SULIT



BAHAGIAN PEPERIKSAAN DAN PENILAIAN JABATAN PENDIDIKAN POLITEKNIK DAN KOLEJ KOMUNITI KEMENTERIAN PENDIDIKAN MALAYSIA

JABATAN MATEMATIK, SAINS & KOMPUTER

PEPERIKSAAN AKHIR SESI JUN 2018

DBM1013: ENGINEERING MATHEMATICS 1

TARIKH : 31 OKTOBER 2018

MASA : 8.30 PAGI - 10.30 PAGI (2 JAM)

Kertas ini mengandungi SEBELAS (11) halaman bercetak.

Bahagian A: Struktur (2 soalan)

Bahagian B: Struktur (4 soalan)

Dokumen sokongan yang disertakan: Formula

JANGAN BUKA KERTAS SOALAN INI SEHINGGA DIARAHKAN

(CLO yang tertera hanya sebagai rujukan)

SULIT

SECTION A: 50 MARKS

BAHAGIAN A: 50 MARKAH

INSTRUCTION:

This section consists of TWO (2) structured questions. Answer ALL questions.

ARAHAN:

SULIT

Bahagian ini mengandungi DUA (2) soalan berstruktur. Jawab SEMUA soalan.

QUESTION 1

SOALAN 1

CLO1 C2 a) Express each of the following expressions in the simplest form:

Ungkapkan setiap yang berikut dalam bentuk termudah:

i.
$$\frac{1}{2}(4b+3a)-5(2b-a)$$

[3 marks]

[3 markah]

ii.
$$\frac{2x+1}{4} - \frac{4x-1}{2x}$$

[4 marks]

[4 markah]

iii.
$$\frac{12x - 4x^2}{6x^2 - 7x + 2} \div \frac{4x}{2x - 1}$$

[3 marks]

[3 markah]

CLO1 C3

- b) Calculate the roots for equations below by using the given method:

 *Kirakan punca-punca bagi persamaan di bawah dengan menggunakan kaedah yang diberi:
 - i. $2x^2 + 5x 12 = 0$ (Using Factorization Method) (Menggunakan Kaedah Pemfaktoran)

[3 marks]

[3 markah]

ii. $3x^2 = 4x + 9$ (Using Quadratic Formula) (Menggunakan Formula Kuadratik)

[5 marks]

[5 markah]

iii. $4x^2 - 12x + 8 = 0$ (Using Completing the Square Method) (Menggunakan Kaedah Penyempurnaan Kuasa Dua)

[7 marks]

[7 markah]

SOALAN 2

CLO1 C2 a) Determine the value of A and B for partial fraction below: Tentukan nilai A dan B bagi pecahan separa di bawah:

$$\frac{-x+10}{x^2+2x-15} = \frac{A}{x+5} + \frac{B}{x-3}$$

[4 marks]

[4 markah]

CLO1 C3 b) Calculate the partial fraction for the following equations:

*Kirakan pecahan separa bagi persamaan yang berikut:

i.
$$\frac{11 - 5x}{x^2 - 8x + 16}$$

[6 marks]

[6 markah]

ii.
$$\frac{10 + 5x - x^2}{(x+1)(x^2+2)}$$

[7 marks]

[7 markah]

iii.
$$\frac{x^2}{x^2 - 5x + 6}$$

[8 marks]

[8 markah]

SECTION B: 50 MARKS

BAHAGIAN B: 50 MARKAH

INSTRUCTION:

This section consists of FOUR (4) structured questions. Answer TWO (2) questions only.

ARAHAN:

Bahagian ini mengandungi EMPAT (4) soalan berstruktur. Jawab DUA (2) soalan sahaja.

QUESTION 3

SOALAN 3

CLO2 C2 a) Given that $\tilde{a} = 5i + 4j + 2k$, $\tilde{b} = 2i + j - 2k$ and $\tilde{c} = -i - j + 4k$. Express each of the following in the term of i, j and k.

i.
$$-\tilde{b}-\tilde{a}$$

[3 marks]

[3 markah]

ii.
$$5\tilde{a} + 3\tilde{c}$$

[3 marks]

[3 markah]

iii.
$$4(\tilde{b}-2\tilde{c})$$

[4 marks]

[4 markah]

CLO2 C3 b) i. Given R(-4,3) is a point in a Cartesian plane. Interpret the vector \overrightarrow{OR} in terms of i and j. Calculate the unit vector in the direction of \overrightarrow{OR} .

