

Real & Fictitious Magnetic Fields in Strained Graphene

Natalie Whitehead

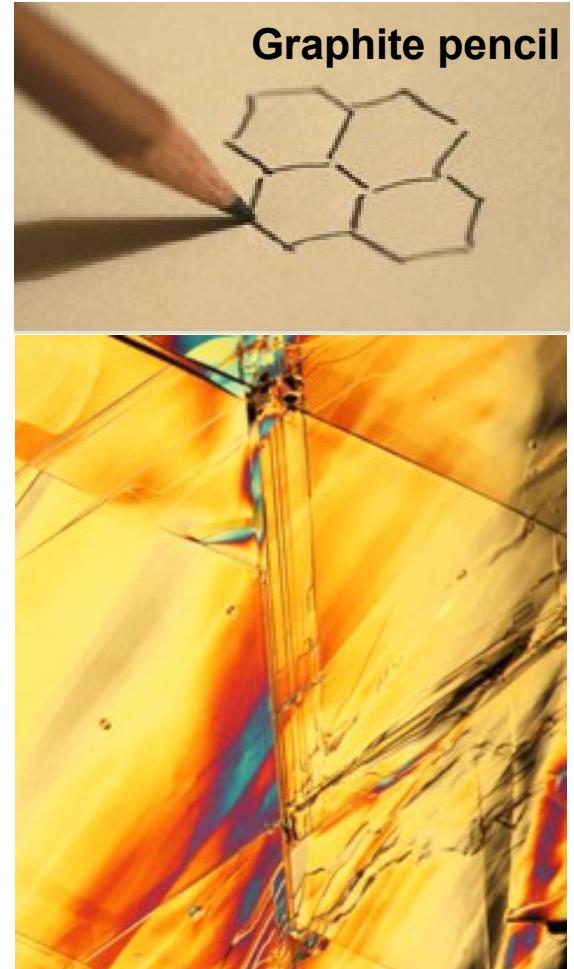
Year 3 MPhys Student

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Quantum Systems & Nanomaterials

Presentation Outline

- **What is Graphene?**
- **How can a 2D structure exist?**
- **How is Graphene produced?**
- **Graphene's special properties**
- **Strained Graphene**
- **Project progress so far**
- **Next steps**



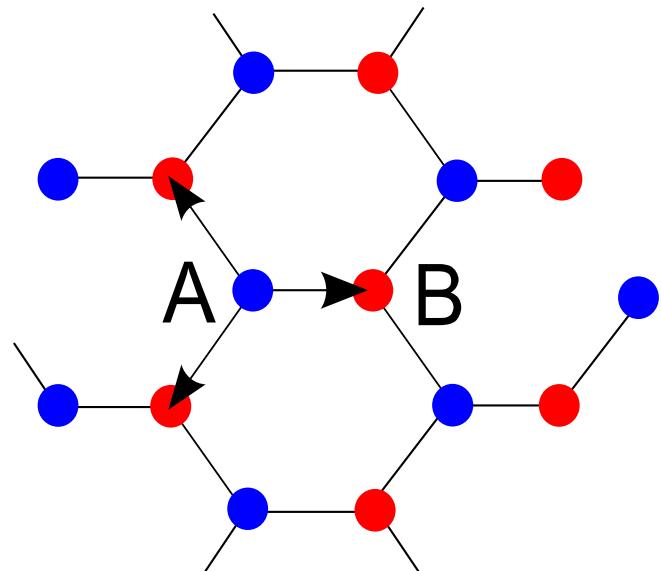
Surface of graphite crystal

Images credit: <http://emps.exeter.ac.uk/physics-astronomy/research/graphene/>

What is Graphene?

- 2D carbon honeycomb lattice [1] with 2 sub-lattices (A & B)
- The only 2D conducting membrane (so far!) [2]

Landau & Peierls:
2D materials can't
exist! [3][4]



[1]: Geim, A. K. & Novoselov, K. S. The rise of graphene. *Nature Materials* 6, 183 - 191 (2007)

