{it+q+1}g_{it} = \gamma^e g_{it+q}g_{it-1} + \theta_q^e \lambda_i + \omega_{it}$$

with  $E_{t-2}(\omega_{it}) = 0$ . Even if  $\text{var}(\lambda_i) = 0$ , an instrumental variable procedure is still required for identification. We then remove individual specific means by

$$(10) \quad (g_{it+q+1}g_{it} - \overline{g_{it+q+1}g_{it}}) = \gamma^e (g_{it+q}g_{it-1} - \overline{g_{it+q}g_{it-1}}) + (\omega_{it} - \overline{\omega_i}),$$

where  $\overline{x_{i(+j)}} = (T-j)^{-1} \sum_{s=1+j}^T x_{is}$  and  $\overline{x_{i(-j)}} = (T-j)^{-1} \sum_{s=1}^{T-j} x_{is}$ . This procedure eliminates the fixed effect but not the endogeneity of  $g_{it+q}g_{it-1}$ , so we still need to use an IV procedure, and more precisely we need instruments lagged  $t-2$ , for instance  $g_{it-2}g_{it-4}$ . It is well known (Nickell (1981)) that the within-group estimator for a dynamic panel data model is biased for short  $T$ . However, the bias decreases when  $T$  gets large and disappears asymptotically when  $T \rightarrow \infty$ . We use individuals with between 9 to 26 time series observations. This leads to a large enough number of usable observations for most individuals to make the within group bias probably very small. In addition, as a sensitivity test both for attrition bias and for this within groups issue, we also report estimates based on individuals observed in the PSID for 16 years or more.

#### 4.2. The Conditional Variance of the Permanent Shock

To identify the parameters of the variance function of the permanent shock in equation (7) we make use of the fact that for an MA( $q$ )-transitory shock:

$$(11) \quad E_{t-q-2} \left[ g_{it} \left( \sum_{j=-(1+q)}^{(1+q)} g_{it+j} \right) \right] = E_{t-q-2}(\xi_{it}^2).$$

It is then easy to prove that the relevant orthogonality condition for this problem is

$$(12) \quad E_{t-q-3} \left[ g_{it} \left( \sum_{j=-(1+q)}^{(1+q)} g_{it+j} \right) - \phi_i^e - \varphi^e g_{it-1} \left( \sum_{j=-(1+q)}^{(1+q)} g_{it+j-1} \right) - \eta_i \right] = 0.$$

Again we only require knowledge of the order of the MA process, not the values of its parameters. Moreover, as for the transitory shock case, the presence of measurement error (even if serially correlated) is allowed for in this moment condition. Thus our estimated ARCH coefficients are robust to the presence of measurement errors.

As before we apply the within groups transformation to eliminate unobserved heterogeneity. We use autocovariances lagged  $t - q - 3$  or more as instruments.

Estimation requires the availability of a panel data set with a large enough time period of observation for each individual. Data requirements become increasingly stringent as the order of the moving average process for the transitory shock increases. For our case with  $q = 1$ , the estimation of (9) and (12) requires at least nine and eleven years of data respectively. In this respect the PSID, which is our data source, is ideal for estimation purposes.

Obviously there is some attrition in the sample and by having to use individuals with at least nine observations each we lose those who stay in the data for less. Thus, although we do not need to assume that panel attrition is random, we do need to assume that attrition only depends on *fixed* unobserved and observed characteristics (e.g. on the initial conditions and on the heterogeneity in the variances) and not on the actual shocks. In the empirical section we provide a test for this hypothesis by comparing our main results to those obtained by limiting the sample to those who are observed for more than 16 periods.

#### 4.3. *Alternative Specifications*

The way that the mean process is specified affects the conditional variance estimates for the shocks. A number of papers before us have found that earnings data are consistent with a process comprising a martingale component and a transitory shock (MaCurdy (1982), Abowd and Card (1989) are two of the most prominent examples). However, this approach is not uncontroversial.

A more general model that nests ours is one where the unobservable components of log earnings have a time varying effect as in  $u_{it} = d_t^e(k_i + p_{it} + e_{it}) + r_{it}$ . The analysis we carry out on the conditional variances could also be carried out on the basis of this mean specification, with a modification to the moment conditions. In other words, this richer specification does not lead to identification problems. Under this model, the long term autocovariances of the residual log earnings growth should not be zero. The results of Table I show not only that

the autocovariances become insignificant after the second lag, but also that they decline rapidly to zero. Both facts are consistent with our specification.

We can also test the null of our model against this one directly. By quasi-differencing we obtain (see Holtz-Eakin, Newey, and Rosen (1988)):

$$(13) \quad y_{it} = m_t^e - a_t^e m_{t-1}^e + a_t^e y_{it-1} + \beta_t^{e'} Z_{it} - a_t^e \beta_t^{e'} Z_{it-1} \\ + d_t^e (\Delta e_{it} + \zeta_{it}) + r_{it} - a_t^e r_{it-1}$$

where  $a_t^e = d_t^e / d_{t-1}^e$  and all parameters in (13) can be identified. Testing that the coefficient on the lagged log earnings is constant over time and equal to one takes us back to the original specification. The joint test that this is true jointly for all three education groups has a  $p$ -value of 13%, which confirms the adequacy of our specification.<sup>21</sup>

In the case discussed by Lillard and Reville (1999),  $u_{it} = tk_i + e_{it} + r_{it}$  and the residuals of log-income in first differences take the form

$$(14) \quad g_{it} = \Delta r_{it} + \Theta^e(L, q) \Delta \varepsilon_{it} + \zeta_{it} + k_i.$$

If the variance of  $k_i$ ,  $\sigma_k^2$ , is small, it may go statistically undetected in high-order earnings growth autocovariances. However, even a small  $\sigma_k^2$  may have important implications for the evolution of earnings (Baker (1997)). In this case the unconditional variance of the permanent shock is overstated (and the unconditional variance of the transitory shock understated). However, the orthogonality condition (9) still has the same form, with a modification for the heterogeneity term:

$$E_{t-2}(g_{it+q+1}g_{it} - \theta_q^e \kappa_t^e - \gamma^e g_{it+q}g_{it-1} - \Lambda_i) = 0$$

where  $\Lambda_i = (1 - \gamma^e)k_i^2 + \theta_q^e \lambda_i$ . Thus the ARCH parameters are still identified with the conditions stated earlier, even if we ignore this linear trend.

