

Using RQT, an R/Bioconductor package for gene-level meta-analysis

Ilya Y. Zhbannikov

December 7, 2016

1 Overview

Despite the recent advances of modern GWAS methods, it is still remains an important problem of addressing calculation an effect size and corresponding p-value for the whole gene rather than for single variant. We developed an R-package `rqt`, which offers gene-level GWAS meta-analysis. The package can be easily included into bioinformatics pipeline or used as stand-alone. Contact: ilya.zhbannikov@duke.edu for questions of usage the `rqt` or any other issues.

Below we provide several examples that show GWAS meta-analysis on gene-level layer.

1.1 Methods in brief

The workflow of gene-level meta analysis consists of the following steps: (i) reducing the number of predictors, thereby alleviating correlation problem in variants (accounting for LD); (ii) then the regression model is fitted on the reduced dataset to obtain corresponding regression coefficient ("effect sizes"); (iii) these coefficients are then to be pooled into a total index representing a total gene-level effect size and corresponding statistics is calculated. P- and q- values are then calculated using this statistics from asymptotic approximation or permutation procedure; (iv) the final step is combining gene-level p-values calculated from each study with Fisher's combined probability method.

2 Installation

2.1 Most-recent version from GitHub

```
> require(devtools)
> devtools::install_github("izhbannikov/rqt")
```

3 Data description

3.1 Single dataset

In `rqt` requires two datasets: phenotype (a n by 1) matrix and genotype (a n by m) matrix, where n - is the total number of individuals in the study and m is the total number of genetic variants. Optionally, `rqt` can accept covariates, in form of n by k matrix, where k is the total number of covariates used in the study. Phenotype can be dichotomous (0/1, where 1 indicates control and 0 case).

3.2 Meta-analysis

In meta-analysis, `rqt` requires a list of M (M - number of datasets used in meta-analysis) and optionally it accepts covariates in form described above.

4 Examples

4.1 Gene-level analysis on a single dataset

4.2 Dichotomous phenotype

```
> library(rqt)
> data <- read.table(system.file("extdata/test.bin1.dat",package="rqt"),
+   header = TRUE)
> pheno <- data$pheno
> geno <- data[, 2:dim(data)[2]]
> obj <- rqtClass(phenotype=pheno, genotype=geno)
> res <- rqtTest(obj, method="pca", out.type = "D")
> print(res)
```

Phenotype:

```
[1] 1 1 1 1 1 1
...
```

Genotype:

| | snp1 | snp2 | snp3 | snp4 | snp5 | snp6 | snp7 | snp8 | snp9 | snp10 | snp11 | snp12 | snp13 | snp14 |
|---|------|------|------|------|------|------|------|------|------|-------|-------|-------|-------|-------|
| 1 | 0 | 0 | 0 | 1 | 0 | 2 | 1 | 0 | 0 | 0 | 2 | 1 | 2 | 0 |
| 2 | 1 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| 3 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 1 | 0 | 0 |
| 4 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 |
| 5 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 1 | 0 | 0 |
| 6 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 1 | 0 |

| | snp15 | snp16 | snp17 | snp18 | snp19 | snp20 | snp21 | snp22 | snp23 | snp24 | snp25 | snp26 | snp27 |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 0 | 2 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 2 | 1 |
| 2 | 0 | 0 | 2 | 1 | 2 | 1 | 0 | 1 | 0 | 0 | 0 | 2 | 1 |
| 3 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 1 | 0 |
| 4 | 0 | 0 | 1 | 0 | 0 | 2 | 0 | 1 | 0 | 0 | 0 | 1 | 0 |
| 5 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 2 |
| 6 | 0 | 2 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 2 | 0 |

| | snp28 | snp29 | snp30 | snp31 | snp32 | snp33 | snp34 | snp35 | snp36 | snp37 | snp38 | snp39 | snp40 |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 |
| 2 | 1 | 2 | 0 | 0 | 0 | 1 | 2 | 1 | 2 | 0 | 1 | 1 | 0 |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 | 2 | 0 | 0 |
| 4 | 2 | 0 | 0 | 0 | 1 | 2 | 2 | 0 | 1 | 1 | 1 | 1 | 0 |
| 5 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| 6 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 2 | 0 |

