SerialExperimentsOlga

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Artificial Intelligence and
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Bachelor's Thesis

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Abstract

Abstract (different language)

Acknowledgement

Contents

1 Introduction

The field of ML on graph-structured data has recently become an active topic of research. One reason for this is the wide range of domains and problems that are expressible in terms of graphs.

1.1 Motivation

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Chapter 2: Related Work Some text

Chapter 3: Problem Description

Chapter 4: Implementation Some text

Chapter 5: Conclusion Finally, the results of this thesis are summarized and a brief outline of promising directions for future research is given.

2 Related Work

Before describing the problem, and later on the experimental setup, we first

1. Revise three common prediction tasks in graph neural networks (GNNs)
2. Give a general overview of how GNNs organize and process graph structured data
3. We further discuss the relation of messasge passing mechanis to the Weisfeiler-Lehman (WL), an algorithm for inspecting wheather two graphs are isomorph.
4. Give an formal definition and description of two GNN architectures, which will be used in our experiments.
5. Discuss typical issues, which occur in GNNs and methods for adressing those issues

2.1 Prediction Tasks and Typical Problems

Graphs naturally appear in numerous application domains, ranging from social analysis, bioinformatics to computer vision. A Graph $G = (V, E)$, where $V = \{v_1, ..., v_n\}$ is a set of $N = |V|$ nodes and $E \subseteq V \times V$ a set of edges betwen those nodes. The unique capability of graphs enables capturing the structural relations among data, and thus allows to harvest more insights compared to analyzing data in isolation [Zha+19]. Graphs therefore can be seen as a general laguage for describing entities and relationships between those entities. Graph neural networks (GNNs) then organize graph structured data to tackle various prediction and classification tasks. Typically, one is interested in one of the following three tasks:

1. **Link prediction:** Predict whether there are missing links between two nodes e.g., knowledge graph completion

2. **Vertex classification & regression:** Predict a property of a node e.g., categorize online users/items

3. **Graph classification & regression:** Here we are interested in classifying or predicting a continous value for the entire graph e.g., predicting a property of a molecule.

In this work the main focus will be on the latter two, node classification (NC) node regression (NR) and graph classification (GC) graph regression (GR) for small- as well as large-sized graphs.

2.2 Passing Messages in GNNs

Graphs, by nature are unstructured. Vertices in graphs have no natural order and can contatin any type of information. In order for machine learning algorithms to be able to make use of graph structured data, a mechanism is needed to organize them in a suitable way [Zho+20a; HYL17; Zha+19].

Message passing is a mechanism [Xu+19; Zho+20a], which embedds into every node information about it's neighbourhood. This can be done in several ways and one way of classifying a GNN is by looking at the underlying message passing machanism. In this paper we will look at a network, where message passing is done via convolutions (graph convolutional network (GCN)). We will however ocasionally use the more general term message passing, as the separation is rather blurred and message passing describes a neighborhood aggregation scheme and is seen as a generalization of other, more specific mechanisms.

Formally, message passing in a GNN can be described as using two functions: AGGREGATE and COMBINE. The expressive and representational power of a GNN can then be determined by looking at the concrete functions and thier properties, used to implement aggregation and combination. AGGREGATE mixes in every iteration the hidden representation of the node with the representation of nodes neighbourhood. COMBINE then combines the mixed representation togheter with the representation of the node. Each node uses the information from its neighbors to update its embeddings, thus a natural extension is to use the information to increase the receptive field by performing AGGREGATE and COMBINE multiple times.

$$a_v^k = \text{AGGREGATE}^{(k)}(\{h_u^{(k-1)} : u \in \mathcal{N}_{(v)}\}), h_v^{(k)} = \text{COMBINE}^{(k)}(h_v^{(k-1)}, a_v^{(k)})$$

For graph-level predictions an additional READOUT- operation is used:

$$h_G = \text{READOUT}(\{h_v^{(K)} | v \in G\})$$

One useful type of information, which the message passing framework should be able to capture, is the local graph structure. This can be done by choosing functions with appropriate properties. A more detailed explanation will follow in section 2.2.2. In spatial GNN we make the assumption of the similarity of neighbor nodes. To exploit this spatial similarity, we perform composition by stacking multiple layers togheter and increase the receptive field.

