



# Coordinated Resource Extraction

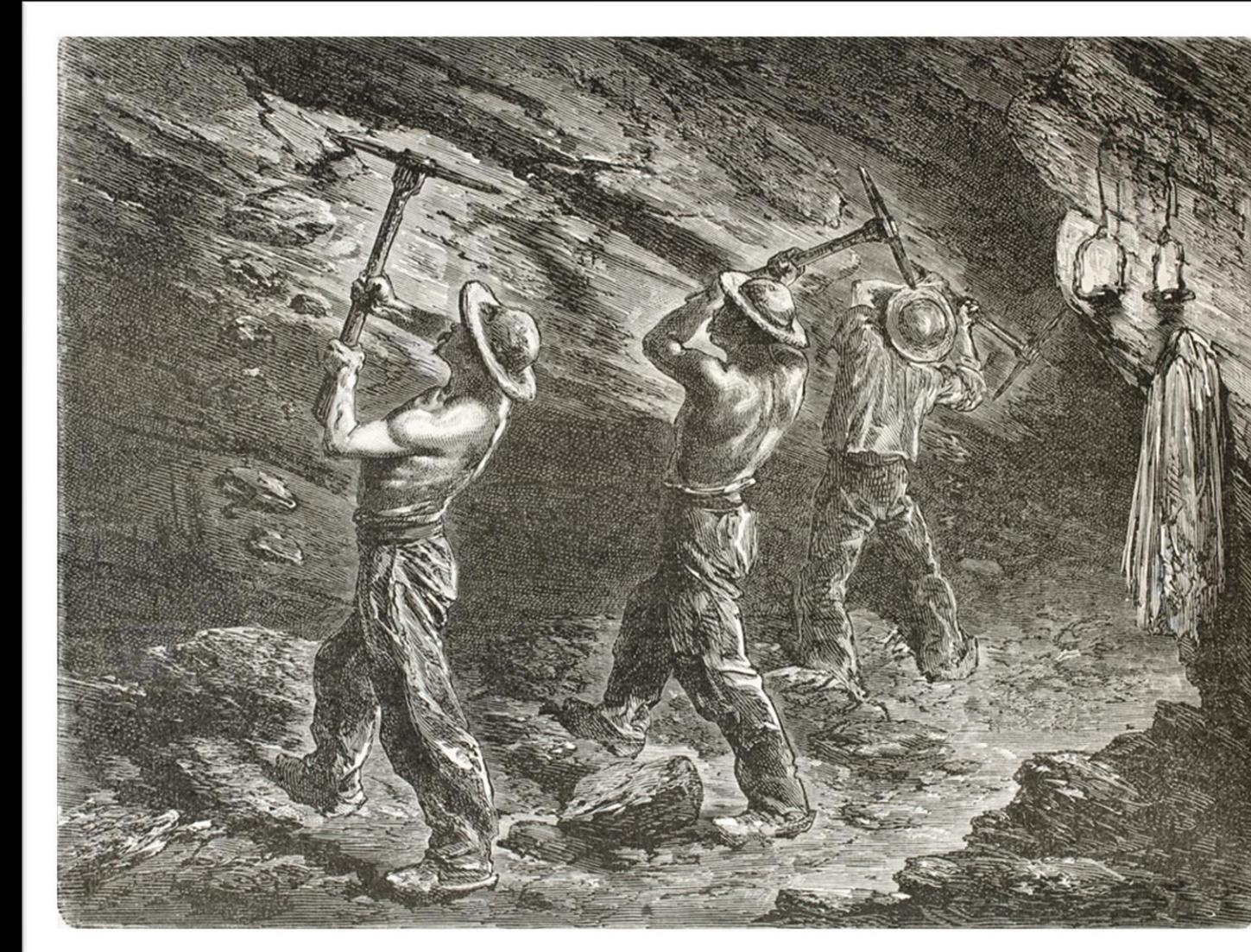
Deep Q-Networks for centralized cooperative multi-agent  
reinforcement learning