Lillard and Reville (1999) also point out that the rate of return to experience as measured by age may be heterogeneous. The previous model allows for that through the linear term, since, in the presence of fixed effects a linear time trend and a linear age term are not distinguishable. However, if a quadratic term in age or experience were heterogeneous, residual growth would be

$$g_{it} = \Delta r_{it} + \Theta^e(L, q) \Delta \varepsilon_{it} + \zeta_{it} + k_i(\alpha_0 + \alpha_1 X_{it})$$

where  $X_{it}$  is a measure of experience. In this case (5) takes the form

$$(15) \quad E \left[ g_{it} \left( \sum_{j=-(1+q)}^{(1+q)} g_{it+j} \right) \right] = E(\zeta_{it}^2) + (3 + 2q)(\alpha_0 + \alpha_1 X_{it})^2 \sigma_k^2,$$

<sup>21</sup>This will also be a test of the special case where  $u_{it} = d_t^e k_i + e_{it} + r_{it}$ .



TABLE IV  
THE IDENTIFICATION OF THE ARCH COEFFICIENTS

|  | Pooled<br>Sample | High<br>School<br>Dropout | High<br>School<br>Graduate | College<br>Graduate |
|--|------------------|---------------------------|----------------------------|---------------------|
| <i>Transitory Shock</i>                  |                  |                           |                            |                     |
| First Differences                        |                  |                           |                            |                     |
| $\chi^2$ statistic, 2 degrees of freedom | 18.84            | 17.40                     | 26.56                      | 0.96                |
| Bootstrap $p$ -value                     | 0.0000           | 0.1700                    | 0.3633                     | 0.6233              |
| Within Groups                            |                  |                           |                            |                     |
| $\chi^2$ statistic, 2 degrees of freedom | 245.52           | 42.83                     | 267.88                     | 66.75               |
| Bootstrap $p$ -value                     | 0.0000           | 0.0033                    | 0.0000                     | 0.0000              |
| <i>Permanent Shock</i>                   |                  |                           |                            |                     |
| First Differences                        |                  |                           |                            |                     |
| $\chi^2$ statistic, 2 degrees of freedom | 2.57             | 1.10                      | 0.10                       | 4.39                |
| Bootstrap $p$ -value                     | 0.2367           | 0.8833                    | 0.9333                     | 0.2033              |
| Within Groups                            |                  |                           |                            |                     |
| $\chi^2$ statistic, 2 degrees of freedom | 360.73           | 65.31                     | 289.26                     | 86.45               |
| Bootstrap $p$ -value                     | 0.0000           | 0.0000                    | 0.0000                     | 0.0000              |

resulting in overestimation of the variance of the permanent shock that declines with labor market experience if earnings profiles are concave. Again this model is not consistent with zero autocovariances of order three or over. In addition, the test of overidentifying restrictions that we use when estimating the ARCH model should reject the ARCH specifications with additive unobserved heterogeneity (equation (9) or (12)). Note that in principle one could generalize our approach to allow for this.

#### 4.4. The Estimation of the ARCH Coefficients

##### 4.4.1. Checking Identification Conditions

We now proceed to the estimation of the processes for the conditional variance of the permanent and the transitory shocks. We start our analysis by examining whether the instruments we use have sufficient explanatory power to estimate the ARCH model. This is particularly important in our case since for identification we have to depend on information lagged several periods. The recent literature on weak instruments has emphasized the importance of such an exercise (see Staiger and Stock (1994), Bound, Jaeger, and Baker (1995)). To examine this issue, we compute the bootstrap  $p$ -value of the  $\chi^2$ -test for the significance of the excluded instruments in the reduced form. Results are reported in Table IV, based on 300 bootstrap replications.

In the first difference specification for the transitory shock, the reduced forms being examined refer to a linear model predicting  $\Delta g_{it+1}g_{it-1}$  using

as instruments  $g_{it-3}g_{it-5}$  and  $g_{it-4}g_{it-6}$ , which are dated  $t - 3$  or earlier. For the within group specification we denote by a bar over a variable its mean over time for individual  $i$ . Then the reduced forms refer to a linear model predicting  $(g_{it+1}g_{it-1} - \overline{g_{i(+1)}g_{i(-1)}})$  in equation (10) using as instruments  $g_{it-2}g_{it-4}$  and  $g_{it-3}g_{it-5}$ . For the permanent shock model in the first difference case we are predicting  $\Delta[g_{it-1}(\sum_{j=-2}^2 g_{it+j-1})]$  using  $g_{it-7}(\sum_{j=-2}^2 g_{it+j-7})$  and  $g_{it-8} \sum_{j=-2}^2 g_{it+j-8}$ . In the within groups case we are predicting

$$\left[ g_{it-1} \left( \sum_{j=-2}^2 g_{it+j-1} \right) - \overline{g_{i(-1)} \left( \sum_{j=-2}^2 g_{i(j-1)} \right)} \right]$$

using  $g_{it-6}(\sum_{j=-2}^2 g_{it+j-6})$  and  $g_{it-7} \sum_{j=-2}^2 g_{it+j-7}$ . All reduced forms and instrument sets include age and time dummies.

For the first difference model, the only case that the instruments have some predictive power is for the transitory model when we pool across all education groups. In all other cases the instruments have little predictive power. By contrast, in the reduced forms corresponding to within groups we find very strong predictive power: a  $p$ -value well below 1 percent in all cases.

