In search of lost time aggregation

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ARTICLE INFO

ABSTRACT

In 1960, Working noted that time aggregation of a random walk induces serial correlation in the first difference that is not present in the original series. This important contribution has been overlooked in a recent literature analyzing income and consumption in panel data. I examine Blundell et al., (2008) as an important example for which time aggregation has quantitatively large effects. Using new techniques to correct for the problem, I find the estimate for the partial insurance to transitory shocks, originally estimated to be 0.05, increases to 0.24. This larger estimate resolves the dissonance between the low partial consumption insurance estimates of Blundell et al., (2008) and the high marginal propensities to consume found in the natural experiment literature. A remaining puzzle is the low estimate I recover for the partial insurance to permanent shocks.

Published by Elsevier B.V.

In a short note in Econometrica, Working (1960) made the simple but important point that time aggregation can induce serial correlation that is not present in the original series. This fact was readily absorbed by the macroeconomic literature, where time aggregated series are common[2] and a small literature has grown around how to account for time aggregation in various settings.[3]

However, the effect of time aggregation has been overlooked in much of the literature studying the covariance structure of household income and consumption dynamics.[4] This oversight can result in significant bias. I examine (Blundell et al., 2008) (henceforth BPP) not only as a way to demonstrate new techniques to overcome the bias, but also because the consumption responses to transitory and permanent income shocks are of significant economic interest in themselves. Indeed, Kaplan and Violante (2010) argue that "the BPP insurance coefficients should become central in quantitative macroeconomics". Using the same

Panel Study of Income Dynamics (PSID) data as in BPP, I update their underlying model to account for time aggregation. I find the estimate for partial insurance to transitory shocks, originally estimated in BPP to be 0.05, to be 0.24 when time aggregation is accounted for. This new estimate resolves the dissonance between BPP's "full insurance of transitory shocks" and a parallel literature that, using natural experiments, finds large consumption responses to transitory income shocks.[5] However, a new puzzle arises from the low estimate for the partial insurance to permanent shocks, now estimated to be around 0.34.

While this letter will focus on the implications of time aggregation for the methodology in BPP, the techniques can be applied to a broad swath of the literature.

1. What is time aggregation?

Time aggregation occurs when a time series is observed at a lower frequency than the underlying data that generates it. For example, income is often observed at an annual frequency

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[1] The analysis and conclusions set forth are those of the author alone and do not indicate concurrence by other members of the research staff or the Board of Governors. Many thanks to Chris Carroll for support and guidance.

[2] For an example see Campbell and Mankiw (1989).

[3] A sample of this literature includes Amemiya and Wu (1972), Weiss (1984) and Drost and Nijman (1993).

[4] The literature goes back to early work such as Hause (1973), Weiss and Lillard (1979) and MaCurdy (1982) that look at the covariance structure of the income process. Following BPP, a number of papers have looked at income and consumption together, for example Arellano et al. (2017).

[5] A small sample of this literature includes Parker et al. (2013), Agarwal and Qian (2014) and Sahm et al. (2010). Consumers also answer that they have a high marginal propensity to consume when asked, see Fuster et al. (2018) and Jappelli and Pistaferri (2014). For an overview of the entire literature on consumption responses to income shocks, see Jappelli and Pistaferri (2010). Note the dissonance between BPP and the natural experiment literature is also addressed by Commault (2017). In contrast to this letter, her approach makes structural changes to the underlying model but does not address time aggregation.
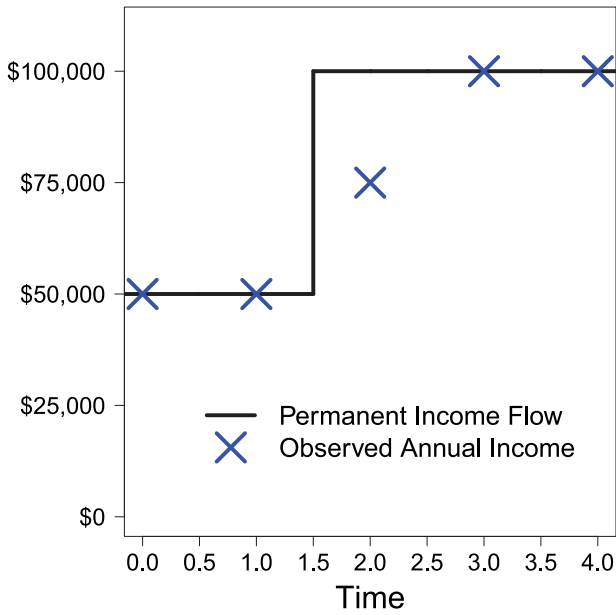
Fig. 1. Income flow and observed income.

