

# Behaviour of the system analysis



## POWER SYSTEM ANALYSIS

- Analysis on transmission + gen level (balanced)
- Transmission system  $\rightarrow$  is not fairly balanced
  - ↳ whereas distribution system is unbalanced (consumer depended)
- 3Ø analysis possible
- When 1Ø analysis is possible, system is balanced & 1Ø can also give analysis of other 2Ø is possible with  $120^\circ$  rotation.
- Positive sequence  $\rightarrow$  balanced system

$120^\circ$  anti-clockwise rotation.

### Three steps

Network modelling  
(Electrical modelling)

Mathematical modelling

form equations  
(Algebraic)+(Diff)

solution.

solving the  
equations

↳ short / medium  $\rightarrow$  lumped system.

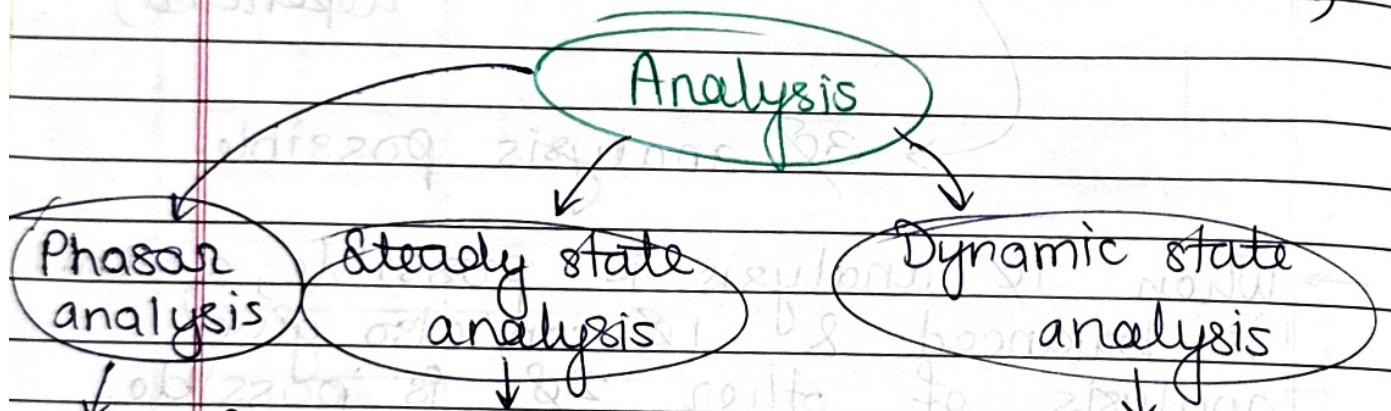
DATE

condition

→ Power system has 2 states

steady      Dynamic

single frequency      (parameters don't change with time)      (system parameters change with time)



But in AC, the magnitude of voltage cannot remain constant.

$$V_m \sin \omega t = V_m \sin(\omega t + T)$$

So, when single freq. is maintained, without harmonics & distortion, the AC system is in steady state.

Here, eqn are differential in math modelling

PS stability analysis

Power flow analysis

Economic dispatch

generation & voltage control

EN → linear system → superposition is applicable



→ Algebraic eqn

Differential eqn

Linear

non-linear

linear

non-linear

order is 1

trigo

func, ar  
have non  
iterative  
solution.  
(one-step)

func, ar  
order > 1



Source

Power

sink

Delivery

(load side)

Power source

generator

99% is inductive load

(everything is a load for generator)

Q) What happens when freq changes?

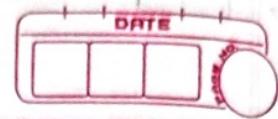
→ The  $B$ ,  $L$ ,  $C$  parameters (reactive part) will change

The voltage at each bus should be

1 pu & freq is 50Hz (within  $\pm 5\%$ ) voltage

( $\pm 1\%$ ) ↴ (good of PS engineer)

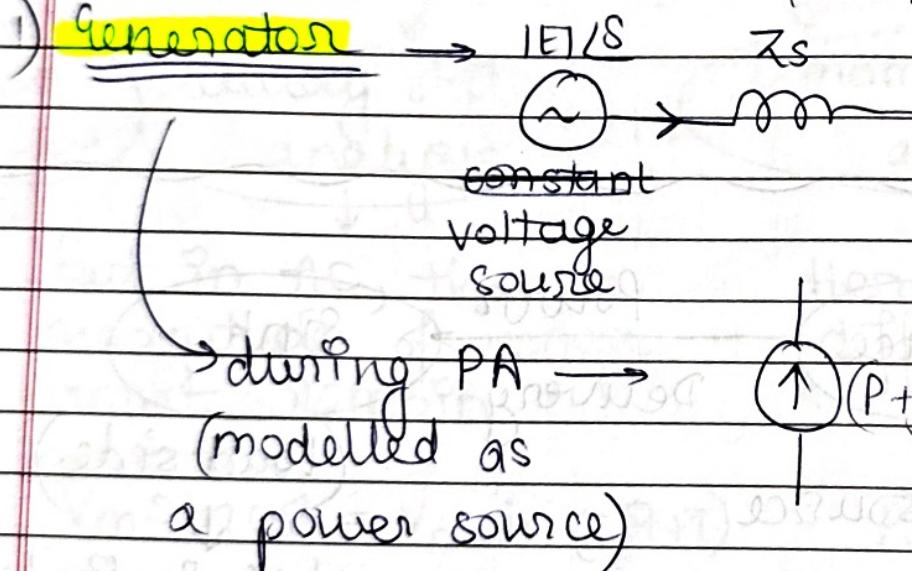
~~A~~ PSA is always done in per unit.



- 1) When freq. changes, T de of the machine depends of on freq (induction machine) so it can cause harm.  
∴ balancing the freq is important.  
↳ so that load performance isn't affected.

## ★ Electrical modelling

### 1) Generator



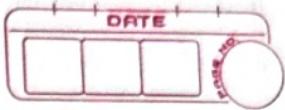
### 2) Transformer → $\frac{mm}{Z \text{ p.u.}}$ (modelled as a series impedance)

because  $Z$  doesn't change in p.u.

### 3) Transmission line (T-model)

med (nominal) long (equivalent)

Always modelled as a  
T-model because  
nodes are less.



(sm short line) → series impedance

y) Load

$$S = \frac{V^2}{Z} \rightarrow S \propto V^2$$

a) constant impedance ( $Z$ )

b) constant current ( $I$ ) →  $S = VI^*$  →  $S \propto V$   
(practically not possible)

ZIP model  
(combined) c) constant power ( $P$ ) →  $S$

→ Synchronous machine → terminal voltage  $|V_t|$   
control

↓  
change real power  
↓ and freq.

controlling the  
PM

by controlling  
excitation

OR

generation

Q) Why is generator modelled as power

→  $|V_t|$  can remain constant irrespective  
of the load by changing the ~~several~~  
excitation

so if  $|V_t|$  is constant

impedance ( $Z_s$ ) doesn't  
matter that's why

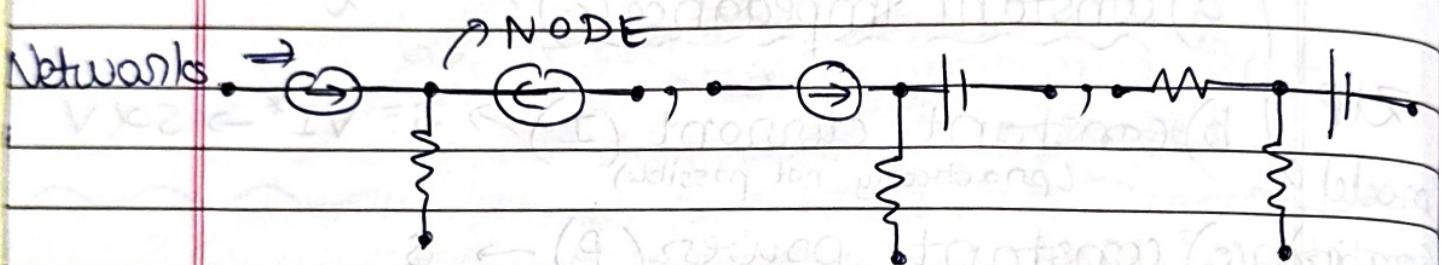
modelled as a

**POWER SOURCE**

# GRAPH THEORY

→ Network's graphical representation

↳ shows the structure of the electrical network



→ Two components in a network →  
1) active  
2) passive

→ Node → Where components are connected

→ Node = represented as a dot (•)

Component = represented as a branch / (-) edge

representation

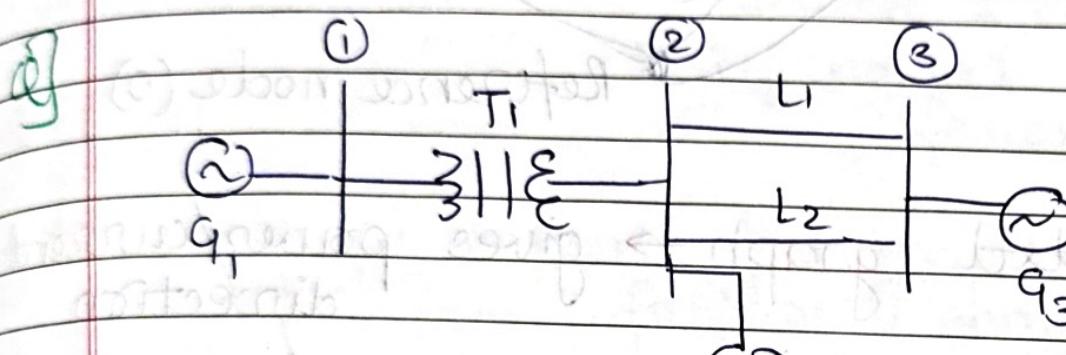
→ KCL & KVL is applicable in the network irrespective of the component connected.