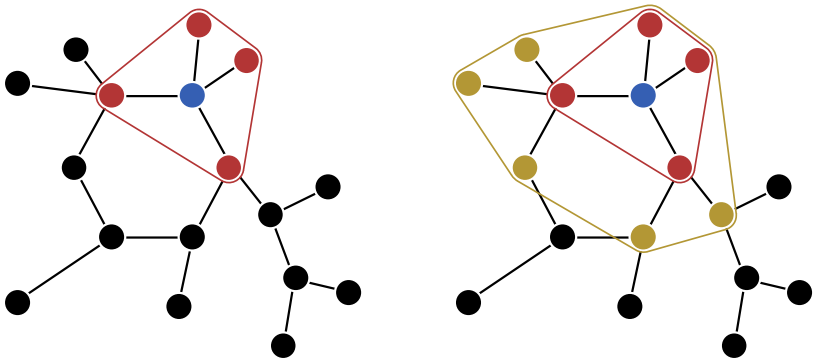

Fig. 2.1.: By performing aggregation k-times we can reach and capture the structural information of the k-hop neighborhood

2.2.1 Weisfeiler-Lehman Graph Colorings

The Message passing mechanism has a close relation, to the way the Weisfeiler-Lehman (WL) test [WL68] [DMH20] [HV22], an algorithm for deciding wheather two graphs are isomorphic works. Before describing the algorithm, we introduce notations and preliminaries.
Let $G = (V, E, X)$ denote an undirected graph where $V = \{v_1, ..., v_n\}$ is a set of $N = |V|$ nodes and $E \subseteq V \times V$ a set of edges between those nodes. For simplicity we represent an edge v, u by $(v, u) \in E$ or (u, v).$X = [x_1, ..., x_n]^T \in \mathbb{R}^{n \times d}$ is the node feature matrix, where $n = |V|$ is the number of nodes and $x_v \in \mathbb{R}^d$ represents the

d-dimensional feature of node v. $\mathcal{N}_v = \{u \in V | (v,u) \in E\}$ is the set of neighboring nodes of node v. A multiset is denoted as $\{\!\{...\}\!\}$ and formally defined as follows.

Definition 2.1 (Multiset)**.** A multiset is a generalized concept of set allowing repeating elements. A multiset X can be formally represented by a 2-tuple as $X = (S_X, m_X)$, where S_X is the underlying set formed by the distinct elements in the multiset and $m_X : S_X \to \mathbb{Z}^+$ gives the multiplicity (i.e, the number of occurrences) of the elements. If the elements in the multiset are generally drawn from a set X (i.e., $S_X \subseteq X$), then $\mathcal{X}$ is the universe of X and we denote it as $X \subseteq \mathcal{X}$ for ease of notation.

Definition 2.2 (Isomorphism)**.** Two Graphs $\mathcal{G} = (V, E, X)$ and $\mathcal{H} = (P, F, Y)$ are *isomorphic,* denoted as $\mathcal{G} \simeq \mathcal{H}$, if there exists a *bijective* mapping $g : V \to P$ such that $x_v = y_{g(v)}$, $\forall v \in V$ and $(v,u) \in E$ iff $(g(v), g(u)) \in F$. Graph Isomorphism is still an open problem without a known polynomial-time solution.

The 1-dimensional WL algorithm (color refinement)

In the 1-dimensional WL algorithm (1-WL), a label, called color c_v^0 is assigned to each vertex of a graph. Then, in every iteration the colors get updated based on the multiset representation of the neighborhood of the node until convergence. If at some iteration the colorings of the graphs differ, 1-WL decides, that the graphs are not isorprphic.

$$c_v^l \leftarrow \text{HASH}(c_v^{l-1}, \{\!\{c_u^(l-1) | u \in \mathcal{N}_v\}\!\})$$

Algorithmically this can be expressed as follows:

Algorithm 1 1-dim. WL (color refinement)

Input: $G = (V, E, X_V)$
1: $c_v^0 \leftarrow hash(X_v)$ for all $v \in V$
2: **repeat**
3: $\quad c_v^l \leftarrow hash(c_v^{l-1}, \{\!\{c_w^{l-1} : w \in \mathcal{N}_G(v)\}\!\})$ forall $v \in V$
4: **until** $(c_v^l)_{v \in V} = (c_v^{l-1})_{v \in V}$
5: **return** $\{\!\{c_v^l : v \in V\}\!\}$

The 1-WL is a heuristic method, which can efficiently distinguish a broad class of non-isomorphic graphs [BK79]. However there exist some corner cases, where the algorithm fails to classify simple shapes as non-isomorphic.