when it may in fact consist of paychecks arriving at a monthly, biweekly or irregular timetable. To transform income into an annual frequency, we sum up all the income that was received by a household during the year. The key insight of Working (1960) is that even if there is no correlation between changes in income at the underlying frequency, changes in the resulting time aggregated series will show positive autocorrelation. The intuition behind this can be seen in Fig. 1, showing the income process of a household that begins with an annual salary of $50,000 and receives a permanent pay rise to $100,000 midway through the second year. The solid line shows this jump in income flow occurring just once. The crosses show the income we actually observe in annual data. During the second year the household receives an annual $50,000 salary for six months, followed by $100,000 in the second six months, resulting in a reported income of $75,000 for the entire year. The single shock to income therefore appears in the time aggregated data as two increases. In this way, an income change in one year is positively correlated with an income change in the following year, even if the underlying income process follows a random walk.

2. Modeling time aggregation in Blundell et al. (2008)

2.1. The model in discrete time without time aggregation

Here I briefly describe the method used by Blundell et al. (2008) to estimate household consumption responses to permanent and transitory income shocks. The model described here is a simplified version of the original in order to highlight the role played by time aggregation.[6]

The core of the model is the assumptions made on the income and consumption processes. Unexplained log income growth for household i follows the process:

$$\Delta y_{i,t} = \zeta_{i,t} + \Delta v_{i,t}$$

where $\zeta_{i,t}$ (the change in permanent income) and $v_{i,t}$ (transitory income) are each mean zero, finite variance, i.i.d. and independent of each other.

The unexplained change in log consumption is modeled as a random walk that moves in response to permanent and transitory income shocks:

$$\Delta c_{i,t} = \phi \zeta_{i,t} + \psi v_{i,t}$$

where ϕ and ψ are the *partial insurance* parameters. A value of zero implies full insurance (consumption does not respond at all to the income shock), while a value of one implies no insurance. The core of the empirical methodology is to identify these insurance parameters in the data from the following identities:

$$\phi = \frac{\text{Cov}(\Delta c_t, \Delta y_{t-1} + \Delta y_t + \Delta y_{t+1})}{\text{Cov}(\Delta y_t, \Delta y_{t-1} + \Delta y_t + \Delta y_{t+1})} \tag{1}$$

$$\psi = \frac{\text{Cov}(\Delta c_t, \Delta y_{t+1})}{\text{Cov}(\Delta y_t, \Delta y_{t+1})} \tag{2}$$

2.2. The model in continuous time with time aggregation

In this section, I show how time aggregation can significantly bias the partial insurance parameter estimates obtained by Eqs. (1) and (2). The model in this section will be the exact analog of the discrete time model just described, but embedded in continuous time where shocks a spread uniformly throughout the year.[7] The new ϕ and ψ estimates do not hinge on the use of continuous time, and similar estimates would be obtained by dividing the year into quarters or months.[8]

Time is continuous and one time unit represents one year. For the income process we will assume two underlying martingale processes, P_t and Q_t such that for all $s_1 > s_2 > s_3 > s_4 > 0$:

$$\text{Var}(P_{s_1} - P_{s_2}) = (s_1 - s_2)\sigma_P^2$$
$$\text{Cov}(P_{s_1} - P_{s_2}, P_{s_3} - P_{s_4}) = 0$$
$$P_s = 0 \quad \text{if } s < 0$$

and similarly for Q_t. Brownian motion fits these assumptions, but the slightly more general definition allows for jumps in the income process. Allowing for jumps accommodates low-frequency events, such changing job or getting a promotion, that may occur only once every few years, but when they do occur they can be at any point in the year. Instantaneous income in a period dt is given by[9]:

$$dy_t = P_t dt + dQ_t \tag{3}$$

that is they receive their permanent income flow ($P_t = \int_0^t dP_s$) multiplied by time dt in addition to a one-off transitory income dQ_t.

Keeping with the assumption that consumption is a random walk with insurance parameters ϕ and ψ, instantaneous consumption is given by:

$$dc_t = \phi P_t dt + \psi Q_t dt \tag{4}$$

that is, they consume a proportion ϕ of their permanent income and a proportion ψ of the cumulation of all the transitory income they have received in their lifetime ($Q_t = \int_0^t dQ_s$).