\* SLD → pu. diagram → graph \*

~~A~~ Ohm's law  $\rightarrow$  current is directly proportional to the voltage and  $R$  is constant

$$V \propto I R$$

\* Directed graph  $\rightarrow$  where the branches have directions defined.



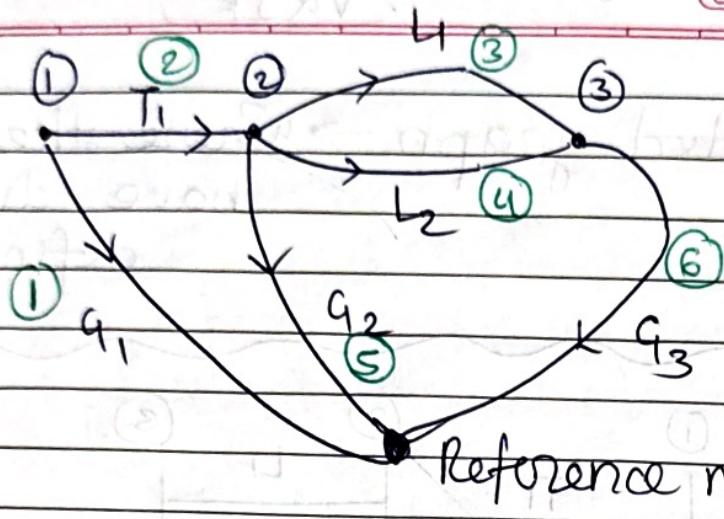
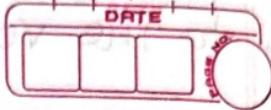
Draw the graph of the SLD.

- Here, components are 1) Active -  $g_1, g_2, g_3$   
2) Passive - Line,  $L_1, L_2, T_1$
- \* Power delivery  $\rightarrow$  lines, transformer, capacitor bank  
\* Power consumption  $\rightarrow$  generators, etc.

- 1] Buses are nodes represented by dot
  - 2] There is always a ground node (not shown in SLD but there is)
  - 3] Generators are grounded together
- ↓  
REMEMBER IN GRAPH.



graph is linear till machine/sink  
is not SATURATED.



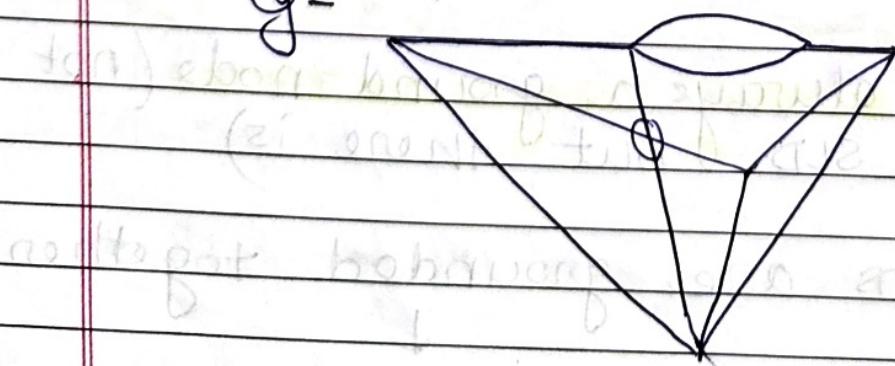
\* Oriented graph  $\rightarrow$  gives power/current direction

i) Current moves from higher to lower potential.

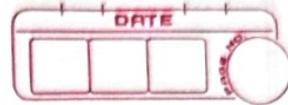
\* Planar graph  $\rightarrow$  linear in nature  
(no criss-cross)  
of line segments

\* Non-planar graph  $\rightarrow$  non-linear eq<sup>n</sup>  
in nature

$\hookrightarrow$  line segments overlap.  
eg -



Rank of matrix  $\rightarrow$  eq. no. of linearly independent eqn (col on rows)



\* Rank of a graph  $\rightarrow$  If there are 'n' nodes in the graph, the rank of the graph = ' $n-1$ '

because 1 eq<sup>n</sup> is dependant due to reference node

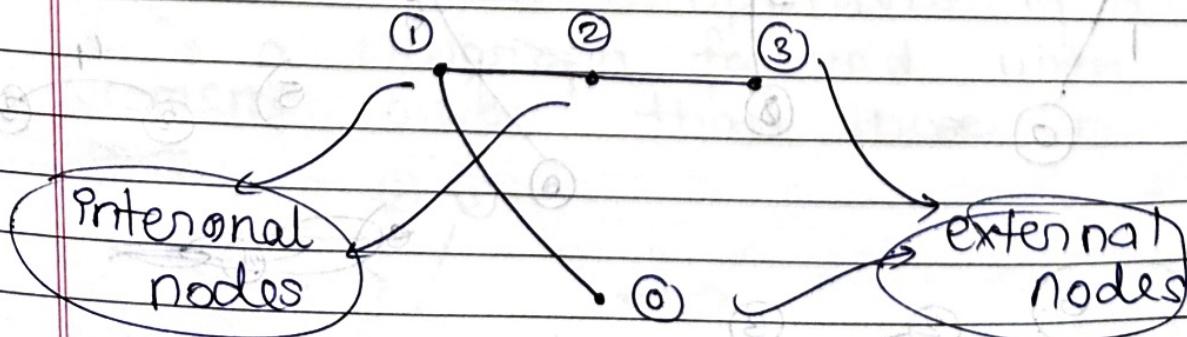
\* Sub-graph  $\rightarrow$  part of a graph take for further analysis

subset of a graph.)

take equivalent of neighbouring grids and then perform analysis on one subset.

\* Path  $\rightarrow$  A path is a subgraph of connected elements with not more than two elements are connected at the internal node

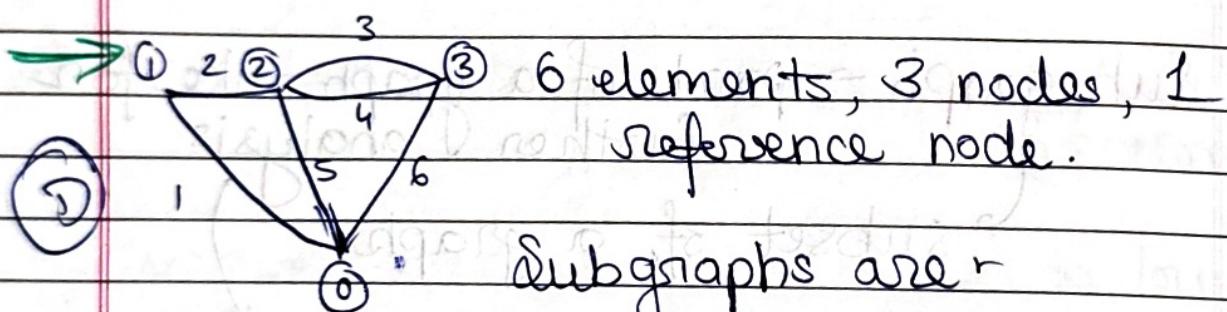
However, at the 2 terminal nodes, only one element is connected.