Diberi R(-4,3) ialah satu titik di dalam Rajah Cartesian. Tafsirkan vektor \overrightarrow{OR} dalam sebutan i dan j. Kirakan vektor unit dalam arah \overrightarrow{OR} .

[4 marks]
[4 markah]

ii. Calculate the area of parallelogram with vertices A = (2, -4, 1), B = (0, 5, 8) and C = (4, 3, -6).

Kirakan luas parallelogram bagi sudut A = (2,-4,1), B = (0,5,8) dan C = (4,3,-6).

[11 marks]
[11 markah]

SOALAN 4

CLO2 C2 a) Given $\cos \theta = \frac{12}{13}$ where $0^{\circ} \le \theta \le 90^{\circ}$. Compute each following value without using calculator:

Diberi $\cos \theta = \frac{12}{13}$. Kira nilai tiap yang berikut tanpa menggunakan kalkulator:

i. $tan \theta$

[3 marks]

[3 markah]

ii. $cosec \theta$

[3 marks]

[3 markah]

iii. $sec \theta$

[2 marks]

[2 markah]

iv. $\sin^2 \theta + \cos^2 \theta$

[2 marks]

[2 markah]

CLO2 C3 b) Calculate the angles between $0^{\circ} \le \theta \le 360^{\circ}$ for the following equations: Kira sudut-sudut antara $0^{\circ} \le \theta \le 360^{\circ}$ bagi persamaan-persamaan berikut:

i. $\cos \theta = 0.866$

[4 marks]

[4 markah]

ii. $\tan \theta = -1$

[3 marks]

[3 markah]

iii. $2 \cos^2 \theta + 3 \sin \theta - 3 = 0$

[8 marks]

[8 markah]

SOALAN 5

CLO2 C2 a) Given x = 4 + 8i and y = -1 - 3i, determine each of the following expression and write the answer in a + bi form:

Diberi $x = 4 + 8i \, dan \, y = -1 - 3i$, tentukan setiap ungkapan yang berikut dan beri jawapan dalam bentuk a + bi:

i.
$$x+y$$

[2 marks]

[2 markah]

[4 marks]

[4 markah]

iii.
$$x - y^2$$

[4 marks]

[4 markah]

CLO2 C3

b) Given $Z_1 = 3 + 2i$ and $Z_2 = 3(\cos 30^\circ + i \sin 30^\circ)$: Diberi $Z_1 = 3 + 2i$ dan $Z_2 = 3(\cos 30^\circ + i \sin 30^\circ)$:

i. Calculate the modulus and the argument for Z_1 . Kirakan modulus dan hujah bagi Z_1 .

[3 marks]

[3 markah]

ii. Sketch the Argand's Diagram for Z_1 . Lakarkan gambarajah Argand bagi Z_1

[2 marks]

[2 markah]

iii. Calculate $Z_1 \times Z_2$ and $\frac{Z_1}{Z_2}$. Express the answer in polar form and exponential form.

Kirakan $Z_1 \times Z_2$ dan $\frac{Z_1}{Z_2}$. Ungkapkan jawapan dalam bentuk polar dan bentuk eksponen.

[10 marks]

[10 markah]



SOALAN 6

CLO2 C2 a) Given matrices $A = \begin{pmatrix} -1 & 0 \\ 2 & 3 \end{pmatrix}$, $B = \begin{pmatrix} -10 & 3 \\ 7 & 12 \\ 6 & -13 \end{pmatrix}$ and $C = \begin{pmatrix} 5 & -7 & 2 \\ 2 & 8 & -1 \\ 9 & -10 & 0 \end{pmatrix}$.

Calculate:

Diberi matriks
$$A = \begin{pmatrix} -1 & 0 \\ 2 & 3 \end{pmatrix}$$
, $B = \begin{pmatrix} -10 & 3 \\ 7 & 12 \\ 6 & -13 \end{pmatrix}$ dan $C = \begin{pmatrix} 5 & -7 & 2 \\ 2 & 8 & -1 \\ 9 & -10 & 0 \end{pmatrix}$. Kira:

i. B^T

[1 mark]

[1 markah]

ii. C^T

[1 mark]

[1 markah]

iii. A

[2 marks]

[2 markah]

iv. $|A|B^T$

[2 marks]

[2 markah]

v. B^TC

[4 marks]

[4 markah]

CLO2 C3 b) i. Calculate the minor, cofactor and adjoint of matrix $M = \begin{pmatrix} 1 & 2 & 3 \\ 0 & 1 & 4 \\ 5 & 6 & 0 \end{pmatrix}$.