| | snp41 | snp42 | snp43 | snp44 | snp45 | snp46 | snp47 | snp48 | snp49 | snp50 | snp51 | snp52 | snp53 |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 |
| 2 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 2 | 0 | 1 | 0 | 1 | 0 |
| 3 | 0 | 1 | 0 | 1 | 0 | 2 | 1 | 1 | 1 | 0 | 0 | 0 | 1 |
| 4 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 2 | 0 | 1 | 0 | 2 |
| 5 | 2 | 2 | 0 | 0 | 0 | 1 | 2 | 1 | 0 | 0 | 0 | 0 | 1 |
| 6 | 1 | 1 | 2 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 1 |

| | snp54 | snp55 | snp56 | snp57 | snp58 | snp59 | snp60 | snp61 | snp62 | snp63 | snp64 | snp65 | snp66 |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 1 | 1 |
| 2 | 2 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 2 | 2 | 1 |
| 3 | 2 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 |
| 4 | 1 | 1 | 0 | 0 | 0 | 0 | 2 | 1 | 0 | 1 | 0 | 0 | 2 |

```

5      1      1      1      0      0      0      2      1      1      0      0      1      1
6      0      1      1      0      0      0      0      0      0      0      1      2      1
  snp67 snp68 snp69 snp70 snp71 snp72 snp73 snp74 snp75 snp76 snp77 snp78 snp79
1      1      0      1      1      2      1      1      1      0      0      2      1      1
2      1      0      1      0      1      0      0      0      0      1      1      2      1
3      1      0      1      2      1      0      1      1      0      0      0      0      1
4      1      0      0      1      1      1      0      0      0      0      0      1      0
5      0      0      1      1      0      0      1      0      1      0      0      1      0
6      1      0      0      0      0      0      1      1      1      1      1      1      2
  snp80 snp81 snp82 snp83 snp84 snp85 snp86 snp87 snp88 snp89 snp90 snp91 snp92
1      1      0      1      1      0      1      1      0      0      0      1      0      1
2      1      2      0      0      0      1      2      0      2      1      0      0      2
3      1      0      0      0      0      2      0      0      2      0      0      0      0
4      1      2      0      1      0      1      2      0      0      0      0      0      0
5      2      0      1      0      0      2      0      0      0      0      1      0      0
6      1      0      0      1      0      0      0      0      2      0      1      0      0
  snp93 snp94 snp95 snp96 snp97 snp98 snp99 snp100
1      1      0      0      0      1      0      1      1
2      1      0      0      0      0      1      1      2
3      1      1      0      0      1      2      0      0
4      1      0      0      0      1      0      0      0
5      1      0      0      1      1      2      1      1
6      0      0      0      1      1      0      1      1
...

```

Covariates:
data frame with 0 columns and 0 rows

Results:

```

$Qstatistic
      Q1      Q2      Q3
1 0.9086994 0.9938212 0.9086994

$p.value
      p.Q1      p.Q2      p.Q3
1 0.3404597 0.9285409 0.5654533

```

4.3 Continuous phenotype

```

> library(rqt)
> data <- read.table(system.file("extdata/test.cont1.dat",package="rqt"),
+   header = TRUE)
> pheno <- data$pheno
> geno <- data[, 2:dim(data)[2]]
> obj <- rqtClass(phenotype=pheno, genotype=geno)
> res <- rqtTest(obj, method="pca", out.type = "C")
> print(res)

```

Phenotype:
[1] 3.422452 2.457394 2.708564 4.589394 5.461723 4.438707

...

Genotype:

| | snp1 | snp2 | snp3 | snp4 | snp5 | snp6 | snp7 | snp8 | snp9 | snp10 | snp11 | snp12 | snp13 | snp14 |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 0 | 0 | 0 | 1 | 0 | 2 | 1 | 0 | 0 | 0 | 2 | 1 | 2 | 0 |
| 2 | 1 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| 3 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 1 | 0 | 0 |
| 4 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 |
| 5 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 1 | 0 | 0 |
| 6 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 1 | 0 |
| | snp15 | snp16 | snp17 | snp18 | snp19 | snp20 | snp21 | snp22 | snp23 | snp24 | snp25 | snp26 | snp27 | |
| 1 | 0 | 2 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 2 | 1 | |
| 2 | 0 | 0 | 2 | 1 | 2 | 1 | 0 | 1 | 0 | 0 | 0 | 2 | 1 | |
| 3 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 1 | 0 | |
| 4 | 0 | 0 | 1 | 0 | 0 | 2 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | |
| 5 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 2 | |
| 6 | 0 | 2 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 2 | 0 | |
| | snp28 | snp29 | snp30 | snp31 | snp32 | snp33 | snp34 | snp35 | snp36 | snp37 | snp38 | snp39 | snp40 | |
| 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | |
| 2 | 1 | 2 | 0 | 0 | 0 | 1 | 2 | 1 | 2 | 0 | 1 | 1 | 0 | |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 | 2 | 0 | 0 | |
| 4 | 2 | 0 | 0 | 0 | 1 | 2 | 2 | 0 | 1 | 1 | 1 | 1 | 0 | |
| 5 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | |
| 6 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 2 | 0 | |
| | snp41 | snp42 | snp43 | snp44 | snp45 | snp46 | snp47 | snp48 | snp49 | snp50 | snp51 | snp52 | snp53 | |
| 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | |
| 2 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 2 | 0 | 1 | 0 | 1 | 0 | |
| 3 | 0 | 1 | 0 | 1 | 0 | 2 | 1 | 1 | 1 | 0 | 0 | 0 | 1 | |
| 4 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 2 | 0 | 1 | 0 | 2 | |
| 5 | 2 | 2 | 0 | 0 | 0 | 1 | 2 | 1 | 0 | 0 | 0 | 0 | 1 | |
| 6 | 1 | 1 | 2 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | |
| | snp54 | snp55 | snp56 | snp57 | snp58 | snp59 | snp60 | snp61 | snp62 | snp63 | snp64 | snp65 | snp66 | |
| 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 1 | 1 | |
| 2 | 2 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 2 | 2 | 1 | |
| 3 | 2 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | |
| 4 | 1 | 1 | 0 | 0 | 0 | 0 | 2 | 1 | 0 | 1 | 0 | 0 | 2 | |
| 5 | 1 | 1 | 1 | 0 | 0 | 0 | 2 | 1 | 1 | 0 | 0 | 1 | 1 | |
| 6 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 2 | 1 | |
| | snp67 | snp68 | snp69 | snp70 | snp71 | snp72 | snp73 | snp74 | snp75 | snp76 | snp77 | snp78 | snp79 | |
| 1 | 1 | 0 | 1 | 1 | 2 | 1 | 1 | 1 | 0 | 0 | 2 | 1 | 1 | |
| 2 | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 2 | 1 | |
| 3 | 1 | 0 | 1 | 2 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | |
| 4 | 1 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | |
| 5 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 0 | |
| 6 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | |
| | snp80 | snp81 | snp82 | snp83 | snp84 | snp85 | snp86 | snp87 | snp88 | snp89 | snp90 | snp91 | snp92 | |
| 1 | 1 | 0 | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | |
| 2 | 1 | 2 | 0 | 0 | 0 | 1 | 2 | 0 | 2 | 1 | 0 | 0 | 2 | |
| 3 | 1 | 0 | 0 | 0 | 0 | 2 | 0 | 0 | 2 | 0 | 0 | 0 | 0 | |
| 4 | 1 | 2 | 0 | 1 | 0 | 1 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | |
| 5 | 2 | 0 | 1 | 0 | 0 | 2 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | |

| | | | | | | | | | | | | | |
|-----|-------|-------|-------|-------|-------|-------|-------|--------|---|---|---|---|---|
| 6 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 2 | 0 | 1 | 0 | 0 |
| | snp93 | snp94 | snp95 | snp96 | snp97 | snp98 | snp99 | snp100 | | | | | |
| 1 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | | | | | |
| 2 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 2 | | | | | |
| 3 | 1 | 1 | 0 | 0 | 1 | 2 | 0 | 0 | | | | | |
| 4 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | | | | | |
| 5 | 1 | 0 | 0 | 1 | 1 | 2 | 1 | 1 | | | | | |
| 6 | 0 | 0 | 0 | 1 | 1 | 0 | 1 | 1 | | | | | |
| ... | | | | | | | | | | | | | |

Covariates:
data frame with 0 columns and 0 rows

Results:

```
$Qstatistic
      Q1      Q2      Q3
1 0.2846585 2.389537 2.219594

$p.value
      p.Q1      p.Q2      p.Q3
1 0.593664 0.7022459 0.2561996
```

4.4 Preprocessing with Partial Least Square regression (PLS)

This method is used for continous outcome, i.e. out.type = "C".

```
> library(rqt)
> data <- read.table(system.file("extdata/test.cont1.dat", package="rqt"),
+   header = TRUE)
> pheno <- data$pheno
> geno <- data[, 2:dim(data)[2]]
> obj <- rqtClass(phenotype=pheno, genotype=geno)
> res <- rQTest(obj, method="pls", out.type = "C")
> print(res)
```

Phenotype:
[1] 3.422452 2.457394 2.708564 4.589394 5.461723 4.438707
...