It is very well known that in a dynamic equation, for sufficiently high autoregressive parameters ( $\gamma^e$  or  $\varphi^e$  in equation (7)), lags have little or no predictive power for current changes (see Arellano and Bond (1991), Blundell and Bond (1999)). The lack of predictive power we find could thus imply a high autoregressive coefficient (and even perhaps a unit root) in the conditional variance. In principle one of the models could still be estimated in first differences. However, Staiger and Stock (1994) show that even with significant  $F$  statistics GMM could be biased considerably when the fit of the reduced form is bad. Our assessment of the results leads us to use the within groups procedure. The latter is likely to be less biased given the weakness of the instruments for the first differenced model and the length of our panel.

#### 4.4.2. *The Conditional Variance of the Earnings Shock*

The estimates of the conditional variance function for the transitory shock are based on the orthogonality condition (9) adapted to the within group case. The estimates in the permanent shock case are based on the within group version of the orthogonality condition (12). The within group-instrumental variable estimator we use is the GMM estimator of Hansen (1982) adapted to our problem.

We take  $q = 1$  from our earlier results and estimate separately for each education group the following specification:

$$(16) \quad \widetilde{\psi}_{it} = \xi_t + \beta_1 \widetilde{age}_{it} + \beta_2 \widetilde{age}_{it}^2 + \gamma \widetilde{\psi}_{it-1} + \widetilde{\omega}_{it}$$

where  $\tilde{x}_{it} = x_{it} - \bar{x}_i$ ,  $\bar{x}_i = T_i^{-1} \sum_{s=1}^{T_i} x_{is}$ . For the transitory variance  $\psi_{it} = \hat{g}_{it+2}\hat{g}_{it}$  and for the permanent variance  $\psi_{it} = [\hat{g}_{it}(\hat{g}_{it-2} + \hat{g}_{it-1} + \hat{g}_{it} + \hat{g}_{it+1} + \hat{g}_{it+2})]$ ;  $\hat{g}_{it}$  is the residual from the estimated mean log earnings process in first differences for individual  $i$  in period  $t$ .

The instruments are lags of  $\psi_{it}$  and are set up as in Arellano and Bond (1991). To avoid overfitting in the reduced forms we do not exploit all the available linear orthogonality conditions. In fact, we truncate the set of available instruments at the first two available lags. Moreover, this should improve the power of the overidentifying restrictions test.<sup>22</sup>

#### 4.4.3. *The Results*

Table V reports the WG-GMM results for the coefficients in the conditional variance, as well as a number of diagnostic tests. We report bootstrap standard errors based on 1000 replications as well as the level of significance of the ARCH coefficients based on the bootstrap critical values. The results are presented by education group. We then consider pooling over the whole sample and test whether the ARCH effects vary by education. All specifications include time dummies and a quadratic in age. However neither time or age effects are significant in this conditional specification.

Turning now to the ARCH coefficients themselves the highest persistence parameter for both the permanent and the transitory shock is obtained for the High School graduates. For this group, which is by far the largest in terms of sample size, the coefficients are unambiguously significant and high, with a 0.67 value for the transitory shock case and nearly 0.9 for the permanent shock. For the High School dropouts the ARCH coefficient for the transitory shock is not significant ( $p$ -value of 13%) but for the permanent shock the effect is quite large and has a  $p$ -value of 7%, for a sample that is about half that of the High School graduates.

For the College graduates the coefficient on the permanent shock is essentially zero, while for the transitory shock the coefficient is not significant and imprecisely estimated, making it difficult to draw a firm conclusion. We also impose the (acceptable) hypothesis that for this group the transitory shocks follow an MA(0) process ( $q = 0$ ). In this case the estimate of  $\gamma^e$  is 0.2004 (bootstrap s.e. 0.2435) and that of  $\varphi^e$  0.0221 (0.2045). Thus for the coefficient of the permanent shock the estimation precision goes up substantially but both coefficients remain insignificant.<sup>23</sup>

In Table V we also present tests of the overidentifying restrictions (OID). These are all acceptable, except for the model of the variance of the perma-

<sup>22</sup>This bias arises in small samples from inflating the degrees of freedom of the test with the inclusion of irrelevant instruments.

<sup>23</sup>The estimated age and age square effects in the transitory shock case are 0.0011 (0.0029) and  $-0.0008$  (0.0034), while in the permanent shock case they are  $-0.0086$  (0.0080) and 0.0107 (0.0093).

TABLE V  
THE CONDITIONAL VARIANCE OF EARNINGS SHOCKS<sup>a</sup>

|  | High School<br>Dropout | High School<br>Graduate | College<br>Graduate      |
|--|------------------------|-------------------------|--------------------------|
| <i>Transitory Shock</i>                                    |                        |                         |                          |
| $\gamma^e$   | 0.1918<br>(0.14)[13%]  | 0.6672<br>(0.152)[0.4%] | 0.3878<br>(0.192)[10.3%] |
| Age  | -0.0030<br>(0.0065)    | -0.0005<br>(0.0029)     | -0.0006<br>(0.0027)      |
| Age <sup>2</sup> /100                                      | 0.0028<br>(0.0082)     | 0.0010<br>(0.0036)      | 0.0007<br>(0.0036)       |
| <i>P</i> -value OID test <sup>b</sup>                      | 19%                    | 14%                     | 15%                      |
| <i>P</i> -value for time effects                           | 95%                    | 99%                     | 99%                      |
| <i>P</i> -value for time and age effects                   | 98%                    | 96%                     | 98%                      |
| <i>P</i> -value test for unobs. heterogeneity <sup>c</sup> | 34.4%                  | 2%                      | 4.3%                     |
| $\gamma^e$ Pooled (all education groups) <sup>d</sup>      |                        | 0.404<br>(0.096)[0%]    |                          |
| <i>Permanent Shock</i>                                     |                        |                         |                          |
| $\varphi^e$  | 0.3299<br>(0.21)[7.4%] | 0.8912<br>(0.18)[0.0%]  | 0.0283<br>(0.33)[90.4%]  |
| Age  | -0.0076<br>(0.0056)    | 0.0017<br>(0.0034)      | -0.0065<br>(0.0055)      |
| Age <sup>2</sup> /100                                      | 0.0090<br>(0.0063)     | -0.0008<br>(0.0040)     | 0.0083<br>(0.0066)       |
| <i>P</i> -value OID test <sup>b</sup>                      | 14%                    | 40%                     | 2%                       |
| <i>P</i> -value for time effects                           | 93%                    | 89%                     | 95%                      |
| <i>P</i> -value for time and age effects                   | 93%                    | 93%                     | 91%                      |
| <i>P</i> -value test for unobs. heterogeneity <sup>c</sup> | 0%                     | 2.7%                    | 37.2%                    |
| $\varphi^e$ Pooled (all education groups) <sup>d</sup>     |                        | 0.56<br>(0.126)[0.3%]   |                          |

<sup>a</sup>Bootstrap standard errors based on 1000 replications reported in round brackets and *p*-values in square brackets.