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[6] In this simplified model I assume insurance parameters are constant across both time and households, that the transitory component of income has no persistence, and that there are no taste shocks. These elements are reintroduced in Section 3 in which I show the quantitative effect of time aggregation.

[7] There is little formal evidence on the distribution of shocks throughout the year. While this assumption is unlikely to be strictly true, it is more reasonable than the implicit assumption of BPP that shocks all occur 1st January each year.

[8] The autocorrelation of a time aggregated random walk is 0.25 in continuous time, compared to 0.23 for a discrete quarterly model and almost indistinguishable from a discrete monthly model. The theoretical moments are however significantly more elegant in continuous time. See online appendix B1.

[9] A more formal treatment of how to relate this to the log income process is given in online appendix B1.

In the Panel Study of Income Dynamics (PSID) data, we observe the total income received over the previous calendar year at time T:

$$y_T^{obs} = \int_{T-1}^{T} dy_t$$

Consumption is measured by a survey at the beginning of the following calendar year, which I map to a snapshot of consumption exactly at the end of the calendar year[10]:

$$c_T^{obs} = \phi P_T + \psi Q_T \qquad (5)$$

The BPP method makes use of the changes in observable income and consumption, which in the time aggregated model relate to:

$$\Delta y_T^{obs} = \left(\int_{T-2}^{T-1} (s-(T-2)) dP_s + \int_{T-1}^{T} (T-s) dP_s \right)$$
$$+ \left(\int_{T-1}^{T} dQ_t - \int_{T-2}^{T-1} dQ_t \right) \qquad (6)$$

$$\Delta c_T^{obs} = \phi \int_{T-1}^{T} dP_s + \psi \int_{T-1}^{T} dQ_s \qquad (7)$$

We see that these observable income and consumption changes in Eqs. (1) and (2) recover the permanent, but not the transitory insurance parameter:

$$\frac{\text{Cov}(\Delta c_T^{obs}, \Delta y_{T-1}^{obs} + \Delta y_T^{obs} + \Delta y_{T+1}^{obs})}{\text{Cov}(\Delta y_T^{obs}, \Delta y_{T-1}^{obs} + \Delta y_T^{obs} + \Delta y_{T+1}^{obs})} = \phi \qquad (8)$$

$$\frac{\text{Cov}(\Delta c_T^{obs}, \Delta y_{T+1}^{obs})}{\text{Cov}(\Delta y_T^{obs}, \Delta y_{T+1}^{obs})} = \psi - \frac{(3\phi - \psi)\sigma_P^2}{6\sigma_Q^2 - \sigma_P^2} \qquad (9)$$

Indeed the transitory insurance coefficient bears little relation to the true value of ψ. For example, if permanent and transitory variances are equal, and households follow the permanent income hypothesis ($\phi = 1$, $\psi = 0$), the estimate for ψ using this method will be *negative* 0.6.

3. Revised BPP estimates

In this section, I repeat the BPP estimation procedure, but with the model moments coming from the continuous time model with time aggregated income. While the core identification in BPP is illustrated in Eqs. (1) and (2), the full estimation procedure minimizes the distance between all the observable covariances (Cov($\Delta y_T^{obs}, \Delta y_S^{obs}$), Cov($\Delta c_T^{obs}, \Delta c_S^{obs}$) and Cov($\Delta c_T^{obs}, \Delta y_S^{obs}$)) and their model implied equivalents.[11] The full set of these model implied moments for the continuous time model, extended to include time varying coefficients, transitory persistence and taste shocks, can be found in appendix A.A1 and online appendix B2.

Table 1 shows the estimates for the transitory and permanent insurance parameters, first using BPP's original method and then with time aggregation. As there is no equivalent to an MA(1) process in continuous time, I consider two alternative ways to introduce persistence in the transitory shock, as well as reporting

results assuming no persistence. First I assume a transitory shock provides a stream of income uniformly distributed over a short period of time (to be estimated). Second I assume the stream of income decays linearly over a short period.[12] The time aggregated results are not very sensitive to these assumptions.

The top row of Table 1 gives the main result showing the transitory insurance parameter increases from 0.05 in BPP to 0.24 with time aggregation. This new estimate is much more in line with the literature that estimates MPCs using natural experiments. Note that this higher estimate is incompatible with the assumption that consumption follows a random walk, at least if the household budget constraint holds. I have chosen to keep this assumption in this letter to isolate the role being played by time aggregation. Crawley and Kuchler (2020) and online appendix B5 extend the model to allow for short-lived consumption responses to transitory shocks.

The new estimate for the permanent insurance parameter is lower than before, around 0.35. This new puzzle is discussed next.