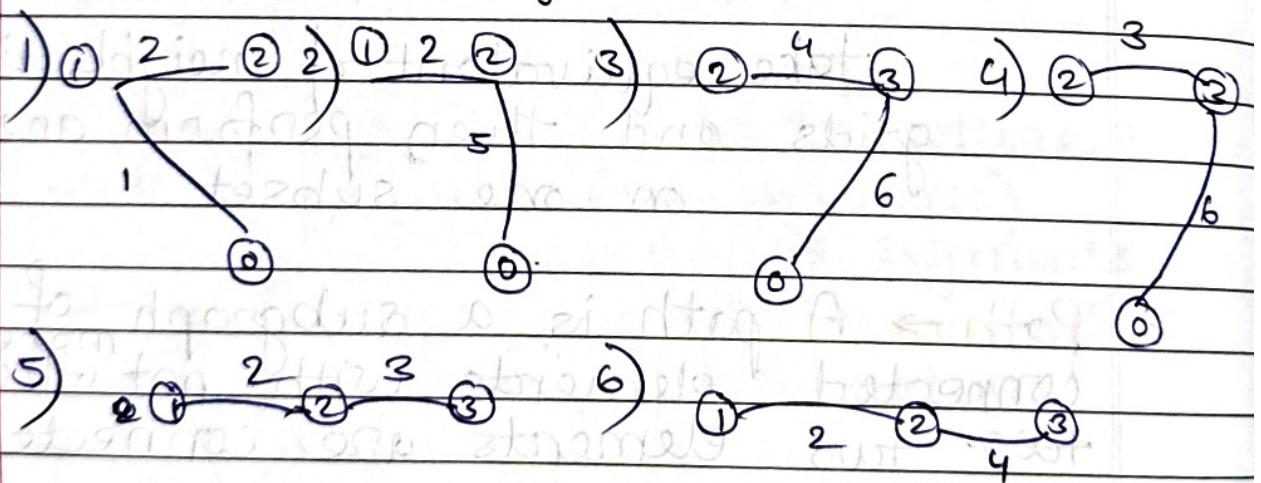
The internal nodes only to be connected by 2 out of the 6 elements

g) make paths & subgraphs of the previous question.

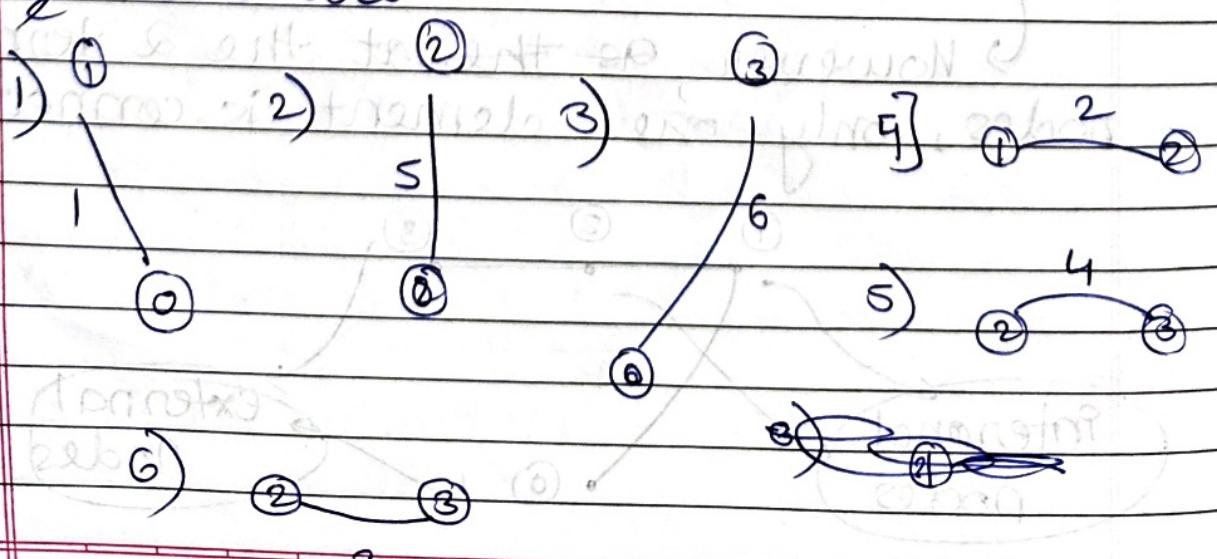
elements are no numbered.



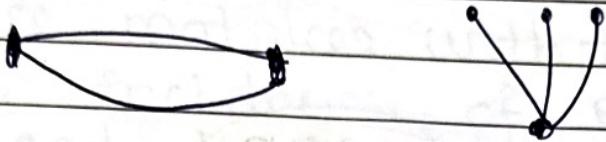
Subgraphs are -



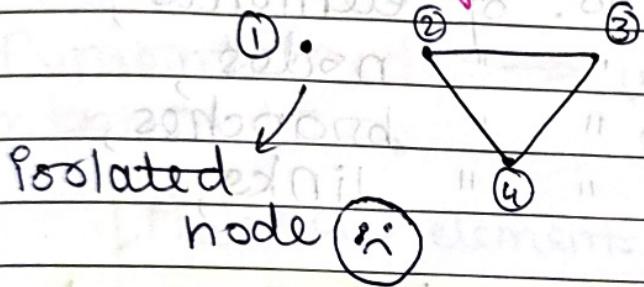
Paths are -



Connected graph  $\rightarrow$  graph or subgraph is said to be connected where there exist atleast one path b/w any two nodes.

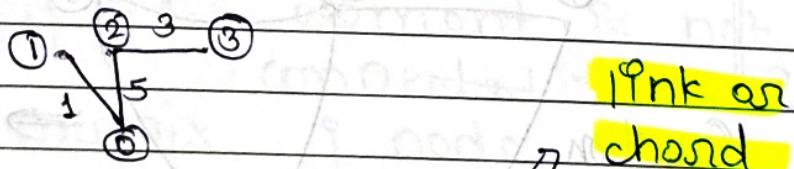


\* Non-connected graph  $\rightarrow$  self explanatory.



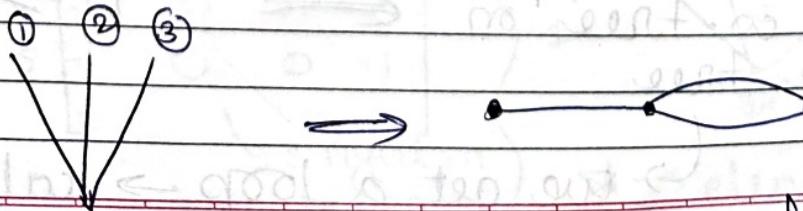
\* Tree  $\rightarrow$

A Tree is a connected subgraph having all the nodes of a graph without any closed loop. That subgraph is a Tree.



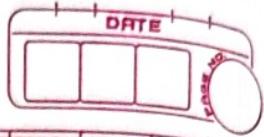
The elements of trees are branch or twig.

\* Co-tree  $\rightarrow$  ~~complement~~ complement of a tree & is a subgraph formed with the elements other than those in the tree.



elements of

★ tree has all nodes but doesn't form a loop.



★ Link/chord of co-tree  $\rightarrow$  connects with tree  
forms a closed loop.

### MATHS

Let  $e$  = total no. of elements,

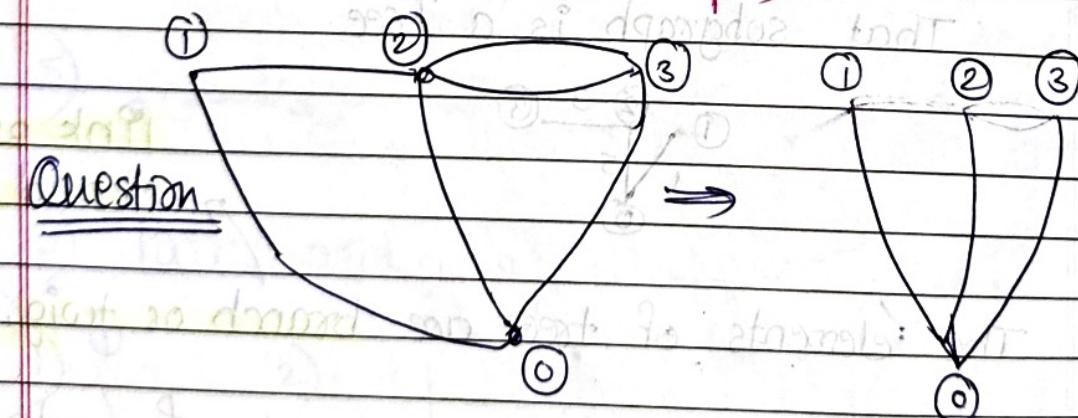
$n$  = " " " nodes

$b$  = " " " branches,

$l$  = " " " " links

$$b = n - 1, \quad l = e - b = e - n + 1$$

★ Basics of fundamental loops (f loops)



When we place the co-tree on the tree

we get a loop  $\rightarrow$  called basic loop

\* Incidence matrices → Every element of a graph is incident bet' any two nodes

↳ Incidence matrices with the info about the incidence of elements to nodes and their orientation. ↳ or direction.

i] Element node → Which element is incident matrices. connected to which node

$[A]$  →  $a_{ij}$  elements

$a_{ij} = 1 \rightarrow$  if the element is a is connected to  $i$  and  $j$  node

$a_{ij} = 0 \rightarrow$  if the element is not connected to  $i$  &  $j$  node

Q) Form an matrix for node

$j$  = nodes

	0	1	2	3
0	+1	0	0	
1	0	+1	-1	0
2	0	0	+1	-1
3	0	0	+1	-1
4	-1	0	+1	0
5	-1	0	0	+1

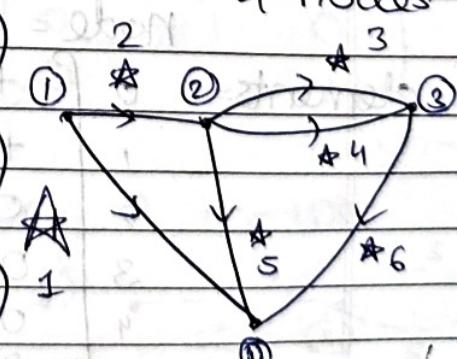
Element 1

connected to 1 and 0

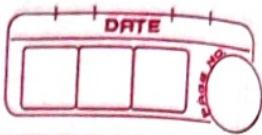
singular matrix

\* → elements

o) 6 elements, 4 nodes



Incident matrix is  
only formed for  
oriented matrix



✓

Sign convention  $\rightarrow$  If the  $i$ th element  
is incident to  $j$ th node  
and oriented tow away from  
 $j$ th node, put +ve and vice  
versa  
 $\rightarrow$  higher potential  $\rightarrow$  +ve  
lower potential  $\rightarrow$  -ve

$\rightarrow$  Observations  $\rightarrow$  i) sum of elements in  
a row is zero.

