

A formal language is composed of a set of non-terminal symbols, which in this case is  $N$ , a set of terminal symbols,  $E$ , a set of production rules, which determines what are the strings within the language (in the simplest case they can be thought as mappings from a set of strings with some specified features to another set of strings with some other specified features), mapping a string to a string, a set of transformation rules (which in the case of a formal logic are the inference rules), each mapping a  $n$ -uple of strings (again with some predefined features) to a string, and a set of axioms.

The production rules are:

1) replace the start symbol “ $S$ ” by the token “ $xB_y$ ”, where  $x, y \in E$ , with  $x \neq y$ ;

2) replace an occurrence of “ $xx$ ”,  $x \in E$  by the symbol “ $T$ ”,  $T \in N$ .

The transformation rule is:

For any two sentences  $\phi, \psi$  of the language, “ $X^s$ ” is a sentence of the language, where  $X$  is the end symbol and  $s$  is the number of occurrences of “ $xx$ ” in  $\phi$  added to the number of occurrences of “ $yy$ ” in  $\psi$ , with  $x, y \in E$  and  $x \neq y$ . “ $X^s$ ” is a string of  $X$ ’s with length  $s$  (“ $XXXX...X$ ”).