<sup>b</sup>The OID test is a Sargan test for the null of instruments validity. It is distributed  $\chi^2$  with degrees of freedom equal to the number of exclusion restrictions.

<sup>c</sup>The test for the null of no unobserved heterogeneity is based on 500 replications.

<sup>d</sup>The pooled estimate and its standard error are obtained by minimum distance.

ment shock for the College graduates, where the *p*-value is 2%. This can occur if the variance includes a persistent stochastic volatility component, which could be correlated with the instruments. To address this issue we lagged the instruments one more period. The OID test now has a *p*-value of 14%. The coefficient  $\varphi^e$  became 0.17 with a standard error of 0.29. Hence, the results are not significantly different from what we obtained before.

We now consider a pooled model where the ARCH coefficients are restricted to be equal across education groups. In fact the differences across education groups are not significant. Based on the estimates of Table V the  $\chi^2$  test that the coefficients are the same for the transitory shock has a  $p$ -value of 15%; for the permanent shock the  $p$ -value is 6.6%.

When we restrict the three coefficients to be the same, while leaving all the other regressors in the variance to have education specific coefficients, we obtain 0.404 persistence for the transitory shock (standard error 0.096) and 0.56 for the permanent one (standard error 0.128), with important improvements in the precision. Both the restricted coefficients are highly significant and we take these as the most reliable estimates of the ARCH coefficients. These estimates for persistence (*vis-à-vis* the 0.89 coefficient for the High School graduates) imply lower fourth moments for the marginal distribution of the innovations to log earnings for our finitely lived individuals.<sup>24</sup>

A key issue is whether unobserved heterogeneity in the variance is an important factor, i.e., whether there are permanent differences in the volatility of income among individuals, over and above what is accounted for by observables, such as education, time, and age. To carry out this test we estimated the model both in levels and within groups; we then used the bootstrap to derive critical values for the  $\chi^2_{(1)}$  statistic for the equality of the two coefficients.

For all groups there is evidence of unobserved heterogeneity, at least for one of the two variances. For the High School graduates unobserved heterogeneity is evident in both the variance of the permanent shock and the variance of the transitory shock. For the dropouts, we find unobserved heterogeneity for the variance of the permanent shock only. Finally for the College graduates heterogeneity seems to be important only for the variance of the transitory shock.

A final issue is the extent to which attrition from the PSID has biased our results. We have assumed that attrition is all accounted for by permanent characteristics that are eliminated by our estimation procedure (first differencing for the mean and within groups for the variances). To provide some evidence for this we compare our estimates to those obtained by using only those individuals who are 16 or more years in the sample; there are 892 such individuals as opposed to 2,069 in the whole sample. This kind of selection mimics attrition bias since it cuts out individuals observed for a shorter time period. This comparison may also be viewed as a sensitivity test for within groups, since we remove the individuals who only contribute a small number of time series observations, thus reducing the potential for within group bias. The estimates based on this restricted sample are reported in Table A6 in the Appendix. There appear to

<sup>24</sup>Engle (1982) has shown that if a random variable is conditionally normal with an ARCH process for the variance, the fourth moment of the unconditional distribution is finite only if the ARCH coefficient is lower than  $3^{-0.5}$ . In our case, with finitely lived individuals the implication of higher levels of variance persistence is a growing fourth order moment of the cross sectional distribution of income innovations over the life-cycle.

be some differences, with the coefficients on this selected sample being lower. This is an indication that, if anything, attrition combined with any within groups bias may have biased the ARCH coefficients up. However, when we compute a test statistic comparing the ARCH coefficients in the two data sets by education group we find that none of the differences are significant at conventional levels as reported in the table.<sup>25</sup> The pooled estimates on the restricted sample, although smaller, are significant and show the same pattern as in the whole sample with ARCH effects being larger for the permanent shock.

## 5. IMPLICATIONS

Given the results above we now provide two examples that illustrate the effects that ARCH can have in explaining a number of important phenomena.

### 5.1. *Income Mobility*

Allowing for ARCH effects will have implications for earnings mobility since state dependence becomes richer relative to allowing for dynamics in the mean only. As an illustration we focus on the probability of being below the poverty line  $q_L$  conditioning on being below  $q_L$  in the previous period, i.e.  $\Pr(y_{it} < q_L | y_{it-1} < q_L)$ .

We compute this measure of poverty persistence using a distribution of income that allows for ARCH effects and a distribution of income that would have been fitted on the same data, but ignoring ARCH effects. In the ARCH case log earnings are generated by the sum of a random walk process where the innovations  $\zeta_{it}$  are normal and have conditional variance  $E_{t-1}(\zeta_{it}^2) = (1 - \varphi)\sigma_\zeta^2 + \varphi\zeta_{it-1}^2$  and a transitory component  $e_{it} = \varepsilon_{it} - \theta\varepsilon_{it-1}$  where the innovations  $\varepsilon_{it}$  are also normal and have conditional variance  $E_{t-1}(\varepsilon_{it}^2) = (1 - \gamma)\sigma_\varepsilon^2 + \gamma\varepsilon_{it-1}^2$ . Alternatively we use i.i.d. innovations whose variances are equal to the unconditional variances of the previous process, namely  $\sigma_\zeta^2$  and  $\sigma_\varepsilon^2$ .