Genotype:

| | | | | | | | | | | | | | | |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| | snp1 | snp2 | snp3 | snp4 | snp5 | snp6 | snp7 | snp8 | snp9 | snp10 | snp11 | snp12 | snp13 | snp14 |
| 1 | 0 | 0 | 0 | 1 | 0 | 2 | 1 | 0 | 0 | 0 | 2 | 1 | 2 | 0 |
| 2 | 1 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| 3 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 1 | 0 | 0 |
| 4 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 |
| 5 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 1 | 0 | 0 |
| 6 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 1 | 0 |
| | snp15 | snp16 | snp17 | snp18 | snp19 | snp20 | snp21 | snp22 | snp23 | snp24 | snp25 | snp26 | snp27 | |
| 1 | 0 | 2 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 2 | 1 | |
| 2 | 0 | 0 | 2 | 1 | 2 | 1 | 0 | 1 | 0 | 0 | 0 | 2 | 1 | |

| | | | | | | | | | | | | | |
|---|-------|-------|-------|-------|-------|-------|-------|--------|-------|-------|-------|-------|-------|
| 3 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 1 | 0 |
| 4 | 0 | 0 | 1 | 0 | 0 | 2 | 0 | 1 | 0 | 0 | 0 | 1 | 0 |
| 5 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 2 |
| 6 | 0 | 2 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 2 | 0 |
| | snp28 | snp29 | snp30 | snp31 | snp32 | snp33 | snp34 | snp35 | snp36 | snp37 | snp38 | snp39 | snp40 |
| 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 |
| 2 | 1 | 2 | 0 | 0 | 0 | 1 | 2 | 1 | 2 | 0 | 1 | 1 | 0 |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 | 2 | 0 | 0 |
| 4 | 2 | 0 | 0 | 0 | 1 | 2 | 2 | 0 | 1 | 1 | 1 | 1 | 0 |
| 5 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| 6 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 2 | 0 |
| | snp41 | snp42 | snp43 | snp44 | snp45 | snp46 | snp47 | snp48 | snp49 | snp50 | snp51 | snp52 | snp53 |
| 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 |
| 2 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 2 | 0 | 1 | 0 | 1 | 0 |
| 3 | 0 | 1 | 0 | 1 | 0 | 2 | 1 | 1 | 1 | 0 | 0 | 0 | 1 |
| 4 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 2 | 0 | 1 | 0 | 2 |
| 5 | 2 | 2 | 0 | 0 | 0 | 1 | 2 | 1 | 0 | 0 | 0 | 0 | 1 |
| 6 | 1 | 1 | 2 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 1 |
| | snp54 | snp55 | snp56 | snp57 | snp58 | snp59 | snp60 | snp61 | snp62 | snp63 | snp64 | snp65 | snp66 |
| 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 1 | 1 |
| 2 | 2 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 2 | 2 | 1 |
| 3 | 2 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 |
| 4 | 1 | 1 | 0 | 0 | 0 | 0 | 2 | 1 | 0 | 1 | 0 | 0 | 2 |
| 5 | 1 | 1 | 1 | 0 | 0 | 0 | 2 | 1 | 1 | 0 | 0 | 1 | 1 |
| 6 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 2 | 1 |
| | snp67 | snp68 | snp69 | snp70 | snp71 | snp72 | snp73 | snp74 | snp75 | snp76 | snp77 | snp78 | snp79 |
| 1 | 1 | 0 | 1 | 1 | 2 | 1 | 1 | 1 | 0 | 0 | 2 | 1 | 1 |
| 2 | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 2 | 1 |
| 3 | 1 | 0 | 1 | 2 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 1 |
| 4 | 1 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| 5 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 0 |
| 6 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 2 |
| | snp80 | snp81 | snp82 | snp83 | snp84 | snp85 | snp86 | snp87 | snp88 | snp89 | snp90 | snp91 | snp92 |
| 1 | 1 | 0 | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 | 1 |
| 2 | 1 | 2 | 0 | 0 | 0 | 1 | 2 | 0 | 2 | 1 | 0 | 0 | 2 |
| 3 | 1 | 0 | 0 | 0 | 0 | 2 | 0 | 0 | 2 | 0 | 0 | 0 | 0 |
| 4 | 1 | 2 | 0 | 1 | 0 | 1 | 2 | 0 | 0 | 0 | 0 | 0 | 0 |
| 5 | 2 | 0 | 1 | 0 | 0 | 2 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 6 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 2 | 0 | 1 | 0 | 0 |
| | snp93 | snp94 | snp95 | snp96 | snp97 | snp98 | snp99 | snp100 | | | | | |
| 1 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | | | | | |
| 2 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 2 | | | | | |
| 3 | 1 | 1 | 0 | 0 | 1 | 2 | 0 | 0 | | | | | |
| 4 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | | | | | |
| 5 | 1 | 0 | 0 | 1 | 1 | 2 | 1 | 1 | | | | | |
| 6 | 0 | 0 | 0 | 1 | 1 | 0 | 1 | 1 | | | | | |

