Final Project

FRAIG:

Functionally Reduced And-Inverter Graph

資料結構與程式設計
Data Structure and Programming

12/14/2017

Functionally – Reduced – AIG (FRAIG)

- ◆AIG: you have learned it in HW#6
- ◆Functionally?
 - Well, AIG represents a circuit, so it represents some Boolean function.
- ◆ Reduced?
 - Reduction on AIG → Simplifying graph
 - How to simplify AIG?
- ◆ Functionally Reduced?
 - Two functionally equivalent nodes can be merged together
 - (e.g.) Simplify circuit by constant propagation

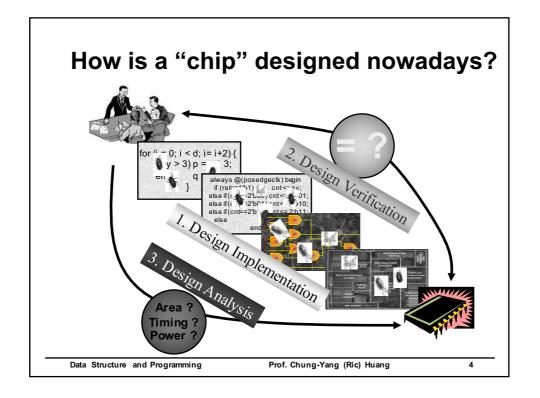
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Electronic Design Automation (EDA)

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How/What to optimize a circuit?

- ◆ Area
 - Reduce the number of gates
 - Moreover, using library cells of smaller sizes
 but they will have weaker driving capability
- Timing
 - Shorten the longest path
 - Additionally, insert buffers and/or enlarge the cells to increase the driving capability
- Power
 - Reduce the switching activities
 - Moreover, shutdown the sub-circuit that is not currently used

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Optimization trade-offs

- ♦ In general, area, timing, power optimizations contradict with each other
- Moreover, different stages of design flow have different granularities and complexities for circuit optimization
 - HDL (e.g. Verilog) // algorithm
 - Gate (Boolean) // logic
 - Schematic (transistor) // cell library
 - Layout (wire length) // RC network

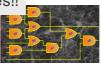
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A simplified view of circuit optimization

- ◆HDL (Verilog)
 - Architectural and algorithmic optimizations

- ◆ Gate (Boolean) What FRAIG focuses!!
 - Minimize gate counts under reasonable timing and power constraints

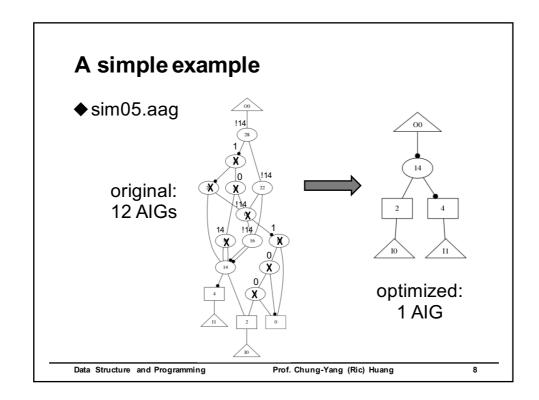


- ◆Layout (transistor)
 - Minimize wire length for timing and power optimizations with limited area overhead



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Functionally Reduced AIG

- 1. Unused gate sweeping
- 2. Trivial optimization
- 3. Simplification by structural hash
- 4. FRAIG: Equivalence gate merging

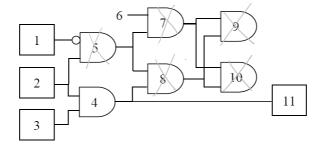
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Unused Gate Sweeping

◆ Sweeping out those gates that are not reachable from POs.

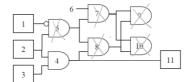


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Unused Gate Sweeping

- ◆ Command: CIRSWeep
 - Can be called whenever necessary.
 - Note: do not remove unused PIs.
 - After this command, all gates except for the unused PIs will be in the DFS list.
 - Note: be sure to update the reporting for "CIRPrint -FLoating".
- ◆ In the previous example (cirp -fl):
 - Before:
 - Defined but not used: 9 10
 - Gates with floating fanin: 7
 - After:
 - Defined but not used: 1