3.1. A new puzzle: Too much permanent insurance?

The low estimate for the permanent insurance parameter, ϕ, conflicts with both consumption theory and other empirical estimates of the consumption response to permanent income shocks.[13] Furthermore, Eq. (8) suggests time aggregation should not alter the permanent insurance estimate, at least in the model without transitory persistence.

I find the low estimate of ϕ to be a robust feature of the data, possibly a result of measurement error in consumption that is correlated with income. Indeed, the relation between income and consumption in the cross-sectional Consumer Expenditure Survey (CEX) is low, where the cross-section mostly represents permanent income differences.[14] Sabelhaus et al. (2014) find "the ratio of spending to income at low-income levels seems implausibly high, and the ratio of spending to income at the top seems implausibly low". This cross-sectional relation in the CEX data is carried over to the imputed PSID consumption data used in BPP, and is reflected in the low estimates for permanent insurance.

Furthermore, the high estimate of ϕ from BPP is not robust. For example, using only Eq. (8), rather than the full minimum distance in BPP, recovers an estimate for ϕ of 0.35–close to the time-aggregated estimate. Restricting the permanent variance to be non-time-varying, but otherwise replicating the minimum distance procedure of BPP, also recovers 0.35. The high estimate for ϕ from BPP appears to come from some interaction between time-aggregation, model misspecification, and time-varying risk. In contrast, the low estimate of ϕ obtained in the time-aggregated model is robust to time-varying risk.[15]

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[10] BPP use data on food consumption to impute total annual consumption. The questionnaire asks about food consumption in a typical week, but unfortunately the timing of this 'typical week' is not clear. The questionnaire is usually given at the end of March in the following year. See Altonji and Siow (1987) and Hall and Mishkin (1982) for differing views. In online appendix B4 I show that controlling for the interview date barely changes the results. However, in online appendix B3 I show that the timing of the 'typical' week can have a large effect on the results. This is an important drawback to using this method with the PSID data. In Crawley and Kuchler (2020) we use expenditure data imputed from Danish administrative records in which the timing of expenditure is very clearly defined.

[11] I follow the exact same diagonally weighted minimum distance procedure in BPP as described in their online appendix D of Blundell et al. (2008)

[12] See online appendix B2 for details.

[13] Standard buffer stock theory suggests ϕ should be close to 1. The literature on consumption responses to permanent shocks is much smaller than for transitory shocks, but tends to find estimates close to 1. See Gelman et al. (2016) and Crawley and Kuchler (2020) for examples.

[14] A simple regression of log nondurable consumption on log after-tax income returns a coefficient of 0.17 in the CEX. Using the imputed BPP data, a regression of 10-year change in log consumption on 10-year change in log income—again picking up predominantly permanent changes—recovers a coefficient of 0.23.

[15] A full understanding of the misspecification that generates the high ϕ estimate is beyond the scope of this letter. See online appendix B5 for an extension of the model that allows for exponentially decaying consumption responses to transitory shocks.

	BPP		Time Agg.		
Persistence type:	None	MA(1)	None	Uniform	Linear decay
ψ	0.0503	0.0501	0.2421	0.2510	0.2403
(Partial insurance tran. shock)	(0.0505)	(0.0430)	(0.0431)	(0.0428)	(0.0417)
ϕ	0.4692	0.6456	0.3384	0.3287	0.3516
(Partial insurance perm. shock)	(0.0598)	(0.0941)	(0.0471)	(0.0580)	(0.0627)

4. Conclusion

This letter highlights the importance of time aggregation when working with panel data, especially when analyzing the covariance matrix of income and consumption growth. It also resolves the dissonance between BPP's estimates of transitory income insurance and the natural experiment literature on marginal propensity to consume. Going forward, I hope the methods used here to correct for the time aggregation problem can be useful for researchers, especially as more and more high quality panel datasets on income and consumption become available.

Appendix A

A.1. Identification in the full model

In this appendix, I calculate the full set of identifying equations for the non-stationary model with measurement error in consumption and taste shocks. Online appendix B2 extends these to add persistence in the transitory shock.