...

Covariates:

data frame with 0 columns and 0 rows

Results:

\$Qstatistic

| | Q1 | Q2 | Q3 |
|---|-----------|----------|----------|
| 1 | 0.1910558 | 71.34471 | 16.59228 |

\$p.value

| | p.Q1 | p.Q2 | p.Q3 |
|---|-----------|--------------|------------|
| 1 | 0.6620394 | 1.293491e-05 | 0.00011429 |

4.5 Preprocessing with Partial Least Square Discriminant Analysis (PLS-DA)

This method of data preprocessing is used for dichotomous outcome.

```
> library(rqt)
> data <- read.table(system.file("extdata/test.bin1.dat",package="rqt"),
+   header=TRUE)
> pheno <- data$pheno
> geno <- data[, 2:dim(data)[2]]
> obj <- rqtClass(phenotype=pheno, genotype=geno)
> res <- rqtTest(obj, method="pls", out.type = "D", scale = TRUE)
```

| | R2X(cum) | R2Y(cum) | Q2(cum) | RMSEE | pre | ort | pR2Y | pQ2 |
|-------|----------|----------|---------|-------|-----|-----|------|-----|
| Total | 0.0187 | 0.301 | -0.292 | 0.2 | 1 | 0 | 1 | 0.7 |

```
> print(res)
```

Phenotype:

```
[1] 1 1 1 1 1 1
...
```

Genotype:

| | snp1 | snp2 | snp3 | snp4 | snp5 | snp6 | snp7 | snp8 | snp9 | snp10 | snp11 | snp12 | snp13 | snp14 |
|---|------|------|------|------|------|------|------|------|------|-------|-------|-------|-------|-------|
| 1 | 0 | 0 | 0 | 1 | 0 | 2 | 1 | 0 | 0 | 0 | 2 | 1 | 2 | 0 |
| 2 | 1 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| 3 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 1 | 0 | 0 |
| 4 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 |
| 5 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 1 | 0 | 0 |
| 6 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 1 | 0 |

| | snp15 | snp16 | snp17 | snp18 | snp19 | snp20 | snp21 | snp22 | snp23 | snp24 | snp25 | snp26 | snp27 |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 0 | 2 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 2 | 1 |
| 2 | 0 | 0 | 2 | 1 | 2 | 1 | 0 | 1 | 0 | 0 | 0 | 2 | 1 |
| 3 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 1 | 0 |
| 4 | 0 | 0 | 1 | 0 | 0 | 2 | 0 | 1 | 0 | 0 | 0 | 1 | 0 |
| 5 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 2 |
| 6 | 0 | 2 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 2 | 0 |

| | snp28 | snp29 | snp30 | snp31 | snp32 | snp33 | snp34 | snp35 | snp36 | snp37 | snp38 | snp39 | snp40 |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 |
| 2 | 1 | 2 | 0 | 0 | 0 | 1 | 2 | 1 | 2 | 0 | 1 | 1 | 0 |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 | 2 | 0 | 0 |
| 4 | 2 | 0 | 0 | 0 | 1 | 2 | 2 | 0 | 1 | 1 | 1 | 1 | 0 |
| 5 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |

| | | | | | | | | | | | | | |
|---|-------|-------|-------|-------|-------|-------|-------|--------|-------|-------|-------|-------|-------|
| 6 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 2 | 0 |
| | snp41 | snp42 | snp43 | snp44 | snp45 | snp46 | snp47 | snp48 | snp49 | snp50 | snp51 | snp52 | snp53 |
| 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 |
| 2 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 2 | 0 | 1 | 0 | 1 | 0 |
| 3 | 0 | 1 | 0 | 1 | 0 | 2 | 1 | 1 | 1 | 0 | 0 | 0 | 1 |
| 4 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 2 | 0 | 1 | 0 | 2 |
| 5 | 2 | 2 | 0 | 0 | 0 | 1 | 2 | 1 | 0 | 0 | 0 | 0 | 1 |
| 6 | 1 | 1 | 2 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 1 |
| | snp54 | snp55 | snp56 | snp57 | snp58 | snp59 | snp60 | snp61 | snp62 | snp63 | snp64 | snp65 | snp66 |
| 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 1 | 1 |
| 2 | 2 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 2 | 2 | 1 |
| 3 | 2 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 |
| 4 | 1 | 1 | 0 | 0 | 0 | 0 | 2 | 1 | 0 | 1 | 0 | 0 | 2 |
| 5 | 1 | 1 | 1 | 0 | 0 | 0 | 2 | 1 | 1 | 0 | 0 | 1 | 1 |
| 6 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 2 | 1 |
| | snp67 | snp68 | snp69 | snp70 | snp71 | snp72 | snp73 | snp74 | snp75 | snp76 | snp77 | snp78 | snp79 |
| 1 | 1 | 0 | 1 | 1 | 2 | 1 | 1 | 1 | 0 | 0 | 2 | 1 | 1 |
| 2 | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 2 | 1 |
| 3 | 1 | 0 | 1 | 2 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 1 |
| 4 | 1 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| 5 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 0 |
| 6 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 2 |
| | snp80 | snp81 | snp82 | snp83 | snp84 | snp85 | snp86 | snp87 | snp88 | snp89 | snp90 | snp91 | snp92 |
| 1 | 1 | 0 | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 | 1 |
| 2 | 1 | 2 | 0 | 0 | 0 | 1 | 2 | 0 | 2 | 1 | 0 | 0 | 2 |
| 3 | 1 | 0 | 0 | 0 | 0 | 2 | 0 | 0 | 2 | 0 | 0 | 0 | 0 |
| 4 | 1 | 2 | 0 | 1 | 0 | 1 | 2 | 0 | 0 | 0 | 0 | 0 | 0 |
| 5 | 2 | 0 | 1 | 0 | 0 | 2 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 6 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 2 | 0 | 1 | 0 | 0 |
| | snp93 | snp94 | snp95 | snp96 | snp97 | snp98 | snp99 | snp100 | | | | | |
| 1 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | | | | | |
| 2 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 2 | | | | | |
| 3 | 1 | 1 | 0 | 0 | 1 | 2 | 0 | 0 | | | | | |
| 4 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | | | | | |
| 5 | 1 | 0 | 0 | 1 | 1 | 2 | 1 | 1 | | | | | |
| 6 | 0 | 0 | 0 | 1 | 1 | 0 | 1 | 1 | | | | | |

...

Covariates:

data frame with 0 columns and 0 rows

Results:

\$Qstatistic

| | | | |
|---|----------|----------|----------|
| | Q1 | Q2 | Q3 |
| 1 | 11.12606 | 2.322913 | 11.12606 |

\$p.value

| | | | |
|---|--------------|--------------|--------------|
| | p.Q1 | p.Q2 | p.Q3 |
| 1 | 0.0008512339 | 0.0008512339 | 0.0008512339 |

4.6 Using additional covariates

Quite often, researchers want to supply not only genetic data but also specific covariates, representing some physiological parameters or environment (for example, to evaluate hypotheses of gene-environment interactions). In such cases, the package `rqt` can accept additional covariates, in form of N by K matrix, as provided below:

```
> library(rqt)
> data <- read.table(system.file("extdata/test.bin1.dat", package="rqt"),
+   header = TRUE)
> pheno <- data$pheno
> geno <- data[, 2:dim(data)[2]]
> covars <- read.table(system.file("extdata/test.cova1.dat", package="rqt"),
+   header=TRUE)
> obj <- rqtClass(phenotype=pheno, genotype=geno, covariates = covars)
> res <- rQTTest(obj, method="pca", out.type = "D")
> print(res)
```

