COMPUTER SCIENCE 61A

November 10, 2016

1 Iterables and Iterators

An **iterable** object is any container that can be processed sequentially. Examples of iterables are lists, tuples, strings, and dictionaries. To process the elements sequentially, call iter on the iterable to retrieve an iterator.

An **iterator** is an object that tracks the position in a sequence of values in order to provide sequential access. It returns elements one at a time and is only good for one pass through the sequence. To access the next element of an iterator, call next on the object. Each time next is called, the iterator advances.

We can create as many iterators as we would like from a single iterable. However, iterators will go through the elements of the sequence they represent only once. To go through an iterable twice, create two iterators!

```
>>> iterable = [4, 8, 15, 16, 23, 42]
>>> iterator1 = iter(iterable)
>>> next(iterator1)
4
>>> next(iterator1)
8
>>> next(iterator1)
15
>>> iterator2 = iter(iterable)
>>> next(iterator2)
4
```

1.1 For Loops

We have already been using iterables to go through the elements of a sequence. This happens all the time in for loops. For example:

```
>>> for n in [1, 2, 3]:
... print(n)
...
1
2
3
```

This works because the for loop implicitly creates an iterator using the **iter** method. Python then repeatedly calls **next** repeatedly on the iterator, until it raises StopIteration. In other words, the loop above is (basically) equivalent to:

```
iterator = iter([1, 2, 3])
try:
    while True:
        n = next(iterator)
        print(n)
except StopIteration:
    pass
```

1.2 Generators

A **generator** function is a special kind of Python function that uses a yield statement instead of a return statement to report values. When a generator function is called, it returns an iterator. The following is a function that returns an iterator for the natural numbers:

```
def gen_naturals():
    current = 0
    while True:
        yield current
        current += 1
```

Calling generate_naturals() will return a generator object, which you can use to retrieve values.

```
>>> gen = gen_naturals()
>>> gen
<generator object gen at ...>
>>> next(gen)
0
>>> next(gen)
1
```

1.3 yield

The yield statement is similar to a **return** statement. However, while a **return** statement closes the current frame after the function exits, a yield statement causes the frame to be saved until the next time **next** is called, which allows the generator to automatically keep track of the iteration state.

Once **next** is called again, execution resumes where it last stopped and continues until the next yield statement or the end of the function. A generator function can have multiple yield statements.

Including a yield statement in a function automatically tells Python that this function will create a generator. When we call the function, it returns a generator object instead of executing the the body. When the generator's **next** method is called, the body is executed until the next yield statement is executed.

1.4 yield from

The yield from statement is similar to a yield statement. yield from takes in an iterator and yields each of the values from that iterator. It can be used in conjunction with other yields and yield froms.

When the list function in Python receives an iterator, it calls the next function on the input until it raises a StopIteration. It puts each of the elements from the calls to next into a new list and returns it.

1.5 Questions

1. Define an generator function that combines two input iterators using a given combiner function. The resulting iterator should have a size equal to the size of the shorter of its two input iterators.

```
>>> from operator import add
>>> evens = combiner(gen_naturals(), gen_naturals(), add)
>>> next(evens)
0
>>> next(evens)
2
>>> next(evens)
4
def combiner(iterator1, iterator2, combiner):

Solution:
    while True:
        yield combiner(next(iterator1), next(iterator2))
```

2. What is the result of executing this sequence of commands?

```
>>> nats = gen_naturals()
>>> doubled_nats = combiner(nats, nats, add)
>>> next(doubled nats)
```

```
Solution: 1
```

```
>>> next(doubled_nats)
```

```
Solution: 5
```

3. Write a generator function that returns all subsets of the positive integers from 1 to n. Each call to this generator's **next** method will return a list of subsets of the set [1, 2, ..., n], where n is the number of times **next** was previously called.

```
Solution:
    subsets = [[]]
    n = 1
    while True:
        yield subsets
        subsets = subsets + [s + [n] for s in subsets]
        n += 1
```

In Python, we can use iterators to represent infinite sequences. However, Scheme does not support iterators. Let's see what happens when we try to use a Scheme list to represent an infinite sequence of natural numbers:

Because the second argument to cons is always evaluated, we cannot create an infinite sequence of integers using a Scheme list.

