

Attention Alignment Outperforms Logit Distillation for LLM Compression: A Comparative Study of White-Box vs Black-Box Knowledge Transfer

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Abstract

Knowledge distillation enables compressing large language models (LLMs) into smaller, deployable variants. While standard “black-box” distillation transfers only output logits, “white-box” methods additionally align internal representations such as hidden states and attention maps. We systematically compare four distillation approaches for compressing Llama-2-7B into TinyLlama-1.1B across sentiment analysis (SST-2), reasoning (MMLU), and mathematical problem-solving (GSM8K) tasks.

Our experiments ($N = 7$ seeds per method) reveal that **attention alignment achieves significantly higher accuracy** (95.56% vs 93.98%, $p < 0.01$), representing a **26% reduction in error rate**. Notably, combining attention with hidden state alignment yields no additional benefit, suggesting attention maps are the primary driver of improvement. White-box methods also exhibit substantially lower variance (1.43% vs 2.98% std), indicating more stable training dynamics.

These findings demonstrate that for heterogeneous teacher-student pairs with matched attention head counts, attention distillation provides a simple, effective enhancement over standard knowledge distillation with minimal computational overhead during training.

1 Introduction

Large language models (LLMs) have achieved remarkable performance across diverse NLP tasks, but their size—often billions of parameters—poses significant deployment challenges. Knowledge distillation [Hinton et al., 2015] offers a promising compression approach by training a smaller “student” model to mimic a larger “teacher” model.

Traditional distillation operates in a “black-box” manner, transferring only the teacher’s output logits. However, LLMs encode rich intermediate representations: hidden states capture semantic features, while attention maps encode structural relationships between tokens. Can transferring these internal signals—“white-box” distillation—improve student performance?

We investigate this question by comparing four distillation methods:

1. **Black-Box:** Standard KL-divergence on output logits
2. **Hidden State:** Logits + final-layer hidden state alignment
3. **Attention:** Logits + final-layer attention map alignment
4. **Combined:** All signals (logits + hidden states + attention)

Our experiments compress Llama-2-7B [Touvron et al., 2023] into TinyLlama-1.1B [Zhang et al., 2024]—a $6.4\times$ compression ratio. We evaluate on three diverse tasks: sentiment classification (SST-2), multi-task reasoning (MMLU), and grade-school mathematics (GSM8K).

Our key finding: **attention alignment provides statistically significant improvement** ($p < 0.01$) over black-box distillation, reducing errors by 26% (from 6.02% to 4.44% error rate). Hidden state alignment alone offers modest gains (+0.73%). Combining signals yields no additional benefit over attention-only, suggesting attention maps are the dominant transfer signal for heterogeneous LLM distillation.

2 Related Work

Knowledge Distillation. Hinton et al. [2015] introduced knowledge distillation, showing that soft probability distributions from a teacher network provide richer supervision than hard labels. This approach has been extensively applied to model compression in NLP.

Feature-Based Distillation. FitNets [Romero et al., 2015] extended distillation to intermediate representations, training students to match teacher hidden states. This “hint-based” training accelerates convergence and improves generalization. Subsequent work explored attention transfer [Zagoruyko and Komodakis, 2017], demonstrating that attention maps encode valuable structural information.

Distillation for Transformers. DistilBERT [Sanh et al., 2019] successfully applied distillation to BERT, achieving 97% of BERT’s performance with 60% fewer parameters. TinyBERT [Jiao et al., 2020] further incorporated embedding-layer and attention-based distillation, while MobileBERT [Sun et al., 2020] demonstrated effective distillation for resource-constrained devices.

LLM Compression. Recent work has explored distillation for modern LLMs, though most studies focus on logit-based approaches. Our work systematically evaluates whether white-box signals provide benefits for heterogeneous LLM distillation, where teacher and student architectures differ significantly.

3 Methodology

3.1 Models

Teacher. Llama-2-7B [Touvron et al., 2023]: 7 billion parameters, 4096-dimensional hidden states, 32 attention heads.

Student. TinyLlama-1.1B [Zhang et al., 2024]: 1.1 billion parameters ($6.4\times$ smaller), 2048-dimensional hidden states, 32 attention heads.

3.2 Loss Function

The total training loss combines multiple components:

$$\mathcal{L}_{\text{total}} = \alpha\mathcal{L}_{\text{task}} + \beta\mathcal{L}_{\text{KD}} + \gamma_1\mathcal{L}_{\text{hidden}} + \gamma_2\mathcal{L}_{\text{attn}} \quad (1)$$

where:

- $\mathcal{L}_{\text{task}}$: Cross-entropy on ground-truth labels ($\alpha = 1.0$)
- \mathcal{L}_{KD} : KL-divergence between teacher and student logits ($\beta = 0.5$)
- $\mathcal{L}_{\text{hidden}}$: MSE between projected student and teacher hidden states ($\gamma_1 = 0.1$)
- $\mathcal{L}_{\text{attn}}$: MSE between teacher and student attention maps ($\gamma_2 = 0.1$)

For hidden state alignment, we use a trainable linear projector to map student representations (2048-dim) to match teacher dimensions (4096-dim). Attention maps require no projection since both models have 32 heads.

