CSE P505, Winter 2009, Assignment 4 Due: Thursday March 5, 2009, 5:00PM

Last updated: February 19

- This assignment covers type-checking, subtyping, and using abstract types to enforce strong interfaces.
- For problems 1 and 2, see also prob1.ml and lang.pdf.
- Problem 3 is independent of the other problems. See also stlc.mli, stlc.ml, stlc2.mli, stlc2.mli, and adversary.ml.
- We have provided a Makefile that creates two programs, prob1 and prob3.
- Turn in your solution via the "Turn-in" link on the course website. Include prob2.ml, stlc.ml, stlc.ml, adversary.ml, and a file for your answer to problem 2. If you do the first challenge problem, include another file. If you do the second challenge problem, include your answer in prob2.ml. Do not modify the .mli files.
- Understand the course policies on academic integrity (see the syllabus) and challenge problems.
- 1. In prob1.ml, complete the functions subtype and typecheck to provide a type-checker for the language described in lang.pdf. For subtype t1 t2, return true if and only if t1 is a subtype of t2. For typecheck, raise the DoesNotTypecheck exception or return the type of the expression. The exception carries a string: you may find it useful to use different strings for different errors, but the strings will not be graded.

For subtyping:

- The only subtype of IntT or BoolT is itself.
- Subtyping for arrow types is as usual.
- Subtyping for records includes:
 - Width and permutation as in class.
 - Depth: Sound yet expressive depth subtyping will depend on a field's access modifier. The correct rules are for you to figure out.
 - Subtyping based on different access modifiers. Again, the correct rules are left to you.

For typechecking:

- The "natural" typechecking rules are mostly left to you. See lang.pdf.
- If (e1,e2,e3) typechecks if e1 has a subtype of BoolT¹ and one of e2 and e3 has a subtype of the other. The supertype of these two types is the type of the whole expression. (This is the rule in languages like Java; see the challenge problems.)
- RecordV e should not typecheck because it should not appear in source programs.
- For Get and Set, be sure to consult the access modifier.
- Call checkType on every explicit type in the program. The result is (), but it may raise an exception. For RecordE, be sure the field names are unique. Together, these two checks ensure no record type will ever have repeated fields.

Hints:

- For subtyping, do not include code for reflexivity and transitivity. In other words, create a straightforward algorithm that is reflexive and transitive, though that may not be obvious.
- The sample solution for subtype is about 15 lines.

¹It happens that means e1 has exactly type BoolT, but in general we always allow subtypes.

- The typechecker does not need a subsumption rule. Instead you just use **subtype** in any place subsumption may be needed. For example, in an application, see if the argument has a subtype of the type the function expects.
- The sample solution for typecheck is about 65 lines.
- 2. Consider these two functions in our language (only their types differ):

```
Lam("x",RecordT[("1",IntT,Read)],
    RecordE[("11",Get(Var("x"),"1")); ("12",Var("x"))])
Lam("x",RecordT[("1",IntT,Both)],
    RecordE[("11",Get(Var("x"),"1")); ("12",Var("x"))])
```

In English, describe:

- A situation where using the first function would typecheck but the second would not
- A situation where using the second function would typecheck but the first would not
- How to use bounded polymorphism to extend our type system to overcome this code duplication
 — A few sentences is plenty, we do not need a full language design and description of the type
 system

Hint: Bounded polymorphism for *types* is one topic in Lecture 8, but here think about access modifiers.

3. This problem investigates several ways to enforce how clients use an interface. The file stlc.ml provides a typechecker and interpreter for a simply-typed lambda-calculus. We intend to use stlc.mli to enforce that the interpreter is never called with a program that does not typecheck. In other words, no client should be able to call interpret such that it raises RunTimeError. We will call an approach "safe" if it achieves this goal.

In parts (a)-(d), you will implement 4 different safe approaches, none of which require more than 2-3 lines of code in stlc.ml. (Do not change stlc.mli.) Files stlc2.mli and stlc2.ml are for part (e).

- (a) Implement interpret1 such that it typechecks its argument, raises TypeError if it does not typecheck, and calls interpret if it does typecheck. This is safe, but requires typechecking a program every time we run it.
- (b) Implement typecheck2 and interpret2 such that typecheck2 raises TypeError if its argument does not typecheck, otherwise it adds its argument to some mutable state holding a collection of expressions that typecheck. Then interpret2 should call interpret only if its argument is pointer-equal (Caml's == operator) to an expression in the mutable state typecheck2 adds to. This is safe, but requires a mutable global data structure and can waste memory.
- (c) Implement typecheck3 to raise TypeError if its argument does not typecheck, else return a thunk that when called interprets the program that typechecked. This is safe.
- (d) Implement typecheck4 to raise TypeError if its argument does not typecheck, else return its argument. Implement interpret4 to behave just like interpret. This is safe; look at stlc.mli to see why!
- (e) Copy your solutions into stlc2.ml. Use diff to see that stlc2.ml and stlc2.mli have one small but important change; part of the abstract syntax is mutable.
 - For each of the four approaches above, decide if they are safe for stlc2. If an approach is not safe, put code in adversary.ml that will cause Stlc2.RunTimeError to be raised. See adversary.ml for details about where to put this code.

- 4. (Challenge Problems) In problem 1, our typing rule for If(e1,e2,e3) is quite restrictive. A better rule might allow that if e2 has type t2 and e3 has type t3, then the whole expression has type t4 where t4 is the least common supertype of t2 and t3. By definition, the least common supertype would be a type t4 such that for all types t5 at least one of the following holds:
 - t5 is not a supertype of t2
 - t5 is not a supertype of t3
 - t5 is a supertype of t4

One minor problem for our language is that due to permutation least common supertypes for our language are not always unique, so we should more properly say a least common supertype. One major problem for our language is that least common supertypes do not always exist even when there are common supertypes.²

- (a) Give an example of two types ta and tb for which there are common supertypes but no least common supertypes. Give two types tc and td such that (1) tc and td are supertypes of ta and tb, (2) neither tc nor td is a subtype of the other, and (3) there is no type that is a supertype of ta and tb and a subtype of tc and td.
 - **Hint:** You can do this with just record types, access modifiers, and IntT no function types needed.
- (b) If we ignore the Read and Write access modifiers, i.e., assume our language has only the Both modifier, then least common supertypes do exist whenever two types have a common supertype. Given this assumption, implement a function least_common_supertype of type typ -> typ -> typ option, returning None if the types have no common supertype, else Some t where t is a least common supertype.

Hint: You will also have to implement a function that computes greatest common subtypes.

 $^{^2}$ By the way, Java and C# also have this problem but for different reasons.