

# COMP 352

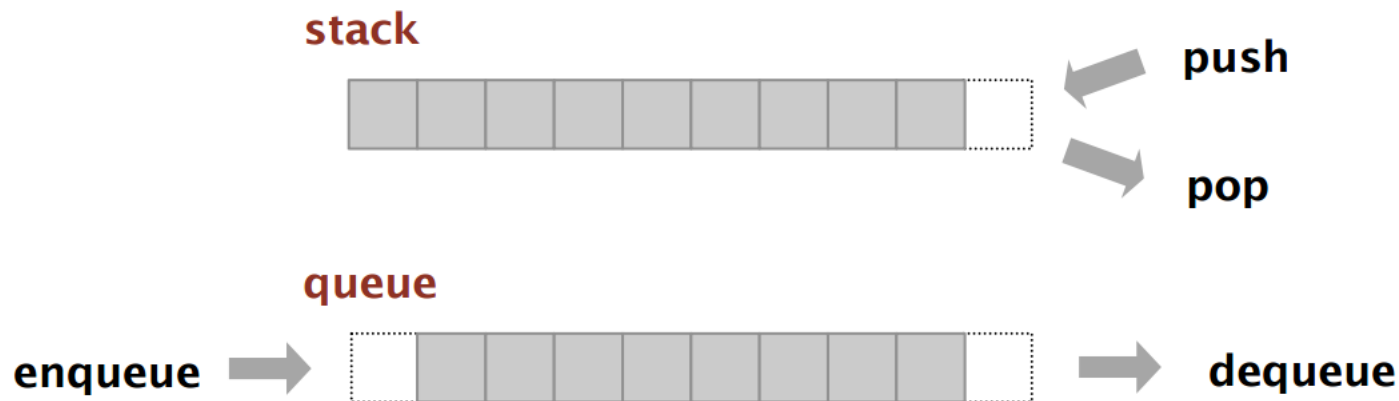
## Tutorial Session 4

# OUTLINE

- Queues and stacks:
  - List implementation
  - Array implementation
  - Exercise on stack

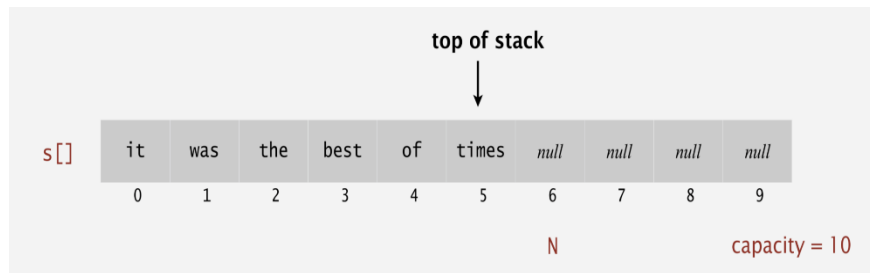
# STACK AND QUEUE

- Stack: examine the item most recently add ☐ **LIFO= Last In First Out**
- Queue: examine the item least recently add ☐ **FIFO= First In First Out**



# STACK ARRAY IMPLEMENTATION

- Simple way to implement stack
- Add element from left to right
- Keep track of the index of the top element



- Problem. Requiring client to provide capacity/ does not implement (a good) API!

**Solution with Resizing array:** If array is full, create a new array of twice the size, and copy items. halve size of array when array is one-quarter full

# STACK SINGLY LINKED LIST IMPLEMENTATION

- Need a class to represent a node in the list

```
Class Node {  
    Type data;  
    Node next;  
}
```

- The list keep track of the head

# STACK IMPLEMENTATION (CON'T)

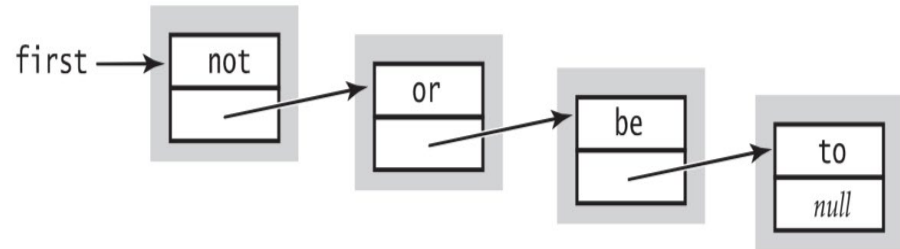
```
Class List{
```

```
Node first;
```

```
// all operations
```

```
}
```

- Add element from right to left.
- Note: one can use doubly linked list to implement stack



# QUEUE: ARRAY IMPLEMENTATION

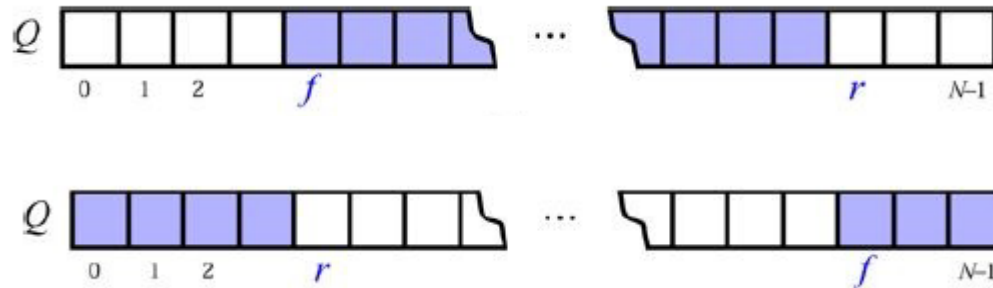
- Simple implementation
- Need to keep track of the index of the front and the rear



