

## Control Week 4:

1.  $A = \begin{pmatrix} -2 & 0 & 0 \\ 0 & -2 & 0 \\ 0 & 3 & -1 \end{pmatrix} \quad 3 \times 3$

$$B = \begin{pmatrix} 0 & 1 \\ 1 & 0 \\ 0 & 1 \end{pmatrix} \quad 3 \times 2$$

$$W_r = \begin{bmatrix} B & AB & A^2 B \end{bmatrix} \quad 3 \times 6$$

Not full rank so not controllable

2. Yes

3.  $C = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \end{pmatrix} \quad 2 \times 3$

$$W_o = \begin{pmatrix} C \\ CA \\ CA^2 \end{pmatrix} \quad 6 \times 3 \quad \text{Not observable}$$

4. Yes