We focus on a single cohort of individuals, assume a life-cycle of 40 periods, and set the parameters  $\sigma_\zeta^2$ ,  $\sigma_\varepsilon^2$ ,  $\varphi$ , and  $\gamma$  to the values estimated in Table III and Table V. To avoid an initial conditions problem in the variance we draw initial shocks for both cases from the unconditional distributions.

Figure 4 plots the difference between  $\Pr(y_{it} < q_L | y_{it-1} < q_L)$  calculated under ARCH-type shocks and the same probability calculated under i.i.d. income shocks over the life cycle. We set the poverty line at  $q_L = -0.16$  corresponding to the bottom 25th percentile of the income distribution,<sup>26</sup> and  $\varphi = \{0.89, 0.56\}$

<sup>25</sup>Fitzgerald, Gottschalk, and Moffitt (1998) examine the effect of attrition in the PSID and conclude that attrition propensities are correlated with individual-specific levels of earnings instability, but that their effects on attrition are not large, suggesting that “they are unlikely to induce significant bias in studies which have [...] dynamic measures as outcome variables” (p. 296).

<sup>26</sup>Since there is no aggregate growth in this model, we set  $q_L$  to a constant value.

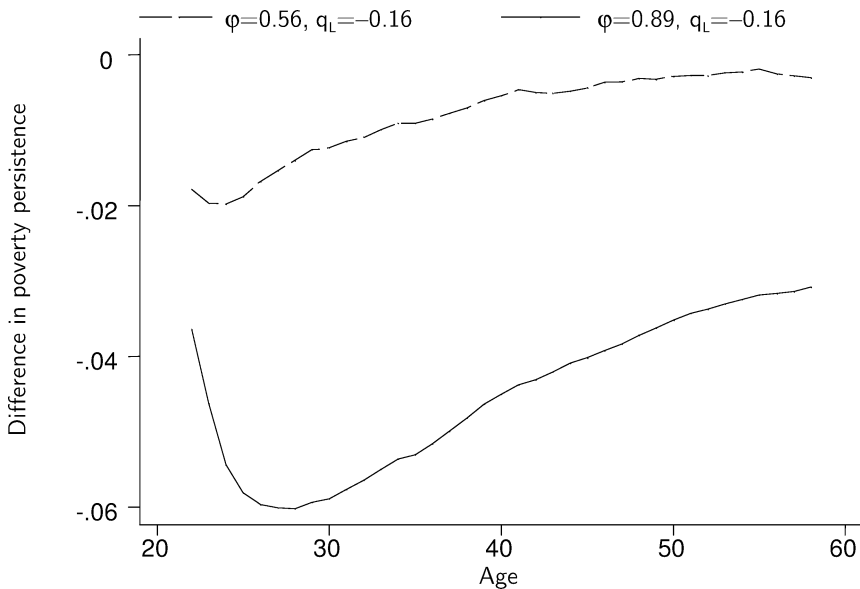


FIGURE 4.—Difference in the persistence of poverty between the ARCH and the i.i.d. case.

corresponding to the ARCH estimates for the permanent shock in the High School graduate and pooled sample case (see Table V).

The difference in poverty persistence is negative throughout the life cycle. The intuition is that in the lower and upper tails of the distribution individuals with large shocks in period  $t - 1$  are over-represented. According to the ARCH specification, they have a higher conditional variance (relative to the i.i.d. case) and thus a higher probability of a large shock that will remove them from the tail and push them back to the center. The reduced persistence on the two extremes of the income distribution is compensated by greater persistence in the central part of the distribution.

Two more facts are worth noting. First, the difference in poverty persistence is higher for the young and tends to decline as time goes by. Second, it is accentuated by higher values of the ARCH parameter  $\phi$ . Similar results are obtained when setting the poverty line at the 10th percentile.

## 5.2. Precautionary Savings

As Caballero (1990) has stated, the presence of stochastic higher order moments in income, to the extent that they relate to uninsurable uncertainty, is capable of explaining a number of important phenomena that have been observed in consumption data, including excess smoothness, excess growth, and excess sensitivity. One mechanism for doing this is the impact of the stochastic

process of income on the volatility of consumption growth and on precautionary savings. His analytical results, although suggestive, are not well suited for our income process, which is in logs.

To see the effect of introducing ARCH shocks we consider an approximation to consumption growth. Preferences for consumption  $c_{it}$  are CRRA ( $u(c_{it}) = (\rho + 1)^{-1} c_{it}^{\rho+1}$ ,  $\rho < 0$ ), and income is  $\log y_{it} = \log y_{it-1} + \zeta_{it}$ , where  $\zeta_{it}$  is conditionally normal with mean zero<sup>27</sup> and  $E_{t-1}(\zeta_{it}^2) = (1 - \varphi)\sigma_\zeta^2 + \varphi\zeta_{it-1}^2$ . The interest rate is taken equal to the intertemporal discount rate. Adapting the results of Banks, Blundell, and Brugiavini (2001) we can write consumption growth as<sup>28</sup>

$$(17) \quad \Delta \log c_{it} = \frac{(1 - \rho)}{2} \pi_{it}^2 \left\{ E_{t-1}(\zeta_{it}^2) + \frac{1}{4} E_{t-1} \left[ (\zeta_{it}^2 - E_{t-1}(\zeta_{it}^2))^2 \right] \right\} + \Delta \log w_{it}$$

where  $\pi_{it}$  is the ratio of lagged income to consumption  $y_{it-1}/c_{it-1}$ , which for the purposes of illustration we take to be 1, and  $\Delta \log w_{it}$  is the change in life-cycle wealth from one period to the next.

Individual consumption growth due to precautionary savings is given by the first term on the right-hand side of (17). For small realizations of  $\zeta_{it-1}$  (in the  $[-\sigma_\zeta, \sigma_\zeta]$  range) consumption growth in the ARCH case is lower than in the i.i.d. case. This is because people forecast a lower variance than the unconditional one—upon which precautionary behavior in the i.i.d. case depends. This can help explain a high degree of heterogeneity in savings behavior.