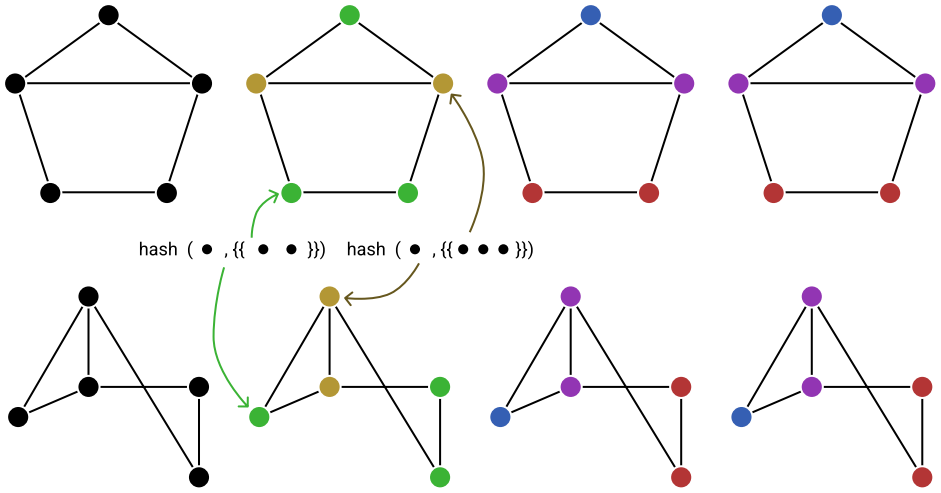

Fig. 2.2.: 1-WLTwo isomorphic graphs. 1-WLassigns same representation

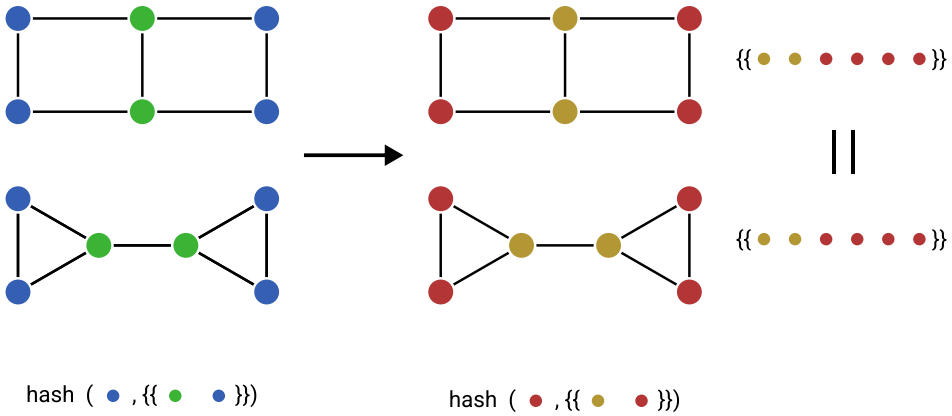

Fig. 2.3.: 1-WL assigned one and the same labeling to two non-isomorphic graphs [LYJ22]

2.2.2 GNN Architectures in this Paper

In the following section we briefly introduce and motivate the choice of two types of networks, which we have chosen to experiementally verify the efficacy of several regularization techniques, which will be discussed in section section 2.2.4.

Since all of GNN encorporate meaasge passing in a way, we decided to chose two interesting architectures for our experiments, which in our view are promising.

Graph Convolutional Network (GCN)

Graph Convolutional Network GCN was originally proposed by Kipf and Welling [KW17] to tackle the problem of semi-supervised node classification, where lables are available for a small subset of nodes. GNNis a simple, but powerful architecture, that scales linearly in the number of graph edges and learns hidden layer representations that encode both local graph structure and features of nodes.

