How Do Agents Form Macroeconomic Expectations? Evidence from Inflation Uncertainty

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Roadmap

Motivations

FIRE benchmark v.s. data

Differentiating non-FIRE models

The role of stochastic volatility

Macroeconomic expectation formation

- Many competing models deviating from FIRE
 - Sticky expectations (SE)
 - Noisy information (NI)
 - Diagnostic expectations (DE)
 - ...

Macroeconomic expectation formation

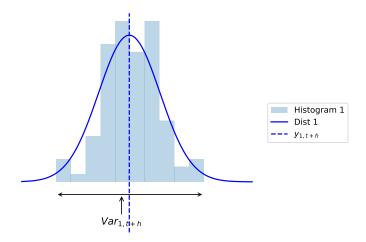
- Many competing models deviating from FIRE
 - Sticky expectations (SE)
 - Noisy information (NI)
 - Diagnostic expectations (DE)
 - ...
- Testing these models using survey expectations
 - e.g. (Coibion and Gorodnichenko, 2012)
 - Forecast errors (FE)
 - Disagreement (Disg)
 - This paper: +Uncertainty (Var)

Why uncertainty?

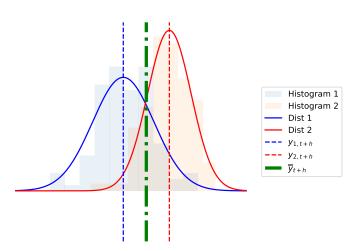
Uncertainty (or higher moments) matters for both

- individual economic decisions
 - precautionary saving motives
 - portfolio investments
 - mortgage choices
 - wage bargaining
- and aggregate outcomes
 - inflation dynamics
 - asset prices

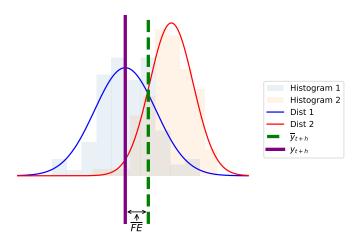
Density forecasts: an example



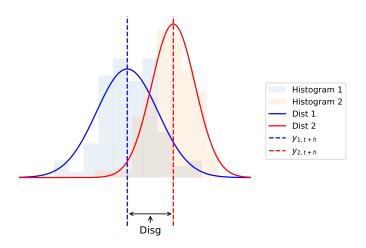
Average expectation



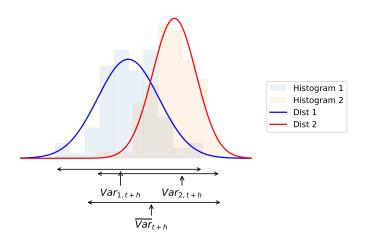
Average forecast errors (FE)



Disagreement (Disg)



Average uncertainty (Var)



Preview of the findings

- Competing theories have distinctive predictions about Var
 - Information rigidity \rightarrow ex-ante \overline{Var} > ex-post \overline{FE}^2
- Additional evidence
 - Uncertainty revision is inefficient
 - SE more robust than NI
 - State-dependence: inflation ↑ rigidity ↓
 - Coexisting with overreaction at the individual level
- Inflation contains persistent and transitory components

Literature

Studies on expectation formation using survey data

- Structural estimation: [Giacomini, Skreta, and Turen, 2020; Xie, 2023; Bordalo, Gennaioli, Ma, et al., 2020; Farmer, Nakamura, and Steinsson, 2021; Ryngaert, 2017]
- Others: [Mankiw, Reis, and Wolfers (2003), Carroll (2003), Branch (2004), Coibion and Gorodnichenko (2015)]

Measures of uncertainty: [Bachmann, Elstner, and E. R. Sims (2013), Jurado, Ludvigson, and Ng (2015), Rossi and Sekhposyan (2015), Binder (2017), Cascaldi-Garcia et al. (2023)]

 Differentiating Disg and Var: [Rich and Tracy (2010), D'Amico and Orphanides (2008), Abel et al. (2016), Glas (2020), and Rich and Tracy (2021)]

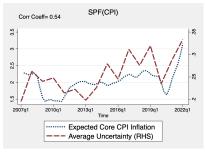
Eliciting probabilistic/density expectations [Manski (2004), Delavande, Giné, and McKenzie (2011), Manski (2018)]

