

Dirichlet Series I

Talip Can Termen

October 14, 2025

Abstract

This talk is the first part of a two-part presentation on Dirichlet series. In this session, we introduce the concept of Dirichlet series and explore their general properties. We discuss how convergence and absolute convergence depend on the real part of the complex variable and describe the corresponding regions. Examples of Dirichlet series generated by well-known arithmetic functions, such as the Möbius function $\mu(n)$ and Euler's totient function $\phi(n)$, are presented to illustrate their connection with the Riemann zeta function $\zeta(s)$.

Keywords: Dirichlet series, Arithmetic functions, Riemann zeta function.

MSC Number: 11M41, 11M06.

Address: Department of Mathematics, Izmir Institute of Technology, Urla, Izmir, Turkey. cantermen@iyte.edu.tr

References

- [1] Apostol, T. M., Introduction to analytic number theory. Springer (1976).