

MATH154 Team Challenge

NAMES

November 08, 2020

Loading the packages:

```
library(e1071)
library(ggplot2)
library(plyr)
library(tidyverse)
```

EDA

We began our analysis by first loading the training data set and then examine the predictors.

```
data_train <- read.csv('data/cs-training.csv')
colnames(data_train)
```

```
## [1] "X"
## [2] "SeriousDlqin2yrs"
## [3] "RevolvingUtilizationOfUnsecuredLines"
## [4] "age"
## [5] "NumberOfTime30.59DaysPastDueNotWorse"
## [6] "DebtRatio"
## [7] "MonthlyIncome"
## [8] "NumberOfOpenCreditLinesAndLoans"
## [9] "NumberOfTimes90DaysLate"
## [10] "NumberRealEstateLoansOrLines"
## [11] "NumberOfTime60.89DaysPastDueNotWorse"
## [12] "NumberOfDependents"
```

Portion of defaulted

```
mean(data_train$SeriousDlqin2yrs)
```

```
## [1] 0.06684
```

We then check each feature with **summary()** and see which of these features have null data and how many.

```
data_col <- colnames(data_train)
for(i in 2:12){
  print(data_col[i])
  print(summary(data_train[,i]))
}
```

```
## [1] "SeriousDlqin2yrs"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
## 0.00000 0.00000 0.00000 0.06684 0.00000 1.00000
## [1] "RevolvingUtilizationOfUnsecuredLines"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      0.00     0.03     0.15     6.05     0.56 50708.00
## [1] "age"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      0.0     41.0     52.0     52.3     63.0    109.0
```

```
## [1] "NumberOfTime30.59DaysPastDueNotWorse"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##    0.000  0.000  0.000  0.421  0.000  98.000
## [1] "DebtRatio"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      0.0    0.2    0.4   353.0    0.9 329664.0
## [1] "MonthlyIncome"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.   NA's
##       0   3400   5400   6670   8249 3008750   29731
## [1] "NumberOfOpenCreditLinesAndLoans"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##    0.000  5.000  8.000  8.453  11.000  58.000
## [1] "NumberOfTimes90DaysLate"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##    0.000  0.000  0.000  0.266  0.000  98.000
## [1] "NumberRealEstateLoansOrLines"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##    0.000  0.000  1.000  1.018  2.000  54.000
## [1] "NumberOfTime60.89DaysPastDueNotWorse"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##    0.0000  0.0000  0.0000  0.2404  0.0000  98.0000
## [1] "NumberOfDependents"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.   NA's
##    0.000  0.000  0.000  0.757  1.000  20.000   3924
```

This suggests that only monthly income and number of dependents have missing data, which we would later either fill in or drop. We then examine each variable to check for the existence of outliers

```
data_train$SeriousDlqin2yrs <- as.factor(data_train$SeriousDlqin2yrs)
```

Revolving-Utilization-Of-Unsecured-Lines

For the second variable **Revolving-Utilization-Of-Unsecured-Lines**, which measures the total balance on credit card divided by sum of credit limits (amounts owing divided by total available for borrowing), the max number is 50708, which is unlikely as we can't borrow beyond the limit by that much.