Emil G. Stålvinge, Anders Köhler & Julián R. Marrades

The State



The Labor



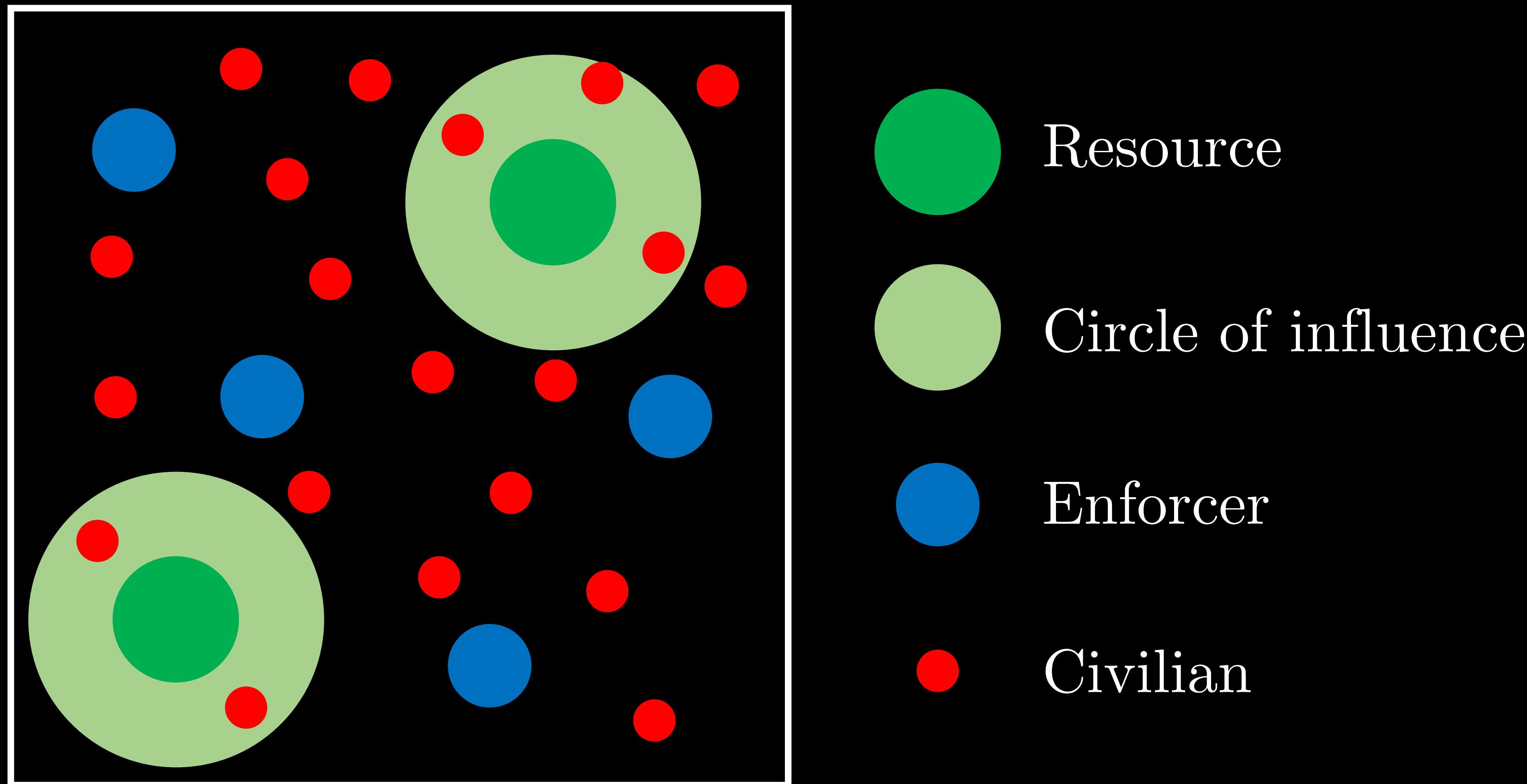
The Riot



How can we model this?