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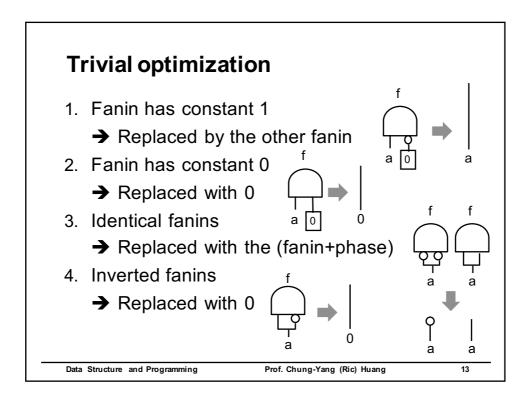
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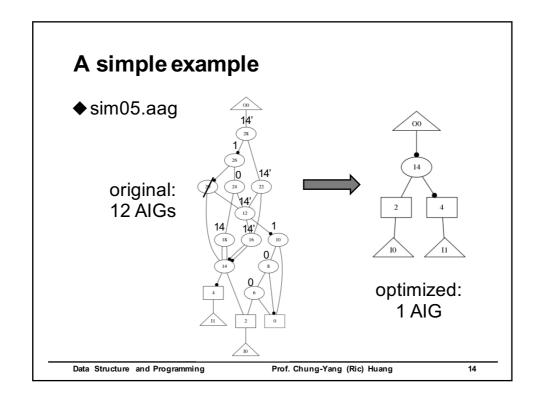
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Trivial optimization

- ◆ Command: CIROPTimize
 - Can be called whenever necessary
 - Scan the DFS list and perform optimization ONCE. Don't repeatedly optimize the circuit. → The latter can be achieved by calling CIROPTimize multiple times.
 - Don't perform optimization during CIRRead
- ◆ Do not remove Pls / POs
- Some UNDEF or defined-but-not-used gates may disappear!
- ◆ Some gates (with side input = constant 0) may become "defined-but-not-used".

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Functionally Reduced AIG

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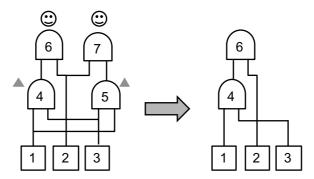
f1 = AND(a, b) f2 = AND(b, a)

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Structural Hash (Strash)

◆ Example:



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Structural Hash (Strash)

◆ Problem: How to identify two AIG gates in a circuit that have the same inputs?

[Method 1] Check for $O(n^2)$ pairs of gates

[Method 2] For each gate, check its fanouts

■ How many checks?

[Method 3] For each gate, create hash table <fanins, this gate>

- How many checks?
- ◆ We will pick method 3 in our project
 - Please modify your "util/myHashSet.h" for this
- ◆ Although it is possible to perform strash during circuit parsing, we choose to make "strash" a separate command. → CIRSTRash
- ◆ Note: Order matters!! You should merge from Pls to POs (Why??)

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Structural Hash Algorithm

- ◆ HashMap<HashKey, HashData> hash;
 - HashKey depends on gate type & list of fanins
 - HashData is Gate*
 - → What if we have only AIG?
 - → How about inverted match?

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Structural Hash Algorithm

```
♦ for_each_gate_from_pi_to_po(gate, hash)
// Create the hash key by gate's fanins
HashKey<...> k(...); // a function of fanins
size_t mergeGate;
if (hash.check(k, mergeGate) == true)
// mergeGate is set when found
mergeGate.merge(gate);
else hash.forceInsert(k, gate);
```

♦ size_t ? → CirGateV
Create a wrapper class on top of a size t!!

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Notes about CIRSTRash

- ◆ Perform strash only on gates in DFS list
 - Do not perform strash on gates which cannot be reached from POs
 - This is to avoid those unreachable gates appearing in DFS list
- ◆ It doesn't make sense to perform strash again before doing other optimizations
 - CIRSTRash cannot be repeated called

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Maintaining Netlist Consistency

- ◆ Once circuit is simplified, some gates may become invalid.
 - How to maintain the netlist consistency?
 - Properly re-connect fanins/fanouts
 - 2. Properly release memory (if necessary)
 - Properly update the lists in CirMgr (Note: PI/PO lists should never be changed)

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Functionally Reduced AIG

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FRAIG: Merging equivalent gates

- Some gates are NOT structurally equivalent, but functionally equivalent.
 - Cannot be detected by strash
 - e.g. $ab + c \equiv (a + c)(b + c)$
- ◆ How to know two gates are functionally equivalent?
 - By simulation? (If two gates have the same value)
 - → Not quite possible, equivalence requires to enumerate "ALL input patterns" // exhaustive simulation
 - Need "formal (mathematical) proof"!!
 - → But, what to prove? O(n²) pairs?
 - → By simulation!! // to check the potential equivalence

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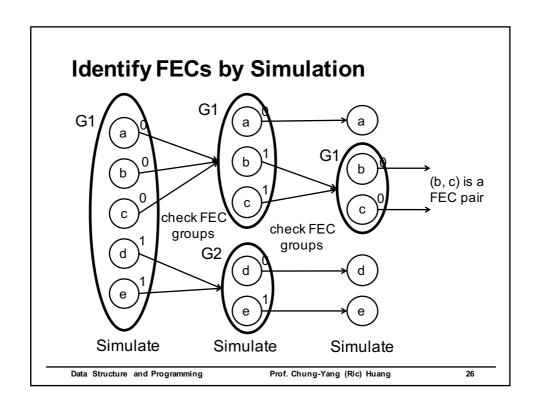
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FEC Pairs