Take a look at Observations with **Revolving-Utilization-Of-Unsecured-Lines** > 1 and > 100. There are 3338 obs with **Revolving-Utilization-Of-Unsecured-Lines** > 1 and 223 obs with **Revolving-Utilization-Of-Unsecured-Lines** > 100.

```
g1 <- subset(data_train,RevolvingUtilizationOfUnsecuredLines>=1)
g2 <- subset(data_train,RevolvingUtilizationOfUnsecuredLines>=100)
summary(g1)
```

```
##      X      SeriousDlqin2yrs RevolvingUtilizationOfUnsecuredLines
##  Min.   : 163      0:2097      Min.    : 1.00
## 1st Qu.: 38548    1:1241    1st Qu.: 1.02
## Median : 76612      Median : 1.07
## Mean   : 75818      Mean   : 258.46
## 3rd Qu.:112457     3rd Qu.: 1.30
## Max.   :149974     Max.   :50708.00
##
##      age      NumberOfTime30.59DaysPastDueNotWorse      DebtRatio
##  Min.   :21.00      Min.    : 0.000      Min.    : 0.001
## 1st Qu.:34.00      1st Qu.: 0.000      1st Qu.: 0.180
## Median :43.00      Median : 1.000      Median : 0.374
```

```
## Mean :44.05 Mean : 1.013 Mean : 244.619
## 3rd Qu.:52.00 3rd Qu.: 2.000 3rd Qu.: 0.806
## Max. :88.00 Max. :10.000 Max. :21395.000
##
## MonthlyIncome NumberOfOpenCreditLinesAndLoans NumberOfTimes90DaysLate
## Min. : 0 Min. : 0.000 Min. : 0.000
## 1st Qu.: 2700 1st Qu.: 3.000 1st Qu.: 0.000
## Median : 4182 Median : 6.000 Median : 0.000
## Mean : 5282 Mean : 6.365 Mean : 0.636
## 3rd Qu.: 6430 3rd Qu.: 8.000 3rd Qu.: 1.000
## Max. :141500 Max. :40.000 Max. :15.000
## NA's :550
## NumberRealEstateLoansOrLines NumberOfTime60.89DaysPastDueNotWorse
## Min. : 0.0000 Min. :0.0000
## 1st Qu.: 0.0000 1st Qu.:0.0000
## Median : 0.0000 Median :0.0000
## Mean : 0.6812 Mean :0.4308
## 3rd Qu.: 1.0000 3rd Qu.:1.0000
## Max. :10.0000 Max. :7.0000
##
## NumberOfDependents
## Min. :0.0000
## 1st Qu.:0.0000
## Median :0.0000
## Mean :0.9204
## 3rd Qu.:2.0000
## Max. :8.0000
## NA's :61
```

```
summary(g2)
```

```
## X SeriousDlqin2yrs RevolvingUtilizationOfUnsecuredLines
## Min. : 294 0:212 Min. : 112
## 1st Qu.: 43785 1: 11 1st Qu.: 1082
## Median : 80200 Median : 2159
## Mean : 77440 Mean : 3848
## 3rd Qu.:110755 3rd Qu.: 4318
## Max. :149280 Max. :50708
##
## age NumberOfTime30.59DaysPastDueNotWorse DebtRatio
## Min. :24.00 Min. :0.00 Min. : 0.001
## 1st Qu.:39.00 1st Qu.:0.00 1st Qu.: 0.213
## Median :48.00 Median :0.00 Median : 0.381
## Mean :50.59 Mean :0.13 Mean : 604.614
## 3rd Qu.:62.50 3rd Qu.:0.00 3rd Qu.: 81.500
## Max. :87.00 Max. :2.00 Max. :21395.000
##
## MonthlyIncome NumberOfOpenCreditLinesAndLoans NumberOfTimes90DaysLate
## Min. : 0 Min. : 1.000 Min. :0.00000
## 1st Qu.: 4800 1st Qu.: 4.000 1st Qu.:0.00000
## Median : 7083 Median : 5.000 Median :0.00000
## Mean : 8629 Mean : 5.637 Mean :0.03139
## 3rd Qu.:10400 3rd Qu.: 7.000 3rd Qu.:0.00000
## Max. :44472 Max. :21.000 Max. :3.00000
## NA's :62
```

