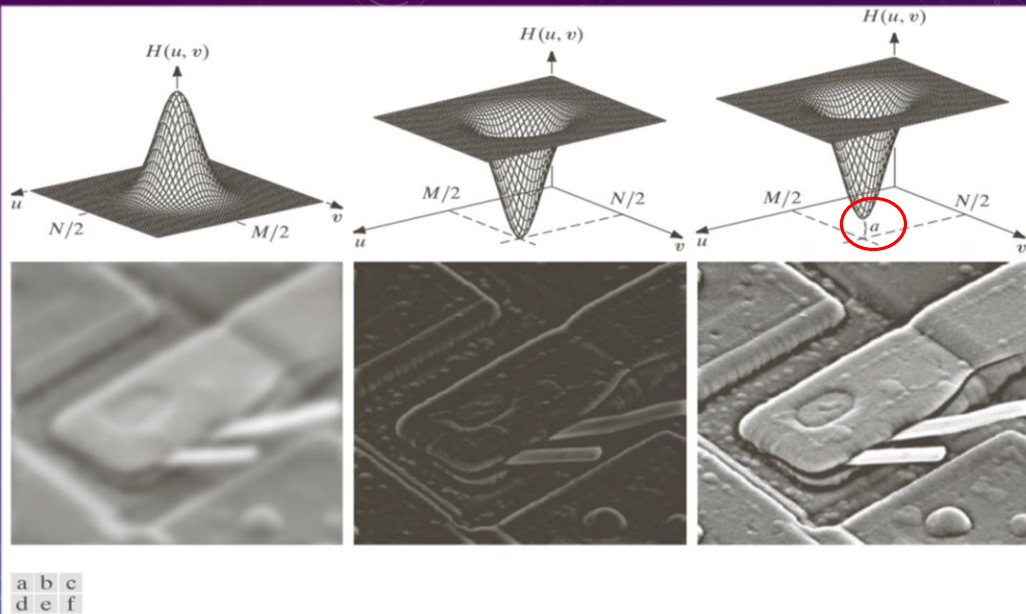


# FREQUENCY DOMAIN FILTERING

- Low frequencies in the transform domain are related to **slowly varying** intensity components
- High frequencies are caused by **sharp** transitions in intensity, such as edges and noise
- Lowpass filter would **blur** an image
- Highpass filter would enhance sharp **detail**, but cause a reduction in contrast in the image



**FIGURE 4.31** Top row: frequency domain filters. Bottom row: corresponding filtered images obtained using Eq. (4.7-1). We used  $a = 0.85$  in (c) to obtain (f) (the height of the filter itself is 1). Compare (f) with Fig. 4.29(a).

## FREQUENCY DOMAIN

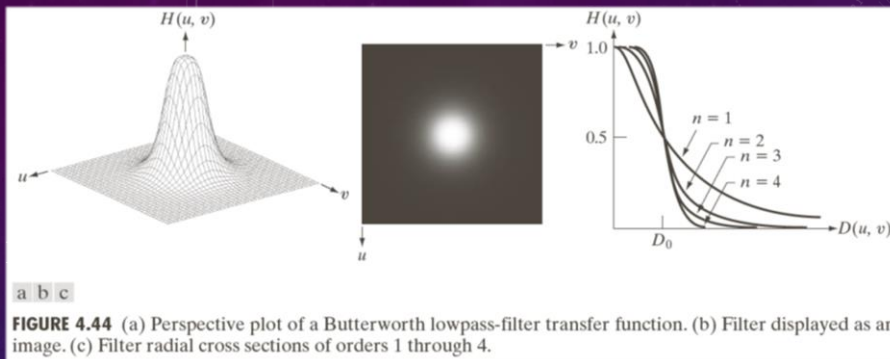
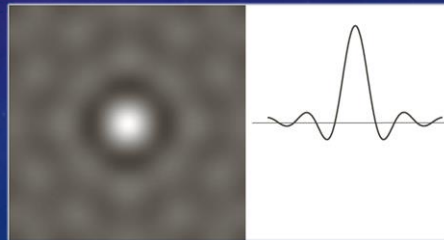
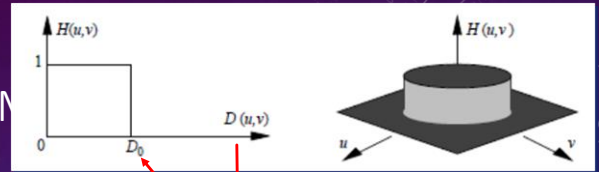
- Ideal LPF:



F:

$$H(u, v) = \begin{cases} 1 & \text{if } D(u, v) \leq D_0 \\ 0 & \text{if } D(u, v) > D_0 \end{cases}$$

$$D(u, v) = \sqrt{(u - P/2)^2 + (v - Q/2)^2}$$



- Butterworth LPF:

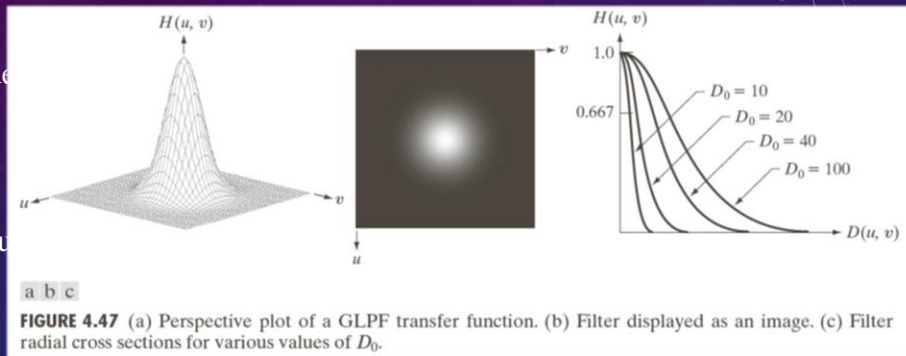
$$H(u, v) = \frac{1}{1 + [D(u, v) / D_0]^{2n}}$$