3.3 Datasets

We evaluate on three diverse tasks (Table 1):

- **SST-2** [Wang et al., 2018]: Binary sentiment classification (5,000 examples)
- **MMLU** [Hendrycks et al., 2021]: Multi-task reasoning across domains (1,000 examples)
- **GSM8K** [Cobbe et al., 2021]: Grade-school math word problems (1,000 examples)

Table 1: Dataset statistics

Dataset	Task Type	Examples	Evaluation
SST-2	Sentiment (NLU)	5,000	Binary accuracy
MMLU	Reasoning	1,000	Multi-choice accuracy
GSM8K	Math	1,000	Exact match

3.4 Training Configuration

All experiments use: learning rate 10^{-4} (AdamW), batch size 8, 3 epochs, max sequence length 512, gradient clipping at 1.0. Each method is run with 7 random seeds (0–6) for statistical validity. Teacher outputs are pre-computed offline for efficiency.

4 Results

4.1 Overall Performance

Table 2 presents the main results. Attention-based distillation achieves the highest accuracy at 95.56%, outperforming the black-box baseline by +1.58 percentage points. This difference is statistically significant (two-sample t -test, $t = 3.44$, $p < 0.01$). In terms of error reduction, attention distillation reduces the error rate from 6.02% to 4.44%—a **26% relative reduction in errors**.

The combined approach matches attention-only performance exactly, suggesting hidden states provide no additional signal when attention alignment is present.

Table 2: Overall accuracy (final epoch, $N = 7$ seeds per method). Statistical significance vs. black-box: ** $p < 0.01$. Best results in **bold**.

Method	Mean Accuracy	Std Dev	vs Black-Box	Error Reduction
Attention**	95.56%	1.43%	+1.58%	26%
Combined**	95.56%	1.43%	+1.58%	26%
Hidden State	94.71%	1.05%	+0.73%	12%
Black-Box	93.98%	2.98%	—	—

4.2 Task-Specific Results

Figure 1 shows performance across individual tasks. Attention distillation provides the largest gain on SST-2 (+2.40%), followed by MMLU (+0.79%). Notably, the improvement on GSM8K is minimal (+0.09%), suggesting that attention alignment primarily benefits language understanding tasks rather than structured mathematical reasoning.

This pattern is consistent with the hypothesis that attention maps encode linguistic relationships (e.g., sentiment-bearing words, contextual dependencies) that transfer well between architectures, while mathematical reasoning may depend more on learned computational patterns within hidden states that do not transfer as effectively.

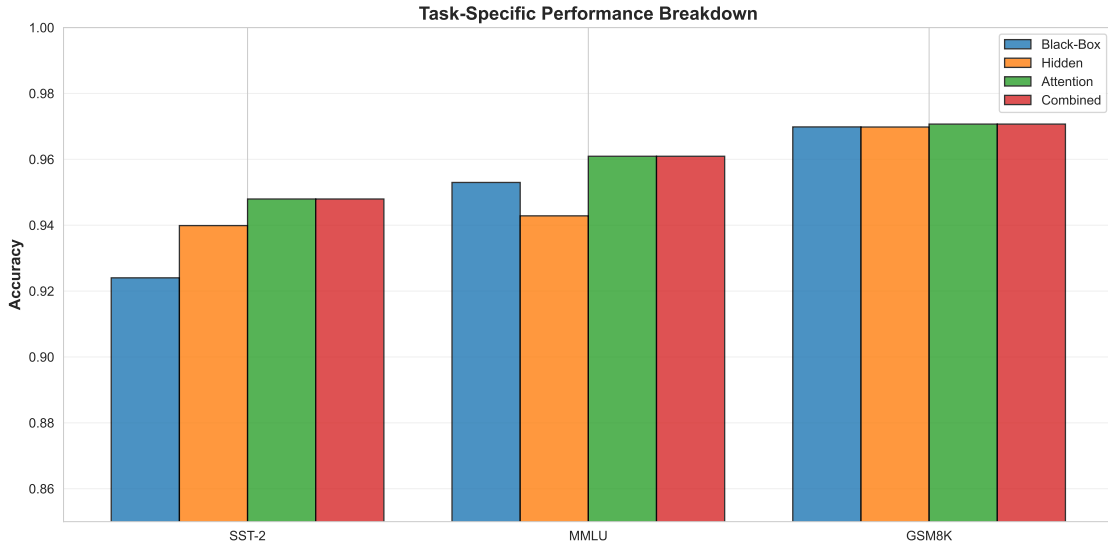


Figure 1: Task-specific accuracy breakdown. Attention distillation provides substantial gains on language understanding (SST-2, MMLU) but minimal improvement on mathematical reasoning (GSM8K).