2) Bus Incidence matrix [A]

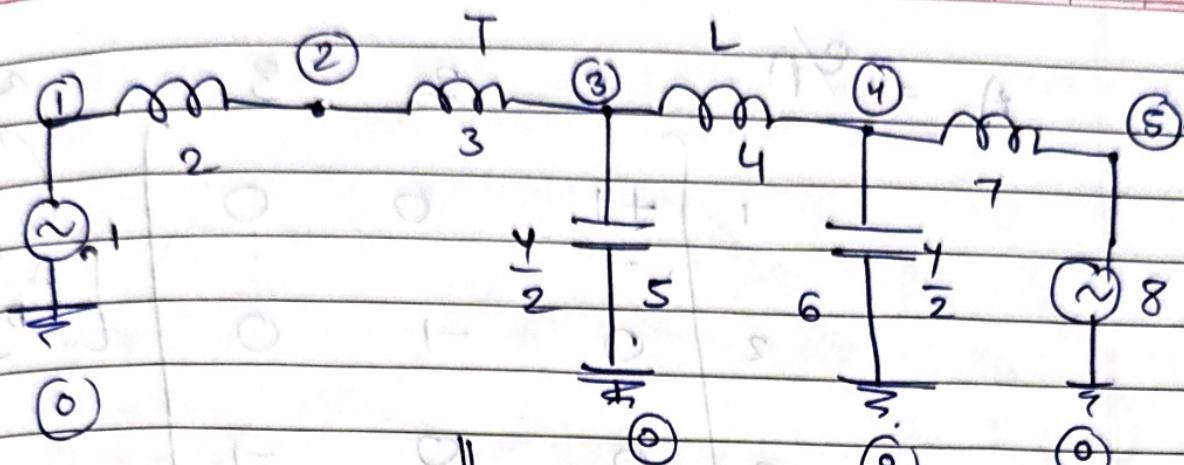
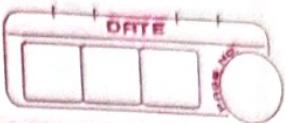
$\hookrightarrow$  Obtained from the e-n  
matrix by eliminating the column  
corresponding to the reference  
node.

$\hookrightarrow$  Remove the 0th node column

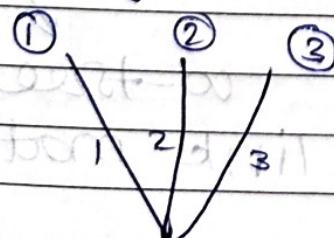
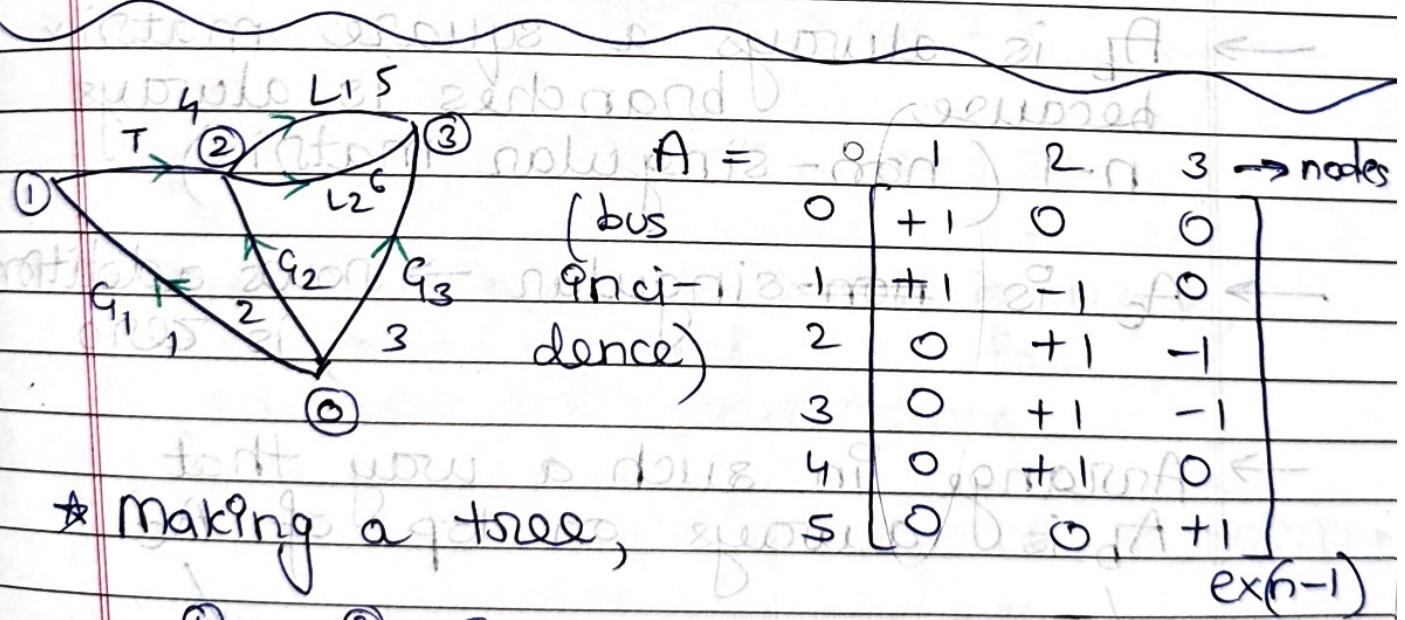
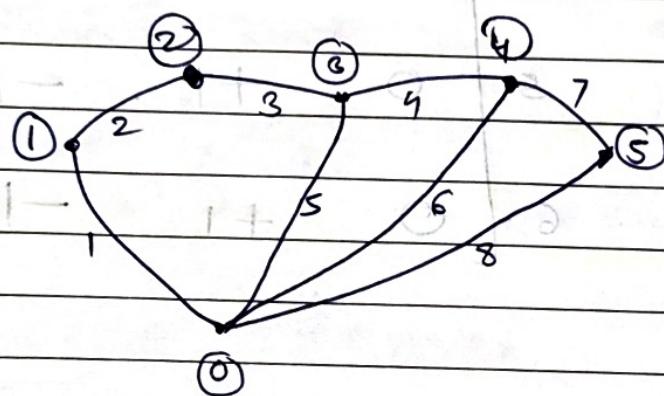
(c) Bus Incidence matrix will be

node =	1	2	3	4	5
elements =	0	+1	0	0	
	1	+1	-1	0	
	2	0	+1	-1	
	3	0	+1	-1	
	4	0	+1	0	
	5	0	0	+1	

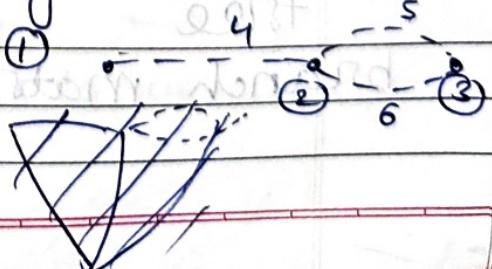
[ISLD]

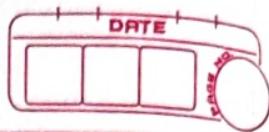


[GRAPH]



\* Making a co-tree





$$A = \frac{e}{n}$$

$$\begin{bmatrix} 1 & +1 & 0 & 0 \\ 2 & 0 & -1 & 0 \\ 3 & 0 & 0 & -1 \\ 4 & +1 & -1 & 0 \\ 5 & 0 & +1 & -1 \\ 6 & 0 & +1 & -1 \end{bmatrix}$$

$[A_b]$

$b \times (n-1)$

$[A_c]$

$l \times (n-1)$

links  $\times n$ .