I am interested in the full set of observable covariances:

$$\text{Cov}(\Delta y_T^{obs}, \Delta y_S^{obs})$$
$$\text{Cov}(\Delta c_T^{obs}, \Delta c_S^{obs})$$
$$\text{Cov}(\Delta c_T^{obs}, \Delta y_S^{obs})$$

for all T and S in $\{1, 2, \ldots\}$. I further make the assumption that while the variance of the permanent and transitory shocks and insurance coefficients can change from year to year, within each year these are constant. The variance the permanent shock in year T is $\sigma_{P,T}^2$ and the transitory shock $\sigma_{Q,T}^2$. I use Eq. (6) for the change in observable log income, and extend Eq. (7) for the change in observable log consumption to include taste shocks (ξ_t) and measurement error (u_T):

$$\Delta c_T^{obs} = \phi \int_{T-1}^T dP_s + \psi \int_{T-1}^T dQ_s + \int_{T-1}^T d\xi_s + u_T - u_{T-1}$$

These two equations allow for the calculation of all the required identification equations:

$$\text{Var}(\Delta y_T^{obs}) = \mathbb{E}\left(\int_{T-2}^{T-1} (s-(T-2))^2 dP_s dP_s \right.$$
$$\left. + \int_{T-1}^T (T-s)^2 dP_s dP_s \right)$$
$$+ \mathbb{E}\left(\int_{T-1}^T dQ_t dQ_t + \int_{T-2}^{T-1} dQ_t dQ_t \right)$$
$$= \frac{1}{3}\sigma_{P,T}^2 + \frac{1}{3}\sigma_{P,T-1}^2 + \sigma_{Q,T}^2 + \sigma_{Q,T-1}^2 \quad \text{(A.1)}$$

$$\text{Cov}(\Delta y_T^{obs}, \Delta y_{T+1}^{obs}) = \mathbb{E}\left(\int_{T-1}^T (T-s)(s-(T-1)) dP_s dP_s \right)$$
$$- \mathbb{E}\left(\int_{T-1}^T dQ_t dQ_t \right)$$
$$= \frac{1}{6}\sigma_{P,T}^2 - \sigma_{Q,T}^2$$

$$\text{Cov}(\Delta y_T^{obs}, \Delta y_{T-1}^{obs}) = \frac{1}{6}\sigma_{P,T-1}^2 - \sigma_{Q,T-1}^2$$

$$\text{Cov}(\Delta y_T^{obs}, \Delta y_S^{obs}) = 0 \quad \forall S, T \text{ such that } |S-T| > 1$$

$$\text{Var}\Delta c_T^{obs} = \phi^2 \mathbb{E}\left(\int_{T-1}^T dP_s dP_s \right) + \psi^2 \mathbb{E}\left(\int_{T-1}^T dQ_s dQ_s \right)$$
$$+ \mathbb{E}\left(\int_{T-1}^T d\xi_s d\xi_s \right) + \sigma_{u,T}^2 + \sigma_{u,T-1}^2$$
$$= \phi^2 \sigma_{P,T}^2 + \psi^2 \sigma_{Q,T}^2 + \sigma_{\xi,T}^2 + \sigma_{u,T}^2 + \sigma_{u,T-1}^2$$

$$\text{Cov}(\Delta c_T^{obs}, \Delta c_{T+1}^{obs}) = -\sigma_{u,T}^2$$
$$\text{Cov}(\Delta c_T^{obs}, \Delta c_{T-1}^{obs}) = -\sigma_{u,T-1}^2$$
$$\text{Cov}(\Delta c_T^{obs}, \Delta c_S^{obs}) = 0 \quad \forall S, T \text{ such that } |S-T| > 1$$

$$\text{Cov}(\Delta c_T^{obs}, \Delta y_T^{obs}) = \mathbb{E}\left(\phi_T \int_{T-1}^T (T-s) dP_s dP_s + \psi_T \int_{T-1}^T dQ_s dQ_s \right)$$
$$= \frac{1}{2}\phi_T \sigma_{P,T}^2 + \psi_T \sigma_{Q,T}^2$$

$$\text{Cov}(\Delta c_T^{obs}, \Delta y_{T+1}^{obs}) = \mathbb{E}\left(\phi_T \int_{T-1}^T (s-(T-1)) dP_s dP_s \right.$$
$$\left. - \psi_T \int_{T-1}^T dQ_s dQ_s \right)$$
$$= \frac{1}{2}\phi_T \sigma_{P,T}^2 - \psi_T \sigma_{Q,T}^2$$

$$\text{Cov}(\Delta c_T^{obs}, \Delta y_{T-1}^{obs}) = 0$$
$$\text{Cov}(\Delta c_T^{obs}, \Delta y_S^{obs}) = 0 \quad \forall S, T \text{ such that } |S-T| > 1$$

Appendix B. Supplementary data

Supplementary material related to this article can be found online at https://doi.org/10.1016/j.econlet.2020.108998.

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