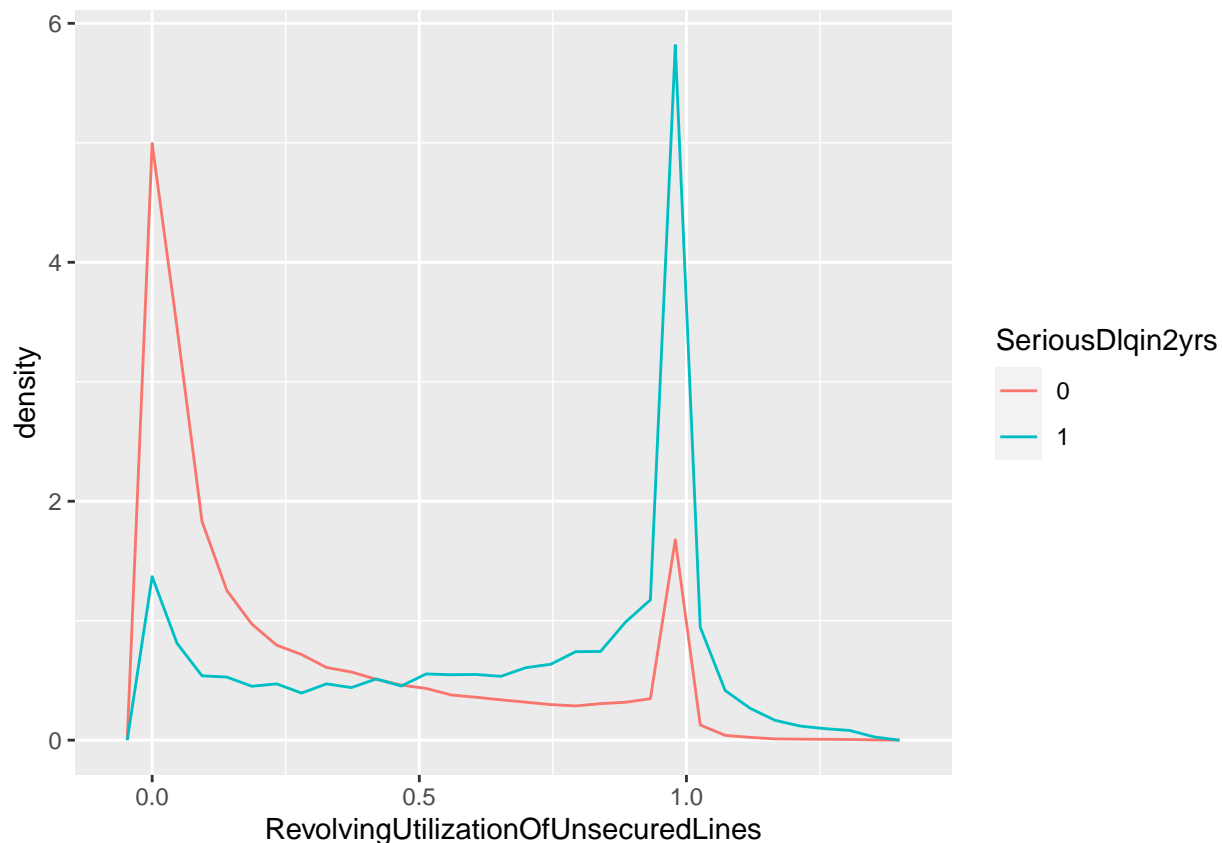
```
## NumberRealEstateLoansOrLines NumberOfTime60.89DaysPastDueNotWorse
## Min. :0.000 Min. :0.00000
## 1st Qu.:0.000 1st Qu.:0.00000
## Median :1.000 Median :0.00000
## Mean :1.197 Mean :0.02242
## 3rd Qu.:2.000 3rd Qu.:0.00000
## Max. :9.000 Max. :1.00000
##
## NumberOfDependents
## Min. :0.000
## 1st Qu.:0.000
## Median :0.000
## Mean :0.684
## 3rd Qu.:1.000
## Max. :4.000
## NA's :11
```