→  $A_b$  is always a square matrix because branches is always  $n-1$  (non-singular matrix)

→  $A_c$  is non-singular → rows addition is zero

→ Arrange in such a way that  $A_b$  is always on top of  $A_c$

free  
branch matrix

co-tree  
link matrix

always  
a square  
matrix

$$Z = R + jX \rightarrow$$

↓  
 R → R (x axis real)  
 jX → X (y axis Imag)



## \* Primitive network (Basic unit)

↓  
 Impedance  
form (Z)

$$\boxed{Z = R + jX}$$

↓  
 Admittance  
form. (Y)

$$\boxed{Y = G + jB}$$

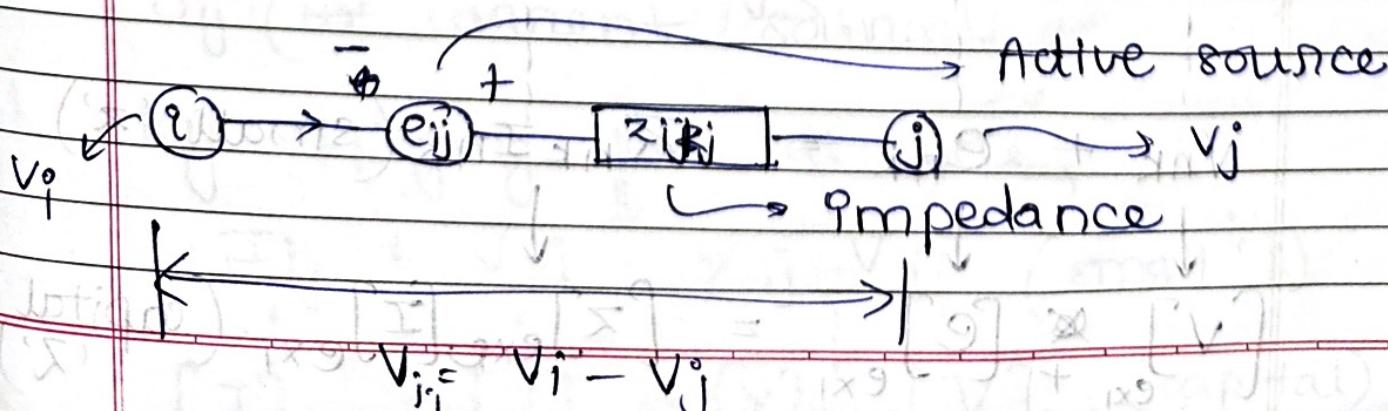
→ Each element of a network can be represented by a decoupled partial network known as a PRIMITIVE NETWORK.

→ Elements → Active (V or I)

Passive (Y and Z)

→ When primitive network is used, we use 'Y' and 'Z' for impedance & admittance.

### i) Primitive network in IMPEDANCE FORM.



Decoupled  $\rightarrow$  one quantity depends on

one variable

$$\begin{bmatrix} 2 & 0 \\ 0 & 5 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 4 \\ 8 \end{bmatrix} \quad 2x_1 = 4 \quad 5x_2 = 8$$



$Z_{ij}$  - self impedance of element  $i-j$

$\therefore$  By applying KVL,

$$V_i + e_{ij} - Z_{ij} I_{ij} = V_j$$

Whenever decoupled matrix is considered  $\rightarrow$  it is a diagonal matrix.

$$V_i - V_j = e_{ij} + Z_{ij} I_{ij}$$

$$V_{ij} + e_{ij} = Z_{ij} I_{ij}$$

Voltage  
betn the nodes

voltage of the

element/voltage  
source

voltage  
drop  
( $Z_{ij} I_{ij}$ )

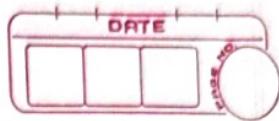
$\rightarrow$  So we will have to make eqn for elements.

$$V_{ij} + e_{ij} = Z_{ij} I_{ij} \text{ (small 'z')}$$

$$V_{nk} + e_{nk} = Z_{nk} I_{nk} \text{ (small 'z')}$$

$$[V]_{\text{ext}} + [e]_{\text{ext}} = [Z]_{\text{ext}} [I]_{\text{ext}} \text{ (capital 'Z')}$$

complete opp  $\rightarrow$  dual  
systems system.



We want a single e matrix on the RHS.

but

$$[z]_{\text{ext}} [I]_{\text{ext}}$$

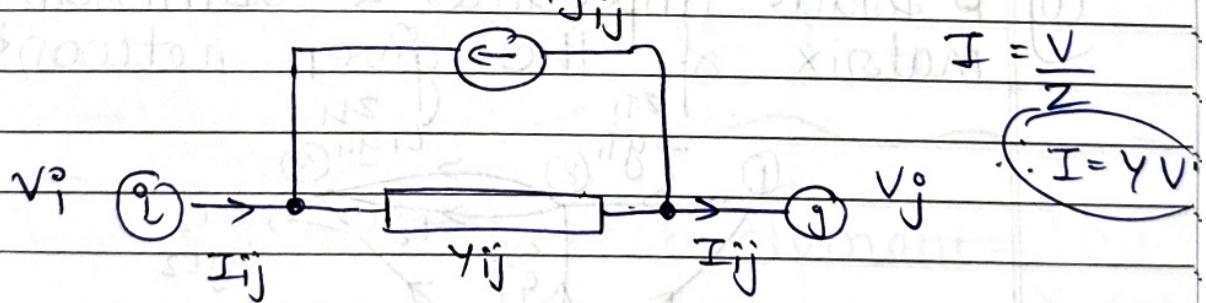
if we do,  $[z]_{\text{ext}} [I]_{\text{ext}} \Rightarrow [\text{Total}]_{\text{ext}}$

$$\downarrow \quad \rightarrow [z]_{\text{ext}} [I]_{\text{ext}}$$

Should be a  
diagonal matrix.  $\rightarrow$  of the  
impedance

→ Primitive impedance matrix is a  
diagonal matrix if there is no  
mutual coupling.

2) Primitive network in ADMITTANCE FORM



$$K \quad V = V_i - V_j \rightarrow$$

→ Just convert  $e_{ij}$  (voltage source) to  
 $J_{ij}$  (current source)

By applying KCL at node,

$$I_{ij} + J_{ij} = Y_{ij} V_{ij} \quad (\text{small } i)$$

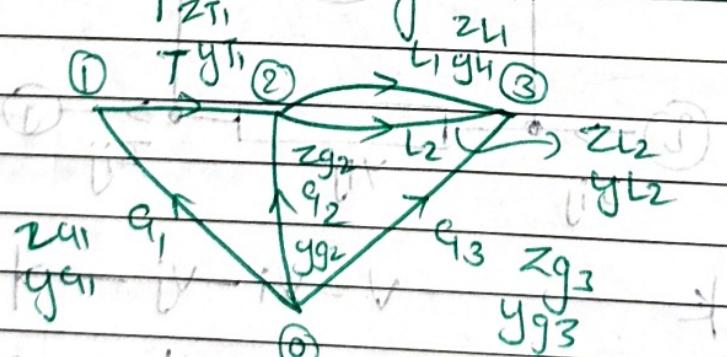
$$[I]_{\text{ext}} + [J]_{\text{ext}} = [Y]_{\text{ext}} [V]_{\text{ext}} \quad (\text{capital})$$

## \* Adv. of Y over Z + I - from sh

- 1) Data of the line will be in form of  $z$
- 2) If no mutual coupling, we can easily convert ' $z$ ' to ' $y$ '.
- 3) Fault analysis, SC analysis  $\rightarrow$  done in form  $\rightarrow$  we need thevenin eqn of impedance

$\hookrightarrow$  so diagonal elements of ( $z$ ) primitive matrix gives thevenin eqn at that bus.

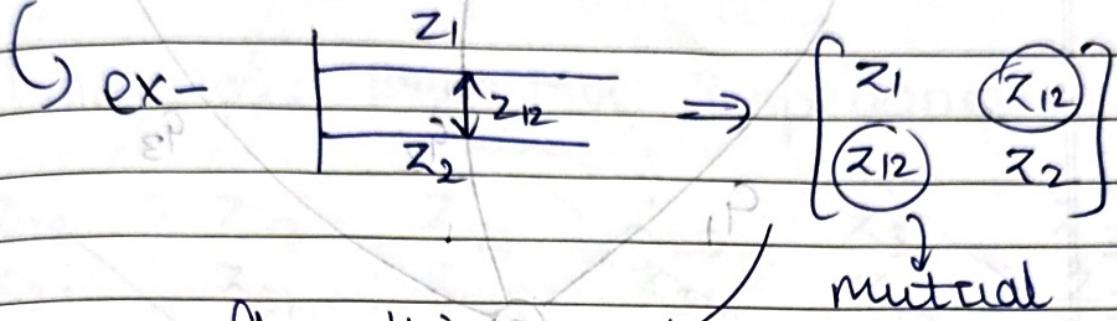
Q) Draw Impedance & admittance matrix of the given network.