With a simple array when we dequeue we need to shift all the elements in the front

**Solution: Make the array circular or use a list !!!!!!!**

# HIGHLIGHTS ON A QUEUE IMPLEMENTATION USING A CIRCULAR ARRAY



- The following variables are defined:
  - $f$ : index to the cell storing the first element in the queue (candidate to be removed)
  - $r$ : index to the next available cell
- Operations:
  - $size() \sqcap (N - f + r) \bmod N$
  - $isEmpty() \sqcap f = r$
  - $enqueue(x) \sqcap r = (r + 1) \bmod N$
  - $dequeue() \sqcap f = (f + 1) \bmod N$



# QUEUE: LIST IMPLEMENTATION

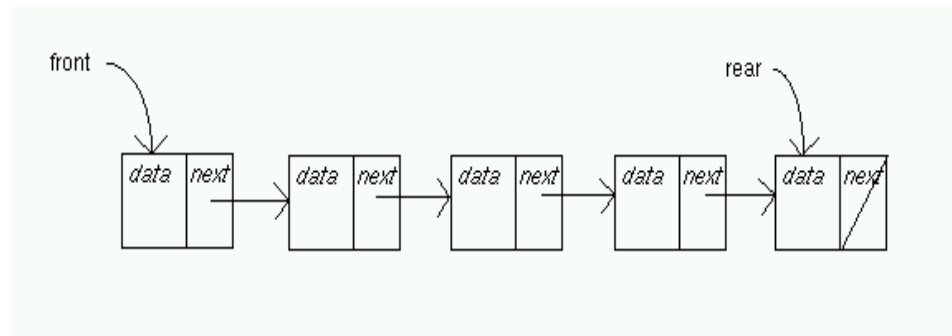
- Use doubly linked list.

*Class Node {*

*Type data;*

*Node next;*

*Node previous;}*



- Need to keep track of the front and rear of the list: *Class List{*

*Node first;*

*Node rear;*

*// all operations}*

# WORST CASE TIME COMPLEXITY LINEAR DATA STRUCTURE

Data Structure	Worst Case Time Complexity			
	Access	Search	Insertions	Delete
Array	$O(1)$	$O(n)$	$O(n)$	$O(n)$
Stack	$O(n)$	$O(n)$	$O(1)$	$O(1)$
Queue	$O(n)$	$O(n)$	$O(1)$	$O(1)$
Singly Linked List	$O(n)$	$O(n)$	Begin: $O(1)$ , End: $O(n)$	Begin: $O(1)$ , End: $O(n)$

# STACK EXERCISES

## Question 1:

Suppose an initially empty stack  $S$  has performed a total of 25 push operations, 12 top operations, and 10 pop operations, 3 of which generated `StackEmptyExceptions`, which were caught and ignored. What is the current size of  $S$ ?

# STACK EXERCISES

## Question 2:

Suppose you have a stack in which the values 1 through 5 must be pushed on the stack in that order, but that an item on the stack can be popped at any time. Give a sequence of push and pop operations such that the values are popped in the following order:

- a) 2,4,5,3,1
- b) 1,5,4,2,3
- c) 1,3,5,4,2

It might not be possible in each case.

# STACK EXERCISES

## **Question 3:**

Give a recursive method for removing all the elements in a stack.

# STACK EXERCISES

## Question 4:

Write a program that reads in a positive integer and prints the binary representation of that integer. Hint: divide the integer by 2.

# STACK EXERCISE

## Question 5:

Given an expression string, write a program to find whether a given string has balanced parentheses or not.

Only consider the parentheses [, ], (, ), {, }

- a) **Input :** `{[]{}()}` **Output :** Balanced
- b) **Input :** `[{}{}]` **Output :** Unbalanced

# QUEUE EXERCISES

## Question 6:

Describe the output for the following sequence of queue operations:

enqueue(5), enqueue(3), dequeue(), enqueue(2),  
enqueue(8), dequeue(), dequeue(), enqueue(9),  
enqueue(1), dequeue(), enqueue(7), enqueue(6),  
dequeue(), dequeue(), enqueue(4), dequeue(),  
dequeue().



# QUEUE EXERCISES

## Question 7:

Suppose an initially-empty queue  $Q$  has performed a total of 32 enqueue operations, 10 front operations, and 15 dequeue operations, 5 of which generated `QueueEmptyExceptions`, which were caught and ignored. What is the current size of  $Q$ ?

# QUEUE EXERCISES

## Question 8:

Give an algorithm for reversing a queue Q. Only the following standard operations are allowed on queue.

- enqueue(x) : Add an item x to rear of queue.
- dequeue() : Remove an item from front of queue.
- empty() : Checks if a queue is empty or not.

# STACK AND QUEUE EXERCISES

## **Question 9:**

Describe how to implement the stack ADT using two queues.

What is the running time of the `push()` and `pop()` methods in this case?