1. Study the given class A below, which uses the methods incr and decr to imitate slow computations.

```
1
    class A {
2
     private final int x;
3
     A() {
4
5
       this(0);
6
7
8
     private A(int x) {
9
       this.x = x;
10
11
12
     void sleep() {
        System.out.println(Thread.currentThread().getName() + " " + x);
13
14
        try {
15
          Thread.sleep(1000);
16
       } catch (InterruptedException e) {
          System.out.println("interrupted");
17
        }
18
      }
19
20
21
      A incr() {
22
       sleep();
23
       return new A(this.x + 1);
24
25
26
     A decr() {
       sleep();
27
28
       if (x < 0) {
29
         throw new IllegalStateException();
30
31
       return new A(this.x - 1);
32
33
     @Override
      public String toString() {
       return "" + x;
36
37
   }
38
     (a) Suppose we have a method
       static A foo(A a) {
     1
```

```
2
   return a.incr().decr();
3
```

Convert the method foo above to a method that returns CompletableFuture so that the body of the method is executed asynchronously. Try different variations by using:

- i. supplyAsync only
- ii. supplyAsync and thenApply
- iii. supplyAsync and thenApplyAsync

Demonstrate how you would retrieve the result of the computation.

See also: thenRun, thenAccept, runAsync

```
Suggested Guide:
      i. Possible code
        static CompletableFuture <A> foo(A a) {
          return CompletableFuture.supplyAsync(
    3
                    () -> a.incr().decr()
    4
                  );
    5
       }
     ii. Possible code
        // Same as above
        static CompletableFuture < A > foo(A a) {
         return CompletableFuture.supplyAsync(() -> a.incr())
    4
                    .thenApply(x -> x.decr());
    5
        }
    iii. Possible code
        // decr() could be run in another thread
        static CompletableFuture <A> foo(A a) {
    3
          return CompletableFuture.supplyAsync(() -> a.incr())
    4
                    .thenApplyAsync(x -> x.decr());
    5
        }
   To wait for the result,
   CompletableFuture <A> a = foo(new A());
1
2
   // do something else
3
   a.join();
```

(b) Suppose now we have another method

```
1 static A bar(A a) {
2 return a.incr();
3 }
```

which we would like to invoke using bar(foo(new A())). Convert the computation within bar to run asynchronously as well. bar should now return a CompletableFuture. In addition, show the equivalent of calling bar(foo(new A())) in an asynchronous fashion, using the method thenCompose.

See also: thenCombine

```
Suggested Guide:

static CompletableFuture < A > bar(A a) {
   return CompletableFuture.supplyAsync(() -> a.incr());
}
```

```
CompletableFuture <A> b =
foo(new A()).thenCompose(x -> bar(x));
System.out.println(b.join());
```

(c) Suppose now we have yet another method

```
1  static A baz(A a, int x) {
2   if (x == 0) {
3     return new A();
4  } else {
5     return a.incr().decr();
6  }
7  }
```

Convert the computation within baz in the else clause to run asynchronously. baz should now return a CompletableFuture. You may find the method completedFuture useful.

```
Suggested Guide:
    static CompletableFuture <A> baz(A a, int x) {
1
2
      if (x == 0) {
3
        return CompletableFuture.completedFuture(new A());
      } else {
4
5
        return CompletableFuture.supplyAsync(
6
                   () -> a.incr().decr()
7
                );
8
      }
    }
9
10
11
    CompletableFuture <A> c = baz1(new A(), 1);
12
    System.out.println(c.join());
    Now that CompletableFuture is a monad:
       • completedFuture is equivalent to of
       • thenCompose is flatMap, and
       • thenApply is map
```

(d) Let's now call foo, bar, and baz asynchronously. We would like to output the string "done!" when *all* three method calls are complete. Show how you can use the allOf() method to achieve this behaviour.

See also: anyOf, runAfterBoth, runAfterEither

(e) Calling new A().decr() would cause an exception to be thrown, even when it is done asynchronously. Show how you would use the handle() method to gracefully handle exceptions thrown (e.g., such as printing them out) within a chain of CompletableFuture calls.

See also: when Complete, exceptionally

```
Suggested Guide:
    CompletableFuture <A> exc = CompletableFuture
1
2
        .supplyAsync(() -> new A().decr().decr())
        .handle((result, exception) -> {
3
          if (exception != null) {
4
          System.out.println("ERROR: " + exception);
5
6
            return new A();
7
          } else {
8
            return result;
9
          }
10
        });
11
12
    System.out.println(exc.join());
```

2. Modify the following sequences of code such that f, g, h, and i are now invoked asynchronously, via CompletableFuture. Assume that a has been initialized as

```
(a) Problem #A

1  B b = f(a);
2  C c = g(b);
3  D d = h(c);
```