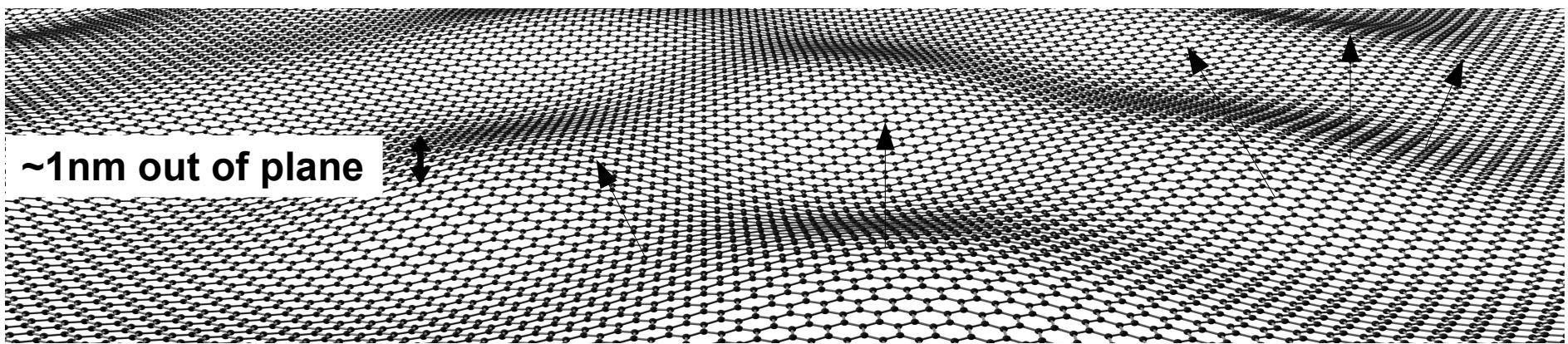
[2]: Mariani, E. et al. Fictitious gauge fields in bilayer graphene. *Phys. Rev. B* 86, 165448 (2012)

[3]: Landau, L. D. Zur Theorie der phasenumwandlungen II. *Phys. Z. Sowjetunion* 11, 26–35 (1937)

[4]: Peierls, R. E. Quelques proprietes typiques des corps solides. *Ann. I. H. Poincaré* 5, 177–222 (1935)

The Predicted Instability

- Thermal fluctuations destroy long term order [1]
=> perfect crystal in 2D too unstable...
- But nearly perfect 2D crystal in 3D space can exist!
- Graphene's inherent corrugation seems to provide stability [1][2]



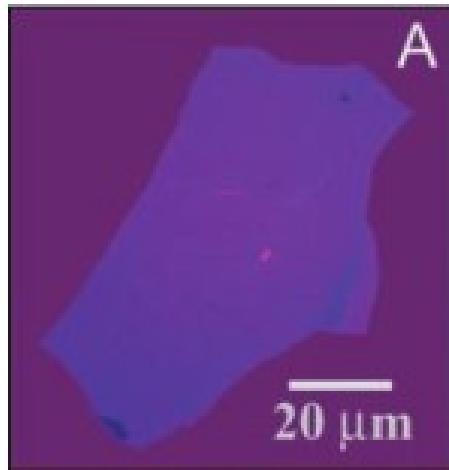
[1]: Meyer, J.C. et al. The structure of suspended graphene sheets. *Nature* 446, 60-63 (1 March 2007)

[2]: Fasolino, A. et al. Intrinsic ripples in graphene. *Nature Materials* 6, 858 - 861 (2007)

Image credit: Jannik Meyer. Obtained from: <http://www.condmat.physics.manchester.ac.uk/imagelibrary/>

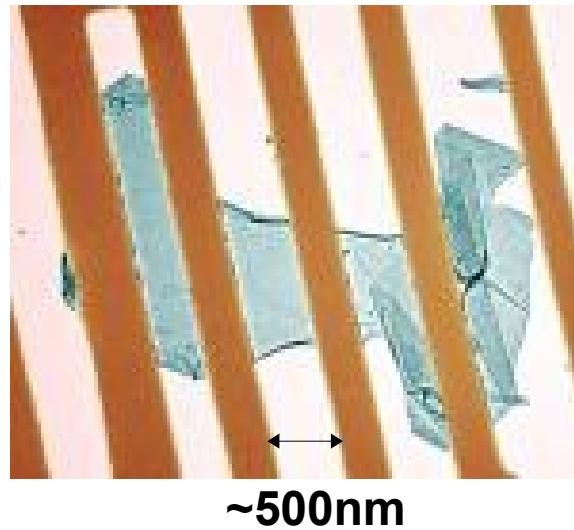
Making Graphene

- 'Mechanical Exfoliation' using Scotch tape – still best method! [1]
- Growth on a substrate – samples generally poorer quality than exfoliated sheets [2]



White light photo of
graphene visible on
oxidised Si wafer

Suspended
graphene sheet
(TEM image)



[1]: Geim, A. K. & Novoselov, K. S. The rise of graphene. *Nature Materials* 6, 183 - 191 (2007)

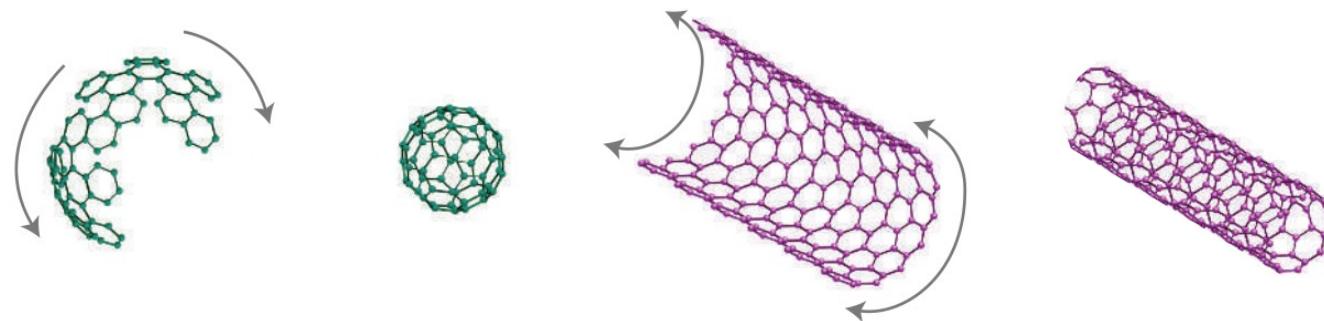
[2]: 'Challenges in Graphene Technology' <http://www.graphene.manchester.ac.uk/research/challenges/>