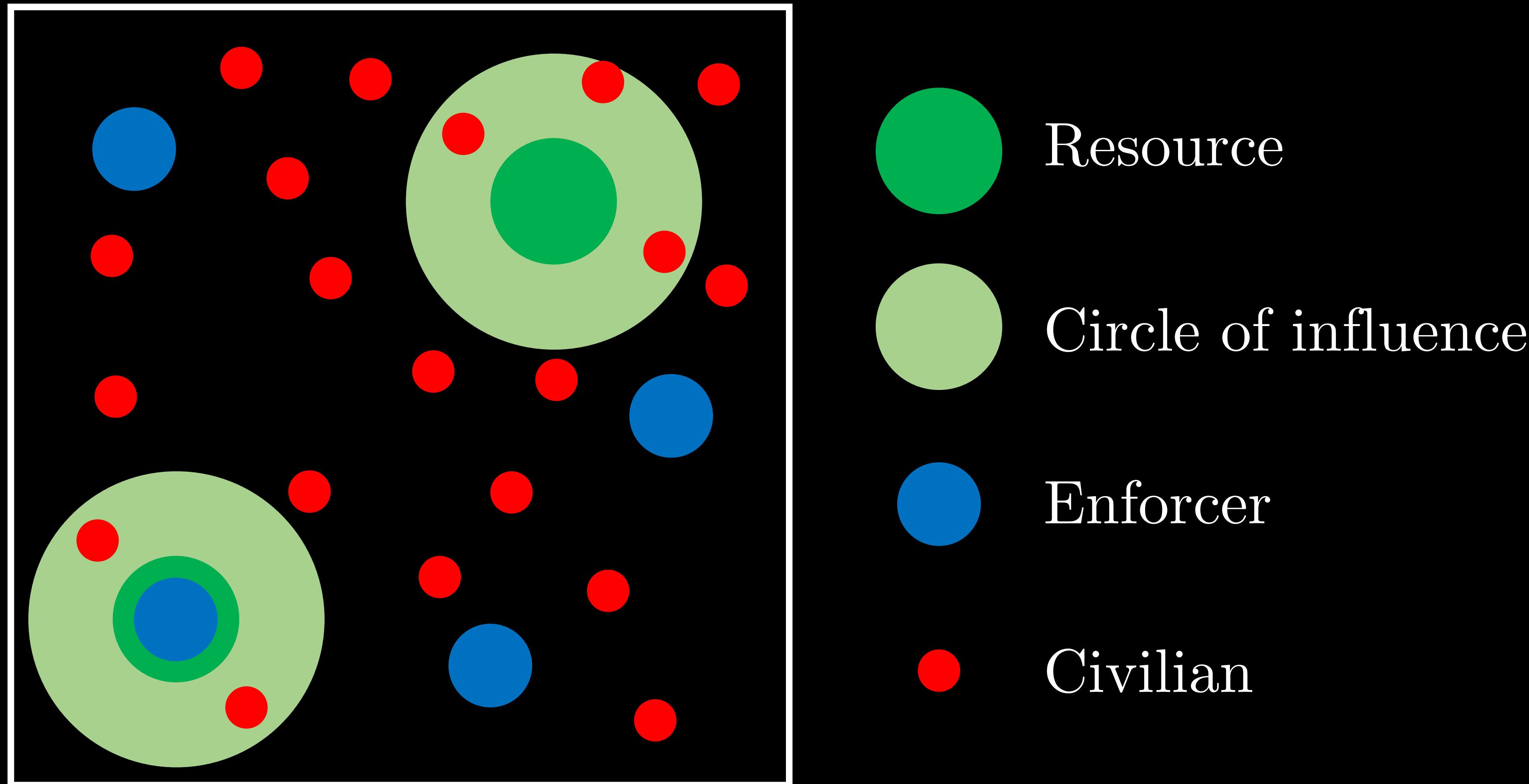
# The game

$$p = 1$$



# The game

$$p = 1$$



Single-Agent RL

Multi-Agent RL

# SARL

Given

- $A, S$
- $\delta: S \times A \rightarrow S$
- $\mathcal{R}: S \times A \rightarrow \mathbb{R}$

