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5  * CSCI 532 Semester Project
6  *
7  * Problem #3 (expanded)
8  * Write a C/C++/Matlab/Java program to compute insertion sort and merge sort.
9  * (You can use the code from the textbooks by Deitel and Deitel or from the
10 * web.)
11 * Obtain the run time of both routines.
12 * The input data should be an int array containing random element values
13 * (between, say, 0 and 1023).
14 * Obtain run time T with 1D (input) array size of n=16, 256, 4096, 65536,
15 * 1048576 (which equal  $2^p$ , where  $p = 4, 8, 12, 16, 20$ ).
16 * The run time for each n should be average with about  $\text{floor}(512/(p*p))$  runs.
17 * Each run (for a given n) should use a different random input.
18 * Plot (with Excel, Matlab, or other available tools) the run time for both
19 * routines on one plot, with the x axis in p values, and y axis in  $\log(T)$ .
20 * Label on the plot which curve is for insertion sort and which is for merge
21 * sort.
22 * Submit C/C++ programs and plot, with instructions in readme.txt on how to
23 * build and run the program. (Include the Dev-C++ or MS Studio or Java
24 * NetBeans project file.)
25 *
26 *****/
27
28 /** References *****/
29 *
30 * Time calculation in C++11
31 * https://solarianprogrammer.com/2012/10/14/cpp-11-timing-code-performance/
32 *
33 * Random numbers in C++11
34 * http://en.cppreference.com/w/cpp/numeric/random
35 *
36 * Using std::copy instead of a for loop for a single-line vector print:
37 * https://stackoverflow.com/questions/10750057/how-to-print-out-the-contents-of-a-vector/11335634#11335634
38 *
39 * Merge Sort from Deitel and Deitel
40 * Insertion Sort from Deitel and Deitel
41 *
42 *****/
43
44 #include <iostream>
45 #include <fstream>
46 #include <vector>
47 #include <random>
48 #include <iterator>
49 #include <chrono>
50 #include <string>
51 #include <functional>
52 #include <algorithm> // For remove_if when setting the save file name
53
54
55 /*
56 By default, the program runs a decreasing number of trials, such that for an
57 array of size  $n=2^p$ , the number of trials is  $\text{floor}(512/(p*p))$ , (per the
58 project instructions).
59 I would like a more scientific approach (i.e. a more) uniform number of

