

# Logic and Algorithms – Recitation 5

## Logic

Basic logic symbols: **logical AND** ( $\wedge$ ), **OR** ( $\vee$ ), **NOT** ( $\sim$  or  $\neg$ ).

What is a **proposition**? A sentence that is either true or false.

Example: 'It is sunny outside' is a proposition. 'What time is it?' is not a proposition.

**Symbols to sentences:** Let p and q be propositions – p: it is raining outside; q: it is snowing outside. Express the following as English sentences:

$p \wedge q$ : It is raining outside and it is snowing outside.

$p \rightarrow q$ : If it is raining outside, then it is snowing outside.

$(p \wedge \sim q) \vee \sim p$ : It is raining and not snowing outside, or it is not raining.

$\sim p \rightarrow q$ : If it is not raining outside, then it is snowing outside.

**Sentences to symbols:** Let r and s be the propositions – r: you are crying; s: you are laughing. Express the following as logical statements:

You are not laughing:  $\sim s$






If you are crying then you are not laughing:  $r \rightarrow \sim s$

You are not crying and you are not laughing:  $\sim r \wedge \sim s$

You are crying or you are laughing:  $r \vee s$

If you are not laughing then you are crying:  $\sim s \rightarrow r$

## Algorithms (flowcharts):

Symbol	Name	Function
	Start/end	An oval represents a start or end point.
	Arrows	A line is a connector that shows relationships between the representative shapes.
	Input/Output	A parallelogram represents input or output.
	Process	A rectangle represents a process.
	Decision	A diamond indicates a decision.

Example of application:

- Start the process of billing
- Order 2 burgers, 3 pizzas (input)
- Calculate the prices (process)
- If cost > \$10 give free coupon (decision box with yes); if cost < \$10 do nothing (decision box with no)
- Display the cost (output)
- End the process