If we remove the outliers using the 1.5IQR rule and plot the density plot grouped by whether there is a financial stress experienced, we observe an interesting shape. The group that has experienced financial stress is more likely to be concentrated on the higher end of the value of the **RevolvingUtilizationOfUnsecuredLines** variable.

```
Q <- quantile(data_train$RevolvingUtilizationOfUnsecuredLines, probs=c(.25, .75), na.rm = TRUE)
iqr <- IQR(data_train$RevolvingUtilizationOfUnsecuredLines, na.rm = TRUE)
data_revu <- subset(data_train,
                    data_train$RevolvingUtilizationOfUnsecuredLines > (Q[1] - 1.5*iqr) &
                    data_train$RevolvingUtilizationOfUnsecuredLines < (Q[2]+1.5*iqr))

ggplot(data = data_revu,
       mapping = aes(x = RevolvingUtilizationOfUnsecuredLines,
                     after_stat(density), colour = SeriousDlqin2yrs)) +
  geom_freqpoly()

## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



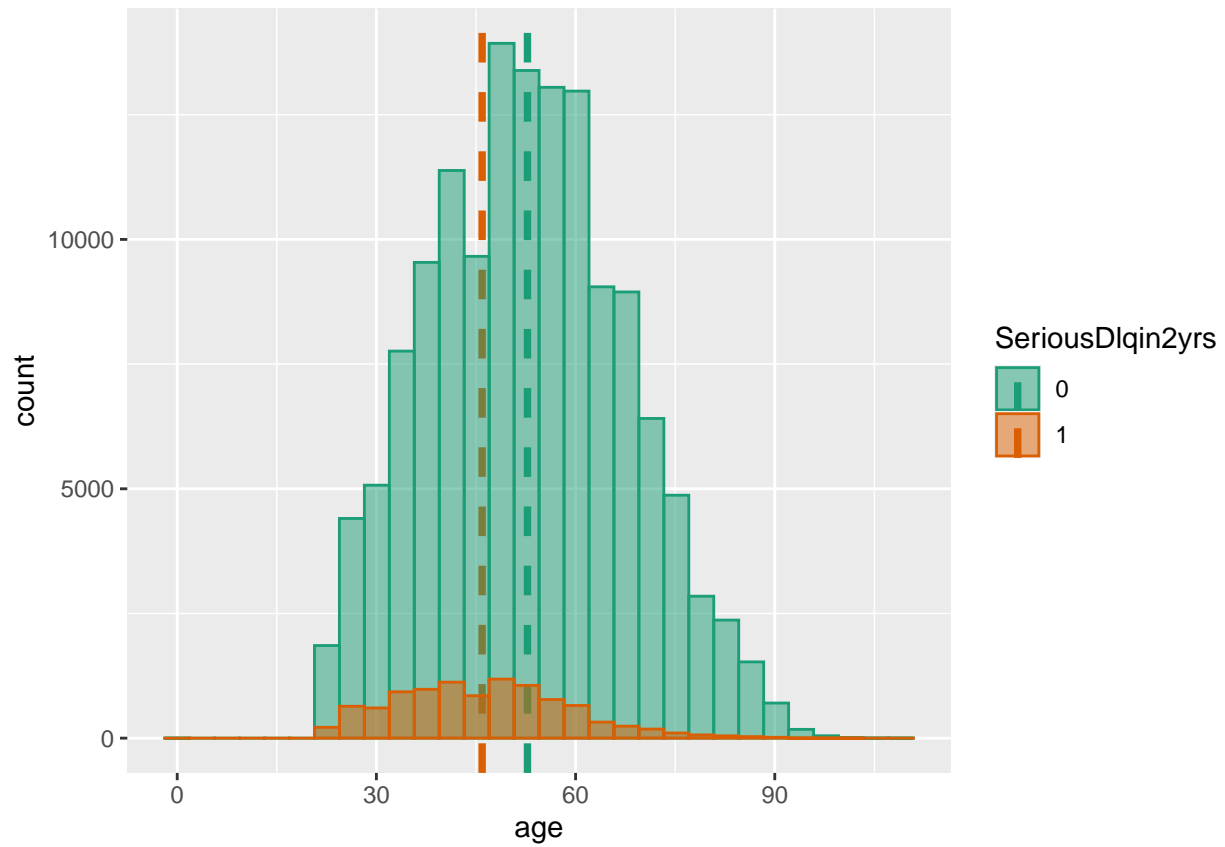
Age

An analysis of the third variable **age** shows that the group who have experienced financial distress in the next two years have an average of age lower than the other group who have not experienced such stress. This may suggest that young people are more likely to experience financial hardships relative to older people. Additionally, the histogram shows that there are far more people who have not experienced any financial distress than the other group.

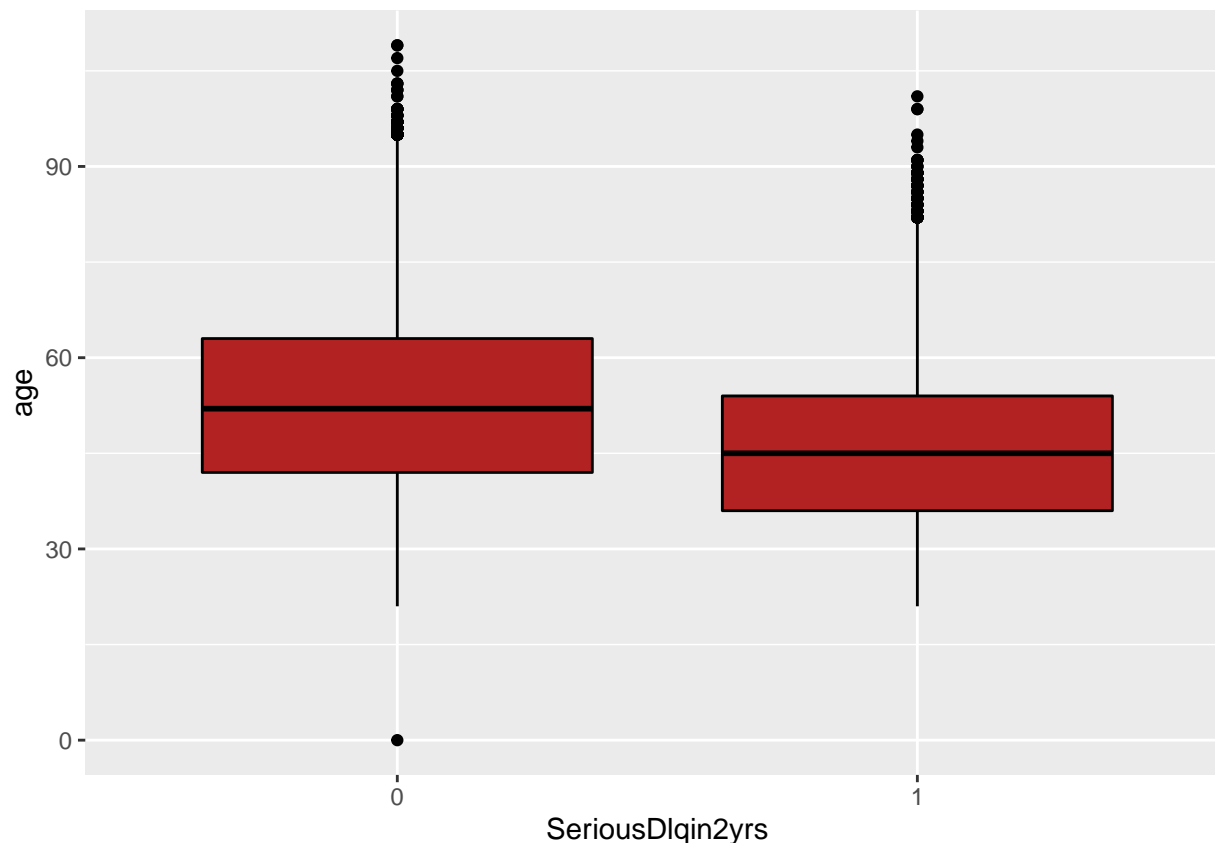
```
mage <- ddpdy(data_train, "SeriousDlqin2yrs", summarise, grp.mean=mean(age))
head(mage)
```