A graph convolutional network (GCN) can formally be expressed via the following layer-wise propagation rule:

$$H^{(l+1)} = \sigma(\tilde{D}^{-\frac{1}{2}}\tilde{A}\tilde{D}^{-\frac{1}{2}}H^{(l)}W^{(l)})$$

Where $\tilde{A} = A + I_N$ is the adjacency matrix of the undirected graph $\mathcal{G}$ with added self-connections. I_N is the identity matrix. $\tilde{D}_{ii} = \sum_j \tilde{A}_{ij}$and W^l is a layer-specific trainable weight-matrix.$\sigma(\cdot)$ denotes an activation function, such as $ReLU(\cdot) = max(0, \cdot)$. $H^l \in N \times D$ is the matrix of activations in the l^{th} layer; $H^0 = X$

Because we consider every neighbor to be of equal importance and therefore normalization is accomplished by dividing by the number of neighbours, one can view this operation as performing an element-wise mean-pooling [Xu+19].

$$h_v^{(k)} = \text{ReLU}(\text{W} \cdot \text{MEAN}\{h_u^{k-1},\ \forall u \in \mathcal{N}_{(v)} \cup \{v\}\})$$

An application of a two-layer GCN is given by:

$$Z = f(X, A) = \text{softmax}(\hat{A}\ \text{ReLU}(\hat{A}XW^0)W^l)$$

where $\hat{A} = \tilde{D}^{-\frac{1}{2}}\tilde{A}\tilde{D^{-\frac{1}{2}}}$ is calculated in a preprocessing step. The model uses a single weight matrix per layer and deals with varying node degrees through an appropriate normalization of the adjacency matrix. This model consisted of a 2-layer GCN performed well in a series of experimental tasks, including semi-supervised document classification, semi-superwised node classification in citation networks and semi-supervised entity classification in a bipartite graph extracted

from a knowledge graph. The prediction accuracy was evaluated on a set of 1000 examples and additional experiments on deeper models with up to 10 layers have been also provided. GCN outperformed related methodslike ManiReg, SemiEmb, LP, DeepWalk, ICA and Platenoid by a significant margin on all of the datasets, which suggests, that the proposed network is capable of encoding both graph structure and node features.

Furthermore it overcame known limitations of existing approaches such as methods based on graph-laplacian regularization, which are limited due to their assumption that edges encode mere similarity of nodes and Skip-gram based methods, that are limited by being based on a multi-step pipeline, which is difficult to optimize.

Overall graph convolutional network (GCN) are widely and successfully used today in many fiels due to thier simplicity and scalability.

Graph Isomorphism Network (GIN)

To overcome the lack of expressivity of popular GNN architectures, [Xu+19] designed a new type of GNN, the graph isomorphism network graph isomorphism network (GIN). They proved that GINs are strictly more expressive than a variety of previous GNN-architectures and that they are in fact as powerful as the commonly used 1-dimensional Weisfeiler-Lehman (WL).

Two requirements must be met for a network to have the same expressive and representational power as the WL- Isomorphism test:

1. The framework must be able to represent the set of feature vectors of a given nodes neighbors as a multiset.

2. Choosing an injective function for the aggregation step. Such a function would never map two different neighborhoods to the same representation.

The more discriminative the multiset function is, the more powerful the representational power of the underlying GNN.

A comparison of three possible aggregation functions shows their power and limitations. Maximally powerful GNNs would map two nodes to the same embedding

space *only if* they have the same subtree structures with identical features on the corresponding nodes.

Formally a graph isomorphism network (GIN) can be expressed as follows:

$$h_v^{(k)} = \mathrm{MLP}^{(k)}\left((1+\epsilon^{(k)})\cdot h_v^{(k-1)} + \sum_{u\in\mathcal{N}(v)} h_u^{(k-1)}\right)$$

The choice of such an architecture, is motivated by the necessity to learn two functions with certain properties, f and ϕ. This task can be accomplished using a multilayer perceptron (MLP). The following lemma and corollary, proven by Xu et al. [Xu+19] show the properties and application of the functions:

Lemma 2.3. *Assume $\mathcal{X}$ is countable. There exists a function $f : \mathcal{X} \to \mathbb{R}^n$ so that $h(X) = \sum_{x\in X} f(x)$ is unique for each multiset $X \subseteq \mathcal{X}$ of bounded size. Moreover, any multiset function g can be decomposed as $g(X) = \phi(\sum_{x\in X} f(x))$ for some function ϕ*