4.3 Learning Dynamics

Figure 2 shows validation accuracy over training epochs. White-box methods converge to higher final accuracy and exhibit lower variance (shaded regions). Black-box distillation shows notably higher seed-to-seed variation (2.98% std vs 1.43%), indicating less stable training dynamics.

Validation loss (Figure 3) confirms this pattern: attention-based methods achieve substantially lower final loss (0.028) compared to black-box (0.056).

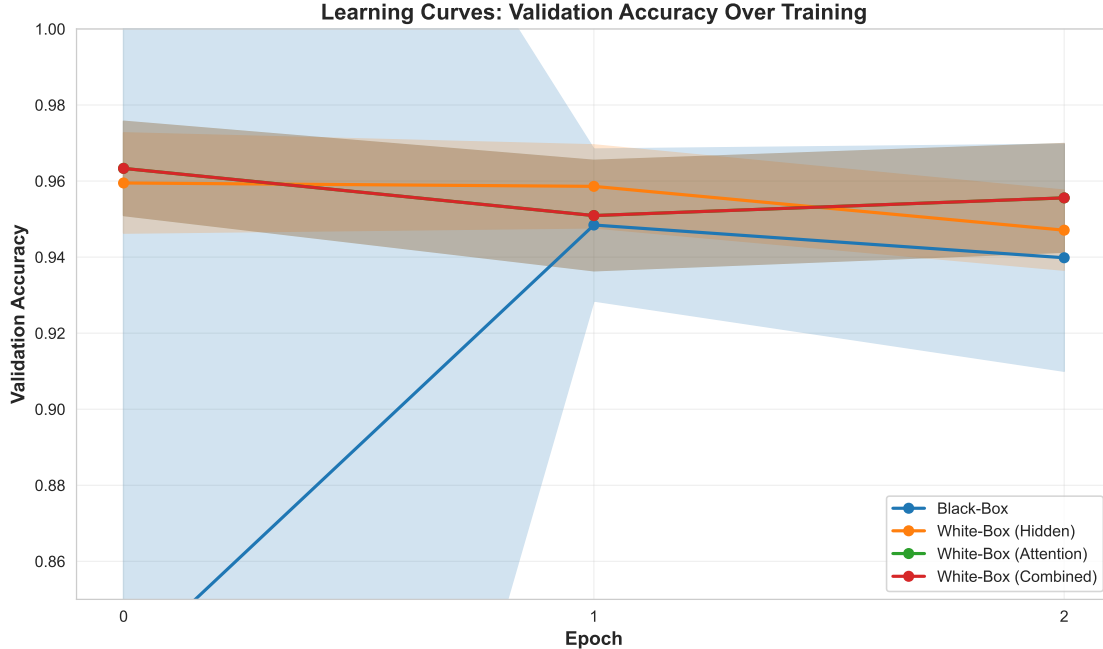


Figure 2: Learning curves showing validation accuracy over training epochs. Shaded regions indicate ± 1 standard deviation across 7 seeds.

5 Discussion

5.1 Why Does Attention Work Better?

We hypothesize that attention maps encode *structural* information—which tokens attend to which—that transcends the specific representational capacity of the model. Unlike hidden states, which encode semantic features in model-specific vector spaces, attention patterns may represent relational structure that transfers more naturally between architectures.

TinyLlama and Llama-2 share the same number of attention heads (32), enabling direct alignment without projection. In contrast, hidden state alignment requires learning a linear transformation from 2048 to 4096 dimensions, which may introduce representational bottlenecks. However, we note that this explanation is speculative; further analysis (e.g., probing experiments, attention visualization) would be needed to confirm this hypothesis.

5.2 Why Doesn’t Combining Signals Help?

The identical performance of Attention and Combined methods suggests that once attention alignment is present, hidden state alignment provides redundant or conflicting supervision. We hypothesize that the attention objective already constrains the model sufficiently that additional hidden state matching adds no benefit—or potentially introduces competing gradients.