Image credit (left): Novoselov, K. S. et al. *Science* 306, 666–669 (2004).

Image credit (right): Jannik Meyer. From: <http://www.condmat.physics.manchester.ac.uk/imagelibrary/>

Special Properties

- High thermal conductivity: $5000 \text{ Wm}^{-1}\text{K}^{-1}$ [1]
- High breaking strength: 42N/m [1]
- High mobility: $>200,000 \text{ cm}^2\cdot\text{V}^{-1}\text{s}^{-1}$ at 300K [2]
- High crystal quality (~ 1 defect per μm) [2]
- Flexible (despite high Young Modulus of $\sim 1\text{TPa}$)



[1]: http://www.nobelprize.org/nobel_prizes/physics/laureates/2010/advanced-physicsprize2010.pdf

[2]: Geim, A. 'Graphene: Magic of Flat Carbon' <http://www2.avs.org/conferences/icnt/pdfs/speakers/geim.pdf>
Image adapted from: Geim, A. K. & Novoselov, K. S. The rise of graphene. *Nature Materials* 6, 183 - 191 (2007)

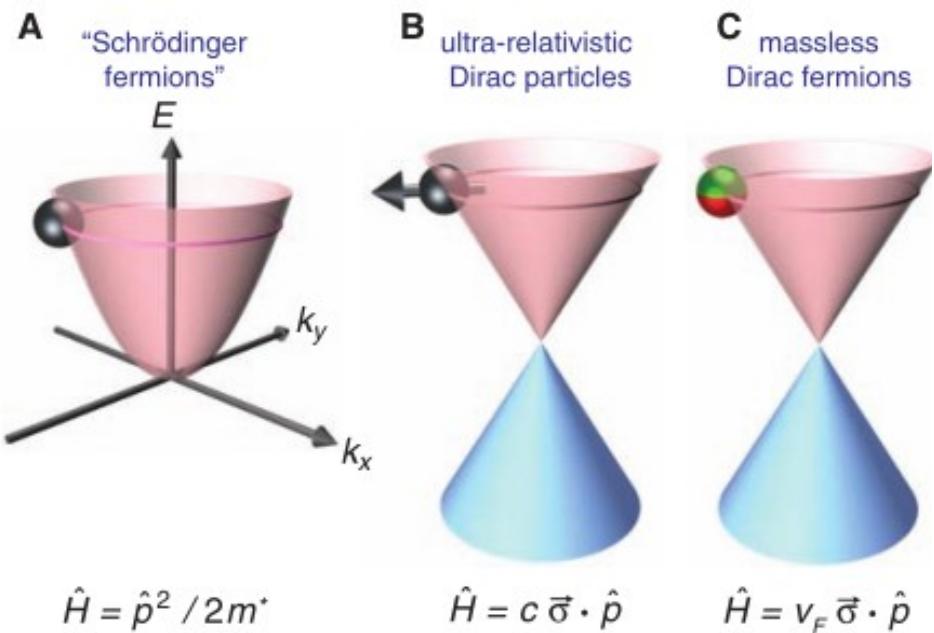
“CERN on one’s desk” [1]

- Electrons → Massless Dirac Fermions [2]

Electron interaction with honeycomb lattice

=>

massless quasi-particles described by **Dirac Equation** (not Schrödinger Equation)