$\rightarrow$  With no-mutual coupling, form 'y' primitive

At with mutual coupling, first form ' $z$ ' matrix with diagonal ' $z_{ij}$ '

and off diagonal is mutual impedance b/w them



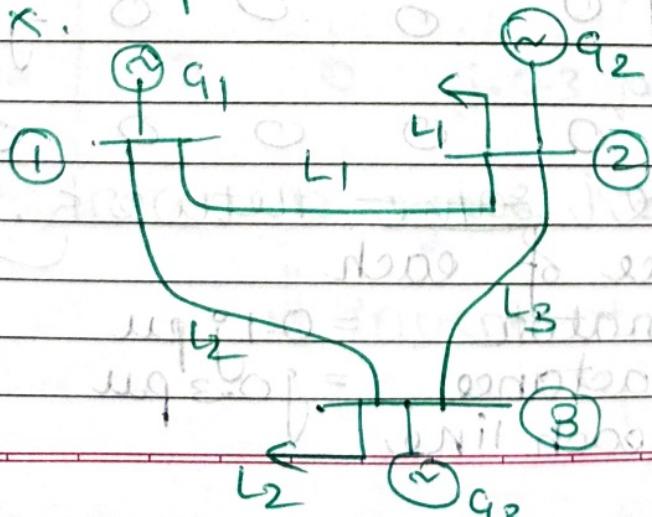
after this invert and form 'y' matrix.

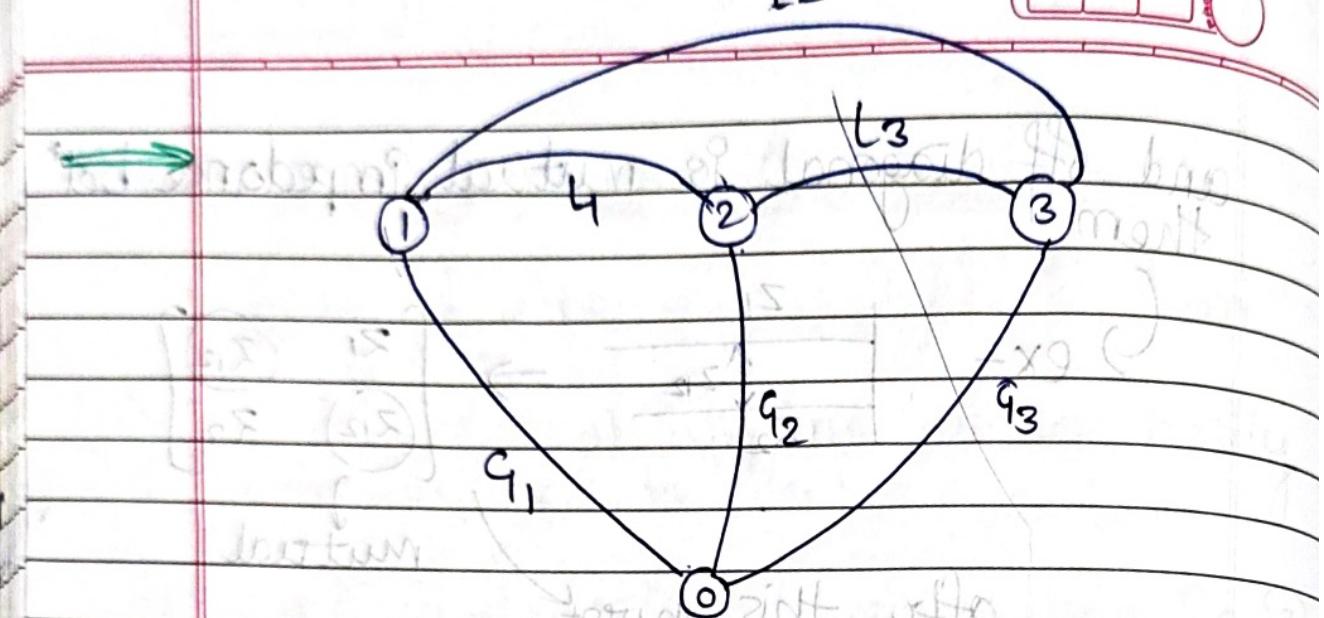
Here, 'y' matrix is

$$y = \begin{bmatrix} y_{11} & & & \\ & y_{12} & & \\ & & y_{13} & \\ & & & y_{1n} \end{bmatrix} = \mu$$

① Reactance of etc each element =  $j0.1$  pu

formulate primitive admittance matrix.





Ignore the load.

$$Z = X = j0.1 \text{ pu} \quad Z = \sqrt{R^2 + X^2}$$

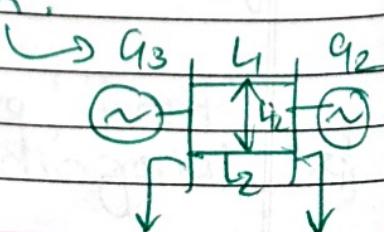
$$-j10 \text{ pu} = \frac{1}{Z}$$

	1	2	3	4	5	6
1	-j10	0	0	0	0	0
2	0	-j10	0	0	0	0
3	0	0	-j10	0	0	0
4	0	0	0	-j10	0	0
5	0	0	0	0	-j10	0
6	0	0	0	0	0	-j10

Use the same network.

CONT'D Reactance of each

generator =  $0.1 \text{ pu}$   
self reactance =  $j0.3 \text{ pu}$   
of each line



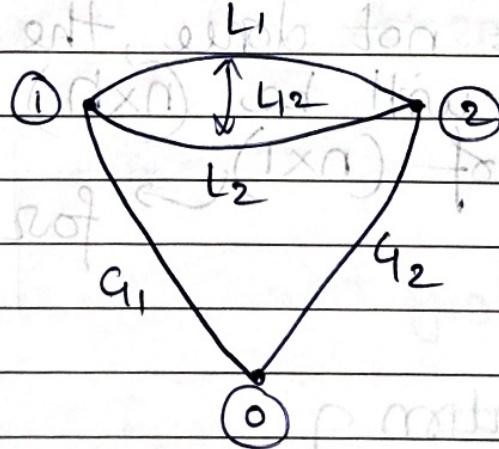
Two lines have mutual Impedance of  $j 0.01 \text{ pu}$ .

Formulate primitive Impedance matrix

$$\Rightarrow \begin{matrix} Z_{12} & Z_{13} & Z_{21} & Z_{23} & Z_{31} & Z_{32} \\ Z_{21} & Z_{31} & Z_{12} & Z_{32} & Z_{13} & Z_{23} \end{matrix}$$

mutual

4 elements, so matrix will be  $4 \times 4$



primitive

$Z = j0.1$	$q_1$	$j0.1$	$0$	$0$	$0$
$q_1$	$0$	$0$	$j0.1$	$0$	$0$
$q_2$	$0$	$0$	$0$	$j0.3$	$j0.3$
$L_2$	$0$	$0$	$+j0.01$	$j0.3$	

Invent to find

# PSA Ybus.

## ★ Ybus methods

1) Inspection

method

2) Step by step

method

3) Singular Transformation

$$\rightarrow Y_{\text{bus}} = Z_{\text{bus}} I_{\text{bus}} \quad (n \times 1) \quad (n \times n) \quad Z, Y \text{ should}$$

$$I_{\text{bus}} = Y_{\text{bus}} V_{\text{bus}} \quad (n \times 1) \quad (n \times n)$$

always  
be written  
first because  
of  $(n \times n)$

If this is not done, the  
answer will be  $(n \times n)$   
instead of  $(n \times 1)$

for  $V_{\text{bus}}$  and  
 $I_{\text{bus}}$   
matrices.

