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Classification

It is categorizing data into predefined classes or categories based on their features.

Terms

- > Classes: The distinct labels or target classes that the data points are assigned to
- > Label: A class or category assigned to a data point
- > Decision Boundary: a boundary that separates different classes in a feature space
- > Binary Classification: A classification problem with only 2 classes
- Multiclass Classification: A classification problem with more than two classes
- Multilabel Classification: A classification problem where each data point can belong to multiple classes simultaneously
- ➤ Imbalanced dataset: A dataset where one class significantly outnumbers the others.

Evaluation

- \rightarrow Accuracy -> (TP + TN) / (TP + TN + FP + FN)
- > Precision -> TP / (TP + FP)
- > Recall Sensitivity, True Positive Rate -> TP / (TP + FN)
- > FPR False Positive Rate -> FP / (FP + TN)
- > Specificity True Negative Rate -> TN / (FP + TN)
- > F1 score -> 2 * (Precision * Recall) / (Precision + Recall)
- > Confusion Metrix
- > ROC curve Receiver Operating Characteristic
- > ROC AUC ROC Area Under Curve
- > PR AUC Area Under the Precision-Recall curve
- MCC Mathew's Correlation Coefficient -> (TP * TN FP * FN) / sqrt((TP + FP) * (TP + FN) * (TN + FP) * (TN + FN))
- \triangleright Log loss Binary Cross Entropy -> $(1/n) * \Sigma (y_i * log(p_i) + (1 y_i) * log(1 p_i))$
- \triangleright Categorical Cross entropy -> Σ (y i * log(p i))
- ➤ Hinge Loss -> max(0, 1 y_i * f(x_i))

Algorithms

- Logistic Regression
 - Logistic Function (Sigmoid)
 - Maximum Likelihood estimation
 - o Odds
 - Odds ratio
 - Logit
 - Newton-Raphson Method
 - Regularized Logistic Regression (Ridge, Lasso)
 - o Confidence intervals
 - Coefficients
 - Threshold

- Link Function
- o Regularization
- Multinomial Logistic Regression
- Ordinary Regression
- Log Likelihood
- Deviance
- Deviance Residuals
- Akaike Information Criterion (AIC)
- Wald Test
- C- Static (Concordance Static)
- o ROC and AUC
- o Penalty

> KNN

- Nearest Neighbors
- o Distance Metric (Euclidean, Manhattan, Minkowski, Mahalanobis)
- o k-Value
- Majority Vote
- Lazy Learning
- o Curse of Dimensionality
- Weighted k-NN
- o Data Scaling
- o Local vs Global Behaviour
- Decision Boundary
- o Parzen Window
- Local Outlier Factor(LOF)
- Radius Neighbors Classifier
- Ball Tree and KD-Tree
- o Distance Weighting
- k-D tree
- o Cover Tree
- Voronoi Tessellation
- Reverse Nearest Neighbors
- Dynamic Time Warping (DTW)
- Instance-based learning

Naive Bayes

- Bayes' Theorem
- Conditional Independence
- Prior Probability
- Posterior Probability
- o Probability Distribution (Gaussian, Multinomial)
- Laplace Smoothing (Adaptive Smoothing)
- Text Classification
- o Spam Detection
- Bag of Words
- o Feature Independence Assumption
- Maximum Likelihood Estimation (MLE)

- Bayesian Inference
- Text Mining
- Laplace Estimation
- Log-odd ratio
- Bayesian Network
- Class Conditional Independence
- Bernoulli Naive Bayes
- Gaussian Naive Bayes
- Multinomial Naive Bayes
- MAP Estimation (Maximum A Posteriori)
- Bayesian Information Criterion (BIC)

Parameter

- Smoothing Parameter (Alpha): Controls additive smoothing (Laplace smoothing).
- o Fit Prior: Whether to learn class prior probabilities.
- Class Prior: User-specified class prior probabilities.

Logistic Regression

Advantages

- > Simple and interpretable
- ➤ Works well in small sample sets
- > Can handle both binary and multiclass problems
- > Robust to outliers

Disadvantages

- > Assumes a linearity
- > It does not capture complex relations
- > Multicollinearity
- > Vulnerable to overfitting

Types

- > Binary Logistic regression
- Multinomial logistic regression
- Ordinal logistic regression: used when the dependent variable is ordinal
- Penalized Logistic regression: Lasso and ridge
- ➤ Logistic regression with interaction terms: Add interaction terms to the independent variables. Eg:- Multiply 2 columns

Terms

- ightharpoonup Logistic Function (Sigmoid) : $f(x) = 1 / (1 + \exp(-x))$
- > Maximum Likelihood estimation: Find the best fitting model parameters that maximize the likelihood of the observed data.
- ➤ Odds: the likelihood of an event occurring compared to the likelihood of it not occurring. In binary outcome - odds= P(Y=1) / (1- P(Y-1))

