Technical Annex

1 Full Results

The complete table of results of explanation-redundancy evaluation is shown in Table 4 and the complete table of results of runtime assessment for computing AXp's are reported in Table 5. Besides, Table 1 summarizes results on path explanation redundancy for DTs included in representative bibliography on DTs, namely textbooks and surveys [15, 6, 17, 7, 8, 18, 4, 20, 3, 9, 26, 12, 1, 21, 11, 2, 22, 16, 24, 5, 25]. Table 2 shows results for DTs learned with recently proposed algorithm that specifically target the learning of optimal (and so indirectly *interpretable*) DTs, concretely [10, 13, 19] and also [23]. Table 3 shows results for DTs learned on more complex datasets (which are also publicly available).

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DT Ref	D	#N	#P	%R	%C	%m	%M	%avg
[1, Ch. 09, Fig. 9.1]	2	5	3	33	25	50	50	50
[2, Ch. 03, Fig. 3.2]	2	5	3	33	25	50	50	50
[5, Ch. 01, Fig. 1.3]	4	9	5	60	25	25	50	36
[7, Figure 1]	3	12	7	14	8	33	33	33
[3, Ch. 08, Fig. 8.2]	3	7	4	25	12	50	50	50
[6, Ch. 01, Fig. 1.1]	3	7	4	50	25	33	33	33
[8, Ch. 01, Fig. 1.2a]	2	5	3	33	25	33	33	33
[8, Ch. 01, Fig. 1.2b]	2	5	3	33	25	33	33	33
[11, Ch. 04, Fig. 4.14]	3	7	4	25	12	50	50	50
[11, Sec. 4.7, Ex. 4]	2	5	3	33	25	50	50	50
[17, Ch. 01, Fig. 1.3]	3	12	7	28	17	33	50	41
[18, Ch. 01, Fig. 1.5]	3	9	5	20	12	33	33	33
[18, Ch. 01, Fig. 1.4]	3	7	4	50	25	33	33	33
[24, Ch. 01, Fig. 1.2]	3	7	4	25	12	50	50	50
[22, Figure 4]	6	39	20	65	63	20	40	33
[9, Ch. 02, Fig. 2.1(right)]	2	5	3	33	25	50	50	50
[12, Figure 1]	3	10	6	33	11	33	33	33
[15, Figure 1]	3	9	5	80	75	33	50	41
[16, Ch. 07, Fig. 7.4]	3	7	4	50	25	33	33	33
[20, Ch. 18, Fig. 18.6]	4	12	8	25	6	25	33	29
[21, Ch. 18, Page 212]	2	5	3	33	25	50	50	50
[26, Ch. 01, Fig. 1.3]	2	5	3	33	25	33	33	33
[4, Figure 1b]	4	13	7	71	50	33	50	36
[25, Ch. 04, Fig. 4.3]	4	14	9	11	2	25	25	25

Table 1: Results on path explanation redundancy for example DTs found in the literature. The table shows tree statistics namely, tree depth **D**, number of nodes **#N**, test accuracy **%A** and number of paths **#P**. The percentage of explanation-redundant paths is given as **%R** while the percentage of data instances (measured for the *entire* feature space) covered by redundant paths is **%C**. Focusing solely on the explanation-redundant paths, a single AXp is extracted and the average (min. or max., resp.) percentage of redundant literals per path is denoted by **%avg** (**%m** and **%M**, resp.).

Dataset	Tool	D	#N	%A	#P	%R	%C	%m	%M	%avg
monk1	BinOCT	3	13	91	7	28	11	66	66	66
	OSDT	5	13	100	7	57	41	33	33	33
tic-tac-toe	BinOCT	4	15	77	8	75	75	33	33	33
	OSDT	5	15	83	8	75	37	25	60	43
compas	OSDT	4	9	67	5	60	37	33	33	33
monk2	CART	6	31	69	16	62	22	20	66	33
	GOSDT	6	17	73	9	55	48	16	40	31

Table 2: Additional results on path explanation redundancy in (optimal) DTs, trained with different training tools: BinOCT [23], CART [6], OSDT [10] and GOSDT [14], that have been presented in [10, 19]. The results for CART are solely included for completeness. Columns **D**, **#N**, **%A**, **#P**, **%R**, **%C**, **%m**, **%M** and **%avg** hold the same meaning in Table 1.