- ◆ Functionally Equivalent Candidate (FEC)
 - For all simulated patterns, if two signals always have the same response, they are very likely to be equivalent.
- Properties
 - Two signals can be separated if they have different simulation values for at least ONE input pattern
 - Two paired signals can be separated by simulation, but two separated signals won't get paired again
 - Singleton signal won't be in any FEC pair anymore

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Identify FECs by Simulation

- 1. Initial: put all the signals in ONE FEC group.
- 2. Add this FEC group into fecGrps (list of FEC groups)
- 3. Randomly simulate the entire circuit
- 4. for each(fecGrp, fecGrps):

5. Repeat 3-4 until no new FEC Group can be identified, or efforts exceed certain limit.

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Simulation Algorithm

◆ All-gate simulation:

Perform simulation for each gate on the DFS list

```
void CirMgr::simulate() {
    for_each_gate(gate,_dfsList) gate->simulate(); }
```

Event-driven simulation:

Perform simulation only if any of the fanins changes value

```
void CirMgr::simulate() {
  for_each_PO(po, _dfsList) po->simulate(); }
bool CirAigGate::simulate() {
  Recursively simulate each fanin.
  If (no fanin has value change) return false;
  Simulate this gate;
  if (value changed) return true;
  return false;
}
```

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Discussions: Simulation algorithm trade-offs

- ◆ All-gate simulation or event-driven?
- ◆ Evaluation
 - By operator? By if-else? By table lookup?
- ◆ To detect FEC pairs, how many simulation patterns are enough?
 - Stop if no new FEC pair is found?
 - (Dynamically) Controlled by "#failTimes"
- ◆ Patterns
 - Single pattern? Parallel pattern?

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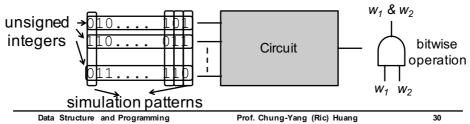
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Parallel-Pattern Simulation for FEC Identification

- ◆ Note: The speed overhead in bitwise operations is very small.
 - Most of the programming languages (e.g. C/C++) support "bit-wise" operations (e.g. &, |, ~ in C).

◆ Idea

 Using 32- or 64-bit unsigned integer to pack 32 or 64 patterns into a word



How many patterns to parallelize?

- ◆ In practice, max parallelization will lead to the best simulation performance
 - Use the max "unsigned int" to store the parallel patterns (e.g. size_t in C/C++)

[Discussion]

- ◆ Can we go beyond 32/64 bits?
 - e.g. 1024-bit
- ♦ What are the pros and cons?
- ♦ How about the FEC detection rate?

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Mass simulation → Identify FEC pairs

How to prove/disprove gates in an FEC pair are equivalent?

Convert it into a SAT problem!!!

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Boolean Satisfiability Problem

- ♦ Given a Boolean function f(X), find an input assignment X = A such that f(A) = 1.
 - Satisfiable: if such an assignment is found
 - Unsatisfiable: if no assignment is possible
 i.e. All assignments make f(X) = 0
 - Undecided: can't find a satisfying assignment, but haven't exhaust the search
 - SAT Game: https://goo.gl/9JJVmJ
- ◆ Complexity?
 - First proven NP-complete problem by Dr. S.
 Cook in 1971 (Turing Award winner)

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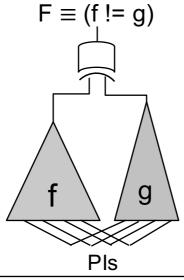
How to prove the equivalence of FEC gates?

- ◆ In general, given two Boolean functions, f, g, how to check if they are equivalent?
- ◆ Note:
 - SAT proves things by contraposition
 - → By showing that it is *impossible* to find an assignment to make f!= g.
 - → Create a SAT problem F = (f!=g), showing that it is unsatisfiable.
 - → Note: f!= g → an XOR gate

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How to prove the equivalence of FEC gates?