A = new A();

```
(b) Problem #B

1    B b = f(a);
2    C c = g(b);
3    h(c); // no return value
```

```
(c) Problem #C

1  B b = f(a);
2  C c = g(b);
3  D d = h(b);
4  E e = i(c, d);
```

```
Suggested Guide:
   CompletableFuture <B> cfb = CompletableFuture
1
       .supplyAsync(() -> f(a));
2
3
   CompletableFuture <C> cfc = cfb
       .thenApply(b -> g(b));
4
5
   CompletableFuture <D> cfd = cfb
6
       .thenApply(b -> h(b));
7
   CompletableFuture <E> cfe = cfc
8
       .thenCombine(cfd, (c, d) -> i(c, d));
9
   cfe.join();
```

3. Run the following program and observe which worker is running which task.

```
1
    class B {
 2
      static class Task extends RecursiveTask<Integer> {
3
        int count:
4
        Task(int count) {
5
6
          this.count = count;
7
        }
9
        public Integer compute() {
          System.out.println(Thread.currentThread().getName()
10
                              + " " + this.count);
11
12
          if (this.count == 4) {
13
            return this.count;
14
15
          Task t = new Task(this.count + 1);
16
          t.fork();
17
          return t.join();
        }
18
      }
19
20
21
      public static void main(String[] args) {
22
        ForkJoinPool.commonPool().invoke(new Task(0));
      }
23
    }
24
```

Suppose the program is invoked with a maximum of three additional workers. What can you observe about the behaviour of a worker when the task that it is running blocks at the call to join?

Suggested Guide:

You should observe that there exists a worker running Task i that also picks up Task j (j > i). Since Task i blocks at join(), this means that the worker does not sit idling waiting at join() but puts the blocking task aside and picks up (i.e., steals) another task to execute.

4. Given below is the classic recursive method to obtain the nth term of the Fibonacci sequence 0, 1, 1, 2, 3, 5, 8, 13, 21, . . . without memoization

```
1  static int fib(int n) {
2    if (n <= 1) {
3       return n;
4    } else {
5       return fib(n - 1) + fib(n - 2);
6    }
7  }</pre>
```

(a) Parallelize the above implementation by transforming the above to a recursive task and inherit from java.util.concurrent.RecursiveTask.

```
Suggested Guide:
1
    import java.util.concurrent.RecursiveTask;
2
    class Fib extends RecursiveTask<Integer> {
3
      final int n;
4
5
      Fib(int n) {
6
        this.n = n;
8
9
      @Override
10
      protected Integer compute() {
11
        if (n <= 1) {
12
          return n;
13
        Fib f1 = new Fib(n - 1);
14
15
        Fib f2 = new Fib(n - 2);
16
        // try different variants here...
17
      }
    }
18
```

(b) Explore different variants and combinations of fork, join, and compute invocations.

Suggested Guide:

```
i. Variant #1
f1.fork();
return f2.compute() + f1.join();
```

This is the same as lecture example.

```
ii. Variant #2
1   f1.fork();
2   return f2.join() + f1.compute();
```

This works, but slow, since in Java subexpressions are evaluated left to right (i.e., for A + B, A is evaluated first before B, by the away this has nothing to do with associativity). So f1.join() needs to wait for f1.fork() to complete before f2.compute() can be evaluated. Compare this with 4(b)i where f2.compute() proceeds while f1.fork() is running.

```
iii. Variant #3
1  return f1.compute() + f2.compute();
```

This is *sequentially recursive*. Not much different from 4(b)ii, but still slightly faster as there is no overhead involved in forking and joining. Everything is done by the main thread.

```
iv. Variant #4

1   f1.fork();
2   f2.fork();
3   return f2.join() + f1.join();
```

Apart from the first recursion, main thread delegates all other work to worker threads in the common pool.

```
v. Variant #5

1    f1.fork();
2    f2.fork();
3    return f1.join() + f2.join();
```

Looks the same as 4(b)iv, but 4(b)iv still preferred as it follows the convention of joins to be returned innermost first. Since a thread forks tasks to the front of its own double-ended queue, the last task forked should be the one that is joined when the thread becomes idle; tasks at the back of the dequeue are stolen by other idle worker threads.

vi. Other non-functional combinations

A fork() must be followed by a join() to get the result back. None of the options that uses fork also join back the result. The only option that gives us the correct result is A. Note that it computes the Fibonacci number *sequentially*.

You can use the version on the next page to test the performance.

```
import java.util.concurrent.RecursiveTask;
2
    import java.time.Instant;
   import java.time.Duration;
3
4
5
   class Fib extends RecursiveTask<Integer> {
6
     final int n;
7
8
     Fib(int n) {
9
       this.n = n;
10
11
12
     private void waitOneSec() {
       try {
13
14
          Thread.sleep(1000);
15
        } catch (InterruptedException e) { }
      }
16
17
18
     @Override
19
      protected Integer compute() {
20
        System.out.println(Thread.currentThread().getName()
        + " : " + n);
21
        waitOneSec();
22
23
        if (n <= 1) {
24
          return n;
25
26
27
        Fib f1 = new Fib(n - 1);
28
        Fib f2 = new Fib(n - 2);
29
30
        // try different variants here...
      }
31
32
33
      public static void main(String[] args) {
        Instant start = Instant.now();
34
35
        System.out.println(new Fib(5).compute());
36
        Instant end = Instant.now();
37
38
        System.out.println(Duration.between(start, end).
       toMillis());
39
      }
   }
40
```