

CSE P505, Winter 2009, Assignment 1

Due: Thursday 22 January 2009, 5:00PM

Last updated: January 5

- This assignment emphasizes Caml programing, pattern matching, and higher-order functions.
 - Understand the course policies on academic integrity (see the syllabus) and challenge problems.
 - Modify `hw1.ml`, available on the course website, to produce your solution.
 - Do *not* use mutation.
 - Do *not* modify the code provided to you.
 - To turn in your solution, follow the “Turn-in” link on the course website and complete a simple file upload. Turn in just one file, named `hw1.ml`.
 - Your solutions should be correct, in good style (including indentation and line breaks), and using features we have used in class.
1. A type `inttree` for representing trees of ints is provided to you, as well as functions `insert`, `member`, and `fold`. The sample solution includes less than 40 additional lines of code.
 - (a) Define `fromList` of type `int list -> inttree` to make a sorted tree containing exactly the ints in the list without repeats. Use `insert` (provided).
 - (b) Define three functions, `sum1`, `prod1`, and `avg1`, to compute the sum, product, and average of the ints in a tree. Each has type `inttree -> int`. The sum and product of an empty tree are 0 and 1, respectively. For average, the empty tree should cause a `DivisionByZero` exception to be raised. For `sum1` and `prod1`, do not use helper functions. For `avg1`, do not traverse the tree more than once. (Hint: Have a helper function do the traversal and return a pair.)
 - (c) Define `map` of type `(int -> int) -> inttree -> inttree` to produce a tree with the same shape as its second argument with the int at each position the result of applying the first argument to the int at the same position in the second argument.
 - (d) Define `negateAll` of type `inttree -> inttree` using `map`. It produces a tree of the same shape where each int is replaced with its negation.
 - (e) In a *short English paragraph* (in an ML comment), explain how a client of `fold` (provided) would use it to compute something about the ints in a tree. Do *not* explain how `fold` is implemented, though obviously you will have to understand its implementation to document it.
 - (f) Define `sum2`, `prod2`, and `avg2` to compute the sum, product, and average of a tree (see above), but using `fold`. You should not need more than 1 line (possibly 2 for `avg2`). Use the same pair technique for average.
 2. In this problem you will define functions over lists of strings (type `string list`), but by *using standard-library functions instead of your own recursion*. Use partial application where appropriate, which is almost every problem. That is, do not write `let f x = g y x` when you can write `let f = g y`. The sample solution is less than 30 lines.
 - (a) Define `only_capitals` to take a `string list` and returns a `string list` containing only strings from the argument that start with an uppercase letter. Use library functions `List.filter` and `Char.uppercase` to produce a 1-line solution. To get the first character of a string `s`, use `s.[0]`.
 - (b) Define `longest_string1` to take a `string list` and return the longest string in the list. If the list is empty, return `""`. In the case of a tie, return the string closest to the beginning of the list. Use `List.fold_left` and `String.length`.

- (c) Define `longest_string2` that is exactly like `longest_string1` except in the case of ties it returns the string closest to the end of the list. Your solution should be almost an exact copy of `longest_string1`. Still use `List.fold_left` and `String.length`.
- (d) Write functions `longest_string_helper`, `longest_string3`, and `longest_string4` such that:
- `longest_string3` has the same behavior as `longest_string1` and `longest_string4` has the same behavior as `longest_string2`.
 - `longest_string_helper` has type `(int -> int -> bool) -> string list -> string`. This function will look a lot like `longest_string1` and `longest_string2` but is more general because it takes a function as an argument.
 - `longest_string3` and `longest_string4` are defined with partial applications of `longest_string_helper`.
- (e) Define `longest_capitalized` to take a `string list` and returns the longest string in the list that begins with an uppercase letter (or "" if there are no such strings). In the case of a tie, return the string closest to the beginning of the list.
3. In this problem, you will write two higher-order functions for lists. Both will be useful in the next problem. The sample solution is less than 15 lines.
- (a) Define `first_answer` of type `('a -> 'b option) -> 'a list -> 'b option`. The first argument should be applied to elements of the second argument until the first time it returns `Some v` for some `v` and then `Some v` is the result of the call to `first_answer`. If the first argument returns `None` for all list elements, then `first_answer` should return `None`.
- (b) Define `all_answers` of type `('a -> 'b list option) -> 'a list -> 'b list option`. The first argument should be applied to elements of the second argument. If it returns `None` for any element, then the result for `all_answers` is `None`. Else the calls to the first argument will have produced `Some lst1, Some lst2, ... Some lstn` and the result of `all_answers` is `Some lst` where `lst` is `lst1, lst2, ..., lstn` appended together (order doesn't matter). Note `all_answers f []` should evaluate to `Some []`. Hints: The sample solution uses a helper function with an accumulator and uses the `@` operator.
4. This problem uses these type definitions, which are similar to ones an ML implementation might use to implement pattern matching:¹

```
type pattern = Wildcard | Variable of string | UnitP | ConstP of int
              | TupleP of pattern list | ConstructorP of string * pattern
type valu = Const of int | Unit | Tuple of valu list | Constructor of string * valu
```