Dataset	**Instance**	**DT**			**XP**				
		D	**#N**	**%A**	**CP**	**m**	**M**	**avg**	**#PI**
	adult_015				16	8	8	8	2
adult	adult_089	17	509	73	14	5	6	5.5	2
	adult_190				16	5	5	5	1
	allhyper_0				14	4	5	4.6	6
allhyper	allhyper_1	14	49	96	9	4	5	4.5	8
	allhyper_4				14	4	5	4.6	6
	ann-thyroid_3				40	5	6	5.6	3
ann-thyroid	ann-thyroid_4	48	222	93	36	5	6	5.6	3
	ann-thyroid_7				20	5	6	5.5	2
	coil2000_045				10	2	4	3.8	39
coil2000	coil2000_218	12	177	91	10	2	4	3.8	39
	coil2000_244				10	2	4	3.8	30
	fars_002				29	11	11	11	2
fars	fars_125	60	9969	76	42	10	14	12.3	9
	fars_354				48	9	9	9	1
	kddcup_01				23	11	12	11.5	16
kddcup	kddcup_02	29	269	99	23	11	12	11.5	16
	kddcup_21				27	12	13	12.5	8

Table 3: Samples of 6 real-world datasets highlighting computed AXp's in decision trees learned with ITI, that require deep DTs. For each dataset, the table displays 3 explained instances. Columns **D**, **#N** and **%A** denote, respectively, depth, number of nodes and accuracy of learned DT with ITI tool. Next, column **CP** reports the consistent path's length in the DT with the input instance. Then, columns **m**, **M** and **avg** report, respectively, the minimum size, maximum size and average length of the AXp's computed given the input instance. Finally, the number of AXp's is shown in column **#PI**.