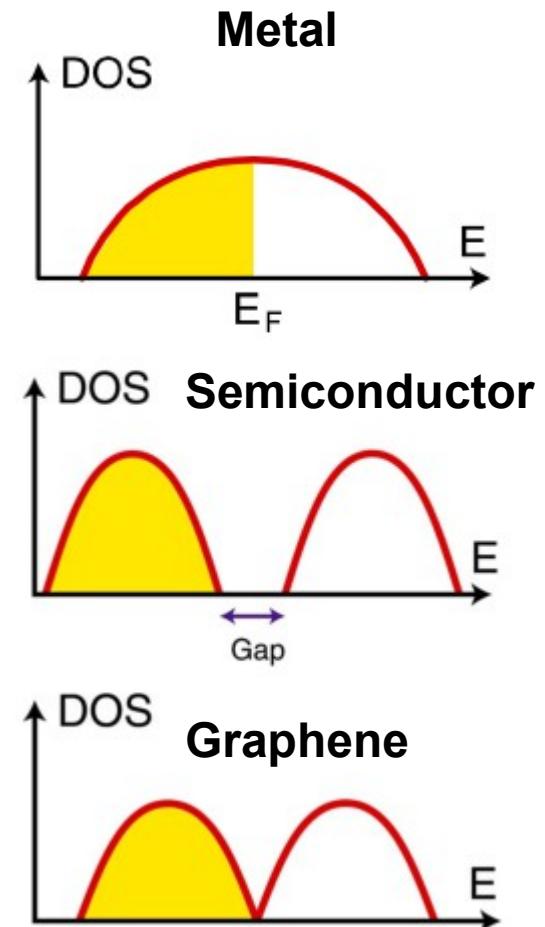


[1]: Katsnelson, M.I. *Graphene - Carbon in Two Dimensions*. New York: Cambridge University Press (2012)

[2]: Geim, A. Graphene: Status and Prospects. *Science* 324 (5934): 1530-1534 (2009)
Image credit: from [2]

Why Should We *Strain* Graphene?

- Graphene has zero-band gap
=>
limitations for nanotechnology –
eg: (traditional) transistors need a
band gap [1]
- Applying **non-uniform** strain =>
control of electrons & hence band
gap [2]



[1]: <http://www.technologyreview.com/view/518426/how-to-save-the-troubled-graphene-transistor/>

[2]: Gui, G. et al. Phys. Rev. B 78, 075435 (2008).

Image credit: 'Quantum Theory of Graphene' lecture slides, University of Pennsylvania, from: www.physics.upenn.edu/~kane/pedagogical/295lec3.pdf

Strain-Induced Gauge Fields

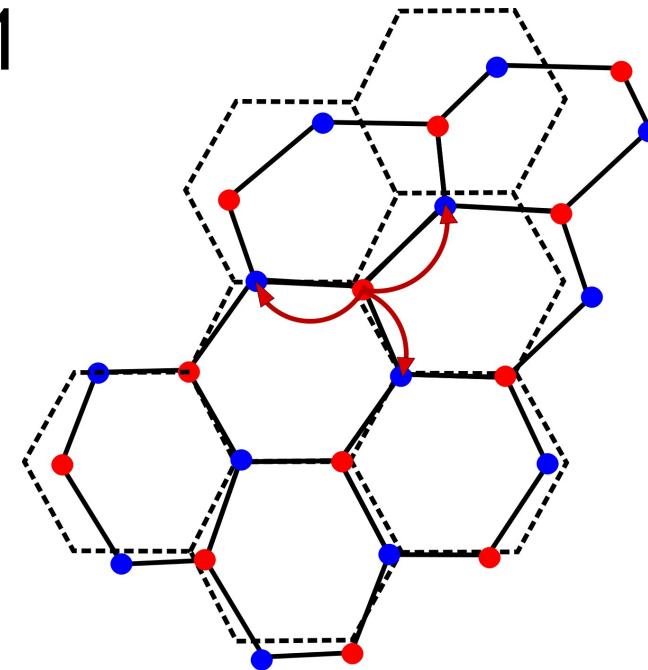
- Massless Dirac Hamiltonian [1]

No strain:

$$\hat{H} = \begin{pmatrix} 0 & v_F(p_x - ip_y) \\ v_F(p_x + ip_y) & 0 \end{pmatrix}$$

With strain:

$$\hat{H} = \begin{pmatrix} 0 & v_F(p^* + A^*) \\ v_F(p + A) & 0 \end{pmatrix}$$

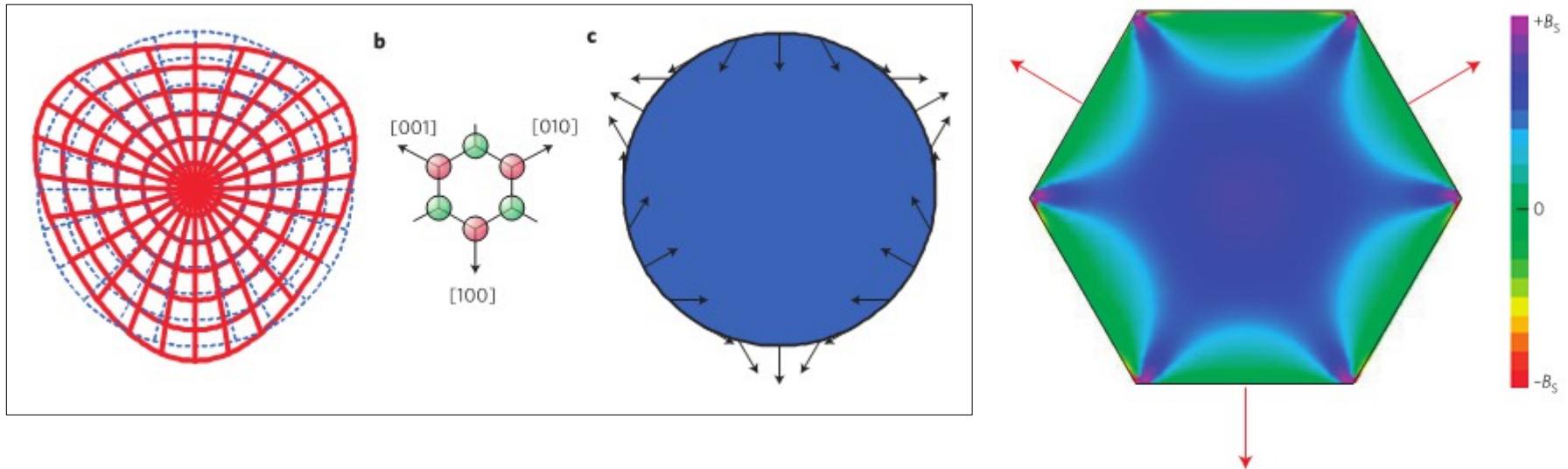


Strain produces a
(fictitious, magnetic)
vector potential!

[1]: Castro Neto, A. H. The electronic properties of graphene. *Rev. Mod. Phys.* 81, 109–162 (2009)

In-Plane Strain of Graphene

Guinea et al: fictitious fields over 10T



Left: uniform fictitious B fields can be created by strain applied as shown.

Right: strain that is more easily applied experimentally – fairly uniform fictitious B field in centre of hexagon.

Image credit: Guinea, F. et al. Energy gaps and a zero-field quantum Hall effect in graphene by strain engineering. *Nature Physics* 6, 30 - 33 (2010)

Out-of-Plane Strain of Graphene

Pyramid-shaped graphene nanobubbles:
fictitious fields of $\sim 350\text{T}$

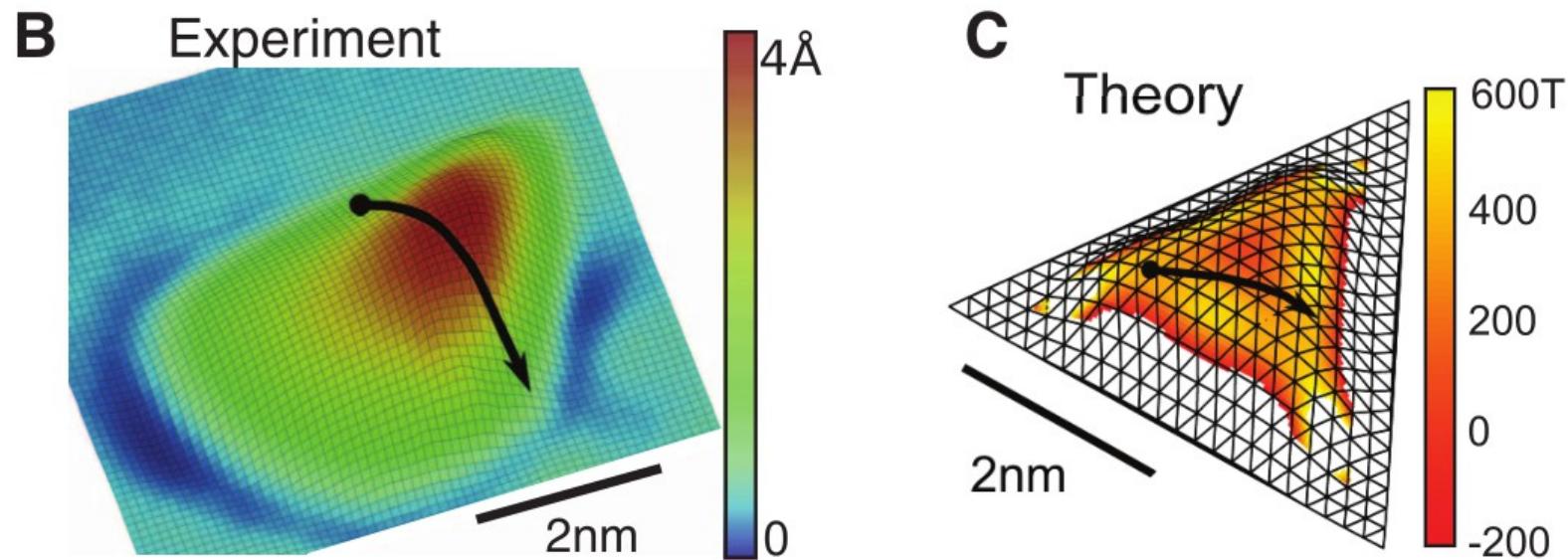
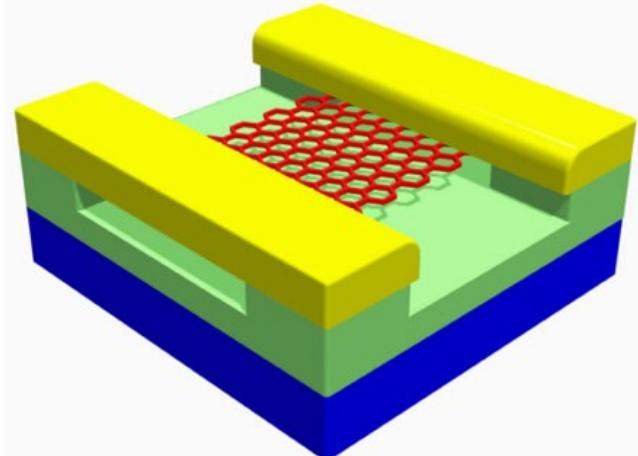
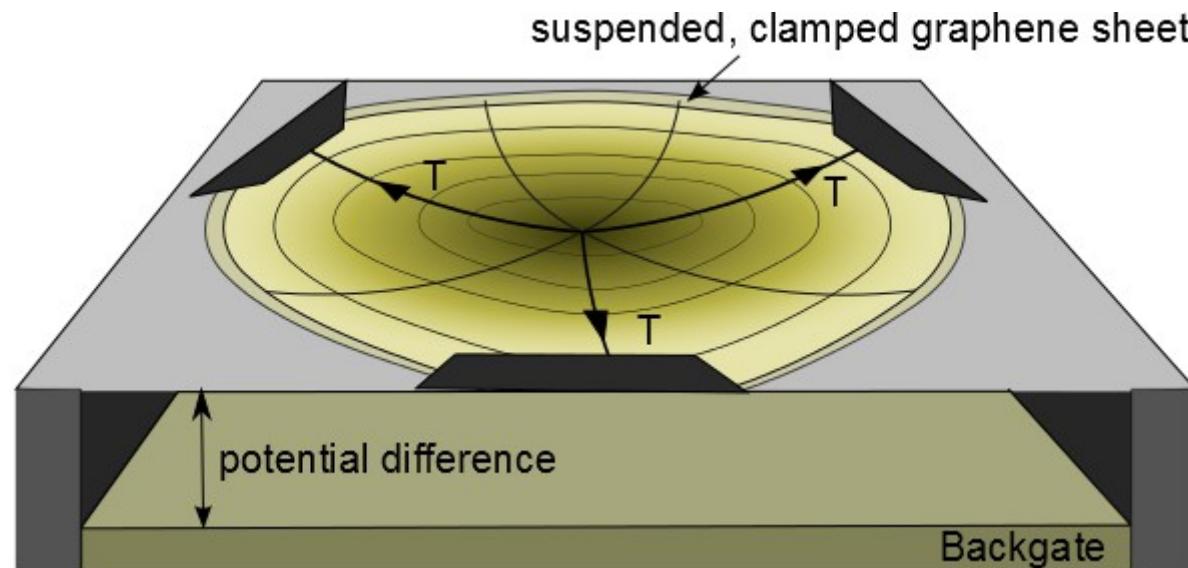
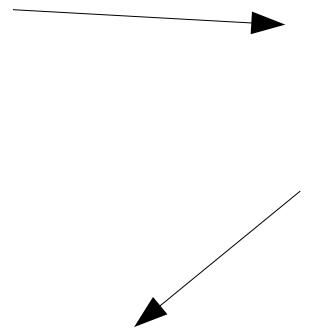