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60     trials), so I have included a command line option to run the same number of
61     trials for each vector size. On my computer, a vector of  $n = 2^{20} = 1048567$ 
62     can be sorted in around 24 minutes using insertion sort, so a batch size of
63     24 allows the entire program to run roughly overnight.
64 */
65 constexpr int STANDARD_BATCH_SIZE = 24;
66
67 /*
68 If, instead, the program is being run as assigned, then calculate the batch
69 size based on the formula  $\text{floor}(512/p^2)$ 
70 */
71 inline int assigned_batch_size( int p ) {
72     return floor ( 512 / ( p * p ) );
73 }
74
75 /*
76 Arrays of size  $n = 20$  take almost half an hour to run, which is far too long
77 for testing. This limits the size of arrays to those that can be processed
78 quickly.
79 */
80 constexpr int MAX_N = 1000000;
81
82 // Struct to allow passing both a function and some name for it
83 struct NamedFunction {
84     std::string function_name;
85     std::function<void( std::vector<int>& )> function;
86 };
87
88
89
90 // Sort a vector in place using insertion sort
91 void insertion_sort( std::vector<int>& );
92
93
94 // Sort a vector in place using merge sort
95 void merge_sort( std::vector<int>& );
96 // Merge sort helper functions
97 void merge( std::vector<int>&, int, int, int, int );
98 void sort_sub_vector( std::vector<int>&, int, int );
99
100
101 // Fill an int vector with random integers
102 void random_fill( std::vector<int>& );
103
104
105 // Overload operator<< for vectors to simplify output of all vector elements
106 template<typename T>
107 std::ostream & operator<<( std::ostream&, const std::vector<T>& );
108
109
110 // Function that allows each different sorting algorithm to be tested and timed
111 // using the same code.
112 void test_sorter( NamedFunction&, std::vector<int>, bool, bool );
113
114 // Demonstrate that a given sorter function actually does sort a vector properly
115 void demo_sorter( NamedFunction );
116
117
118
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120 int main(int argc, char **argv) {
121     // Put the command line arguments into a vector for easier access
122     std::vector<std::string> args{argv + 1, argv + argc};
123
124     // Flags to determine run-time behavior.
125     // Default values are the problem as assigned.
126     // Changing these through command line options results in more interesting tests.
127     bool run_insertion_sort = true;
128     bool run_merge_sort = true;
129     bool limit_n = false;
130     bool demo = false;
131     bool time = true;
132
133     // p determines both the array size and the number of tests per array
134     // Arrays of size 2^p will be tested either floor(512/(p*p)) times or 32 times
135     // Having a vector of ps will make things easier later
136     std::vector<int> ps { 4, 8, 12, 16, 20 };
137
138     // Determine the sizes of the test runs.
139     // If false, then each vector of size 2^p will be tested floor(512/(p*p)) times
140     // If true, each vector will be tested the same number of times (set above)
141     bool equal_batch_sizes = false;
142
143
144     // Adjust run-time flags according to command line arguments
145     for ( auto flag : args ) {
146         if ( flag == "merge-only" ) { run_insertion_sort = false; }
147         if ( flag == "insertion-only" ) { run_merge_sort = false; }
148         if ( flag == "equal-batches" ) { equal_batch_sizes = true; }
149         if ( flag == "limit-n" ) { limit_n = true; }
150         if ( flag == "demo-sorters" ) { demo = true; }
151         if ( flag == "no-time" ) { time = false; }
152     }
153
154     // Create a vector of functions to test based on command line options
155     // Default is both Insertion Sort and Merge Sort,
156     // but these can be stopped by command line options above
157     std::vector<NamedFunction> sorters;
158     if ( run_insertion_sort ) {
159         sorters.push_back( NamedFunction{ "Insertion Sort", insertion_sort } );
160     }
161     if ( run_merge_sort ) {
162         sorters.push_back( NamedFunction{ "Merge Sort", merge_sort } );
163     }
164
165     // Demonstrate that the sort functions sort correctly (disabled by default)
166     if ( demo ) {
167         for ( auto sorter : sorters ) {
168             demo_sorter ( sorter );
169         }
170     }
171
172     // The heart of the project
173     // Test the run-time of each sort function as assigned (enabled by default)
174     if ( time ) {
175         for ( auto sorter : sorters ) {
176             test_sorter( sorter, ps, equal_batch_sizes, limit_n );
177         }
178     }
179

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180     return 0;
181 }
182
183
184
185 // Sort a vector in place using insertion sort
186 void insertion_sort( std::vector<int> &v ) {
187     // Loop through the elements of the array
188     for ( int j = 1; j < v.size(); j++ )
189     {
190         int key = v[j];
191         int i = j - 1;
192
193         while ( i >= 0 && v[i] > key )
194         {
195             v[ i + 1 ] = v[i];
196             i -= 1;
197         }
198
199         v[ i + 1 ] = key;
200     }
201 }
202
203
204
205 // Sort a vector in place using merge sort
206 void merge_sort( std::vector<int> &v ) {
207     sort_sub_vector( v, 0, v.size() - 1 );
208 }
209
210
211
212 // Helper function to merge subvectors
213 void merge( std::vector<int> &v, int left, int mid1, int mid2, int right ) {
214     int left_index = left;
215     int right_index = mid2;
216     int combined_index = left;
217     std::vector<int> combined( v.size() );
218
219     // Merge subvectors until reaching the end of either
220     while ( left_index <= mid1 && right_index <= right ) {
221         // Place the smaller of the two current elements into result
222         // and move to next space in vector
223         if ( v[ left_index ] <= v[ right_index ] ) {
224             combined[ combined_index++ ] = v[ left_index++ ];
225         } else {
226             combined[ combined_index++ ] = v[ right_index++ ];
227         }
228     }
229
230     // Put any leftover elements into the combined vector
231     if ( left_index == mid2 ) { // if at the end of the left vector
232         while ( right_index <= right ) { // copy rest of right vector
233             combined[ combined_index++ ] = v[ right_index++ ];
234         }
235     } else { // if at the end of the right vector
236         while ( left_index <= mid1 ) { // copy rest of left vector
237             combined[ combined_index++ ] = v[ left_index++ ];
238         }
239     }