Corollary 2.4. *Assume $\mathcal{X}$ is countable. There exists a function $f : \mathcal{X} \to \mathbb{R}^n$ so that for infinetly many choices of ϵ, including all irrational numbers, $h(c, X) = (1+\epsilon)\cdot f(c) + \sum_{x\in X} f(x)$ is unique for each pair (c,X), where $c \in \mathcal{X}$ and $X \subseteq \mathcal{X}$ is a multiset of bounded size. Moreover, any function g over such pairs can be decomposed as $g(c, X) = \varphi(1+\epsilon)\dot{f}(c) + \sum_{x\in X} f(x)$ for some function φ*

2.2.3 Weaknesses and Obstacles in GNN Architectures

Because of the way GNNs operate, they tend to suffer from two main obstacles: overfitting and oversmoothing.

Overfitting hinders the generalization ability of a neural network (NN), making it perform poorly on previously unseen data. This problematic occurs expecially when using small datasets, since the model thends to 'memorize' instead of learn the pattern.

Oversmoothing is a condition, where the performance and predictive power of a NN does not imporve of even gets worse when more layers are added. This happens

because by stacking multiple layers togheter togheter aggregation is being performed over and over again. This way, the representation of a node is being smoothed - mixed with features of very distant, possibly unrelated nodes. Oversmoothing is a problem mainly for node classification tasks. There is a trade-off between the expressivness of the model (capturing) graph structure by applying multiple layers and oversmoothing, which leads to a model where nodes have the same representation, because they all converge to indistinguishable vectors [Zho+20b; Has+20].[1]

A closer examination of underlying causes of oversmoothing was conducted by Chen et al. [Che+20], who suggested, that not message passing itself, but the type of interacting nodes cause this issue. For node classification (NC) tasks, intra-class communication (interaction between two nodes sharing the same class) is useful (signal), whereas inter-class communication (the communication between two nodes sharing different lables) is considered harmful, because it brings interference noise into the feature-representations by mixing unrelated features and therefore making unrelated nodes more similar to each other. Because of that, the the quality of shared information is essencial and should therefore be considered as a benchmark for improvement.

2.2.4 Regularization Techniques

Kukacka et al. [KGC17] define Regularization as any supplementary technique that aims at making the model generalize better, i.e. produce better results on the test set, which can include various properties of the loss function, the loss optimization algorithm, or other techniques.

One subgroup of regularization is via data, where the training set $\mathcal{D}$ is transformed into a new set $\mathcal{D}_R$ using some stochastic parameter π, which can be used in various ways, including to manipulate the feature space, create a new, augmented dataset or to change (e.g, thin out the hidden layers of the NN)

An example of such a transformation would is corruption of inputs by Gaussian noise.

$$\tau_0(x) = x + \theta, \theta \backsim \mathcal{N}(0, \Sigma) \tag{2.1}$$

[1] In spatial GNNs we make the assumption of relatedness by proximity.

In this work we focus on stochastic regularization techniques, which perform data augmentation in one way or another and whose main benefits lie in the alliviation of overfitting and oversmoothing[Has+20]. We will use the following notations:

Notation	Description
$H^{(l)} = [h_0^{(l)}, ...h_n^{(l)}]^T \in \mathbb{R}^{n \times f_t}$	Output of the $l-th$ hidden layer in GNN
n	Number of nodes
f_t	The number of output features at the l-th layer
$H^0 = X \in \mathbb{R}^{n \times f^0}$	Input matrix of node attributes
f_0	Number of nodes features
$W^l \in \mathbb{R}^{f_t \times f_{t+1}}$	The GNN parameters at the l-th layer
$\sigma(\cdot)$	Corresponding activation function
$\mathcal{N}(v)$	Neighborhood of node v
$\tilde{\mathcal{N}}(v) = \mathcal{N}(v) \cup v$	$\mathcal{N}(v)$ with added self-connection
$\mathfrak{N}(\cdot)$	Normalizing operator
$\odot$	Hadamard product

DropOut (Srivastava et al.)