Image credit: Levy, N. et al. Strain-Induced Pseudo-Magnetic Fields Greater Than 300 Tesla in Graphene Nanobubbles. *Science* 329, 544 (2010)

Our Gedankenexperiment

Graphene sheets have been successfully suspended in experiments



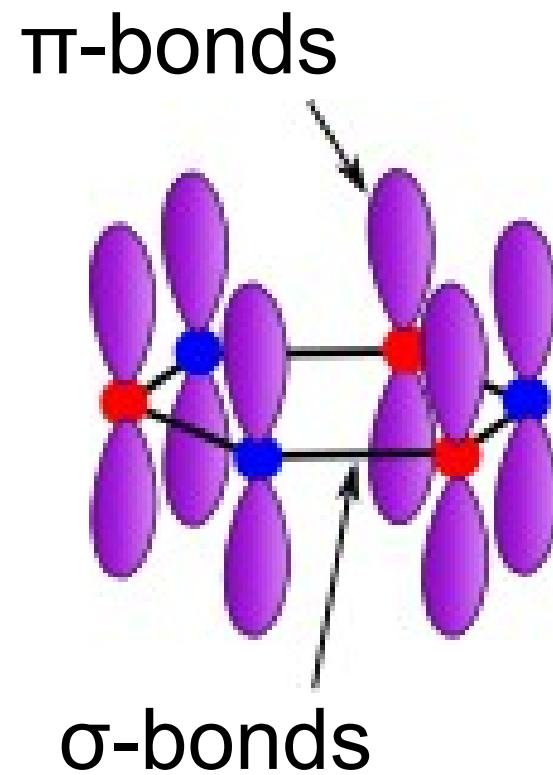
We will describe analytically:

How applied voltage induces (non-uniform) triangular strain

Image credit (top right): <http://physicsworld.com/cws/article/news/2009/sep/29/graphene-works-as-a-highly-sensitive-mass-detector>

Progress so Far: Tight Binding Method

- First solved for graphite by Wallace in 1947 [1]
- π -bonds contribute to conduction
- Electrons 'hop' to nearest neighbours



[1] Wallace, P. R. *The band theory of graphite*. Phys. Rev. 71, 622–634 (1947).