Kira minor, ko-faktor dan adjoin bagi matriks $M = \begin{pmatrix} 1 & 2 & 3 \\ 0 & 1 & 4 \\ 5 & 6 & 0 \end{pmatrix}$.

[4 marks]

ii. Calculate the value of x, y and z for the following equation by using Cramer's Rule:

Kirakan nilai x, y dan z bagi persamaan berikut dengan menggunakan Petua Cramer:

$$2x + y + z = 5$$
$$x - y - z = 4$$
$$x + 2y + 3z = 6$$

[11 marks]

[11 markah]

SOALAN TAMAT



FORMULA SHEET FOR ENGINEERING MATHEMATICS (DBM1013)

QUADRATIC EQUATION

- 1. Quadratic formula, $x = \frac{-b \pm \sqrt{b^2 4ac}}{2a}$
- 2. Completing the square,

$$\left(x + \frac{b}{2}\right)^2 - \left(\frac{b}{2}\right)^2 + c = 0$$

FORMULA OF TRIANGLE

- 1. Sine Rules; $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$
- 2. Cosine Rules; $a^2 = b^2 + c^2 2bc \cos A$
- 3. Area of Triangle = $\frac{1}{2}ab \sin C$

MATRIX

- 1. *Cofactor*; $C = (-1)^{i+j} M_{ij}$
- 2. Adjoin; $Adj(A) = C^T$
- 3. Inverse of Matrix; $A^{-1} = \frac{1}{|A|}Adj(A)$
- 4. Cramer's Rule;

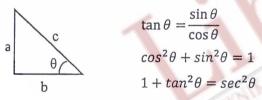
$$x = \frac{|A_1|}{|A|}$$
, $y = \frac{|A_2|}{|A|}$, $z = \frac{|A_3|}{|A|}$

COMPLEX NUMBER

- 1. Modulus of $z = \sqrt{a^2 + b^2}$
- 2. Argument of $z = tan^{-1} \left(\frac{b}{a}\right)$
- 3. Cartesian Form; z = a + bi
- 4. Polar Form; $z = r \angle \theta$
- 5. Exponential Form; $z = re^{i\theta}$
- 6. Trigonometric Form; $z = r(\cos \theta + i \sin \theta)$

TRIGONOMETRY

Pythagoras' Theorem



$$c^2 = a^2 + b^2$$

Trigonometric Identities

$$\tan\theta = \frac{\sin\theta}{\cos\theta}$$

$$\cos^2\theta + \sin^2\theta = 1$$

$$1 + tan^2\theta = sec^2\theta$$

$$c^2 = a^2 + b^2 \qquad 1 + \cot^2\theta = \csc^2\theta$$

VECTOR & SCALAR

- 1. Unit Vector; $\hat{u} = \frac{\overline{u}}{|u|}$
- 2. $\cos \theta = \frac{\overline{A} \cdot \overline{B}}{|A||B|}$
- 3. Scalar Product:

$$\vec{A} \bullet \vec{B} = a_1 a_2 + b_1 b_2 + c_1 c_2$$

4. Vector Product:

$$\vec{A} \times \vec{B} = \begin{vmatrix} i & j & k \\ a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \end{vmatrix}$$

5. Area of parallelogram ABC;

$$|\overrightarrow{AB} \times \overrightarrow{BC}|$$

COMPOUND-ANGLE

- 1. $sin(A \pm B) = sin A cos B \pm cos A sin B$
- 2. $cos(A \pm B) = cos A cos B \mp sin A sin B$
- 3. $tan(A \pm B) = \frac{tan A \pm tan B}{1 \mp tan A tan B}$

DOUBLE-ANGLE

- 1. $\sin 2A = 2 \sin A \cos A$
- 2. $\cos 2A = \cos^2 A \sin^2 A$ $= 1 - 2\sin^2 A$

$$=2\cos^2 A-1$$

3. $\tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$