- > Odds ratio: Measure of the change in the odds of an event occurring due to the one-unit change in a predictor variable
- > Odds Radio = exp (Coefficient of the predictor variable)
- ightharpoonup Logit: Natural logarithm (log base e) of the odds of the dependent variable logit (p) = In (p / (1 p))
 - Where p is the probability of the binary outcome 1 and 1-p is the binary outcome 0
- Newton-Raphson Method: It is an iterative optimization technique used to find the maximum likelihood estimates of the parameters in logistic regression
- Regularized Logistic Regression (Ridge, Lasso): In ridge and lasso logistic regression, it adds a penalty term to the logistic regression cost function that discourages large values of coefficients
- Confidence intervals: Provides a range of values within which we can be reasonably confident that the true parameter values lie.
 - Confidence Interval=Estimated Parameter±(Critical Value×Standard Error)
- > Coefficients: represent the strength and direction of the relation between predictor variables and the log odds of the binary outcome
- > Threshold: It is the decision boundary, usually considered as 0.5
- Link Function: connects the linear combination of predictor variables. Usually use sigmoid in logistic regression
- ➤ Regularization: It is adding a penalty to prevent overfitting. Ridge adds an L2 penalty (squared) and lasso adds an L1 penalty (absolute) to the cost function.
- Multinomial Logistic Regression: Allows more than 2 categories in the dependent variable
- > Ordinary Regression: refers to linear regression
- ➤ Log Likelihood: yi . In (pi) + (1 yi) . In(1 pi)

 Where yi is the actual outcome and pi is the predicted probability
- ➤ Deviance: Measure the goodness of fit in logistic regression Deviance = - 2 [In (L full_mode) - In(L null_model)]

L refers to the log likely hood

The null model is intercept-only, The probability of the outcome being 1 in the null model is the overall proportion of 1s in the data

> Deviance Residuals: the difference between the observed outcome and the predicted outcome based on the model

Deviance Residuali = 2 [yi In (yi / pi) + (1 - yi) In ((1 - yi) / (1 - pi))]

Where yi is the observed outcome for the ith observation (0 or 1)

pi is the predicted probability of the outcome being 1 in the observation

➤ Akaike Information Criterion (AIC): Model Selection criterion used to compare different models. Lower AIC indicates a better trade-off between model fit AIC = - 2 x Log likelihood + 2 x Number of parameters

Where the number of parameters refers to the intercept term + number of coefficients

Wald Test: Used to assess the significance of individual coefficients in logistic regression

W = ((specific coeff - Null hypothesis) / Standard Error) Where the Null hypothesis will usually be 0

- > C- Static (Concordance Static): Associated with ROC
- > ROC and AUC: ROC stands for (Reciever operating Characteristic), it is a graphical tool for evaluating the performance of binary classification models

- AUC refers to the Area Under the Curve of ROC. It quantifies the model's ability to discriminate between the 2 outcome classes
- Penalty: Refers to a regularization term added into the cost function

Hyperparameters

- > Penalty (Regularization Type): L1 or L2 regularization.
- > C (Inverse of Regularization Strength): Controls the trade-off between fitting the training data and preventing overfitting.
- > Solver: Optimization algorithm (e.g., 'liblinear', 'newton-cg', 'sag', 'lbfgs').
 - Liblinear (Library for Large Linear Classification): suited for binary classification
 - Newton-cg (Newton-Conjugate Gradient): uses the Newton-Raphson method, well suited for multi-class problems
 - Sag(Stochastic Average Gradient): designed for large datasets, uses SGD
 - Lbfgs (Limited-memory Broyden–Fletcher–Goldfarb–Shanno): Works well with many features. It is also a memory solver
- ➤ Multi_class: Specifies the strategy for multiclass classification ('ovr' or 'multinomial').
- Class Weight: Optional weights for classes.
- > Max Iterations: Maximum number of iterations for the solver.
- > Dual: Formulation ('True' or 'False') for the dual problem

KNN

Advantages

- Simple to understand and implement
- > No training period
- No assumption about data distribution
- > Robust to noisy data
- > Effective multiclass classification

Disadvantages

- Sensitivity to feature scaling
- > The optimal value for k
- > Curse of dimensionality
- Not suitable for large dataset

Terms

- Nearest Neighbors: data points from the training dataset that are closest to the given input data point in features
- > Distance Metric (Euclidean, Manhattan, Minkowski, Mahalanobis): Math formula used to measure the distance between 2 data points
- > k-Value: Number of nearest neighbors
- > Majority Vote: predicts by taking the majority vote from the class labels
- ➤ Lazy Learning: KNN is a lazy learner because it doesn't build a model during the training
- > Curse of Dimensionality: challenges arise as the number of features increases
- Weighted k-NN: Assign different weights to the nearest neighbors while predicting