(f, g) is an FEC pair

→ SAT? (F = 1)

If UNSAT \rightarrow f = g

If SAT → f!= g with an input assignment A that can distinguish (f, g) and potentially distinguish other pairs

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FRAIG flow

- 1. Simulation
 - a) Put all signals in the same group
 - b) Simulate the circuit. If two signals have different simulation results, separate them into different groups
 - c) Repeat (b) until no more signals can be distinguished, or the simulation efforts exceed a preset limit
 - d) Collect the functionally equivalence candidate (FEC) pairs

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FRAIG flow

- 2. For each FEC pair, call Boolean Satisfiability (SAT) engine to prove their equivalence
 - If they are equivalent, merge them together
 → remove one of them
 - If they are NOT equivalent, acquire the counter-example (CEX) to distinguish them
 - Repeat until all the FEC pairs have been proved, or enough CEXes (2.2) have been collected → Repeat simulation

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In short...

- 1. Simulation identifies a group of FEC pairs
- 2. For each FEC pair, say (f, g), call SAT engine to check if (f!= g) is satisfiable
- 3. If UNSAT \rightarrow f = g \rightarrow f can replace g
- 4. If SAT
 - → collect the pattern that witness (f!= g)
 - → simulate again to see if it can distinguish other FEC pairs
- 5. Repeat 2 ~ 4
- → So the remaining problems are: How to call SAT engine? How to create SAT proof instance?

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Boolean Satisfiability Engine

- ◆ A engine (i.e. a program/library/function) that can prove or disprove a Boolean Satisfiability problem
 - Called a "SAT engine" or "SAT solver"
- ◆ A well-studied CS problem, but was once generally thought as an intractable problem.
 - Many practical, powerful, and brilliant ideas were brought up by EDA researchers in early 2000 → Orders of improvement
 - → Made a revolutionary change on the applications of SAT

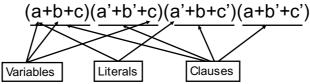
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Creating Proof Instance

- ◆ Proof instance: the formula under proof
- ◆ Conjunctive Normal Form (CNF)
 - Most modern SAT engines represent the proof instances in CNF
 - Actually a "product of sum" representation



• To be satisfied, all the clauses need to be 1

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Converting circuit to CNF

- ◆ Each gate is assigned a variable ID
- ◆ Each gate is converted to a set of CNF clauses based on its fanin variables
 - g = AND(a, b)
 - 1. $a = 0 \rightarrow g = 0$

$$(a + !g)$$

2. $b = 0 \rightarrow g = 0$ (b + !g)

$$(b + !g)$$

- 3. $a = 1 \& b = 1 \rightarrow g = 1$ (!a + !b + g)
- ➤ To solve (f = 1), add a (f) clause
 - SAT engine is to check if all the clauses can be satisfiable at the same time.

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Converting circuit to CNF

◆ Example:

SAT [6] = 1
$$(1 + !4)(3 + !4)(!1 + !3 + 4)$$

$$(4 + !6)(2 + !6)(!2 + !4 + 6)$$

$$(6)$$

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Calling SAT engine

- ◆ Create a solver object
- ◆ Add clauses → proof instance
- ◆ (optional) Set proof limits
- **♦** Solve()!!
- → We provide a SAT interface in "sat.h"
- ◆(FYI) Incremental SAT
 - Reuse the partial learned information

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Using SAT to prove FEC pair

```
    Create a solver object
SatSolver solver;
```

solver.initialize();

- 2. Create CNF for the circuit
 - •For each gate in the circuit, create a variable for it
 - solver.newVar();
 - •For each gate in the circuit, create CNF clauses for it
 - solver.addAigCNF(v, v1, ph1, v2, ph2);
 - •Remember to take care of CONST gate
- 3. Create the proof instance for $F \equiv (f!=g)$
 - Add clauses for F
 - solver.addXorCNF(FVar, fVar, fPh, gVar, gPh);
 - Call SAT to prove
 - solver.assumeRelease();
 - solver.assumeProperty(newV, true);
 - bool isSat = solver.assumpSolve();
 - getSatAssignment(solver, patterns);

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Notes about FEC proof

- ◆ Order matters!!
 - Proving from PIs to POs can greatly reduce the proof effort
 - DFS or BFS?
- ◆ Don't waste SAT-generated patterns (for f!= g)
 - Pack them for parallel pattern simulation
- ◆ Many FEC pairs are actually (f, 1) or (f, 0).
 - Should we do anything special for them?
- ◆ It's OK to skip some proofs. (Why?)
 - Skip it or limit the proof effort (e.g. #conflicts)
- Incremental SAT
- ◆ Balance between simulation and proof efforts

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Some advices

- ◆ Please do not fall into 軍備競賽...
 - Although it is possible you can implement a version that is 10X faster than mine...
- ◆ It's OK that you CANNOT finish the project.
 - I don't expect many people to finish the project.
 - Think: 你的電子學有拿 100 分嗎?
- ◆ Please DO NOT spend 80% time on 20% points
 - e.g. parser error message, circuit optimization
- Always keep your code simple and straight!!
 - Always modularize your code
 - Compile and test from time to time

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References

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