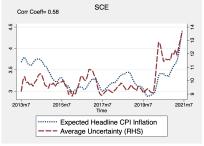
Data

Density forecast of inflation

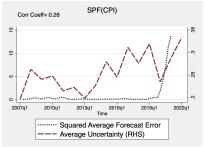
	SCE	SPF		
Time period	2013-2021M7	2007-2022Q2		
Frequency	Monthly	Quarterly		
Sample Size	1,300	30-50		
Density Variables	1 and 3-yr-ahead infla-	current-year and 1-		
	tion	yr-ahead q4/q4 Core		
		CPI and Core PCE in-		
		flation		
Survey Structure	fix-horizon	fix-event		
Panel Structure	unbalanced, stay up	unbalanced, average		
	to 12 months	stay for 5 years		
Individual Info	Education, Income,	Industry		
	Age, Location			

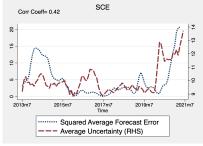
Expected inflation and uncertainty



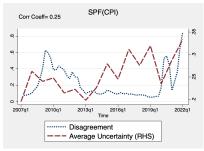


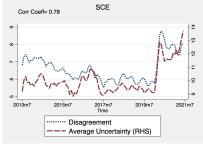
Forecast error and uncertainty





Disagreement and uncertainty





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FIRE predictions

Inflation process (AR1)

$$y_t = \rho y_{t-1} + \omega_t, \quad \omega_t \sim N(0, \sigma_\omega^2)$$

FIRE

$$\overline{FE}_{t+1|t}^* = -\omega_{t+1} \to \overline{FE}_{\bullet+1|\bullet}^{*2} = \sigma_{\omega}^2$$

$$\overline{\text{Var}}_{\bullet+1|\bullet}^* = \sigma_{\omega}^2$$

$$\overline{Disg}_{\bullet+1|\bullet}^* = 0$$

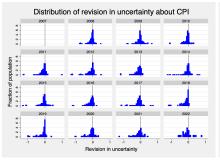
A first look at the data

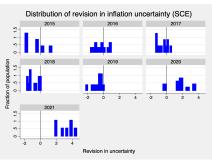
	SPF	SCE
InfAV	0	0
InfVar	0.219	1.282
InfATV	ATV 0.194 1.2	
FE	0.125	1.812
FEVar	0.136	0.935
Disg	0.161	2.805
Var	0.213	1.749

- Demeaned realized inflation and inflation expectations.
- Household fixed effects controlled.
- Before 2020.

Uncertainty revision

More certain when getting closer to realization?





Efficiency tests with uncertainty

Do revisions reflect only common resolution of uncertainty?

$$\mathsf{Var}_{i,t|t} - \mathsf{Var}_{i,t|t-1} = \alpha^{\mathsf{var}} + \underline{\beta}^{\mathsf{Var}}(\mathsf{Var}_{i,t-1|t-1} - \mathsf{Var}_{i,t-1|t-2}) + \psi_t^{var} + \zeta_{i,t}^{var}$$

- $\beta^{var} = 0$ under FIRE
- $\alpha^{var} < 0$ time-invariant uncertainty reduction
- ψ_t^{var} : time-varying innovations

Efficiency tests: professionals

	Mean revision	4q before	4q before	5q before
L4.InfExp_Var_rv		0.448***	0.456***	
		(0.056)	(0.058)	
L5.InfExp_Var_rv				0.440***
				(0.053)
Constant	-0.091***	-0.049***	-0.048***	-0.049***
	(0.000)	(800.0)	(0.005)	(0.005)
R2	0.047	0.196	0.248	0.249
Ν	1529	1157	1157	1021
Time FE	Yes	No	Yes	Yes

Taking stock

- Evidence rejecting FIRE
 - Inefficient revisions in Var
 - \blacksquare Disg > 0
 - $Var \neq \sigma_{\omega}^2 \neq FE^2$