```
##   SeriousDlqin2yrs grp.mean
## 1                0 52.75138
## 2                1 45.92659
```

```
ggplot(data_train, aes(x=age, color=SeriousDlqin2yrs,
                       fill=SeriousDlqin2yrs)) +
  geom_vline(data=mage, aes(xintercept=grp.mean, color=SeriousDlqin2yrs),
            linetype="dashed", size=1.3) +
  geom_histogram(alpha = 0.5, position = "identity") +
  scale_color_brewer(palette="Dark2") +
  scale_fill_brewer(palette="Dark2")
```



```
data_train %>%  
  ggplot(aes(x = SeriousDlqin2yrs, y = age)) +  
  geom_boxplot(color = 'black', fill = 'firebrick') +  
  labs(x = "SeriousDlqin2yrs", y = "age")
```



```
t.test(age ~ SeriousDlqin2yrs, data = data_train, var.equal = TRUE)
```

```
##
## Two Sample t-test
##
## data: age by SeriousDlqin2yrs
## t = 44.989, df = 149998, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##  6.527456 7.122113
## sample estimates:
## mean in group 0 mean in group 1
##      52.75138      45.92659
```

Since p-value is much smaller than the conventional 0.05 threshold, we say that we have found statistical significance in comparing the average of age between the two groups.

NumberOfTime30.59DaysPastDueNotWorse

In this variable, the max number is 98, which is not possible since $98 \times 30 = 2940$ days, which is equivalent to 8 years. However, the variable measures how many times the person has been 30-59 days past dues for the past 2 years, which makes the value 98 impossible. We should remove any value > 24.33 as outliers.

Still, looking at the summary statistics stated below, we found that for the group who have experienced financial stress, their mean and standard deviation are both significantly higher than the group who have not.