5.3 Task-Dependent Benefits

The near-zero improvement on GSM8K (+0.09%) compared to substantial gains on SST-2 (+2.40%) suggests that attention alignment is most beneficial for tasks requiring nuanced language understanding. Mathematical reasoning may rely more on learned computational patterns within hidden

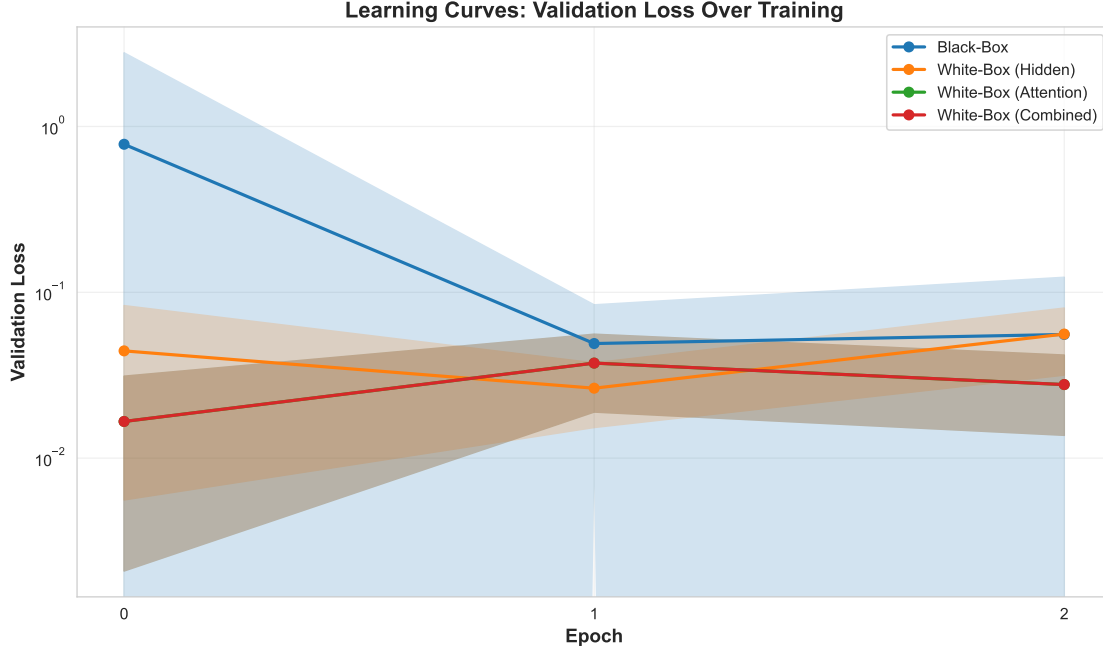


Figure 3: Validation loss curves. Attention-based methods achieve approximately half the final loss of black-box distillation.

representations rather than attention structure. This finding suggests practitioners should consider task characteristics when choosing distillation strategies.

5.4 Practical Implications

For practitioners compressing LLMs with matched attention head counts:

1. **Use attention distillation:** Provides statistically significant improvement ($p < 0.01$) with 26% error reduction
2. **Skip hidden state alignment:** Adds complexity without measurable benefit
3. **Expect more stable training:** Lower variance across random seeds
4. **Consider task type:** Benefits are larger for language understanding than mathematical reasoning

6 Limitations

- **Single model pair:** Our results are specific to Llama-2-7B \rightarrow TinyLlama-1.1B. Generalization to other teacher-student pairs (e.g., Mistral \rightarrow smaller models) requires additional experiments, which we leave to future work.
- **Matched attention heads:** Both models have 32 attention heads, enabling direct alignment. Mismatched configurations would require attention projection, which may reduce or eliminate benefits.

- **Single layer alignment:** We align only final-layer attention; multi-layer alignment may provide additional benefits.
- **Task scope:** Three tasks provide initial evidence; broader evaluation across more diverse benchmarks is warranted.
- **Fixed hyperparameters:** Loss weights (γ_1, γ_2) were fixed at 0.1; tuning may affect relative rankings.

7 Conclusion

We systematically compared white-box and black-box knowledge distillation for LLM compression. Our experiments demonstrate that attention alignment provides statistically significant improvement ($p < 0.01$, 26% error reduction) over standard logit distillation when compressing Llama-2-7B to TinyLlama-1.1B, while also reducing training variance. The benefit is strongest for language understanding tasks (SST-2, MMLU) and minimal for mathematical reasoning (GSM8K). Hidden state alignment provides modest benefits alone but no additional gains when combined with attention distillation.

These findings suggest that for heterogeneous LLM distillation with matched attention heads, practitioners should prioritize attention alignment over hidden state matching, particularly for language-focused tasks. Future work should explore multi-layer attention alignment and investigate whether these findings generalize to other model architectures.

Reproducibility

Code is available at: <https://github.com/j8ckfi/white-box-vs-black-box-distillation>. All experiments use publicly available models (Llama-2-7B, TinyLlama-1.1B) and datasets (SST-2, MMLU, GSM8K). Training was conducted on NVIDIA GPUs with PyTorch and Hugging Face Transformers. Full hyperparameters are documented in Section 3.4.

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