Taking stock

- Evidence rejecting FIRE
 - Inefficient revisions in Var
 - \blacksquare Disg > 0
 - \blacksquare Var $\neq \sigma_{\omega}^2 \neq FE^2$
- Also, observed rankings help identify theories
 - SE> NI, DE, DENI \leftarrow Var > σ_{ω}^2 > FE²

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Sticky expectations (SE)

[Mankiw and Reis, 2002, Carroll, 2003, etc]

With an updating rate of λ (FIRE when $\lambda = 1$)

$$\begin{split} \overline{FE}_{t+1|t}^{se} &= (1-\lambda)\rho \overline{FE}_{t|t-1}^{se} - \lambda \omega_{t+1} \\ &\to \overline{FE}_{\bullet+1|\bullet}^{se2} = \frac{\lambda^2}{1-(1-\lambda)^2\rho^2} \sigma_\omega^2 \leq \overline{FE}_{\bullet+t|\bullet}^{*2} = \sigma_\omega^2 \\ \overline{\operatorname{Var}}_{\bullet+1|\bullet}^{se} &= \sum_{\tau=0}^{+\infty} \lambda (1-\lambda)^\tau \overline{\operatorname{Var}}_{t+1|t-\tau}^* = \frac{1}{1-(1-\lambda)\rho^2} \sigma_\omega^2 \geq \overline{\operatorname{Var}}_{\bullet+1|\bullet}^* = \sigma_\omega^2 \\ \overline{Disg}_{\bullet+1|\bullet}^{se} &\geq 0 \end{split}$$

Noisy information (NI)

[Lucas, 1972, Woodford, 2001, C. A. Sims, 2003 and Maćkowiak and Wiederholt, 2009, etc]

With noisiness of public and private signals σ_{pb}^2 and σ_{pr}^2

$$\begin{split} \overline{FE}_{t+1|t}^{ni} &= (1-PH)\rho\overline{FE}_{t|t-1}^{ni} + \rho P_{\epsilon}\epsilon_{t} + \overline{FE}_{t+1|t}^{*} \\ &\rightarrow \overline{FE}_{\bullet+1|\bullet}^{ni2} = \frac{\rho^{2}P_{\epsilon}^{2}\sigma_{pb}^{2} + \sigma_{\omega}^{2}}{(PH)^{2}} \geq \overline{FE}_{\bullet+1|\bullet}^{*2} = \sigma_{\omega}^{2} \\ \operatorname{Var}_{\bullet+1|\bullet}^{ni} &= \rho^{2}\operatorname{Var}_{\bullet|\bullet}^{ni} + \sigma_{\omega}^{2} \geq \operatorname{Var}_{\bullet+1|\bullet}^{*} = \sigma_{\omega}^{2} \\ \overline{Disg}_{\bullet+1|\bullet}^{ni} &= \frac{\rho^{2}P_{\xi}^{2}}{1 - (1-PH)^{2}\rho^{2}}\sigma_{pr}^{2} \geq 0 \end{split}$$

Kalman gain: $P = [P_{\epsilon}, P_{\xi}] = \overline{\mathrm{Var}}_{\bullet|\bullet-1}^{ni} H(H' \overline{\mathrm{Var}}_{\bullet|\bullet-1}^{ni} H + \Sigma^{v})^{-1}$

Diagnostic expectations (DE)

[Bordalo, Gennaioli, and Shleifer, 2018, Bordalo, Gennaioli, Ma, et al., 2020, etc]

With overreaction parameter $\hat{\theta}(>0)$ and dispersion σ_{θ}^2

$$\begin{split} &\overline{FE}_{t+1|t}^{de} = \overline{FE}_{t+1|t}^* - \hat{\boldsymbol{\theta}} \rho \mathrm{FE}_{t|t-1}^{de} \\ &\rightarrow \overline{FE}_{\bullet+1|\bullet}^{de2} = \frac{1}{1 + \hat{\boldsymbol{\theta}}^2 \rho^2} \sigma_\omega^2 \leq \overline{FE}_{\bullet+1|\bullet}^{*2} = \sigma_\omega^2 \\ &\overline{\mathrm{Var}}_{\bullet+1|\bullet}^{de} = \overline{Var}_{\bullet+1|\bullet}^* = \sigma_\omega^2 \\ &\overline{Disg}_{\bullet+1|\bullet}^{de} \geq 0 \end{split}$$