```
data_train %>%
  group_by(SeriousDlqin2yrs) %>%
```

```

summarise(
  count = n(),
  mean_ntimes = mean(NumberOfTime30.59DaysPastDueNotWorse),
  sd_ntimes = sd(NumberOfTime30.59DaysPastDueNotWorse),
  min_ntimes = min(NumberOfTime30.59DaysPastDueNotWorse),
  max_ntimes = max(NumberOfTime30.59DaysPastDueNotWorse)
)

## # A tibble: 2 x 6
##   SeriousDlqin2yrs count mean_ntimes sd_ntimes min_ntimes max_ntimes
##   <fct>           <int>     <dbl>     <dbl>     <int>     <int>
## 1 0               139974     0.280     2.95         0         98
## 2 1               10026     2.39      11.7         0         98

```

DebtRatio

There seem to be some abnormalities in the distribution of the debt ratio, which should be a percentage that is the Monthly debt payments, alimony, living costs divided by monthly gross income. It is possible for this number to be greater than one, but for some observations, the number is already over 1000, which seem to be quite impossible in real life.

```

data_train %>%
  group_by(SeriousDlqin2yrs) %>%
  summarise(
    count = n(),
    mean = mean(DebtRatio),
    sd = sd(DebtRatio),
    min = min(DebtRatio),
    max = max(DebtRatio)
  )

## # A tibble: 2 x 6
##   SeriousDlqin2yrs count mean    sd    min    max
##   <fct>           <int> <dbl> <dbl> <dbl> <dbl>
## 1 0               139974 357. 2083.    0 329664
## 2 1               10026 295. 1238.    0 38793

quantile(data_train$DebtRatio, probs=c(.25, .75), na.rm = TRUE)

##           25%           75%
## 0.1750738 0.8682538

```

In the following steps, we first remove the outliers contained in the training data based on the **DebtRatio** variable, and instead of plotting the counts, we choose to plot the density plot and observe how the curves changes as the **DebtRatio** variable increases on the horizontal axis.