Instead, our Scheme interpreter (and scheme.cs61a.org) supports *streams*, which are *lazy* Scheme lists. The first element is represented explicitly, but the rest of the stream's elements are computed only when needed. This evaluation strategy, where we don't compute a value until it is needed, is called *lazy evalutation*. Let's try to implement the sequence of natural numbers again using a stream!

We use the special form <code>cons-stream</code> to create a stream. Note that <code>cons-stream</code> is a special form, because the second operand (<code>naturals</code> (+ n 1))) is not evaluated when <code>cons-stream</code> is called. It's only evaluated when <code>cdr-stream</code> is used to inspect the rest of the stream.

- nil is the empty stream
- cons-stream creates a non-empty stream from an initial element and an expression to compute the rest of the stream
- car returns the first element of the stream
- cdr-stream computes and returns the rest of stream

Streams are very similar to Scheme lists. The cdr of a Scheme list is either another Scheme list or nil; likewise, the cdr-stream of a stream is either a stream or nil. The difference is that the expression for the rest of the stream is computed the first time that cdr-stream is called, instead of when cons-stream is used. Subsequent calls to cdr-stream return this value without recomputing it. This allows us to efficiently work with infinite streams like the naturals example above. We can see this in action by using a non-pure function to compute the rest of the stream:

```
scm> (define (compute-rest n)
...> (print 'evaluating!)
...> (cons-stream n nil))
compute-rest
scm> (define s (cons-stream 0 (compute-rest 1)))
s
scm> (car (cdr-stream s))
evaluating!
1
scm> (car (cdr-stream s))
```

Note that the symbol evaluating! is only printed the first time cdr-stream is called.

2.1 Questions

1. What would Scheme display?

```
Solution:
ones
```

```
scm> (define twos (cons-stream 2 twos))
```

```
Solution:
twos
```

scm> ones

```
Solution:
(1 . #[promise (not forced)])

scm> (cdr ones)

Solution:
#[promise (not forced)]

scm> (cdr-stream ones)

Solution:
(1 . #[promise (forced)])

scm> (has-even? ones)

Solution:
# Runs forever

scm> (has-even? twos)

Solution:
True
```

2. Write map-stream, which takes a function f and a stream s and returns a new stream, which has all the elements from s, but with f applied to each one.

```
(define (map-stream f s)
```

```
scm> (define evens (map-stream (lambda (x) (* x 2)) nat))
evens
scm> (car (cdr-stream evens))
2
```

3. Using streams can be tricky! Compare the following two implementations of filter-stream, the first is a correct implementation whereas the second is wrong in some way. What's

wrong with the second implementation?

Solution: Evaluating rest will result in infinite recursion if s is an infinite stream!

4. Write a function range-stream which takes a start and end argument, and returns a stream that represents the integers between included start and end - 1. (define (range-stream start end)

```
Solution:
   (if (eq? start end)
     nil
     (cons-stream start (range-stream (+ start 1) end))
   )
)
```

5. Write a function slice which takes in a stream, a start, and an end. It should return a Scheme list that contains the elements of stream between index start and end, not including end. If the stream ends before end, you can return nil.

(**define** (slice stream start end)

```
scm> (slice nat 4 12)
(4 5 6 7 8 9 10 11)
```

6. Since streams only evaluate the next element when they are needed, we can combine infinite streams together for intersting results! We've defined the function <code>zip-with</code> for you below. Use it to define a few of our favorite sequences.

```
Solution:

(cons-stream 1 (zip-with * (naturals 1) factorials)))
```

```
scm> (slice factorials 0 10)
(1 1 2 6 24 120 720 5040 40320 362880)
(define fibs
```

Solution: (cons-stream 0 (cons-stream 1 (zip-with + fibs (cdr-stream fibs)))))

```
scm> (slice fibs 0 10)
(0 1 1 2 3 5 8 13 21 34)
```