Given `valu v` and `pattern p`, either `p matches v` or not. If it does, the match produces a list of `string * valu` pairs representing what variables would be bound to what values. Order in the list does not matter. The rules for matching should be unsurprising:

- `Wildcard` matches everything and produces the empty list.
- `Variable s` matches any value `v` and produces the one-element list holding `(s,v)`.
- `UnitP` matches only `Unit`.
- `ConstP 17` matches only `Const 17` (and similarly for other integers).
- `TupleP ps` matches a value of the form `Tuple vs` if `ps` and `vs` have the same length and for all i , the i^{th} element of `ps` matches the i^{th} element of `vs`. The list produced is all the lists from the nested pattern matches appended together.
- `ConstructorP(s1,p)` matches `Constructor(s2,v)` if `s1` and `s2` are the same (strings can be compared with `=`) and `p` matches `v`. The list produced is the list from the nested pattern match.
- Nothing else matches.

¹Don't be confused that an ML implementation might itself be implemented in ML.

Problems (a)–(d) use the `pattern` type definition, but aren't about implementing pattern matching. Problems (e)–(g) are about implementing pattern matching. The sample solution is less than 35 additional lines of code.

- (a) A function `g` has been provided to you. In an ML comment, describe in a few English sentences the arguments that `g` takes and what `g` computes (not how `g` computes it, though you will have to understand that to determine what `g` computes).
- (b) Use `g` to define a function `count_wildcards` that takes a pattern and returns how many `Wildcard` patterns it contains.
- (c) Use `g` to define a function `count_wild_and_variable_lengths` that takes a pattern and returns the sum of the number of `Wildcard` patterns it contains and the string lengths of all the variables in the variable patterns it contains. (Use `String.length`.)
- (d) Use `g` to define a function `count_some_var` that takes a string and a pattern (as a pair) and returns the number of times the string appears as a variable in the pattern.
- (e) Write a function `check_pat` that takes a pattern and returns true if and only if all the variables appearing in the pattern are distinct from each other (i.e., use different strings). Note the choice of strings for constructors does not matter. Hints: The sample solution uses two helper functions. The first takes a pattern and returns a list of all the strings it uses for variables. Using `List.fold_left` with a function that uses `append` is useful in one case. The second takes a list of strings and decides if it has repeats. It uses `List.exists`.
- (f) Write a function `get_match` that takes a `valu * pattern` (notice this is a pair) and returns a `(string * valu) list option`, namely `NONE` if the pattern does not match and `SOME lst` where `lst` is the list of bindings if it does. Hints: Sample solution has one match expression with 7 branches. The branch for tuples uses `List.length`, `all_answers`, and `List.combine`.
- (g) Write a function `first_match` that takes a value and a list of patterns and returns a `(string * valu) list option`, namely `None` if no pattern in the list matches or `Some lst` where `lst` is the list of bindings for the first pattern in the list that matches. Hint: Sample solution is one line, using two functions previously defined.

See the next page for *challenge problems*.

5. **Challenge Problem** This problem continues problem 1 with a function `iter` (provided).
- (a) In a *short English paragraph*, explain how a client of the `iter` function (provided) would use it to process all the ints in a tree. In a second *short English paragraph*, explain how `iter` is implemented (e.g., “when” and “how” it traverses the tree).²
 - (b) Define `sum3`, `prod3`, and `avg3` to compute the sum, product, and average of a tree (see above), but using `iter` (provided). For product, the code must “stop as soon as it sees a 0” (this is easier than when using `fold`). Hint: You should need about 5 lines for each function. For each, use a local helper function as a “loop” that takes the iterator and the answer-so-far.
6. **Challenge Problem** This problem continues problem 4. Write a function `typecheck_patterns` that “type-checks” a `pattern list`. Types for our made-up pattern language are defined by:

```
type typ = Anything (* any type of value is okay *)
          | UnitT (* type for Unit *)
          | IntT (* type for integers *)
          | TupleT of typ list (* tuple types *)
          | Datatype of string (* some named datatype *)
```

`typecheck_patterns` should have type `((string * string * typ) list) -> (pattern list) -> typ option`. The first argument contains elements that look like `("foo", "bar", IntT)`, which means constructor `foo` makes a value of type `Datatype "bar"` given a value of type `IntT`. You may assume list elements all have different first fields (the constructor name), but there are probably elements with the same second field (the datatype name). Under the assumptions this list provides, you “type-check” the `pattern list` to see if there exists some `typ` (call it `t`) that *all* the patterns in the list can have. If so, return `Some t`, else return `None`.

You must return the “most lenient” type that all the patterns can have. For example, if the patterns are `TupleP[Variable("x");Variable("y")]` and `TupleP[Wildcard;Wildcard]`, you must return `TupleT[Anything;Anything]` even though they could both have type `TupleT[IntT;IntT]`. As another example, if the only patterns are `TupleP[Wildcard;Wildcard]` and `TupleP[Wildcard;TupleP[Wildcard;Wildcard]]`, you must return `TupleT[Anything;TupleT[Anything;Anything]]`.

Warning: The sample solution does not include this challenge problem.

²You might also try implementing `iter` using mutation instead of higher-order functions. It is not very pleasant.