- Gaussian LPF

## FREQUENCY DOMAIN FILTERING

- Ideal

- Butterworth



- Gaussian LPF

$$H(u, v) = e^{-\frac{D^2(u, v)}{2D_0^2}}$$

$$H(u, v) = \exp \left\{ - \left[ \frac{D(u, v)}{D_0} \right]^n \right\}$$

## FREQUENCY DOMAIN FILTERING

- Ideal LPF:

$$H(u, v) = \begin{cases} 1 & \text{if } D(u, v) \leq D_0 \\ 0 & \text{if } D(u, v) > D_0 \end{cases}$$

- Butterworth LPF:

$$H(u, v) = \frac{1}{1 + [D(u, v) / D_0]^{2n}}$$

- Gaussian LPF

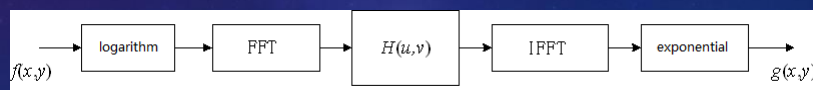
$$H(u, v) = e^{-\frac{D^2(u, v)}{2D_0^2}}$$

$$H_{HP}(u, v) = 1 - H_{LP}(u, v)$$

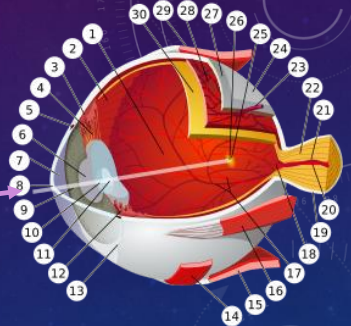


## HOMOMORPHIC FILTERING

- Homomorphic filtering is a generalized technique for signal and image processing, involving a **nonlinear** mapping to a different domain in which **linear** filter techniques are applied, followed by mapping back to the original domain.
- It **simultaneously** normalizes the brightness across an image and increases contrast



## BASIC CONCEPTS



$$I = f(x, y, \lambda, t)$$

$$0 < f(x, y) < \infty$$

- $I(.)$**  represents the **spatial energy distribution** of an image source of **radiant**.

## HOMOMORPHIC FILTERING

- **Illumination** and **reflectance** combine multiplicatively :

$$f(x, y) = f_i(x, y) \cdot f_r(x, y)$$

$$0 < f_i(x, y) < \infty$$

$$0 < f_r(x, y) < 1$$

- Illumination  $f_i(x, y)$  and reflectance  $f_r(x, y)$  are not separable, but their approximate locations in the frequency domain may be located.

## HOMOMORPHIC FILTERING

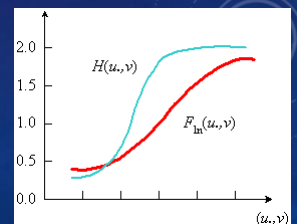
$$\ln f(x, y) = \ln[f_i(x, y) \cdot f_r(x, y)] = \ln f_i(x, y) + \ln f_r(x, y)$$

$$\begin{aligned} F_{\ln}(u, v) &= F[\ln f(x, y)] = F[\ln f_i(x, y) + \ln f_r(x, y)] \\ &= F_{i,\ln}(u, v) + F_{r,\ln}(u, v) \end{aligned}$$

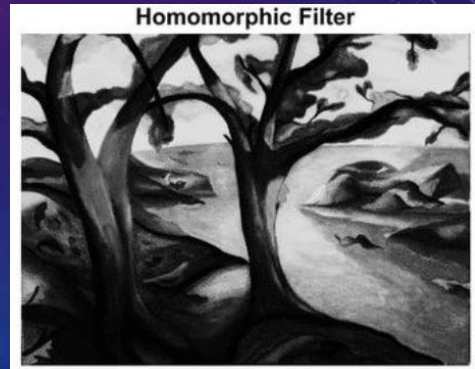
$$\begin{aligned} G_{\ln}(u, v) &= F_{i,\ln}(u, v) \cdot H(u, v) + F_{r,\ln}(u, v) \cdot H(u, v) \\ &= G_{i,\ln}(u, v) + G_{r,\ln}(u, v) \end{aligned}$$

$$\begin{aligned} F^{-1}[G_{\ln}(u, v)] &= \ln g_i(x, y) + \ln g_r(x, y) \\ &= \ln[g_i(x, y) \cdot g_r(x, y)] \end{aligned}$$

$$g(x, y) = \exp\{\ln[g_i(x, y) \cdot g_r(x, y)]\} = g_i(x, y) \cdot g_r(x, y)$$



## HOMOMORPHIC FILTERING



## SUMMARY

- Spatial domain processing
  - Spatial filtering
    - image sharpening (gradient/laplacian/unsharp masking & highboost filtering), smoothing (averaging/median filter)
  - Intensity transformation
    - Contrast manipulation, thresholding, histogram equalization, histogram specification
- Frequency domain processing
  - Homomorphic filtering

$$g(x, y) = T[f(x, y)]$$

$$g(x, y) = F^{-1}\{T[F[f(x, y)]]\}$$