```

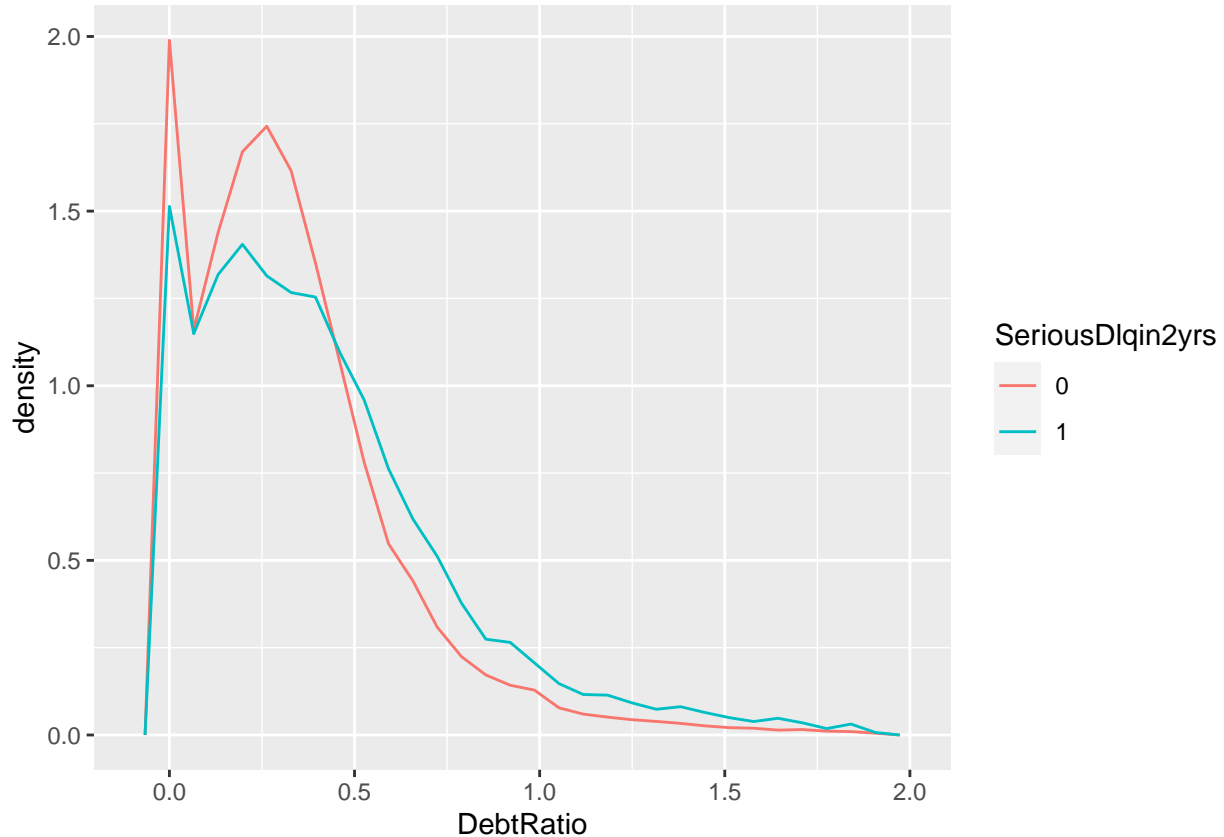
Q <- quantile(data_train$DebtRatio, probs=c(.25, .75), na.rm = TRUE)
iqr <- IQR(data_train$DebtRatio, na.rm = TRUE)
data_dbtratio <- subset(data_train,
  data_train$DebtRatio > (Q[1] - 1.5*iqr) &
  data_train$DebtRatio < (Q[2]+1.5*iqr))

```

We observe that for the group without experiencing any financial stress, it has a distribution that is higher than the other group on the lower end of the debt ratio. As the ratio increases, we observe that the density curve for the group with experience of financial stress becomes higher.


```
ggplot(data = data_dbtratio,
       mapping = aes(x = DebtRatio, after_stat(density), colour = SeriousDlqin2yrs)) +
  geom_freqpoly()
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



MonthlyIncome

The summary statistics show that the group without financial stress has a higher mean/median monthly income than the group with financial stress, but we also observe that some people have a monthly income of 3008750, which is unusually high.

```
data_train %>%
  group_by(SeriousDlqin2yrs) %>%
  summarise(
    count = n(),
    mean = mean(MonthlyIncome, na.rm = TRUE),
    median = median(MonthlyIncome, na.rm = TRUE),
    sd = sd(MonthlyIncome, na.rm = TRUE),
    min = min(MonthlyIncome, na.rm = TRUE),
    max = max(MonthlyIncome, na.rm = TRUE)
  )
```

```
## # A tibble: 2 x 7
##   SeriousDlqin2yrs count mean median    sd  min    max
##   <fct>           <int> <dbl> <dbl> <dbl> <int> <int>
## 1 0               139974 6748.  5466 14814.    0 3008750
```

```
## 2 1          10026 5631.    4500  6172.    0 250000
```

