

secondPI

May 8, 2021

1 Second order PI

```
[1]: import numpy as np
import sympy as sym
import matplotlib.pyplot as plt
from control.matlab import *

sym.init_printing()
```

```
[2]: z, Wn, Kg, Kp, tau, Ti = sym.symbols('zeta omega_n K_G K_p tau T_i')
```

```
[3]: eq1 = sym.Eq(2*z*Wn, (1+Kg*Kp)/tau);
eq2 = sym.Eq(Wn**2, (Kg*Kp)/(tau*Ti));
sym.solve((eq1, eq2), (Kp, Ti));
```

1.1 Example

```
[4]: import control as ct
import numpy as np
```

```
[5]: # System
num = [29870]
den = [1, 414.7, 33610]
G = ct.tf(num, den)
print('Process:')
print(G)

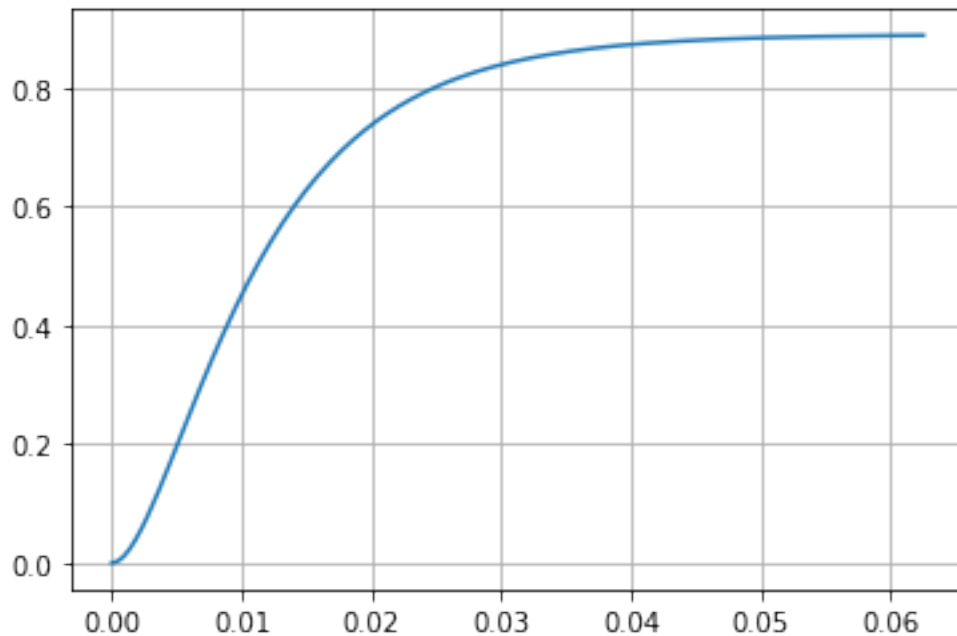
t, out = ct.step_response(G)
print('Step response:')
plt.plot(t, out)
plt.grid()
plt.show()

print('Step info:')
stepinfo(G)
```

Process:

$$\frac{2.987e+04}{s^2 + 414.7 s + 3.361e+04}$$

Step response:



Step info:

```
[5]: {'RiseTime': 0.0217480341475997,
      'SettlingTime': 0.039871395937266116,
      'SettlingMin': 0.8000456798025747,
      'SettlingMax': 0.8873280912347106,
      'Overshoot': 0,
      'Undershoot': 0,
      'Peak': 0.8873280912347106,
      'PeakTime': 0.06252559817434913,
      'SteadyStateValue': 0.8887235941684023}
```

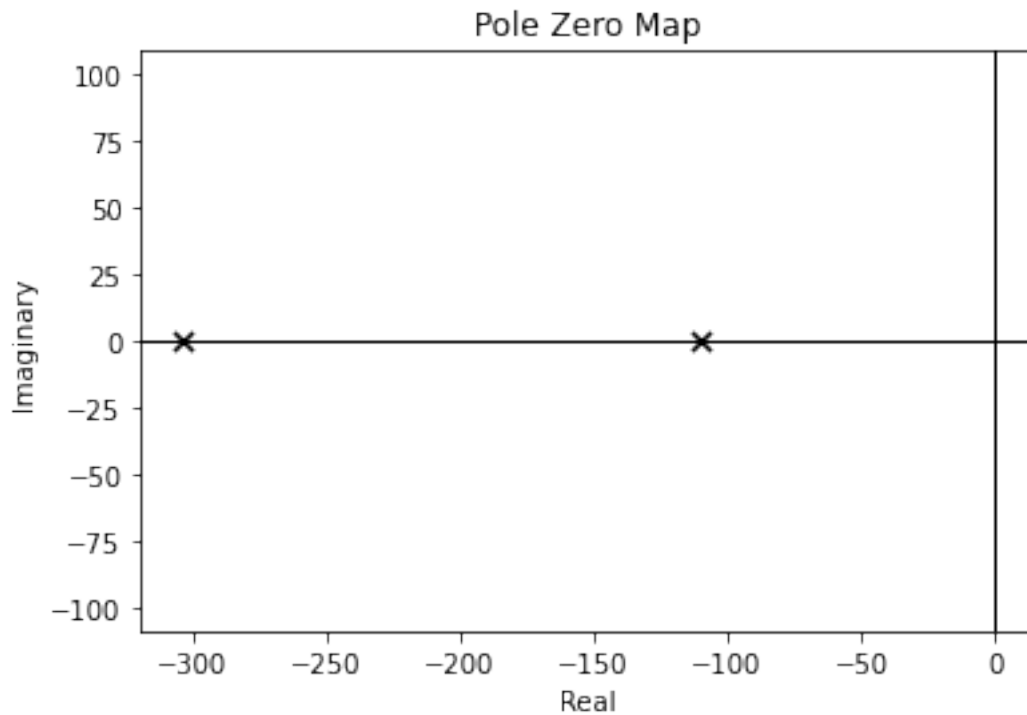
```
[6]: # Damping and natural frequency
ct.damp(G);
```