Dataset	IAI									ITI								
	D	**#N**	**%A**	**#P**	**%R**	**%C**	**%m**	**%M**	**%avg**	**D**	**#N**	**%A**	**#P**	**%R**	**%C**	**%m**	**%M**	**%avg**
IndiansDiabetes	6	33	67	17	35	2	20	25	21	21	67	60	34	38	22	20	33	26
adult	6	83	78	42	33	25	20	40	25	17	509	73	255	75	91	10	66	22
allhyper	6	47	95	24	25	2.5	20	33	23	14	49	96	25	64	25	12	50	35
ann-thyroid	6	61	97	31	25	30	20	50	36	48	223	93	112	65	46	11	75	22
anneal	6	29	99	15	26	16	16	33	21	9	31	100	16	25	4	12	20	16
appendicitis	2	7	68	4	0	0	—	—	—	3	7	81	4	50	3	50	66	58
australian	6	45	61	23	17	8	20	33	23	7	33	82	17	35	51	16	33	26
auto	6	33	53	17	23	1	16	33	23	10	47	75	24	33	53	14	40	26
backache	4	17	72	9	33	39	25	33	30	3	9	91	5	80	87	50	66	54
balance	6	93	81	47	61	41	25	50	27	12	105	81	53	50	62	25	50	26
bank	6	113	88	57	5	12	16	20	18	19	1467	86	734	69	64	7	63	27
banknote	3	9	67	5	20	0	66	66	66	35	71	54	36	83	2	33	50	43
biodegradation	5	19	65	10	30	1	25	50	33	8	71	76	36	50	8	14	40	21
biomed	3	9	66	5	20	1	50	50	50	8	33	64	17	29	9	25	50	33
breast-cancer	6	61	74	31	41	13	16	33	20	7	25	70	13	23	33	25	33	30
bupa	6	47	62	24	29	5	20	33	25	24	49	59	25	64	25	16	50	25
cancer	6	37	87	19	36	9	20	25	21	5	21	84	11	54	10	25	50	37
car	6	43	96	22	86	89	20	80	45	11	57	98	29	65	41	16	50	30
cleveland	6	81	31	41	24	15	16	33	20	7	65	31	33	33	71	16	40	30
coil2000	6	99	92	50	18	9	16	33	18	12	177	91	89	79	98	9	77	42
colic	6	55	81	28	46	6	16	33	20	4	17	80	9	33	27	25	25	25
compas	6	77	34	39	17	8	16	20	17	15	183	37	92	66	43	12	60	27
contraceptive	6	99	49	50	8	2	20	60	37	17	385	48	193	27	32	12	66	21
dermatology	6	33	90	17	23	3	16	33	21	7	17	95	9	22	0	14	20	17
divorce	5	15	90	8	50	19	20	33	24	2	5	96	3	33	16	50	50	50
ecoli	6	45	75	23	4	5	20	20	20	53	109	59	55	25	19	20	66	36
fars	6	75	79	38	10	86	33	66	52	60	9969	76	4985	35	90	6	50	12
german	6	25	61	13	38	10	20	40	29	10	99	72	50	46	13	12	40	22
heart-c	6	43	65	22	36	18	20	33	22	4	15	75	8	87	81	25	50	34
heart-h	6	37	59	19	31	4	20	40	24	8	25	77	13	61	60	20	50	32
heart-statlog	6	33	55	17	29	5	20	33	30	4	13	81	7	71	31	25	50	35
hepatitis	5	17	77	9	33	6	20	33	24	3	11	80	6	33	14	33	33	33
house-votes-84	6	49	91	25	68	67	16	50	27	3	9	90	5	80	75	33	50	41
hungarian	6	33	69	17	29	2	25	40	31	4	19	77	10	40	30	33	33	33
ionosphere	4	9	70	5	60	3	33	50	38	5	17	80	9	33	0	33	60	47
iris	5	23	90	12	41	25	25	33	30	10	21	63	11	36	13	50	50	50
irish	4	13	97	7	71	54	33	50	36	3	7	100	4	0	0	—	—	—
kddcup	6	91	99	46	0	0	—	—	—	29	269	99	135	22	0.9	6	20	9
kr-vs-kp	6	49	96	25	80	75	16	60	33	13	67	99	34	79	43	7	70	35
lending	6	45	73	23	73	80	16	50	25	14	507	65	254	69	80	12	75	25
letter	6	127	58	64	1	0	20	20	20	46	4857	68	2429	6	7	6	25	9
lymphography	6	61	76	31	35	25	16	33	21	6	21	86	11	9	0	16	16	16
messidor	3	7	50	4	50	1	50	66	58	22	107	52	54	88	99	10	57	28
promoters	6	17	86	9	33	19	16	33	23	3	9	81	5	20	14	33	33	33
mushroom	6	39	100	20	80	44	16	33	24	5	23	100	12	50	31	20	40	25
mux6	6	55	61	28	85	78	20	50	37	4	15	46	8	37	31	25	33	30
new-thyroid	3	11	95	6	33	4	33	33	33	14	29	79	15	26	5	20	50	30
pendigits	6	121	88	61	0	0	—	—	—	38	937	85	469	25	86	6	25	11
postoperative	6	43	50	22	59	44	16	50	25	6	15	56	8	75	25	16	50	36
primary-tumor	6	55	71	28	35	21	16	33	21	6	21	82	11	54	31	16	50	31
promoters	1	3	90	2	0	0	—	—	—	3	9	81	5	20	14	33	33	33
recidivism	6	105	61	53	28	22	16	33	18	15	611	51	306	53	38	9	44	16
schizo	6	17	55	9	55	5	50	66	58	13	51	52	26	30	64	20	25	21
segmentation	4	15	38	8	0	0	—	—	—	27	57	23	29	48	2	11	71	39
seismic_bumps	6	37	89	19	42	19	20	33	24	8	39	93	20	60	79	20	60	42
shuttle	6	63	99	32	28	7	20	33	23	23	159	99	80	33	9	14	50	30
soybean	6	63	88	32	9	5	25	25	25	16	71	89	36	22	1	9	12	10
spambase	6	63	75	32	37	12	16	33	19	15	143	91	72	76	98	7	58	25
spect	6	45	82	23	60	51	20	50	35	6	15	86	8	87	98	50	83	65
splice	3	7	50	4	0	0	—	—	—	88	177	55	89	0	0	—	—	—
student-mat	6	109	35	55	9	3	20	25	21	22	177	25	89	6	6	11	20	15
student-por	6	119	30	60	1	0	20	20	20	22	259	26	130	9	5	7	20	10
tram_2000	1	3	100	2	0	0	—	—	—	1	3	100	2	0	0	—	—	—
uci_mammo	6	53	11	27	51	43	16	40	24	9	23	38	12	66	25	25	55	39
vehicle	6	79	49	40	10	0	16	20	19	24	141	58	71	45	54	9	41	23
wdbc	2	7	87	4	0	0	—	—	—	57	115	61	58	94	10	14	73	49
yeast	6	45	49	23	4	0	25	25	25	64	493	37	247	14	0	11	25	16