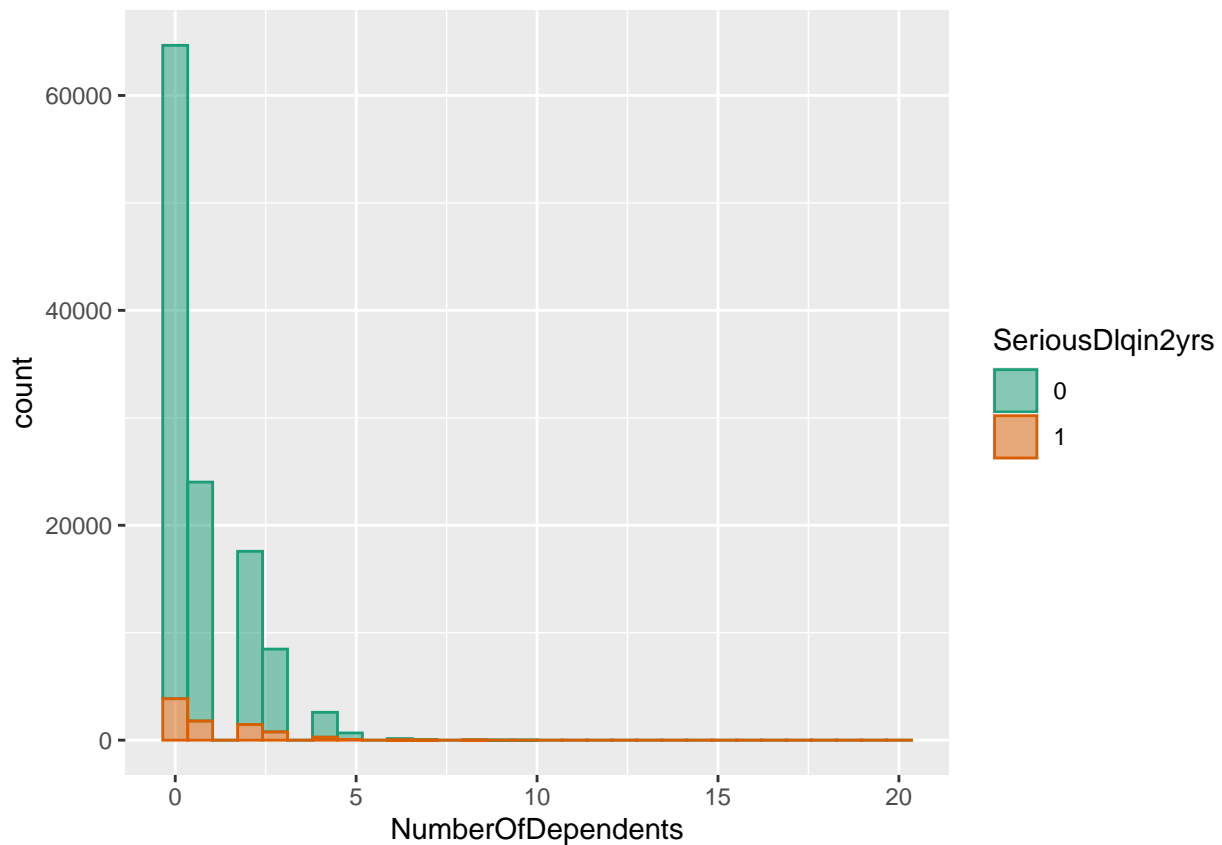
Number of Dependents

```
data_train %>%
  group_by(SeriousDlqin2yrs) %>%
  summarise(
    count = n(),
    mean = mean(NumberOfDependents, na.rm = TRUE),
    median = median(NumberOfDependents, na.rm = TRUE),
    sd = sd(MonthlyIncome, na.rm = TRUE),
    min = min(NumberOfDependents, na.rm = TRUE),
    max = max(NumberOfDependents, na.rm = TRUE)
  )
```

```
## # A tibble: 2 x 7
##   SeriousDlqin2yrs count mean median    sd  min  max
##   <fct>          <int> <dbl>  <int> <dbl> <int> <int>
## 1 0              139974 0.743    0 14814.    0   20
## 2 1              10026 0.948    0  6172.    0    8
```

```
ggplot(data_dbtratio, aes(x=NumberOfDependents, color=SeriousDlqin2yrs,
  fill=SeriousDlqin2yrs)) +
  geom_histogram(alpha = 0.5) +
  scale_color_brewer(palette="Dark2") +
  scale_fill_brewer(palette="Dark2")
```

```
## Warning: Removed 476 rows containing non-finite values (stat_bin).
```



Data Cleaning

We thought about dropping the missing values, replacing missing values with medians, and using regressions to replace missing values

These code above give us the dataframe with incompleted observations dropped

```
train_complete <- complete.cases(data_train)
data_drop <- cbind(data_train, train_complete)
data_drop <- subset(data_drop, data_drop$train_complete == TRUE)
```

These code gave us data_median which uses the respective medians to fill in NAs in MonthlyIncome and NumberOfDependents