Phenotype:

```
[1] 1 1 1 1 1 1
...
```

Genotype:

| | snp1 | snp2 | snp3 | snp4 | snp5 | snp6 | snp7 | snp8 | snp9 | snp10 | snp11 | snp12 | snp13 | snp14 |
|---|------|------|------|------|------|------|------|------|------|-------|-------|-------|-------|-------|
| 1 | 0 | 0 | 0 | 1 | 0 | 2 | 1 | 0 | 0 | 0 | 2 | 1 | 2 | 0 |
| 2 | 1 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| 3 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 1 | 0 | 0 |
| 4 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 |
| 5 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 1 | 0 | 0 |
| 6 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 1 | 0 |

| | snp15 | snp16 | snp17 | snp18 | snp19 | snp20 | snp21 | snp22 | snp23 | snp24 | snp25 | snp26 | snp27 |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 0 | 2 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 2 | 1 |
| 2 | 0 | 0 | 2 | 1 | 2 | 1 | 0 | 1 | 0 | 0 | 0 | 2 | 1 |
| 3 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 1 | 0 |
| 4 | 0 | 0 | 1 | 0 | 0 | 2 | 0 | 1 | 0 | 0 | 0 | 1 | 0 |
| 5 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 1 | 2 |
| 6 | 0 | 2 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 2 | 0 |

| | snp28 | snp29 | snp30 | snp31 | snp32 | snp33 | snp34 | snp35 | snp36 | snp37 | snp38 | snp39 | snp40 |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 |
| 2 | 1 | 2 | 0 | 0 | 0 | 1 | 2 | 1 | 2 | 0 | 1 | 1 | 0 |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 2 | 2 | 0 | 0 |
| 4 | 2 | 0 | 0 | 0 | 1 | 2 | 2 | 0 | 1 | 1 | 1 | 1 | 0 |
| 5 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| 6 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 2 | 0 |

| | snp41 | snp42 | snp43 | snp44 | snp45 | snp46 | snp47 | snp48 | snp49 | snp50 | snp51 | snp52 | snp53 |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 |
| 2 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 2 | 0 | 1 | 0 | 1 | 0 |
| 3 | 0 | 1 | 0 | 1 | 0 | 2 | 1 | 1 | 1 | 0 | 0 | 0 | 1 |
| 4 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 2 | 0 | 1 | 0 | 2 |
| 5 | 2 | 2 | 0 | 0 | 0 | 1 | 2 | 1 | 0 | 0 | 0 | 0 | 1 |
| 6 | 1 | 1 | 2 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 1 |

| | snp54 | snp55 | snp56 | snp57 | snp58 | snp59 | snp60 | snp61 | snp62 | snp63 | snp64 | snp65 | snp66 |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 1 |

| | | | | | | | | | | | | | |
|---|-------|-------|-------|-------|-------|-------|-------|--------|-------|-------|-------|-------|-------|
| 2 | 2 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 2 | 2 | 1 |
| 3 | 2 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 |
| 4 | 1 | 1 | 0 | 0 | 0 | 0 | 2 | 1 | 0 | 1 | 0 | 0 | 2 |
| 5 | 1 | 1 | 1 | 0 | 0 | 0 | 2 | 1 | 1 | 0 | 0 | 1 | 1 |
| 6 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 2 | 1 |
| | snp67 | snp68 | snp69 | snp70 | snp71 | snp72 | snp73 | snp74 | snp75 | snp76 | snp77 | snp78 | snp79 |
| 1 | 1 | 0 | 1 | 1 | 2 | 1 | 1 | 1 | 0 | 0 | 2 | 1 | 1 |
| 2 | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 2 | 1 |
| 3 | 1 | 0 | 1 | 2 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 1 |
| 4 | 1 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| 5 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 0 |
| 6 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 2 |
| | snp80 | snp81 | snp82 | snp83 | snp84 | snp85 | snp86 | snp87 | snp88 | snp89 | snp90 | snp91 | snp92 |
| 1 | 1 | 0 | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 | 1 |
| 2 | 1 | 2 | 0 | 0 | 0 | 1 | 2 | 0 | 2 | 1 | 0 | 0 | 2 |
| 3 | 1 | 0 | 0 | 0 | 0 | 2 | 0 | 0 | 2 | 0 | 0 | 0 | 0 |
| 4 | 1 | 2 | 0 | 1 | 0 | 1 | 2 | 0 | 0 | 0 | 0 | 0 | 0 |
| 5 | 2 | 0 | 1 | 0 | 0 | 2 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 6 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 2 | 0 | 1 | 0 | 0 |
| | snp93 | snp94 | snp95 | snp96 | snp97 | snp98 | snp99 | snp100 | | | | | |
| 1 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | | | | | |
| 2 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 2 | | | | | |
| 3 | 1 | 1 | 0 | 0 | 1 | 2 | 0 | 0 | | | | | |
| 4 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | | | | | |
| 5 | 1 | 0 | 0 | 1 | 1 | 2 | 1 | 1 | | | | | |
| 6 | 0 | 0 | 0 | 1 | 1 | 0 | 1 | 1 | | | | | |

...