DropOut (DO) randomly removes elements of its previous hidden layer $H^{(l)}$ based on independent Bernoulli random draws with a constant success rate at each training iteraration:

$$H^{(l+1)} = \sigma(\mathfrak{R}(A)(Z^{(l)} \odot H^{(l)})W^{(l)})$$

where Z^l is a ramdom binary matrix, with the same dimensions as H^l, whose elements are samples of Bernoulli(π)

The random drop of units (along with their connections) from the neural network during training prevents units from co-adapting too much. A neural net with n units can be seen as a collection of 2^n possible networks. Applying dropout with a certain probability p can be interpreted as sampling "thinned" networks from all possible 2^n networks. In the end, since averaging over all possible networks is computationally expensive, an approximation for combining the prediction is used. This averaging method entails using a single neural net with weights, which are scaled-down weights obtained during training time. Since a feature is present with

probability p at training time, we can average by multiplying the outgoing weights of that unit by p at test time.

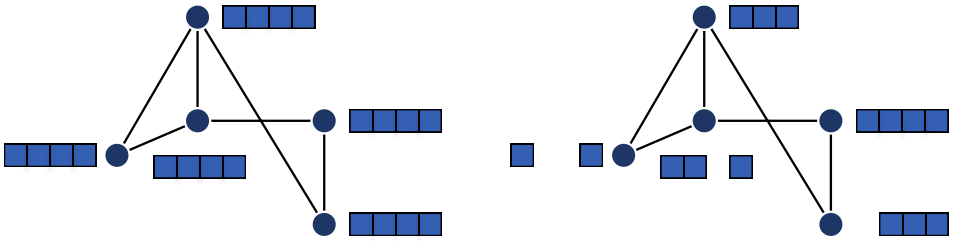

Fig. 2.4.: DropOut (DO) preserves connections between nodes as well as the nodes itself, unless we chose a large probability p, which drops all of the nodes features

DropEdge (Rong et al.)

DropEdge (DE) randomly removes a certain number of edges from the input graph at each training epoch, acting like a data augmenter and also a message passing reducer.

$$H^{(l+1)} = \sigma(\mathfrak{R}(A \odot Z^{(l)})H^{(l)}W^{(l)})$$

The random binary mask Z^l has the same dimensions as A. Its elements are the random samples of Bernoulli(π) where their corresponding elements in A are non-zero and zero everywhere else. Message passing in GNNs happens along the edges between neighbours. Randomly removng edges makes the connections more sparse, which leads to slower convergence time and thus prevents the network from oversmoothing and allows for a deeper architecture. The random deformation of the graph, resulting from DE acts as data augmentation, which prevents over-fitting. The combination of DropOut and DropEdge reaches the best performance in terms of mitigating overfitting in GNNs

NodeSampling (Chen et al.)

This method of regularization, also known as FastGCN was developed to improve the GCN[KW17] architecture and adress the bottleneck issues of GCN caused by recursive expansion of neighborhoods. It reduces the expensive computation in

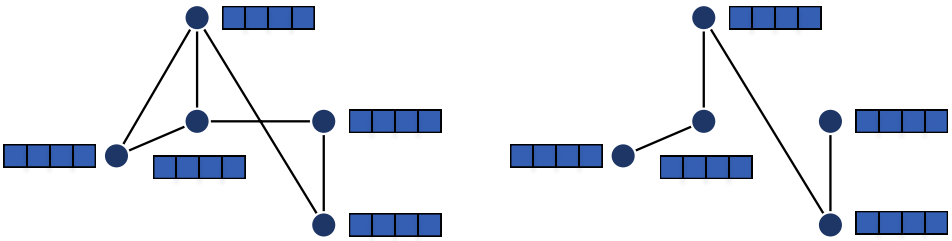

Fig. 2.5.: DropEdge (DE) preserves nodes and all of nodes featurs, but randomly removes edges, leading to a smaller number of neighbors, which results in slower conversion times and allowes for architectures with more hidden layers.

batch training of GNN by relaxing the requirement of simultaneous availability of test data.

$$H^{(l+1)} = \sigma(\Re(A)diag(z^{(l)})H^{(l)}W^{(l)})$$

where $z^{(l)}$ is a random vector whose elements are drawn from Bernoulli(π). This is a special case of DO, since all of the output features are either kept or completely dropped.