- Local vs Global Behaviour: KNN exhibits local behavior as it considers only a subset of nearby points to make predictions. In a decision tree, exhibit global behavior by considering all of them
- Decision Boundary: Boundary that separates different classes in feature space
- > Parzen Window: Technique that can be used to estimate the probability density function, used for density-based classification or regression
- Local Outlier Factor(LOF): An algorithm used to detect anomalies and outliers
- > Radius Neighbors Classifier: A variation of KNN where we only specify the radius instead of k neighbors
- > Ball Tree and KD-Tree: Data structure can be used to increase the performance of KNN
- > Distance Weighting: In weighted KNN, the contribution of each neighbor to the majority vote is weighted based on their distance.
- Cover Tree: A data structure design for KNN
- > Voronoi Tessellation: divides the features into regions, each corresponding to different data points.
- > Reverse Nearest Neighbors: Instead of finding the neighbor, find a data point in which the given data point is one of their nearest neighbors
- > Dynamic Time Warping (DTW): It is a distance metric used in time series data
- > Instance-based learning: KNN is an instance-based learning algorithm

Hyperparameters

- Number of Neighbors (k): Number of nearest neighbors to consider.
- > Distance Metric: The distance metric used (e.g., Euclidean, Manhattan).

$$\circ$$
 Euclidean (L2 Norm) : $\sqrt{(x_1-x_2)^2+(y_1-y_2)^2+(z_1-z_2)^2+\dots}$

$$\begin{array}{l} \circ \quad \text{Manhattan (L1 Norm): } |(x_1-x_2)|+|(y_1-y_2)|+|(z_1-z_2)|+\dots \\ \circ \quad \text{Minkowski: } \sqrt[p]{(|x_1-x_2|)^p+(|y_1-y_2|)^p+(|z_1-z_2|)^p+\dots} \end{array}$$

• Minkowski:
$$\sqrt[p]{(|x_1-x_2|)^p+(|y_1-y_2|)^p+(|z_1-z_2|)^p+\dots}$$

o Mahalanobis:

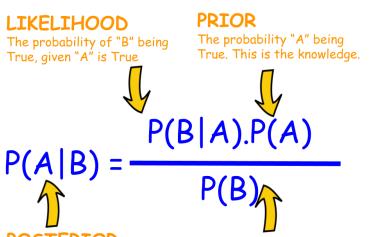
$$\sqrt{(x_1-x_2)^2 \cdot \Sigma_x^{-1} \cdot (x_1-x_2) + (y_1-y_2)^2 \cdot \Sigma_y^{-1} \cdot (y_1-y_2) + \dots}$$

- Weighting: How to weight neighbors ('uniform' or 'distance').
- > Algorithm: Algorithm used for nearest neighbor search (e.g., 'ball_tree', 'kd_tree', 'brute').
- ➤ Leaf Size (for 'ball tree' or 'kd tree'): Size of leaves in the data structure.
- > P (for Minkowski distance): Power parameter for Minkowski distance.

Types

- > Standardized KNN: Normal
- Weighted KNN: have higher weight for nearest value
- Radius Neighbour: check the radius of the point
- > KNN for imbalance: modify the distance metric

Naive Bayes



POSTERIOR

The probability of "A" being True, given "B" is True

MARGINALIZATION

The probability "B" being True.

Advantages

- > Works well with a small dataset
- > Handle high-dimensional data
- > Low computation power compared to others
- > Robust to irrelevant features

Disadvantages

- > Sensitivity of data quality
- > Zero probability problem
- > Class Imbalance
- > Ineffective for regression

Types

Gaussian: Fon continuousMultinomial: for discrete

Terms

- > Bayes' Theorem: Fundamental theorem for naive Bayes classifier
- Conditional Independence: Assumes features are independent of each other in the given class
- > Prior Probability: The probability of a class occurring before considering any evidence.
- > Posterior Probability: The probability of a class occurring after considering the evidence.
- > Probability Distribution (Gaussian, Multinomial): types of probability distributions
- ➤ Laplace Smoothing (Adaptive Smoothing): A technique to handle "zero probability problem"
- > Bag of Words: A representation of text data where the order of words is ignored.
- Maximum Likelihood Estimation (MLE): A method used to estimate probability in naive Bayes by counting the occurrences of events

- > Text Mining: The process of extracting information from text data
- > Laplace Estimation: Another name for Laplace Smoothing
- > Log-odd ratio: A measure used in text classification

ODDS =
$$\frac{\text{Probability of winning}}{\text{Probability of losing}} = \frac{p}{1-p}$$

Where p = probability of winning (event occurring)

- > Bayesian Network: A graphical model representing probabilistic relationships among a set of variables
- Class Conditional Independence: Features are conditionally independent in the given class
- > Bernoulli Naive Bayes: A variant of naive Bayes for binary data
- > MAP Estimation (Maximum A Posteriori): An approach in Bayesian statistics that estimates the most likely values for model parameters.
- ➤ Bayesian Information Criterion (BIC): A model selection criterion that penalizes model complexity.

Hyperparameters

- Smoothing Parameter (Alpha): Controls additive smoothing (Laplace smoothing).
- > Fit Prior: Whether to learn class prior probabilities.
- Class Prior: User-specified class prior probabilities.