-----Eigenvalue-----	Damping---	Frequency_
-304.2	1	304.2
-110.5	1	110.5

```
[7]: # Root locus
print('Poles: ',ct.pole(G))
```

```
ct.pzmap(G);
```

Poles: [-304.22116444 -110.47883556]



```
[8]: # Data
ts = 0.03
Mp = 25

b0 = num
a1 = den[1]
a0 = den[2]
```

```
[9]: # Requirements
z = np.sqrt(np.square(np.log(Mp/100))/(np.pi**2 + np.square(np.log(Mp/100))))
Wn = 4/(z*ts)

print('z= ', z)
print('Wn= ', Wn)
```

```
z= 0.40371275194342066
Wn= 330.2678270415884
```

```
[10]: # Desired characteristic equation and poles
print('delta = s^2 + {a}s + {b:1.4f}'.format(a=2*z*Wn,b=Wn**2))
```

```
print('s = {a} + j{b:1.4}'.format(a=-z*Wn, b=Wn*np.sqrt(1-z**2)))
```

```
delta = s2 + 266.6666666666667s + 109076.8376  
s = -133.33333333333334 + j302.2
```

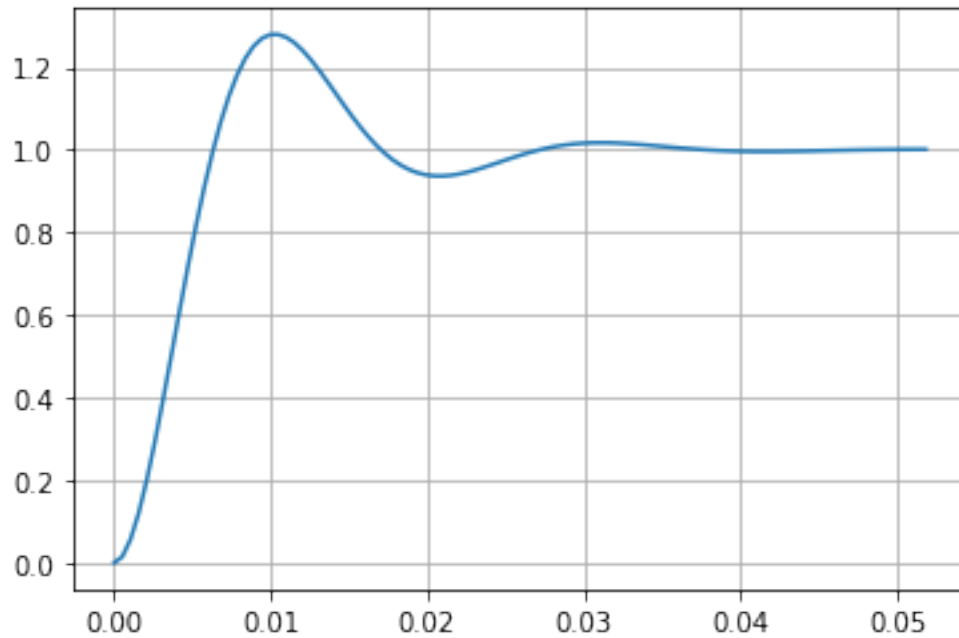
```
[11]: # PI controller  
B = a1/(z*Wn) - 2  
Kp = ((2*B*z**2 + 1)*Wn**2 - a0)/b0  
Ti = (Kp*b0)/(B*z*Wn**3)  
  
Kp = float(Kp)  
Ti = float(Ti)  
  
Gc = ct.tf([Kp*Ti, Kp],[Ti, 0])  
print('Feedback PI- controlled system:')  
print(Gc)
```

Feedback PI- controlled system:

```
0.02739 s + 3.848  
-----  
0.007118 s
```

```
[12]: # PI response  
sys = ct.feedback(Gc*G)  
t, out = ct.step_response(sys)  
print('Step response:')  
plt.plot(t,out)  
plt.grid()  
plt.show()  
  
print('Step info:')  
stepinfo(sys)
```

Step response:



Step info:

```
[12]: {'RiseTime': 0.004186518350898264,
      'SettlingTime': 0.025642424899251864,
      'SettlingMin': 0.9097057284224213,
      'SettlingMax': 1.279404750312783,
      'Overshoot': 27.9404750312783,
      'Undershoot': 0,
      'Peak': 1.279404750312783,
      'PeakTime': 0.010466295877245659,
      'SteadyStateValue': 1.0}
```

```
[13]: ct.pzmap(sys);
      print('Poles: ', ct.pole(sys))
```

```
Poles: [-133.33333333+302.15734279j -133.33333333-302.15734279j
        -148.03333333 +0.j          ]
```