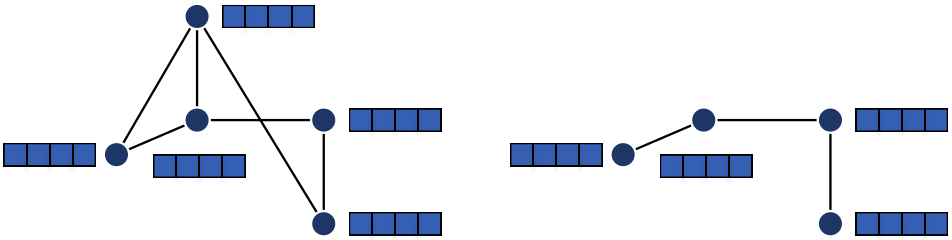

Fig. 2.6.: In NodeSampling (NS), a node is either removed or preserved along with the whole feature vector with a certain probability p.

GraphDropConnect (Hasanzadeh et al.)

Finally GraphDropConnect (GDC), which can be seen as a generalization of all the above proposed methods, is a stochastic regularization approach, which has been shown to be the most effective among all the above and even more effective than the combination of DO and DE. The regularization is done via adaptive connection sampling and can be interpreted as an approximation of Bayesian GNNs.

$$H^{(l+1)}[:,j] = \sigma\left(\sum_{i=1}^{f_t} \mathfrak{R}\left(A \odot Z_{i,j}^{(l)}\right) H^{(l)}[:,i] W^{(l)}[i,j]\right)$$
$$\text{for } j = 1, ..., f_{t+1}$$

where f_t and f_{t+1} are the number of features at layers l and $l+1$, respectively, and $Z_{i,j}^{(l)}$ is a sparse random matrix (with the same sparcity as A), whose non-zero elements are randomly drawn by Bernoulli(π_l), where $\pi_l$can be different for each layer.

All the methods are somewhat related and share some similarities [Ron+20]. DropOut (DO) has been successful in alleviating overfitting by preturbing the feature matrix and setting some entries to zero. The issue of over-smoothing is not affected by this measure. DropEdge (DE) achieved great results in reducing both overfitting as well as oversmoothing. Intuitively this makes sence, bacause smoothing comes from the aggrgation of the neighbours of a certain node and by dropping the connections to some neighbours, the feature- vectors of those neighbours are no longer smoothed in. NodeSampling (NS) has been proven to be effective in addressing the memory bottleneck issue of GCN caused by recursive expansion of neighborhoods.NS is a special case of DropOut, as all of the output features for a node are either completely kept or dropped while DropOut randomly removes some of these related output elements associated with the node. Also, along with the dropped node the edges of this node are dropped. The method itself, however is node-oriented and the edge-drop is a "side-effect".

Lastly GDC is a regularization tchnique, that combines all of the above by drawing different random masks for each channel and edge independently, which yield better performance results then all of the previous methods or even combinations of them.

3 Problem Description

[Has+20]

4 Implementation

This section provides a brief overview of experimental setup as well as used libraries and frameworks and gives an explanation for the choices. Despite GNNs being such a big deal and widely used in various domains, there is a lack of standartisation in machine learning on graphs. Tensorflow has no build-in structure for graph representation and expects the input to be tensors or dictionaries. A few attempts were made towards dealing with graph-structured data in a standardized way Spektral is Despite graph neural networks (GNNs) being a hot topic, there still is no standardized way of dealing with graphs in terms of representation, ...

A few efforts have been made to create standardized frameworks and libraries. Such examples are Spektral, and NetworX

4.1 Scope and Limitations

4.2 Experimental Setup

4.3 Evaluation

5 Conclusion

5.1 Future Work

Another proposed regularization technique https://arxiv.org/pdf/2106.07971.pdf

Appendix A

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Declaration

Ich, Olga Yakobson (Matrikel-Nr. 11591478), versichere, dass ich die Masterarbeit mit dem Thema SerialExperimentsOlga selbstständig verfasst und keine anderen als die angegebenen Quellen und Hilfsmittel benutzt habe. Die Stellen der Arbeit, die ich anderen Werken dem Wortlaut oder dem Sinn nach entnommen habe, wurden in jedem Fall unter Angabe der Quellen der Entlehnung kenntlich gemacht. Das Gleiche gilt auch für Tabellen, Skizzen, Zeichnungen, bildliche Darstellungen usw. Die Bachelorarbeit habe ich nicht, auch nicht auszugsweise, für eine andere abgeschlossene Prüfung angefertigt. Auf § 63 Abs. 5 HZG wird hingewiesen. München, 1. Februar 2023

Munich, February 4, 2022

Olga Yakobson