Tight Binding: 1 Atom per Unit Cell

Hamiltonian:

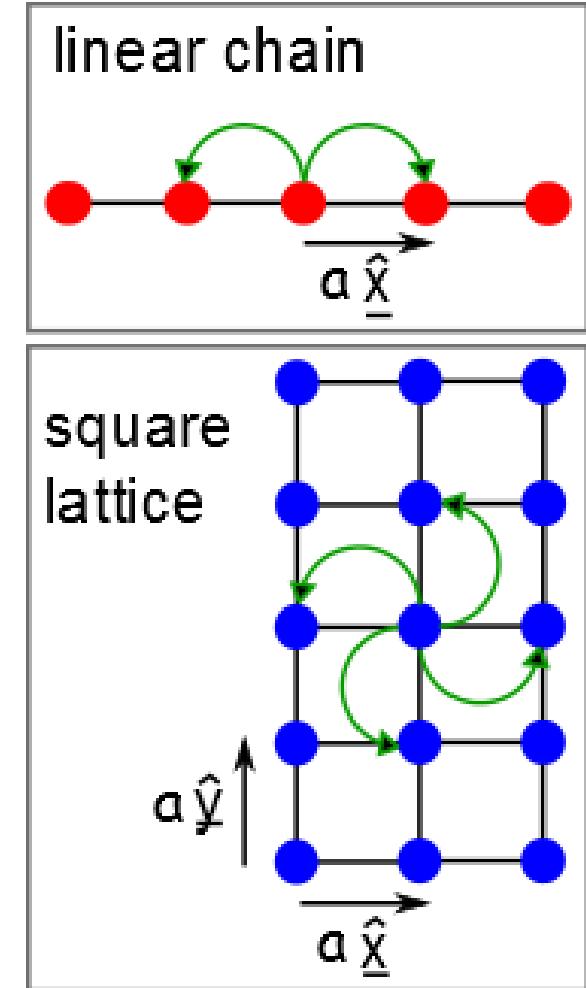
$$\hat{H} = -t \sum_j (|R_j><R_j + a|)$$

Wavefunction:

$$|\Psi_k(\mathbf{r})> = \sum_j (ce^{i\mathbf{k}\cdot\mathbf{R}_j}|R_j>)$$

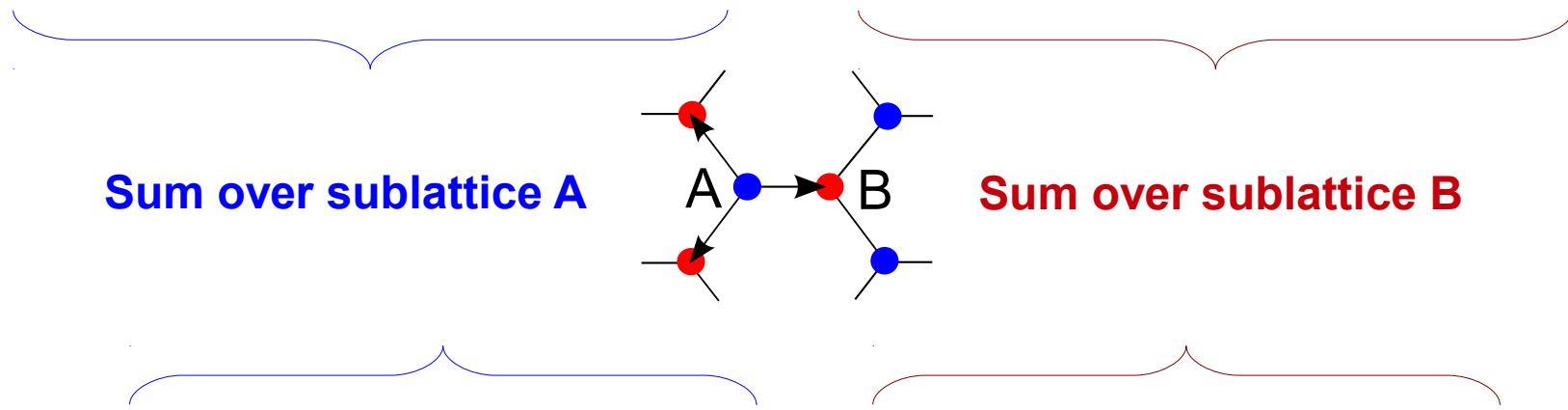
Solve Schrödinger Equation:

$$\hat{H}|\Psi> = E|\Psi>$$



Tight Binding: Graphene (Two Inequivalent Sublattices)

$$\hat{H} = -t \sum_{R_A} \sum_{i=1}^3 \{|R_A>< R_A + d_i|\} - t \sum_{R_B} \sum_{i=1}^3 \{|R_B>< R_B - d_i|\}$$