Find  $\pi$  so that

$$V^\pi(s_t) := \sum_{i=1}^{\infty} \gamma^i \cdot r_{t+i}$$

is maximized

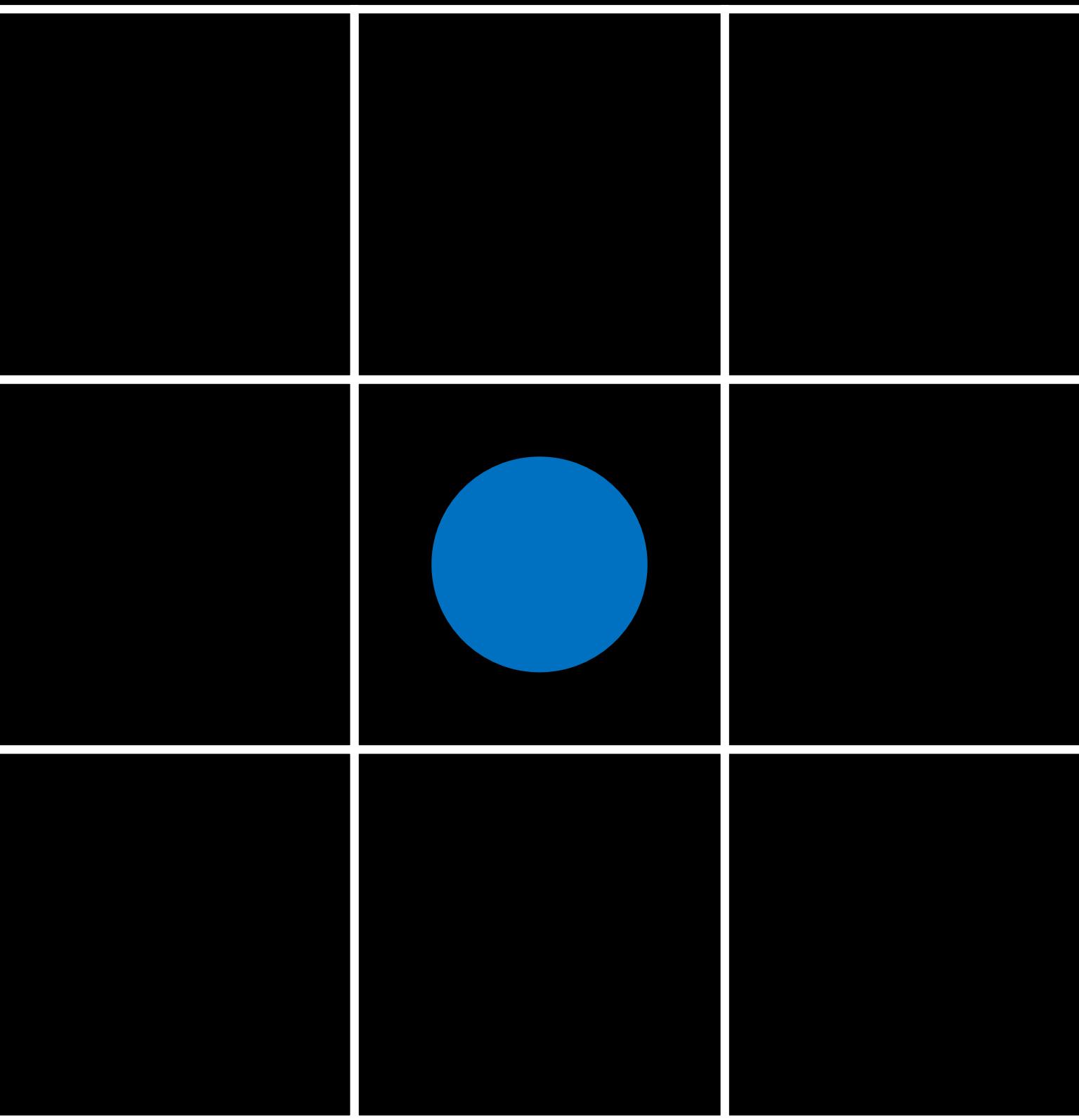
# MARL

Let  $m$  be the number of agents

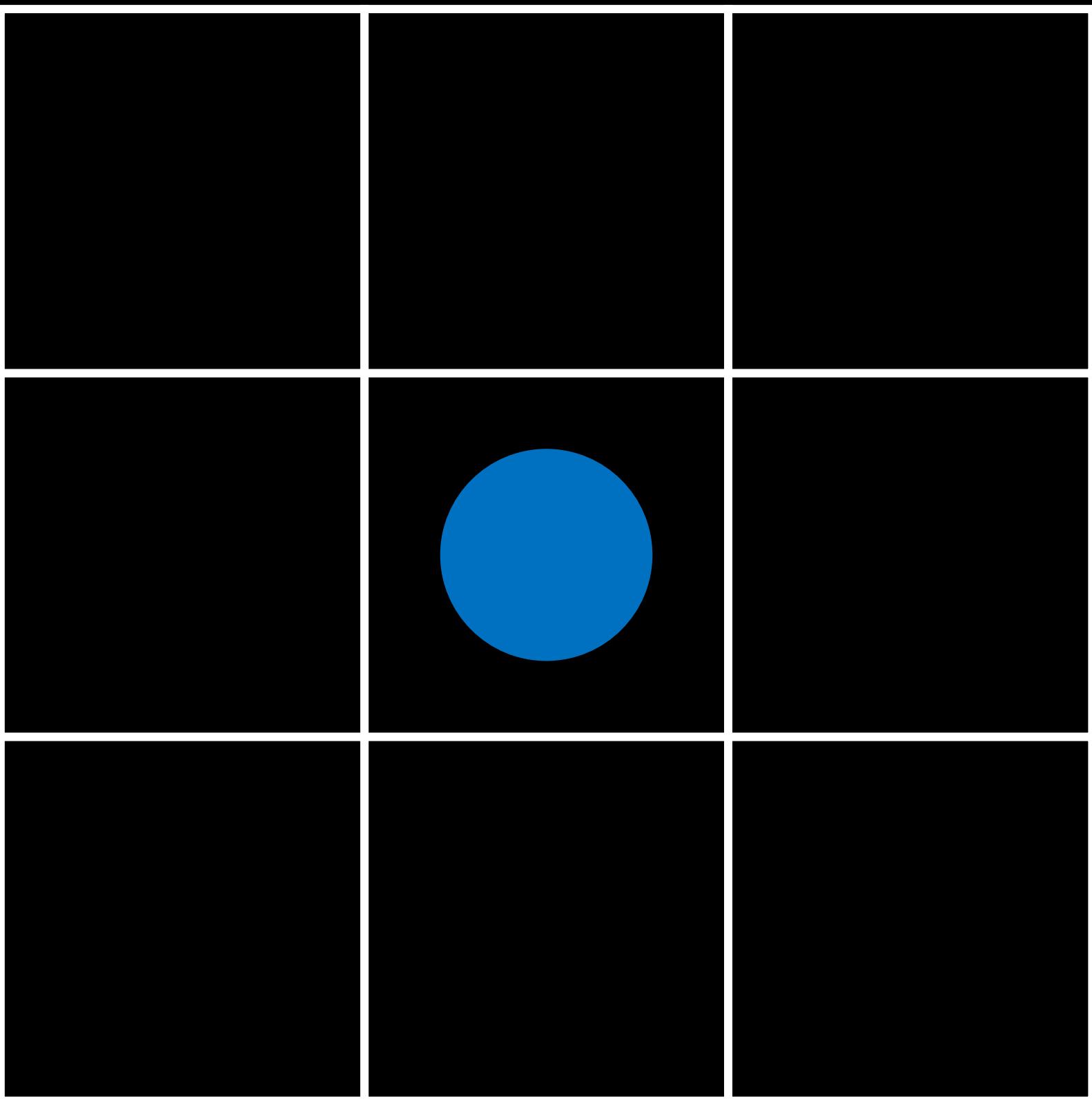
- $S$  grows exponentially with  $m$
- $A := A_1 \times A_2 \times \cdots \times A_n$
- $\delta: S \times A_1 \times A_2 \times \cdots \times A_n \rightarrow S$
- $\mathcal{R}: S \times A_1 \times A_2 \times \cdots \times A_n \rightarrow \mathbb{R}$  or  $\mathbb{R}^m$

Train with DQN!