In the aggregate there is no such ambiguity however and ARCH always predicts more saving. To see this, note that when  $\varphi < 3^{-0.5}$  the fourth moment of the ARCH process converges to

$$3\sigma_\zeta^4 \left( \frac{1 - \varphi^2}{1 - 3\varphi^2} \right),$$

which is larger than the fourth moment of the long run cross-sectional income distribution in the absence of ARCH effects (i.e.  $3\sigma_\zeta^4$ ). Thus under ARCH, aggregate consumption growth due to precautionary savings increases by

$$\frac{(1 - \rho)}{2} \frac{\varphi^2}{1 - 3\varphi^2} \sigma_\zeta^4$$

relative to the i.i.d. case. Using our estimates of  $\varphi$  and  $\sigma_\zeta^2$ , this is roughly 0.8% when  $\rho = -2$  (Attanasio and Weber (1995)) and 1.6% when  $\rho = -5$ . With aggregate consumption growth averaging 3% in the last few decades, these are sizeable changes.

<sup>27</sup>We neglect the effect of transitory shocks given that they are smoothed away through savings.

<sup>28</sup>Detailed calculations are available from the authors on request.



When the persistence coefficient  $\varphi \geq 3^{-0.5}$ , the fourth order moment does not converge. With finite lived consumers, the moments never become infinite of course, but this means that aggregate consumption growth within a cohort can be very high. In other words ARCH effects can rationalize steep consumption growth over the life-cycle, even with moderate or small levels of variance in the income shocks.

Both examples are just illustrative of the potential importance of understanding the form of the income process and should not be taken as a full blown analysis, which would need to take into account a number of other important issues in the respective fields.

## 6. CONCLUSIONS

In this paper we have estimated an income process for individual annual earnings in the U.S., allowing for differences across education groups and taking into account changes over time. In line with earlier studies we have confirmed that earnings are best described as being driven by a permanent income shock and a serially correlated transitory shock. We have also emphasized the importance of measurement error. We test our specification against a number of alternatives and find ours to be a good description of the data.

We then estimate conditional variance processes for both the transitory and the permanent component, having shown that these processes are separately identified, even in the presence of nonclassical measurement error. We find that there is strong evidence of sizeable ARCH effects for both the variances of the transitory and permanent shocks. We also find strong evidence for fixed differences across individuals in the variance of shocks. We then illustrate some potential implications that ARCH effects may have in the field of income mobility and savings. A more complete analysis of these issues, with our richer income process is of course an important area for further work.

Finally there are two issues (among others) that require further research: the extent to which the income shocks we have been modelling represent uninsurable income uncertainty (see Blundell and Preston (1998)); and distinguishing between employment and wage risk separately allowing for endogenous job mobility (see Low, Meghir, and Pistaferri (2003)).

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## APPENDIX: STEP-BY-STEP DETAILS ON SAMPLE SELECTION

The 1968–1993 PSID individual file contains information on 53,013 individuals (all those ever present in the sample). We drop members of the Latino sample added in 1990 (10,022 individ-

TABLE A1  
DISTRIBUTION OF OBSERVATIONS, BY YEAR

| Year | Number of<br>observations | Year | Number of<br>observations |
|------|---------------------------|------|---------------------------|
| 1967 | 746                       | 1980 | 1393                      |
| 1968 | 787                       | 1981 | 1425                      |
| 1969 | 831                       | 1982 | 1455                      |
| 1970 | 878                       | 1983 | 1501                      |
| 1971 | 923                       | 1984 | 1539                      |
| 1972 | 1008                      | 1985 | 1491                      |
| 1973 | 1078                      | 1986 | 1436                      |
| 1974 | 1163                      | 1987 | 1383                      |
| 1975 | 1234                      | 1988 | 1329                      |
| 1976 | 1258                      | 1989 | 1280                      |
| 1977 | 1300                      | 1990 | 1230                      |
| 1978 | 1319                      | 1991 | 1177                      |
| 1979 | 1365                      | 1992 | 1102                      |

uals), and those who are never heads of their household (26,962 individuals). This reduces the sample to 16,029 individuals. We keep only those who are continuously heads of their household, who are in the sample for nine years or more, and are aged 25 to 55 over this period. This leaves us with a sample of 4,539 individuals.

TABLE A2  
DISTRIBUTION OF OBSERVATIONS, BY EDUCATION

| Number of Years | Number of Individuals |                        |                         |                     |
|-----------------|-----------------------|------------------------|-------------------------|---------------------|
|                 | Pooled<br>Sample      | High School<br>Dropout | High School<br>Graduate | College<br>Graduate |
| 9               | 231                   | 64                     | 131                     | 36                  |
| 10              | 185                   | 50                     | 96                      | 39                  |
| 11              | 182                   | 51                     | 92                      | 39                  |
| 12              | 154                   | 28                     | 93                      | 33                  |
| 13              | 144                   | 42                     | 81                      | 21                  |
| 14              | 142                   | 35                     | 80                      | 27                  |
| 15              | 139                   | 34                     | 83                      | 22                  |
| 16              | 121                   | 27                     | 67                      | 27                  |
| 17              | 123                   | 40                     | 54                      | 29                  |
| 18              | 86                    | 20                     | 43                      | 23                  |
| 19              | 109                   | 21                     | 60                      | 28                  |
| 20              | 93                    | 22                     | 49                      | 22                  |
| 21              | 92                    | 16                     | 48                      | 28                  |
| 22              | 54                    | 12                     | 25                      | 17                  |
| 23              | 52                    | 16                     | 26                      | 10                  |
| 24              | 45                    | 12                     | 20                      | 13                  |
| 25              | 37                    | 10                     | 17                      | 10                  |
| 26              | 80                    | 19                     | 39                      | 22                  |