Table: Model-implied ranking of moments

Model	Predictions
FIRE	$\overline{Var}^* = \overline{FE}^{*2} = \sigma_\omega^2; \overline{Disg}^* = 0$

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FIRE	$\overline{Var}^* = \overline{FE}^{*2} = \sigma_\omega^2; \overline{Disg}^* = 0$
SE	$\overline{FE}^2 < \overline{FE}^{*2} = \overline{Var}^* = \sigma_\omega^2 < \overline{Var}; \overline{Disg} > 0$

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FIRE	$\overline{Var}^* = \overline{FE}^{*2} = \sigma_\omega^2; \overline{Disg}^* = 0$
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NI	$\overline{FE}^2 > \overline{FE}^{*2}; \overline{Var} > \overline{Var}^*; \overline{Disg} > 0$

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NI	$\overline{FE}^2 > \overline{FE}^{*2}; \overline{Var} > \overline{Var}^*; \overline{Disg} > 0$
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NI	$\overline{FE}^2 > \overline{FE}^{*2}; \overline{Var} > \overline{Var}^*; \overline{Disg} > 0$
DE	$\overline{FE}^2 < \overline{FE}^{*2} = \overline{Var}^* = \overline{Var}; \overline{Disg} > 0$
DENI	$\overline{FE}^2 > < \overline{FE}^{*2}, \overline{Var} > \overline{Var}^*, \overline{Disg} > 0$

Structural Estimation: SMM

$$\widehat{\Omega}^o = \underset{\{\Omega^o \in \Gamma^o\}}{argmin} (M_{\text{data}} - F^o(\Omega^o, H)) W(M_{\text{data}} - F^o(\Omega^o, H))'$$

- $o \in \{se, ni, de, deni\} \times \{ar, sv\}$
- Γ^o : parameter space
- H: real-time historical realizations
- W: weighting matrix

Model estimates for professionals

SE as an example

SE					
Moments Used 2-Step Estimate					
	$\hat{\lambda}$	ρ	σ_{ω}		
FE	0.36	0.99	0.23		
FE+Disg	0.28	0.99	0.23		
FE+Disg+Var	0.26	0.99	0.23		

Evidence for subjective models

[Jain, 2019, Macaulay and Moberly, 2022, Farmer, Nakamura, and Steinsson, 2021]

SE						
Moments Used	2-Step Estimate		Joint	te		
	$\hat{\lambda}$	ρ	σ_{ω}	$\hat{\lambda}$	ρ	σ_{ω}
FE	0.36	0.99	0.23	0.18	0.97	0.11
FE+Disg	0.28	0.99	0.23	0.22	0.95	0.14
FE+Disg+Var	0.26	0.99	0.23	0.32	0.9	0.22

NI requires highly noisy signals

NI								
Moments Used	2-Ste	2-Step Estimate Joint Estimate						
	$\hat{\sigma}_{\epsilon}$	$\hat{\sigma}_{\xi}$	ρ	σ_{ω}	$\hat{\sigma}_{\epsilon}$	$\hat{\sigma}_{\xi}$	ρ	σ_{ω}
FE	0	0.87	0.99	0.23	0	0.15	0.97	0.11
FE+Disg	1.5	2.26	0.99	0.23	1.48	2.33	0.97	0.11
FE+Disg+Var	2.64	3	0.99	0.23	3	3	0.94	0.16

Patterns of households

Sticky, underreactive and widely dispersed

SE					
Moments Used	nts Used 2-Step Estimate				
	$\hat{\lambda}$	$\hat{\lambda}$ $ ho$ σ_{ω}			
FE	0.36	0.98	0.45		
FE+Disg	0.36	0.98	0.45		
FE+Disg+Var	0.36	0.98	0.45		
NI					
Moments Used	2-Step Estimate				
	$\hat{\sigma}_{\epsilon}$	$\hat{\sigma}_{\xi}$	ρ	σ_{ω}	
FE	0	1	0.98	0.45	
FE+Disg	3	1.18	0.98	0.45	
FE+Disg+Var	2.06	3	0.98	0.45	
DENI					
Moments Used	2-Step Estimate				
	$\hat{ heta}$	$\hat{\sigma}_{\xi}$	ρ	σ_{ω}	
FE	N/A	N/A	0.98	0.45	
FE+Disg	-0.54	3	0.98	0.45	
FE+Disg+Var	-0.35	2.43	0.98	0.45	