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240
241 // Copy values back into the original vector
242 for ( int i = left; i <= right; i++ ) {
243     v[i] = combined[i];
244 }
245 }
246
247
248
249 // Helper function to recursively sort sub-vectors
250 void sort_sub_vector( std::vector<int> &v, int low, int high ) {
251     // Test against base case where size of vector is 1
252     if ( ( high - low ) >= 1 ) { // if NOT base case then
253
254         // Calculate midpoint of the vector,
255         // and the next element to the right.
256         int mid1 = ( low + high ) / 2;
257         int mid2 = mid1 + 1;
258
259         // Split vector in half and sort each half recursively
260         sort_sub_vector( v, low, mid1 ); // left half
261         sort_sub_vector( v, mid2, high ); // right half
262
263         // Merge the two sorted vectors
264         merge( v, low, mid1, mid2, high );
265     } // end if not base case
266 }
267
268
269
270 // Fill a vector in place with random integers
271 void random_fill( std::vector<int> &v ) {
272     // Initialize the C++11 random device
273     static std::random_device rd{};
274     static std::mt19937 mt{ rd() };
275     static std::uniform_int_distribution<int> dist{ 1, 1024 };
276
277     for ( int i = 0; i < v.size(); i++ )
278     {
279         v[i] = dist( mt );
280     }
281 }
282
283
284
285 // Overload operator<< for vectors to simplify output of all vector elements
286 template <typename T>
287 std::ostream& operator<< ( std::ostream &out, const std::vector<T> &v ) {
288     std::copy( v.begin(), v.end(), std::ostream_iterator<T>( out, " " ) );
289     return out;
290 }
291
292
293
294 // Given a NamedFunction, a vector of values for p, and booleans to determine
295 // whether or not to process equal batch sizes and whether or not to limit
296 // the size of the vector to vectors that can be sorted quickly, calculate the
297 // execution times for each of the sort algorithms
298 void test_sorter( NamedFunction &f, std::vector<int> ps,
299                 bool equal_batch_sizes,

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300         bool limit_n ) {
301     // Create a file to output the results
302     std::string file_name{ f.function_name };
303     file_name.erase( std::remove_if( file_name.begin(), file_name.end(), isspace ) );
304     std::transform( file_name.begin(), file_name.end(), file_name.begin(), tolower );
305     file_name += ".csv";
306
307     std::ofstream fout( file_name );
308
309     std::cout << std::endl << f.function_name << std::endl;
310
311     // Iterate through each of the p values (i.e. p = 4, 8, 12, ...)
312     for ( int p : ps ) {
313         // Vector size
314         int n = pow( 2, p );
315
316         // If n is being limited to certain fast-running small values,
317         // then skip this iteration
318         if ( limit_n && n > MAX_N ) { continue; }
319
320         // Calculate batch size
321         int batch_size = equal_batch_sizes ?
322             STANDARD_BATCH_SIZE :
323             assigned_batch_size( p );
324
325         // First column of the output is the size of the vector
326         std::cout << n << "\t" << std::flush;
327         fout << n << "\t" << std::flush;
328
329         for ( int trial = 0; trial < batch_size; trial++ ) {
330             // Create a vector and fill it with random numbers
331             std::vector<int> v( n );
332             random_fill( v );
333
334             // Time execution of the sort
335             auto start = std::chrono::steady_clock::now();
336             f.function( v );
337             auto end = std::chrono::steady_clock::now();
338
339             std::cout
340                 << std::chrono::duration<unsigned long long, std::nano>(end - start).count()
341                 << "\t" << std::flush;
342             fout
343                 << std::chrono::duration<unsigned long long, std::nano>(end - start).count()
344                 << "\t" << std::flush;
345         }
346
347         std::cout << std::endl;
348         fout << std::endl;
349     }
350
351     fout.close();
352 }
353
354
355 // Demonstrate that the sorter actually does sort a vector properly
356 void demo_sorter( NamedFunction sorter ) {
357     std::cout << std::endl << "==== Demonstrating "
358         << sorter.function_name

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360         << "  =====" << std::endl;
361
362     for ( int i = 0; i < 10; i++ ) {
363         std::vector<int> v( 10 );
364         random_fill( v );
365         std::cout << std::endl << "Before: " << v << std::endl;
366         sorter.function(v);
367         std::cout << "After: " << v << std::endl;
368     }
369 }
```