Table 4: Path explanation redundancy in decision trees obtained with IAI and ITI. The table shows tree statistics for IAI and ITI, namely, tree depth **D**, number of nodes **#N**, test accuracy **%A** and number of paths **#P**. The percentage of explanation-redundant paths (XRP's) is given as **%R** while the percentage of data instances (measured for the *entire* feature space) covered by XRP's is **%C**. Focusing solely on the XRP's, a single path-restricted AXp is extracted and the average (min. or max., resp.) percentage of explanation redundant features per path is denoted by **%avg** (**%m** and **%M**, resp.).

Dataset	IAI								ITI							
	Traversal				Horn				Traversal				Horn			
	m	**M**	**avg**	**Tot**	**m**	**M**	**avg**	**Tot**	**m**	**M**	**avg**	**Tot**	**m**	**M**	**avg**	**Tot**
IndiansDiabetes	0.001	0.003	0.001	0.73	0.001	0.002	0.001	0.63	0.001	0.003	0.002	1.19	0.001	0.002	0.001	1.02
adult	0.001	0.059	0.002	3.52	0.001	0.005	0.002	2.93	0.005	0.065	0.008	0.93	0.008	0.071	0.013	1.53
allhyper	0.001	0.006	0.002	1.88	0.001	0.005	0.001	1.23	0.001	0.004	0.002	2.39	0.001	0.002	0.001	1.20
ann-thyroid	0.001	0.005	0.002	3.67	0.001	0.005	0.001	2.85	0.002	0.041	0.006	12.14	0.004	0.029	0.005	9.64
anneal	0.001	0.005	0.001	1.22	0.001	0.003	0.001	0.75	0.001	0.006	0.001	0.96	0.001	0.004	0.001	0.70
appendicitis	0.000	0.000	0.000	0.029	0.000	0.000	0.000	0.032	0.000	0.001	0.000	0.028	0.000	0.001	0.000	0.033
australian	0.001	0.003	0.001	0.93	0.001	0.002	0.001	0.71	0.001	0.004	0.001	0.94	0.001	0.002	0.001	0.61
auto	0.001	0.005	0.001	0.22	0.001	0.005	0.001	0.18	0.001	0.005	0.002	0.33	0.001	0.005	0.001	0.24
backache	0.001	0.001	0.001	0.13	0.000	0.001	0.001	0.094	0.000	0.001	0.000	0.077	0.000	0.001	0.000	0.065
balance	0.001	0.004	0.001	0.82	0.002	0.005	0.002	1.15	0.001	0.057	0.001	0.86	0.002	0.006	0.002	1.23
bank	0.002	0.062	0.003	34.45	0.002	0.008	0.002	25.53	0.013	0.090	0.027	19.64	0.025	0.092	0.033	24.21
banknote	0.000	0.001	0.000	0.12	0.000	0.001	0.000	0.14	0.001	0.002	0.001	0.47	0.001	0.003	0.001	0.54
biodegradation	0.000	0.003	0.001	0.21	0.000	0.002	0.001	0.18	0.002	0.007	0.003	0.98	0.001	0.003	0.002	0.48
biomed	0.000	0.001	0.000	0.064	0.000	0.001	0.000	0.073	0.001	0.002	0.001	0.17	0.001	0.001	0.001	0.16
breast-cancer	0.001	0.003	0.002	0.42	0.001	0.004	0.001	0.35	0.000	0.001	0.001	0.19	0.001	0.001	0.001	0.17
bupa	0.001	0.003	0.001	0.33	0.001	0.002	0.001	0.34	0.001	0.002	0.001	0.33	0.001	0.005	0.001	0.35
cancer	0.001	0.003	0.001	0.53	0.001	0.003	0.001	0.39	0.001	0.004	0.001	0.32	0.001	0.002	0.001	0.26
car	0.001	0.004	0.001	0.52	0.001	0.002	0.001	0.48	0.001	0.002	0.001	0.47	0.001	0.002	0.001	0.59
cleveland	0.001	0.005	0.001	0.25	0.001	0.004	0.002	0.31	0.001	0.002	0.001	0.23	0.001	0.002	0.001	0.25