→ Sign convention

n tells the no. of currents flowing  
in & out

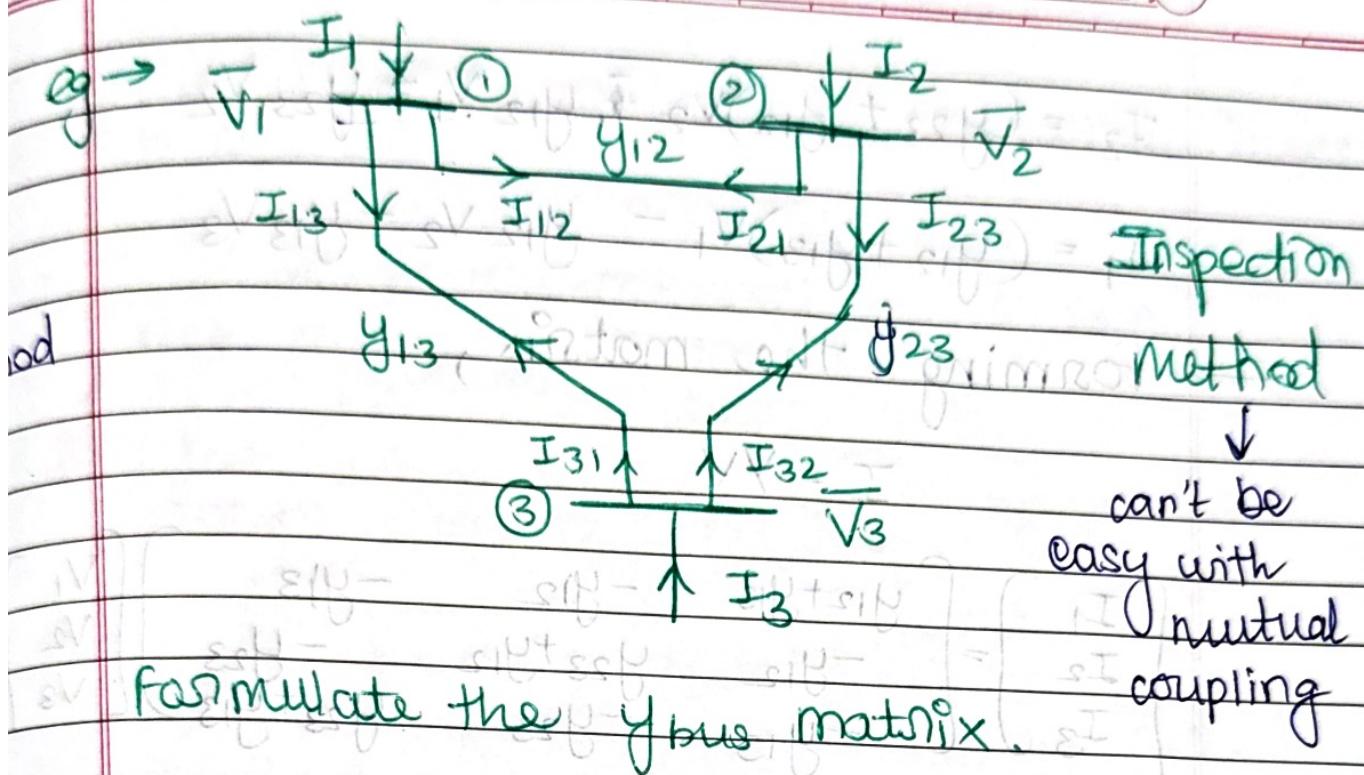
↳ injection current = +ve sign

current is going out = -ve sign.

→ Large voltages like 400 kV are  
measured using potential

transformers

~~star~~ singular transformation method  
 In star connections, usually resistance values are very low.



By applying KCL at each node,

$$I_1 = Y_{12}V_2 + Y_{13}V_3 \quad \text{from node 1}$$

2nd row out resulted

$$= Y_{12}(V_1 - V_2) + Y_{13}(V_1 - V_3) - [ \because I = yV ]$$

$$I_2 = Y_{21}V_1 + Y_{23}V_3$$

$$\text{3rd row} = -Y_{12}(V_2 - V_1) + Y_{23}(V_2 - V_3)$$

because  $y_{21} = -y_{12}$

$$I_3 = -Y_{13}(V_3 - V_1) - Y_{23}(V_3 - V_2)$$

Now, separating voltages & admittance

$$I_2 = -V_3(Y_{13} + Y_{23}) + Y_{13}V_1 + Y_{23}V_2$$



$j0.3 \rightarrow$  impedance

$-j0.2 \rightarrow$  admittance

VIP



$$I_2 = (Y_{23} + Y_{12})V_2 - Y_{12}V_1 - Y_{23}V_2$$

$$I_1 = (Y_{12} + Y_{13})V_1 - Y_{12}V_2 - Y_{13}V_3$$

→ forming the matrix,

$$I = YV$$

$$\begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} Y_{12} + Y_{13} & -Y_{12} & -Y_{13} \\ -Y_{12} & Y_{23} + Y_{12} & -Y_{23} \\ -Y_{13} & -Y_{23} & Y_{23} + Y_{13} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix}$$

### ★ Observations

1) Diagonal elements are the sum of admittance between two nodes.

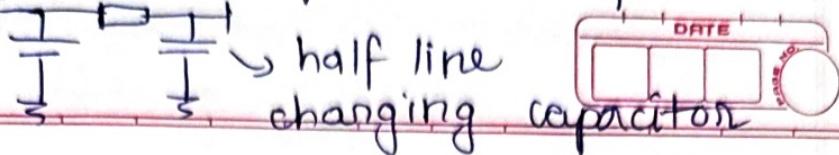
2) off diagonal elements are the  $Y$ -bus

→ We prefer  $Y$  over  $Z$ -bus, because network topologies changes can be incorporated way easily than  $Z$  bus  
 ↳ which requires more complex operations.

→  $Z$  bus is always a full-matrix and  $Y$  bus is a sparse-matrix

↳ because a substation is often connected with 3-4 other substations

Size of y-bus  $\rightarrow$  no. of bus  $\times$  no. of bus.



The matrix entries of the other buses is 0.

$\hookrightarrow$  so, faster computation & less memory allocation.

\* Y bus will not always be symmetric (in case of mutual coupling)

e.g -

Diagram of a transmission line section with two buses. A horizontal line connects the two buses. A shunt admittance  $Z_{12}$  is connected between the two buses. The admittance is labeled with circled numbers 1 and 2 above and below it respectively.

$$Y = \frac{B}{2} \begin{matrix} 1 \\ \text{---} \\ 2 \end{matrix}$$

formulate the y-bus.

$$Y_{\text{bus}} = \begin{bmatrix} \frac{1}{Z_{12}} + \frac{B}{2} & -\frac{1}{Z_{12}} \\ -\frac{1}{Z_{12}} & \frac{1}{Z_{12}} + \frac{B}{2} \end{bmatrix}_{2 \times 2}$$

sum of admittance bet^n the elements bet^n 2 nodes

This is not singular matrix because there is a shunt element coming in the diagonal elements

$\hookrightarrow \frac{B}{2}$  element

VIP

$\rightarrow$  In case of a short transmission line, where no shunt elements

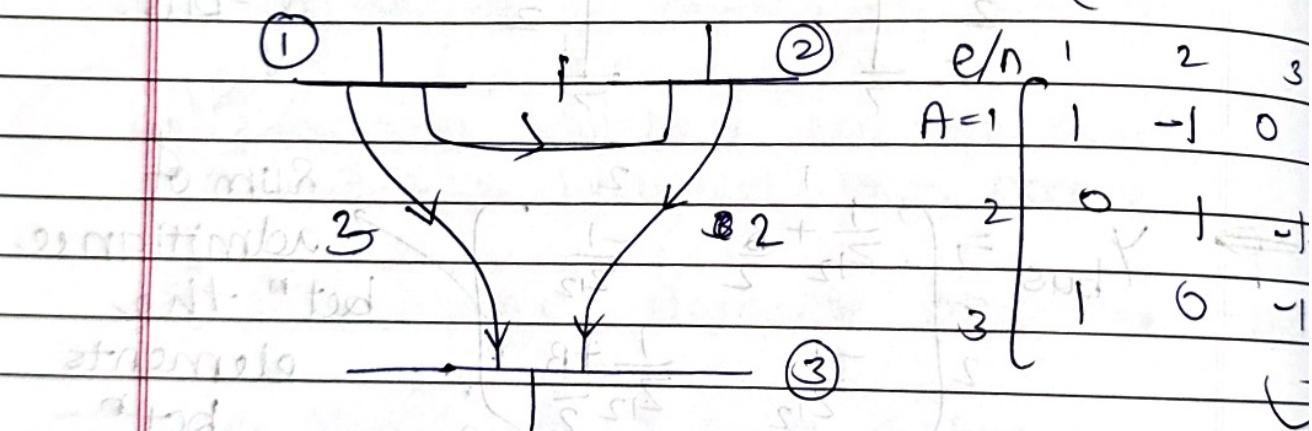
$\therefore Y_{\text{bus}}$  is singular

## ★ Singular Transformation Matrix Method.

- use for large complex network.
- used when there is mutual coupling

Relation bet<sup>n</sup> v (element voltage)  
and v (bus voltage)

related with the bus  
incidence matrix (A)



$$\therefore [v] = [A][v]$$

(ex1)       $(e \times n-1) \quad ((n-1) \times 1)$

$$\begin{aligned} V_1 &= V_1 - V_2 \\ V_2 &= V_2 - V_3 \\ V_3 &= V_1 - V_3 \end{aligned}$$

$$v = \begin{bmatrix} 1 & -1 & 0 \\ 0 & 1 & -1 \\ 1 & 0 & -1 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix}$$

Element voltages      bus voltages

$\hookrightarrow A$  (bus incidence matrix)

Proof

\* Network eq<sup>n</sup> in Y form

$$[I]_{\text{ext}} + [J]_{\text{ext}} = [Y]_{\text{ext}} [V]_{\text{ext}}$$

element voltage matrix

primitive admittance matrix

Pre-multiply the eq<sup>n</sup> with  $A^T$ ,

$$[A]^T [I]_{\text{ext}} + [A]^T [J]_{\text{ext}} = [A]^T [Y]_{\text{ext}} [V]_{\text{ext}}$$