TABLE A3  
DESCRIPTIVE STATISTICS: DEMOGRAPHIC CHARACTERISTICS<sup>a</sup>

|                      | 1967               | 1979               | 1992               |
|----------------------|--------------------|--------------------|--------------------|
| Age                  | 36.91<br>(6.34)    | 37.24<br>(9.35)    | 41.21<br>(5.64)    |
| High School Dropout  | 0.46               | 0.25               | 0.12               |
| High School Graduate | 0.38               | 0.53               | 0.61               |
| Hours                | 2,250<br>(558)     | 2,134<br>(534)     | 2,151<br>(540)     |
| Married              | 0.96               | 0.88               | 0.87               |
| White                | 0.66               | 0.67               | 0.70               |
| Children             | 2.81<br>(2.11)     | 1.40<br>(1.31)     | 1.33<br>(1.23)     |
| Family Size          | 4.95<br>(2.06)     | 3.58<br>(1.58)     | 3.51<br>(1.44)     |
| Family Income        | 27,146<br>(13,254) | 36,216<br>(17,542) | 43,181<br>(24,062) |
| North-East           | 0.20               | 0.17               | 0.16               |
| North-Central        | 0.25               | 0.26               | 0.24               |
| South                | 0.41               | 0.42               | 0.43               |
| SMSA                 | 0.70               | 0.67               | 0.53               |

<sup>a</sup>Standard deviations of non-binary variables in parentheses.

TABLE A4  
ESTIMATED VARIANCES OF THE PERMANENT SHOCK<sup>a</sup>

| Year | Pooled Sample <sup>b</sup> | High School Dropout | High School Graduate | College Graduate   |
|------|----------------------------|---------------------|----------------------|--------------------|
| 1969 | 0.0280<br>(0.0125)         | 0.0221<br>(0.0155)  | 0.0244<br>(0.0241)   | 0.0576<br>(0.0321) |
| 1970 | 0.0242<br>(0.0124)         | 0.0119<br>(0.0105)  | 0.0117<br>(0.0042)   | 0.0847<br>(0.0657) |
| 1971 | 0.0136<br>(0.0077)         | 0.0144<br>(0.0163)  | 0.0067<br>(0.0043)   | 0.0296<br>(0.0189) |
| 1972 | 0.0223<br>(0.0135)         | -0.0175<br>(0.0251) | 0.0222<br>(0.0107)   | 0.1155<br>(0.0413) |
| 1973 | 0.0124<br>(0.0073)         | 0.0045<br>(0.0145)  | 0.0049<br>(0.0092)   | 0.0579<br>(0.0182) |
| 1974 | 0.0165<br>(0.0061)         | 0.0154<br>(0.0147)  | 0.0127<br>(0.0082)   | 0.0321<br>(0.0123) |

TABLE A4  
(CONTINUED)

| Year   | Pooled<br>Sample <sup>b</sup> | High School<br>Dropout | High School<br>Graduate | College<br>Graduate |
|--|-------------------------------|------------------------|-------------------------|---------------------|
| 1975   | 0.0332<br>(0.0112)            | 0.0434<br>(0.0234)     | 0.0175<br>(0.0174)      | 0.0482<br>(0.0150)  |
| 1976   | 0.0155<br>(0.0089)            | 0.0105<br>(0.0158)     | 0.0189<br>(0.0149)      | 0.0186<br>(0.0091)  |
| 1977   | 0.0222<br>(0.0092)            | -0.0165<br>(0.0153)    | 0.0259<br>(0.0112)      | 0.0662<br>(0.0282)  |
| 1978   | 0.0421<br>(0.0124)            | 0.0470<br>(0.0333)     | 0.0282<br>(0.0118)      | 0.0634<br>(0.0280)  |
| 1979   | 0.0199<br>(0.0079)            | 0.0191<br>(0.0198)     | 0.0061<br>(0.0069)      | 0.0489<br>(0.0224)  |
| 1980   | 0.0533<br>(0.0178)            | 0.0524<br>(0.0356)     | 0.0382<br>(0.0119)      | 0.0881<br>(0.0624)  |
| 1981   | 0.0660<br>(0.0204)            | 0.1355<br>(0.0763)     | 0.0567<br>(0.0191)      | 0.0150<br>(0.0097)  |
| 1982   | 0.0540<br>(0.0122)            | 0.0778<br>(0.0371)     | 0.0521<br>(0.0161)      | 0.0354<br>(0.0133)  |
| 1983   | 0.0495<br>(0.0101)            | 0.0645<br>(0.0301)     | 0.0443<br>(0.0132)      | 0.0445<br>(0.0129)  |
| 1984   | 0.0616<br>(0.0158)            | 0.0567<br>(0.0359)     | 0.0710<br>(0.0237)      | 0.0386<br>(0.0126)  |
| 1985   | 0.0413<br>(0.0101)            | 0.0824<br>(0.0467)     | 0.0412<br>(0.0106)      | 0.0142<br>(0.0081)  |
| 1986   | 0.0253<br>(0.0093)            | 0.0462<br>(0.0495)     | 0.0213<br>(0.0080)      | 0.0205<br>(0.0096)  |
| 1987   | 0.0289<br>(0.0077)            | 0.0251<br>(0.0182)     | 0.0304<br>(0.0100)      | 0.0260<br>(0.0159)  |
| 1988   | 0.0309<br>(0.0095)            | 0.0128<br>(0.0200)     | 0.0371<br>(0.0146)      | 0.0227<br>(0.0089)  |
| 1989   | 0.0340<br>(0.0087)            | 0.0865<br>(0.0428)     | 0.0283<br>(0.0101)      | 0.0173<br>(0.0054)  |
| 1990   | 0.0293<br>(0.0070)            | 0.0498<br>(0.0254)     | 0.0290<br>(0.0095)      | 0.0159<br>(0.0048)  |
| 1991   | 0.0438<br>(0.0209)            | 0.0516<br>(0.0248)     | 0.0550<br>(0.0335)      | 0.0123<br>(0.0083)  |
| $\chi^2$ goodness of fit <sup>c</sup><br>(d.o.f) | 322.81<br>(275)               | 1648.65<br>(275)       | 354.89<br>(275)         | 1784.31<br>(275)    |

<sup>a</sup> Asymptotic standard errors in parentheses.

<sup>b</sup> In Table A4 and A5 we impose equality of the permanent shock variances in the first two and in the last two years of the sample period. This is to avoid instability when few moments are used for identification.