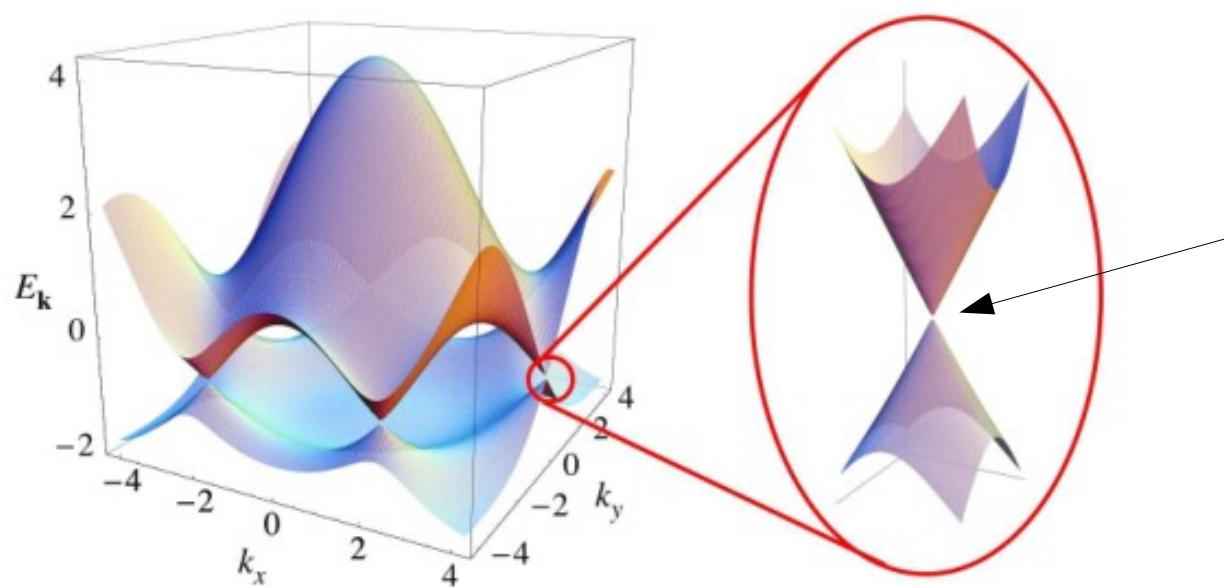


$$|\Psi_k(\mathbf{r})> = \sum_{R_A} (c_A e^{i\mathbf{k} \cdot \mathbf{R}_m} |R_A>) + \sum_{R_B} (c_B e^{i\mathbf{k} \cdot \mathbf{R}_m} |R_B>)$$

Image credit: www.physics.upenn.edu/~kane/pedagogical/295lec3.pdf

Tight Binding: Dispersion Relation for Graphene

$$E(\mathbf{k}) = \pm t \sqrt{1 + 4\cos\left(\frac{\sqrt{3}ak_y}{2}\right) \cos\left(\frac{3ak_x}{2}\right) + 4\cos^2\left(\frac{\sqrt{3}ak_y}{2}\right)}$$



Next step:
probe deeper
to describe
form of $E(\mathbf{k})$
near Dirac
Points

Image credit: Castro Neto, A. H. et al. The Electronic Properties of Graphene. Rev. Mod. Phys. 81, 109 (2009)

Next Steps

- Resolve detail of $E(k)$ - Dirac Points
- Understand electron propagation
- Predict 0% backscattering probability
- Membrane deformation theory
- Fictitious gauge field theory

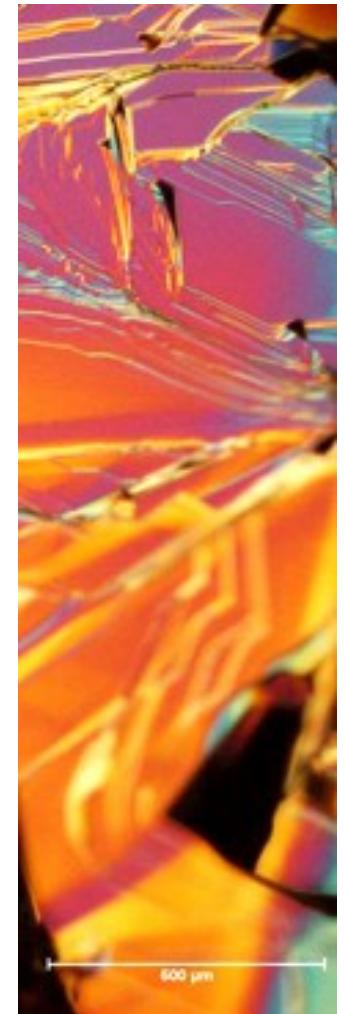


Image credit: <http://emps.exeter.ac.uk/physics-astronomy/research/graphene/>