coil2000	0.003	0.036	0.009	21.56	0.002	0.009	0.002	5.77	0.004	0.044	0.018	44.26	0.003	0.029	0.004	11.02
colic	0.001	0.005	0.002	0.71	0.001	0.002	0.001	0.43	0.000	0.001	0.001	0.24	0.000	0.001	0.000	0.18
compas	0.001	0.004	0.002	0.66	0.001	0.004	0.002	0.52	0.002	0.065	0.004	1.37	0.003	0.005	0.004	1.28
contraceptive	0.001	0.005	0.002	0.70	0.002	0.004	0.002	0.78	0.003	0.064	0.006	2.64	0.006	0.012	0.007	2.87
dermatology	0.001	0.005	0.001	0.50	0.001	0.002	0.001	0.31	0.000	0.001	0.001	0.27	0.000	0.001	0.001	0.19
divorce	0.000	0.002	0.001	0.10	0.000	0.001	0.001	0.076	0.000	0.001	0.000	0.033	0.000	0.002	0.000	0.041
ecoli	0.001	0.003	0.001	0.25	0.001	0.002	0.001	0.32	0.001	0.057	0.001	0.46	0.002	0.004	0.002	0.62
fars	0.001	0.004	0.002	3.26	0.001	0.004	0.002	2.86	0.066	0.18	0.093	172.34	0.19	0.32	0.20	374.52
german	0.001	0.004	0.001	0.76	0.001	0.002	0.001	0.65	0.002	0.007	0.003	3.19	0.002	0.003	0.002	2.03
heart-c	0.001	0.003	0.001	0.42	0.001	0.003	0.001	0.30	0.000	0.001	0.001	0.17	0.000	0.001	0.000	0.14
heart-h	0.001	0.004	0.001	0.39	0.001	0.005	0.001	0.27	0.001	0.001	0.001	0.21	0.001	0.001	0.001	0.18
heart-statlog	0.001	0.003	0.001	0.26	0.001	0.002	0.001	0.23	0.000	0.001	0.001	0.14	0.000	0.001	0.000	0.11
hepatitis	0.001	0.002	0.001	0.12	0.000	0.002	0.001	0.084	0.000	0.001	0.000	0.064	0.000	0.002	0.000	0.062
house-votes-84	0.001	0.006	0.002	0.56	0.001	0.002	0.001	0.32	0.000	0.000	0.000	0.10	0.000	0.001	0.000	0.100
hungarian	0.001	0.003	0.001	0.27	0.001	0.005	0.001	0.24	0.001	0.002	0.001	0.23	0.000	0.002	0.001	0.18
ionosphere	0.000	0.001	0.000	0.15	0.000	0.002	0.001	0.18	0.001	0.003	0.001	0.36	0.000	0.002	0.001	0.26
iris	0.000	0.003	0.001	0.094	0.001	0.001	0.001	0.094	0.000	0.001	0.000	0.050	0.000	0.001	0.001	0.082
irish	0.000	0.002	0.000	0.20	0.000	0.001	0.000	0.21	0.000	0.001	0.000	0.092	0.000	0.001	0.000	0.14
kddcup	0.002	0.032	0.003	9.54	0.002	0.007	0.002	5.69	0.003	0.045	0.011	31.00	0.005	0.010	0.006	16.17
kr-vs-kp	0.001	0.008	0.002	2.17	0.001	0.004	0.001	1.22	0.001	0.009	0.004	3.41	0.001	0.003	0.002	1.49
lending	0.001	0.003	0.001	1.99	0.001	0.003	0.001	1.51	0.004	0.065	0.007	0.73	0.008	0.069	0.011	1.12
letter	0.002	0.062	0.002	13.36	0.002	0.007	0.003	14.30	0.034	0.11	0.052	19.50	0.078	0.16	0.11	40.77
lymphography	0.001	0.007	0.002	0.32	0.001	0.003	0.001	0.20	0.000	0.002	0.001	0.13	0.001	0.001	0.001	0.090
messidor	0.000	0.001	0.000	0.096	0.000	0.001	0.000	0.11	0.001	0.006	0.003	1.06	0.002	0.004	0.002	0.74
promoters	0.000	0.001	0.001	0.063	0.000	0.001	0.000	0.053	0.000	0.002	0.000	0.046	0.000	0.001	0.000	0.045
mushroom	0.001	0.004	0.001	3.11	0.001	0.002	0.001	2.20	0.001	0.003	0.001	2.46	0.001	0.002	0.001	1.54