<sup>c</sup> Goodness of fit statistic for the estimated model. It is defined as  $(\mathbf{c} - \mathbf{f}(\boldsymbol{\beta}))' \mathbf{R}^- (\mathbf{c} - \mathbf{f}(\boldsymbol{\beta}))$ , where  $\mathbf{c}$  is the vector of estimated moments,  $\mathbf{f}(\boldsymbol{\beta})$  is the theoretical counterpart we attempt to fit, and  $\mathbf{R}^-$  is a generalized inverse of  $\mathbf{R} = \mathbf{V}\mathbf{V}'$  with  $\mathbf{W} = \mathbf{I} - \mathbf{G}(\mathbf{G}'\mathbf{G})^{-1}\mathbf{G}'$  and  $\mathbf{V}$  the matrix of empirical fourth moments. The test statistic is asymptotically distributed  $\chi^2$  with degrees of freedom equal to the difference between the number of elements in  $\mathbf{c}$  and the rank of the gradient matrix  $\mathbf{G}$ . See Newey (1985) for more details.

TABLE A5  
CONDITIONING ON AN EXTERNAL ESTIMATE OF  $\sigma_r^{2a}$

| Year | $E(\zeta_{it}^2)$  | $E(\varepsilon_{it}^2)$ | Year                                 | $E(\zeta_{it}^2)$   | $E(\varepsilon_{it}^2)$ |
|------|--------------------|-------------------------|--------------------------------------|---------------------|-------------------------|
| 1967 | —                  | 0.0119<br>(0.0212)      | 1981                                 | 0.0652<br>(0.0200)  | 0.0168<br>(0.0106)      |
| 1968 | —                  | 0.0074<br>(0.0064)      | 1982                                 | 0.0525<br>(0.0123)  | 0.0509<br>(0.0151)      |
| 1969 | 0.0298<br>(0.0134) | 0.0132<br>(0.0069)      | 1983                                 | 0.0500<br>(0.0100)  | 0.0430<br>(0.0153)      |
| 1970 | 0.0274<br>(0.0124) | 0.0153<br>(0.0068)      | 1984                                 | 0.0623<br>(0.0158)  | 0.0345<br>(0.0153)      |
| 1971 | 0.0173<br>(0.0081) | 0.0352<br>(0.0126)      | 1985                                 | 0.0429<br>(0.0099)  | 0.0230<br>(0.0074)      |
| 1972 | 0.0248<br>(0.0133) | 0.0605<br>(0.0210)      | 1986                                 | 0.0269<br>(0.0094)  | 0.0266<br>(0.0084)      |
| 1973 | 0.0136<br>(0.0071) | 0.0242<br>(0.0067)      | 1987                                 | 0.0312<br>(0.0077)  | 0.0090<br>(0.0057)      |
| 1974 | 0.0158<br>(0.0062) | 0.0313<br>(0.0125)      | 1988                                 | 0.0316<br>(0.0095)  | 0.0224<br>(0.0122)      |
| 1975 | 0.0334<br>(0.0112) | 0.0819<br>(0.0219)      | 1989                                 | 0.0368<br>(0.0087)  | 0.0005<br>(0.0063)      |
| 1976 | 0.0166<br>(0.0091) | 0.0618<br>(0.0286)      | 1990                                 | 0.0309<br>(0.0069)  | 0.0212<br>(0.0111)      |
| 1977 | 0.0218<br>(0.0098) | 0.0136<br>(0.0064)      | 1991                                 | 0.0483<br>(0.0210)  | 0.0058<br>(0.0057)      |
| 1978 | 0.0417<br>(0.0125) | 0.0113<br>(0.0067)      | 1992                                 | —                   | 0.0227<br>(0.0237)      |
| 1979 | 0.0213<br>(0.0079) | 0.0267<br>(0.0094)      | $\theta$                             | —0.2030<br>(0.0308) |                         |
| 1980 | 0.0552<br>(0.0178) | 0.0156<br>(0.0062)      | $\chi^2$ goodness of fit<br>(d.o.f.) | 325.06<br>(275)     |                         |

<sup>a</sup>Asymptotic standard errors in parentheses.

We then drop female heads and remain with a sample of 3,663 male heads. We eliminate those with a spell of self-employment over the sample period, missing earnings, and unusable (zero or top-coded) earnings data. This leaves 2,340 individuals. We also drop those with missing education and race records, and those with inconsistent education records. We are left with 2,153 individuals. Finally, we eliminate individuals with outlying earnings records, defined as a change in log earnings greater than 5 or less than  $-1$ . The final sample includes 2,069 individuals.

The composition of the sample by year and by education is reported in Tables A1 and A2, respectively. Selected demographic and socio-economic characteristics are reported in Table A3 for selected sample years (1967, 1979, and 1991).

TABLE A6  
ARCH ESTIMATES USING INDIVIDUALS OBSERVED 16 YEARS OR MORE<sup>a</sup>

|                               | HS Dropout              | HS Graduate            | College Graduate         |
|-------------------------------|-------------------------|------------------------|--------------------------|
| <i>Transitory Shock</i>       |                         |                        |                          |
| $\gamma^e$                    | 0.215<br>(0.119)[13.8%] | 0.190<br>(0.102)[7.8%] | 0.232<br>(0.156)[13.2%]  |
| P-value Attrition Test        | 84.2%                   | 5.4%                   | 51%                      |
| $\gamma$ Pooled <sup>b</sup>  |                         | 0.21<br>(0.07)[2%]     |                          |
| <i>Permanent Shock</i>        |                         |                        |                          |
| $\varphi^e$                   | 0.289<br>(0.216)[17.4%] | 0.584<br>(0.214)[5.8%] | -0.041<br>(0.417)[93.2%] |
| P-value Attrition Test        | 30.8%                   | 19.2%                  | 81.2%                    |
| $\varphi$ Pooled <sup>b</sup> |                         | 0.381<br>(0.14)[0%]    |                          |

<sup>a</sup>Bootstrap standard errors in round parentheses; *p*-values in square parentheses. All *p*-values are estimated using the bootstrap.

<sup>b</sup>The pooled estimate and its standard error are obtained by minimum distance.

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