# MARL to SARL

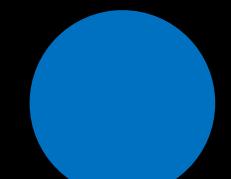
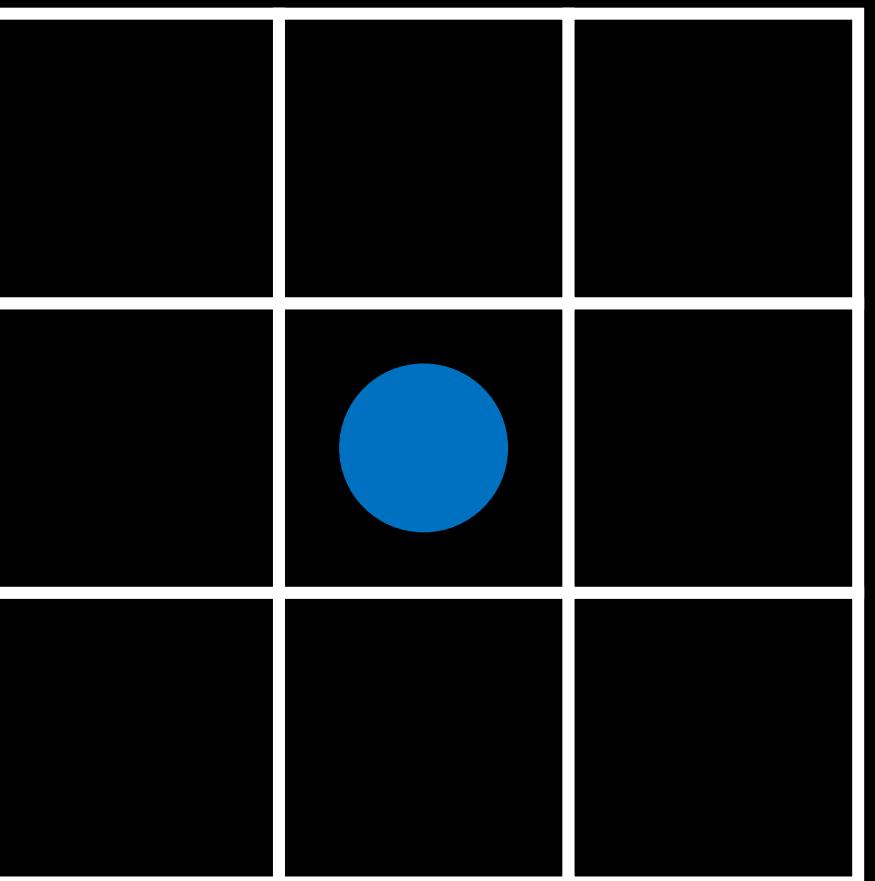
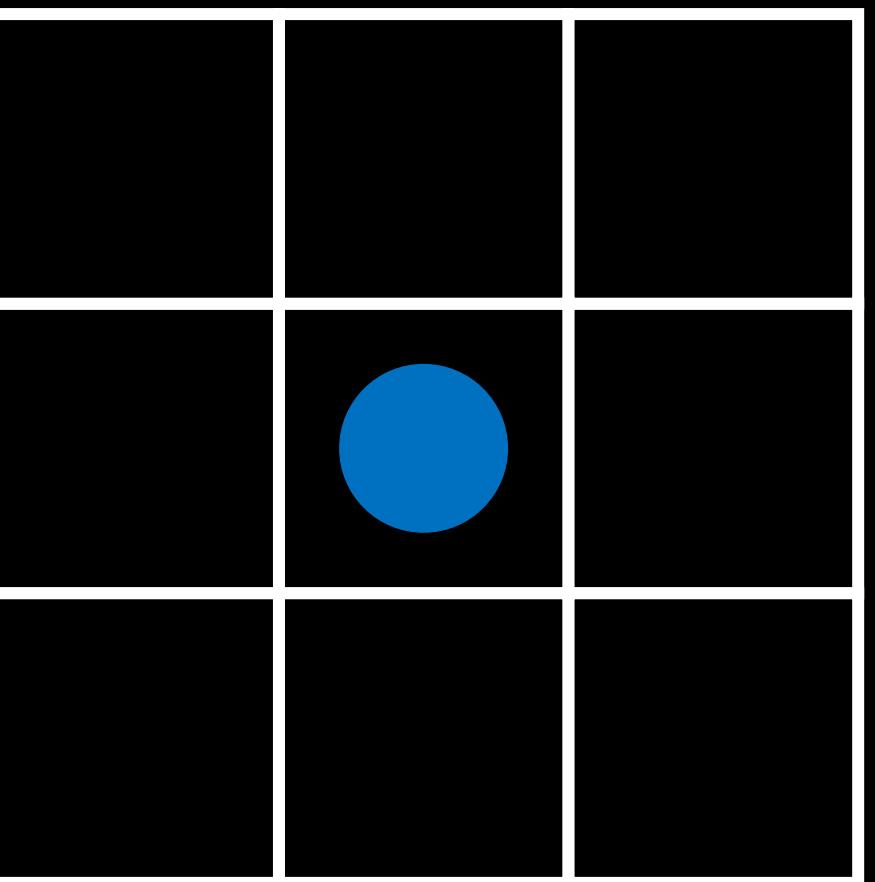