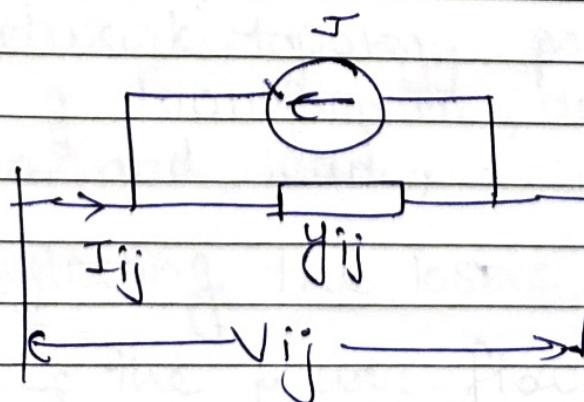
Since,  $V = [A]^T [Y]$ ,

$$\therefore [A]^T [I]_{\text{ext}} + [A]^T [J]_{\text{ext}} = [A]^T [Y]_{\text{ext}} [A] [V]$$

$$A^T = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & -1 \end{bmatrix}$$

J (Injection matrix)

I (element current), J (source current)





Bus Injection  $\rightarrow$  current getting injected in the grid.



$[A]^T [I] \rightarrow$  always is zero  
 element current

Transpose bus Incidence matrix

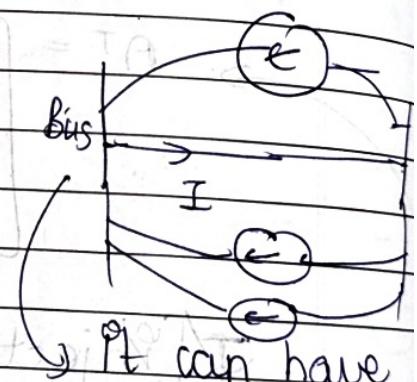
$$\therefore [A]^T [I] + [A]^T [J] = [A]^T [Y] [A]^T [V_{bus}]$$

$$[I_{bus}] = [Y_{bus}] [V_{bus}]$$

VxIP

Injection due  
to source  
current matrix

bus



It can have  
generator  
and load  
at the same bus

→ generation → load → freq changes  
→ demand + loss

## STEADY STATE ANALYSIS



→ The eq<sup>n</sup> will be algebraic in form.

1) Power flow analysis (load flow analysis)

\* generation > load → freq ↑ es.

\* generation < load → freq ↓ es.

$$\sum P_g = \sum P_d + P_L$$

**VVIP** Here, freq is constant

\* Assumptions:

1) gen & load is constant, balanced in steady state.

2) frequency is constant here.

→ Given network topology, parameters of line & transformer, and the generation and load,

(b) neglecting the losses temporarily,

we do the power flow analysis

determines voltage at each bus of the network.



Modes of sync gen  
↳ operated in over excited mode → fan injecting more than 1 p.u.

→ When a lightly loaded or long transmission line, the  $V_R > V_S$

so to compensate this, add an inductor a shunt inductance

↳ because it absorbs reactive power

→ Reactive power is supplied on the load end

↳ if its supplied in generator end, the active power to be transmitted decreases.

→ To supply reactive power, put a capacitor bank towards the load end.

→ Generating generator cannot be operated in under excited mode.

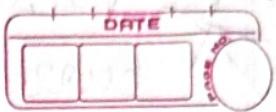
Q) Why is LFA (load flow analysis) done?

- 1) To monitor voltage at each bus
- 2) To determine power flow of each element

$$S = V^2 / Z \rightarrow \text{Voltage at bus}$$

$\rightarrow$   $Z = R + jX$   $\rightarrow$  impedance

sync gen if it is not locally managed.



power in the circuit

3) We monitor this because if voltage varies

↳ we need to seek a solution for reactive power management

4) We monitor LFA to see if any line is overloaded or no, if more power is flowing than the rating.

↳ all transmission lines and transformers

5) Then, find the losses in the power system

LFA

Stage-1 → To find magnitude of voltage  $|V|$  and angle  $\angle S$

Stage-2 → To find current phasors in transmission lines,

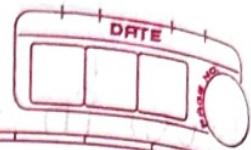
$$I = \sqrt{S^2 - V^2}$$

(Induction)

$$S_R = V_R I_R^*$$

→ load forecasting → generation → dispatch

~~★~~ voltage  $\rightarrow$  generation  
current  $\rightarrow$  size of conductor



## ★ Merit order dispatch?

Scheduling of the generators

### ★ Power system constraints

$$1) \sum P_g = \sum P_d + \sum P_L \quad (\text{equality/operational constraint})$$

2) At every bus,  $|V|$  must be within a range ( $\pm 5\%$  in transmission system)

$$\hookrightarrow |V_{imin}| \leq |V_i| \leq |Vimax| \quad (\text{voltage constraint})$$

3) At every generator, there is a limit for power generation when it is started

$$\hookrightarrow P_{gimin} \leq P_{gi} \leq P_{gimax} \quad (\text{real power constraint})$$

$$\hookrightarrow Q_{gimin} \leq Q_{gi} \leq Q_{gimax} \quad (\text{reactive power constraint})$$

These are equipment constraints, hardware can get damaged

$\hookrightarrow$  operational constraint  $\rightarrow$  can affect the system

$$\hookrightarrow f_{min} \leq f \leq f_{max}$$

## load angle



→  $S_i$  decides the power flow

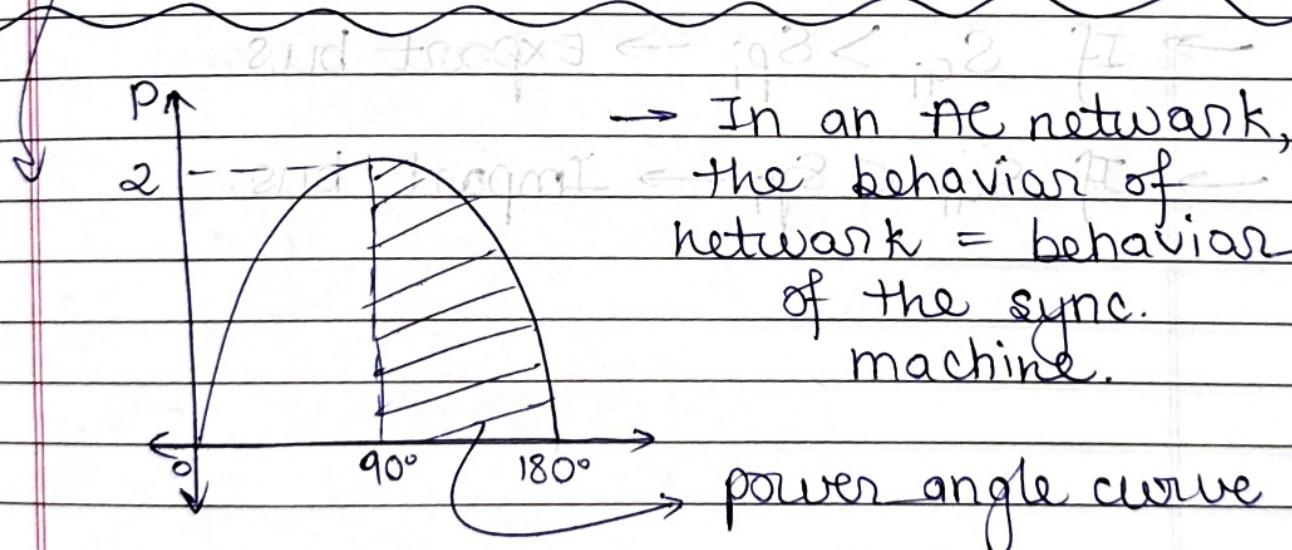
↳  $S_i$  is greater, the power will flow from there.

g-  $|V| \angle S_i$   $|V| \angle S_j \rightarrow$  voltage angle



$$\delta = |\delta_i - \delta_j| \leq 35^\circ$$

4) The diff bet<sup>n</sup> angle  $\leq 35^\circ$  is also an operational constraint.



→ Beyond  $\delta = 90^\circ$ , operation is unstable.

↳ to avoid this, a margin of  $35^\circ$  is kept

$\delta$  is always kept bet<sup>n</sup>  $35^\circ - 40^\circ$

→ At every bus in the power system there are 4 quantities always mentioned

- 1)  $V_{il}$  → voltage magnitude
- 2)  $\delta_i$  → load angle
- 3)  $P_i$  → active power injection
- 4)  $Q_i$  → reactive power injection

→ If  $S_{qi} > S_{pi}$  → Export bus

→ If  $S_{qi} < S_{pi}$  → Import bus.