Covariates:

| | |
|---|--------------|
| | COV1 |
| 1 | -0.612463927 |
| 2 | -0.464158885 |
| 3 | 0.006153597 |
| 4 | -0.732109468 |
| 5 | -0.223530136 |
| 6 | -0.744903822 |

Results:

\$Qstatistic

| | | | |
|---|----------|----------|----------|
| | Q1 | Q2 | Q3 |
| 1 | 2.012625 | 3.761859 | 2.012625 |

\$p.value

| | | | |
|---|-----------|-----------|-----------|
| | p.Q1 | p.Q2 | p.Q3 |
| 1 | 0.1559952 | 0.8258796 | 0.2895166 |

5 Meta-analysis

```
> library(rqt)
> data1 <- read.table(system.file("extdata/phengen2.dat",package="rqt"), skip=1)
> obj1 <- rqtClass(phenotype=data1[,1], genotype=data1[, 2:dim(data1)[2]])
> data2 <- read.table(system.file("extdata/phengen3.dat",package="rqt"), skip=1)
> obj2 <- rqtClass(phenotype=data2[,1], genotype=data2[, 2:dim(data2)[2]])
> data3 <- read.table(system.file("extdata/phengen.dat",package="rqt"), skip=1)
> obj3 <- rqtClass(phenotype=data3[,1], genotype=data3[, 2:dim(data3)[2]])
> res.meta <- rQTestMeta(list(obj1, obj2, obj3))
> print(res.meta)
```

```
$final.pvalue
[1] 0.004276623
```

```
$pvalueList
[1] 0.000858092 0.367634896 0.245240026
```

```
$df
[1] 6
```

```
$chi.comb
[1] 18.93396
```

6 Session information

```
> sessionInfo()
```

```
R version 3.2.4 (2016-03-10)
Platform: x86_64-apple-darwin13.4.0 (64-bit)
Running under: OS X 10.12.1 (unknown)
```

```
locale:
[1] C
```

```
attached base packages:
[1] stats      graphics  grDevices  utils      datasets  methods   base
```

```
other attached packages:
[1] rqt_0.99.0      ropls_1.2.14    plyr_1.8.4      pls_2.5-0       glmnet_2.0-5
[6] foreach_1.4.3  Matrix_1.2-7.1
```

```
loaded via a namespace (and not attached):
[1] CCP_1.1          parallel_3.2.4  tools_3.2.4     Rcpp_0.12.8
[5] codetools_0.2-15 grid_3.2.4       iterators_1.0.8  CompQuadForm_1.4.1
[9] lattice_0.20-34
```

7 References

References

- [1] Wu, M. C., Lee, S., Cai, T., Li, Y., Boehnke, M., and Lin, X. (2011) Rare Variant Association Testing for Sequencing Data Using the Sequence Kernel Association Test (SKAT). *The American Journal of Human Genetics*, 89, 82-93.
- [2] Li, B. and Leal, S.M. (2008) Methods for Detecting Associations with Rare Variants for Common Diseases: Application to Analysis of Sequence Data. *The American Journal of Human Genetics*, 83, 311-321.
- [3] Liu D., Leal S. (2010) A Novel Adaptive Method for the Analysis of Next-Generation Sequencing Data to Detect Complex Trait Associations with Rare Variants Due to Gene Main Effects and Interactions, *PLoS Genet.*, 6(10).
- [4] Madsen, B.E, Browning, S.R. (2009) A Groupwise Association Test for Rare Mutations Using a Weighted Sum Statistic, *PLoS Genet.*, 5(2).
- [5] Lee, J., Kim, Y.J., Lee, J., T2D-Genes Consortium, Kim, B-J., Lee, S., Park T. (2016) Gene-set association tests for next-generation sequencing data, *Bioinformatics*, 32(17).
- [6] Tibshirani, R. (1996) Regression shrinkage and selection via the lasso. *J. Royal. Statist. Soc B.*, Vol. 58, No. 1, pages 267-288.