mux6	0.001	0.002	0.001	0.076	0.001	0.002	0.001	0.069	0.000	0.001	0.001	0.040	0.000	0.002	0.001	0.035
new-thyroid	0.000	0.002	0.000	0.078	0.000	0.001	0.000	0.086	0.000	0.001	0.001	0.17	0.001	0.001	0.001	0.15
pendigits	0.002	0.063	0.003	10.03	0.002	0.007	0.003	8.45	0.008	0.093	0.014	3.11	0.016	0.089	0.022	4.81
postoperative	0.001	0.002	0.001	0.093	0.001	0.002	0.001	0.077	0.000	0.002	0.001	0.048	0.000	0.002	0.001	0.040
primary-tumor	0.001	0.005	0.002	0.47	0.001	0.004	0.001	0.28	0.001	0.001	0.001	0.17	0.001	0.001	0.001	0.13
promoters	0.000	0.000	0.000	0.017	0.000	0.000	0.000	0.024	0.000	0.001	0.000	0.039	0.000	0.001	0.000	0.037
recidivism	0.002	0.061	0.003	3.65	0.002	0.006	0.002	2.59	0.005	0.087	0.010	11.69	0.010	0.084	0.015	18.26
schizo	0.000	0.002	0.001	0.22	0.000	0.001	0.001	0.17	0.001	0.003	0.002	0.58	0.001	0.002	0.001	0.37
segmentation	0.000	0.001	0.000	0.098	0.000	0.001	0.000	0.096	0.001	0.002	0.001	0.30	0.001	0.002	0.001	0.25
seismic_bumps	0.001	0.003	0.001	1.08	0.001	0.002	0.001	0.68	0.001	0.004	0.002	1.83	0.001	0.002	0.001	0.69
shuttle	0.001	0.006	0.001	22.65	0.001	0.005	0.001	22.35	0.002	0.061	0.002	2.85	0.003	0.060	0.003	3.56
soybean	0.001	0.058	0.002	1.17	0.001	0.005	0.001	0.82	0.001	0.005	0.003	1.65	0.001	0.003	0.002	0.95
spambase	0.001	0.008	0.003	3.43	0.001	0.003	0.001	1.81	0.002	0.069	0.009	11.20	0.003	0.062	0.003	4.18
spect	0.001	0.006	0.002	0.52	0.001	0.004	0.001	0.24	0.000	0.001	0.001	0.17	0.000	0.001	0.000	0.11
splice	0.000	0.001	0.000	0.22	0.000	0.002	0.000	0.30	0.001	0.064	0.002	1.48	0.003	0.069	0.004	3.43
student-mat	0.002	0.061	0.003	1.14	0.002	0.007	0.002	0.92	0.002	0.058	0.005	1.98	0.003	0.060	0.004	1.56
student-por	0.002	0.059	0.003	1.94	0.002	0.004	0.002	1.53	0.003	0.062	0.008	5.05	0.004	0.072	0.006	3.63
tram_2000	0.000	0.001	0.000	0.10	0.000	0.001	0.000	0.15	0.000	0.001	0.000	0.10	0.000	0.001	0.000	0.15
uci_mammo	0.001	0.003	0.002	0.23	0.001	0.002	0.001	0.15	0.001	0.002	0.001	0.12	0.001	0.001	0.001	0.079
vehicle	0.001	0.008	0.002	1.74	0.001	0.006	0.002	1.52	0.002	0.060	0.003	2.81	0.002	0.061	0.003	2.51
wdbc	0.000	0.001	0.000	0.16	0.000	0.001	0.000	0.18	0.002	0.062	0.007	3.85	0.002	0.004	0.002	1.41
yeast	0.001	0.002	0.001	0.33	0.001	0.002	0.001	0.42	0.004	0.10	0.007	3.06	0.008	0.072	0.011	5.04

Table 5: Assessing runtimes of the tree traversal algorithm and the propositional horn encoding approach for extracting one AXp. The table reports the results for DTs trained with ITI and IAI learning tools. Columns **m**, **M** and **avg** report, respectively, the minimal, maximal and average runtime (in second) to compute an AXp, while column **Tot** reports the total runtime (in second) of all tested instances in a dataset.