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The role of stochastic volatility

Stochastic volatility (SV)

[Stock and Watson, 2007]

Process of inflation

Permanent component Transitory
$$y_t = \overbrace{\zeta_t} + \overbrace{\eta_t}$$

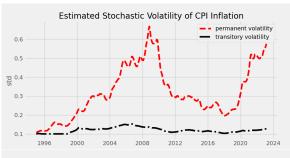
$$\zeta_t = \zeta_{t-1} + z_t$$

$$z_t = \sigma_{z,t} \xi_{z,t}, \quad \eta_t = \sigma_{\eta,t} \xi_{\eta,t}, \quad \xi_t = [\xi_{\eta,t}, \xi_{\epsilon,t}] \sim N(0,I)$$

$$\log \sigma_{\eta,t}^2 = \log \sigma_{\eta,t-1}^2 + \mu_{\eta,t}, \qquad \log \sigma_{z,t}^2 = \log \sigma_{z,t-1}^2 + \mu_{z,t}$$

$$\mu_t = [\mu_{\eta,t}, \mu_{z,t}]' \sim N(0,\gamma I)$$

Estimated SV





More sensible est of NI for professionals

Before March 2020			Till March 2023	
SE				
Moments Used	2-Step Estimate		2-Step Estimate	
	$\hat{\lambda}$		$\hat{\lambda}$	
FE	0.2		0.3	
FE+Disg	0.25		0.36	
FE+Disg+Var	0.36		0.36	
NI				
Moments Used	2-Step Estimate		2-Step Estimate	
	$\hat{\sigma}_{pb}$	$\hat{\sigma}_{pr}$	$\hat{\sigma}_{pb}$	$\hat{\sigma}_{pr}$
FE	0.68	0.24	2.3	3
FE+Disg	0.67	0.24	2.3	3
FE+Disg+Var	0.64	0.21	2.3	3

NI remains a poor fit of households

Before March 2020			Till March 2023		
SE	SE				
Moments Used	2-Step Estimate		2-Step Estimate		
	$\hat{\lambda}$		$\hat{\lambda}$		
FE	0.27		0.36		
FE+Disg	0.2		0.27		
FE+Disg+Var	0.26		0.26		
NI					
Moments Used	2-Step Estimate		2-Step Estimate		
	$\hat{\sigma}_{\epsilon}$	$\hat{\sigma}_{\xi}$	$\hat{\sigma}_{\epsilon}$	$\hat{\sigma}_{\xi}$	
FE	N/A	N/A	N/A	N/A	
FE+Disg	N/A	N/A	N/A	N/A	
FE+Disg+Var	N/A	N/A	N/A	N/A	

Higher inflation, less rigidity

[Coibion and Gorodnichenko, 2015, Weber et al., 2023]

Before March 20	20		Till March 2023		
SE					
Moments Used	2-Step Estimate		2-Step Estimate		
	$\hat{\lambda}$		$\hat{\lambda}$		
FE	0.27		0.36		
FE+Disg	0.2		0.27		
FE+Disg+Var	0.26		0.26		
DENI					
Moments Used	2-Step Estimate		2-Step Estimate		
	$\hat{ heta}$	$\hat{\sigma}_{\xi}$	$\hat{ heta}$	$\hat{\sigma}_{\xi}$	
FE	-0.48	0.64	0.43	0.26	
FE+Disg	-0.48	0.64	0.43	0.26	
FE+Disg+Var	-0.48	0.64	0.43	0.26	
	·		·		

Scoring card of model robustness

Criteria	SE	NI	DE	DENI
Sensitive to moments used for estimation?		Yes	Yes	No
Sensitive to the assumed process?		Yes	Yes	No
Sensitive to two-step or joint estimate?		No	No	Yes
Sensitive to the type of agents?		Yes	Yes	Yes

• But no single model explains all aspects of survey expectations

Conclusion
 Belief is not just expectations, but also second or higher moments

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