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# One line implementation of Cost and Gradient computation

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For a one variable linear regression model, the cost is

$$J = \frac{1}{2} (\theta x - y)^2$$

So I guess the J in this exercise is

$$J = \frac{1}{2} \sum_{i,j} (X\Theta - Y)^2$$

As the sum is for non-trivial items of Y, so it shall be modified a little bit:

$$J = \frac{1}{2} \sum_{i,j} (X\Theta - Y)^2 \cdot *R$$

This is very easy to be transformed into a OCTAVE representation.

For a one variable linear regression model, the gradient is

$$J' = (\theta x - y)x$$

So I guess the J' (the gradient) in this exercise is

$$\text{Grad}(\Theta) = (X\Theta - Y)X$$

$$\text{Grad}(X) = (X\Theta - Y)\Theta$$

As the sum is for non-trivial items of  $Y$ , so it shall be modified a little bit:

$$\text{Grad}(\Theta) = ((X\Theta - Y) \cdot *R)X$$

$$\text{Grad}(X) = ((X\Theta - Y) \cdot *R)\Theta$$

These are also very easy to be transformed into OCTAVE representations

I tried and succeeded.

The regularized version of these equations are :

$$J = \frac{1}{2} \sum_{i,j} (X\Theta - Y)^2 \cdot *R + \frac{\lambda}{2} \sum_{i,j} \Theta \cdot * \Theta + \frac{\lambda}{2} \sum_{i,j} X \cdot * X$$

$$\text{Grad}(\Theta) = ((X\Theta - Y) \cdot *R)X + \lambda \Theta$$

$$\text{Grad}(X) = ((X\Theta - Y) \cdot *R)\Theta + \lambda X$$

Is it simple and elegant?

↑ 21 ↓ · flag

shawn · 6 days ago

You are not the first one to figure it out, but you are the first one to relase it out. Do not get too much excited, please.

↑ -18 ↓ · flag

Jianwei Tao · 6 days ago

Thank you very much for your comment, Shawn!

Of course I am not the first one. There are definitely countless people who have worked out better solutions. I just wanted to share my trivial efforts with co-learners, and I also hope that others could share their better approaches, and learn something interesting from them.

↑ 9 ↓ · flag

Dimitri Liakhovitski · 5 days ago

I am confused about the dimensions for Theta\_grad and X\_grad.

$$\text{Grad}(\Theta) = ((X\Theta - Y) \cdot *R)\Theta$$

$$\text{Grad}(X) = ((X\Theta - Y) \cdot *R)X$$

I thought the size of  $((X\Theta - Y) \cdot R)$  is 1682 by 944 (number of movies x number of people). How can we multiply both by Theta (size 944 by 10) and by X (size 1682 by 944)?

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Dimitri Liakhovitski · 5 days ago

Isn't there an error in the formulas above? Shouldn't it rather be:

$$\text{Grad}(\Theta) = ((X\Theta - Y) \cdot R)X$$

$$\text{Grad}(X) = ((X\Theta - Y) \cdot R)\Theta$$

↑ 4 ↓ · flag

Sundee Laxman · 5 days ago

You're correct, Dimitri.

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Jianwei Tao · 5 days ago

Thank you, Dimitri. You are perfectly right. I have changed my writing fault.

↑ 0 ↓ · flag

刘凯 · 5 days ago

I am confused by  $\text{Grad}(\Theta)$ . The result of  $((X\Theta - Y) \cdot R)$  is  $\text{number\_movies} * \text{number\_users}$ , how could it time X ( $\text{num\_movies} * \text{num\_features}$ ), the dimensions for  $\text{Grad}(X)$  must equal to X ( $\text{num\_movies} * \text{num\_features}$ )

↑ 0 ↓ · flag

Jianwei Tao · 5 days ago

A transpose will make it work. Of course,  $\text{Grad}(\Theta)$  has the same size of  $\Theta$ ,  $\text{Grad}(X)$  has the same size of X.

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Anonymous · a day ago

One other thing....why compute  $X\Theta - Y$  over and over? Compute it once and use it for calculating J and both the gradients.

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Raúl Solera Rallo · 21 hours ago

I think there are a couple of mistakes taking into account the dimensions of each matrix:

- $Y = 1.682 \times 944$
- $\Theta = 944 \times 10$
- $X = 1.682 \times 10$

So, the first term of the equation should be  $X * \Theta'$  to get a  $1.682 \times 10 * 10 \times 944 = 1.682 \times 944$  matrix compatible with  $Y$  and  $R$ .

And after you get the  $1.682 \times 944$  matrix:  $M = ((X * \Theta' - Y) * R)$  then you have to transpose it to multiply it by  $X$  (as this is a  $1.682 \times 10$  matrix).

So I think that the correct final equations should be as follows:

- $M = ((X * \Theta' - Y) * R)$
- $Grad(\Theta) = M' * X + \lambda \Theta$
- $Grad(X) = M * \Theta + \lambda X$

Thank you for opening this post.

↑ 1 ↓ · flag

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Saddique Khan · 4 days ago

@Jianwei Tao

your work is tremendously amazing. There is an other mistake. I observed it. If it is not then clarify it. In Regularized cost function the last parameter need to sum two times because the simple  $J$  has  $1 \times 1$  dimension and Last parameters have  $1 \times 3$  dimensions. If you will sum it up again then it will also become  $1 \times 1$  element. I found this mistake while I was simulating the regularized cost function. Thanks btw,

↑ 0 ↓ · flag

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Kai Mysliwicz · 2 days ago

The vectorized one-liners are pretty fast compared to using two nested for-loops. The slow version took over half an hour, the fast one less than 5 seconds to compute the final recommendations.

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[+ Comment](#)**Daniel Rodrigo Ramírez Rebollo** · 2 days ago 

Great implementation, I really like how you figured out how to just choose the rated movies.

Thanks for sharing.

Best Regards from MExico

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