# MARL to SARL

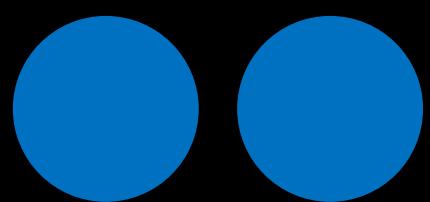


$A = [0, 1, 2, 3, 4]$   
 $\text{size}(A) = 5$

# MARL to SARL

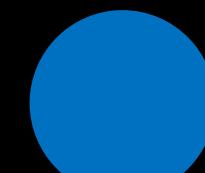
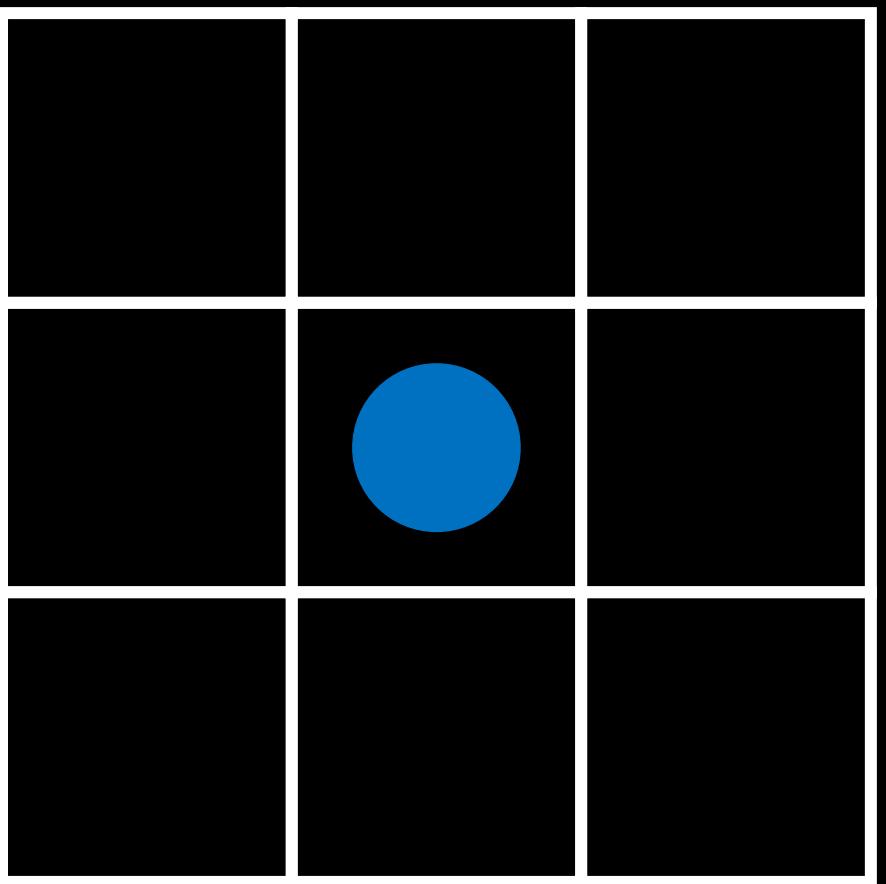
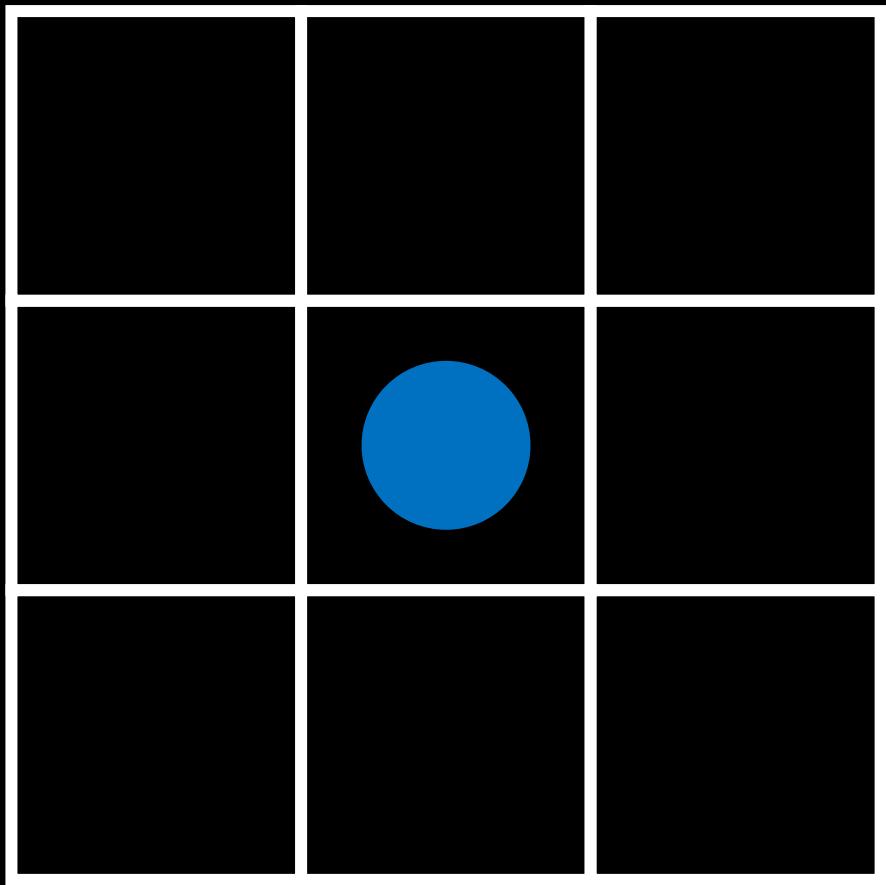
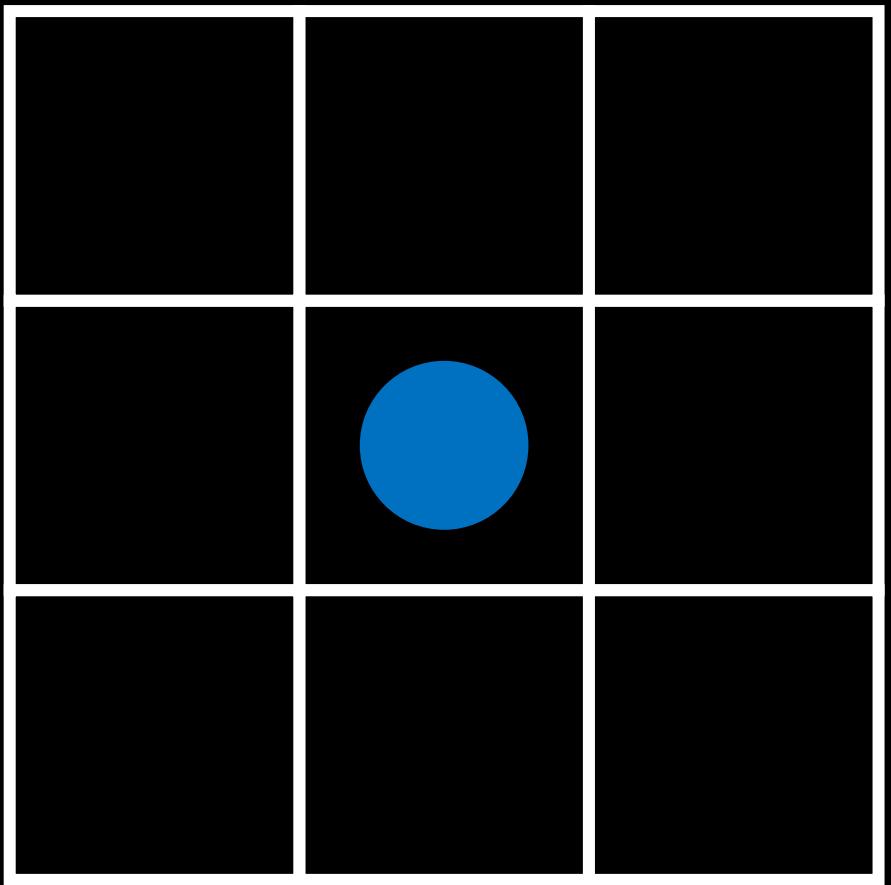


$$A = [0, 1, 2, 3, 4]$$
$$\text{size}(A) = 5$$

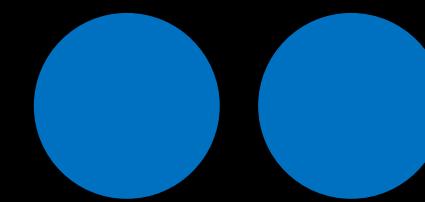


$$A = [(0, 0), (0, 1), (0, 2), \dots]$$
$$\text{size}(A) = 5^2 = 25$$

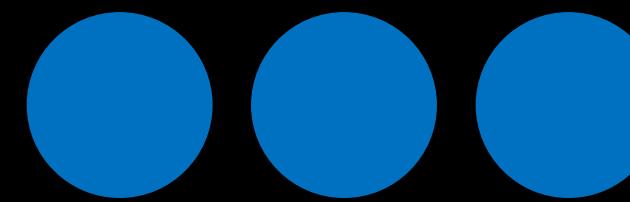
# MARL to SARL



$A = [0, 1, 2, 3, 4]$   
 $\text{size}(A) = 5$



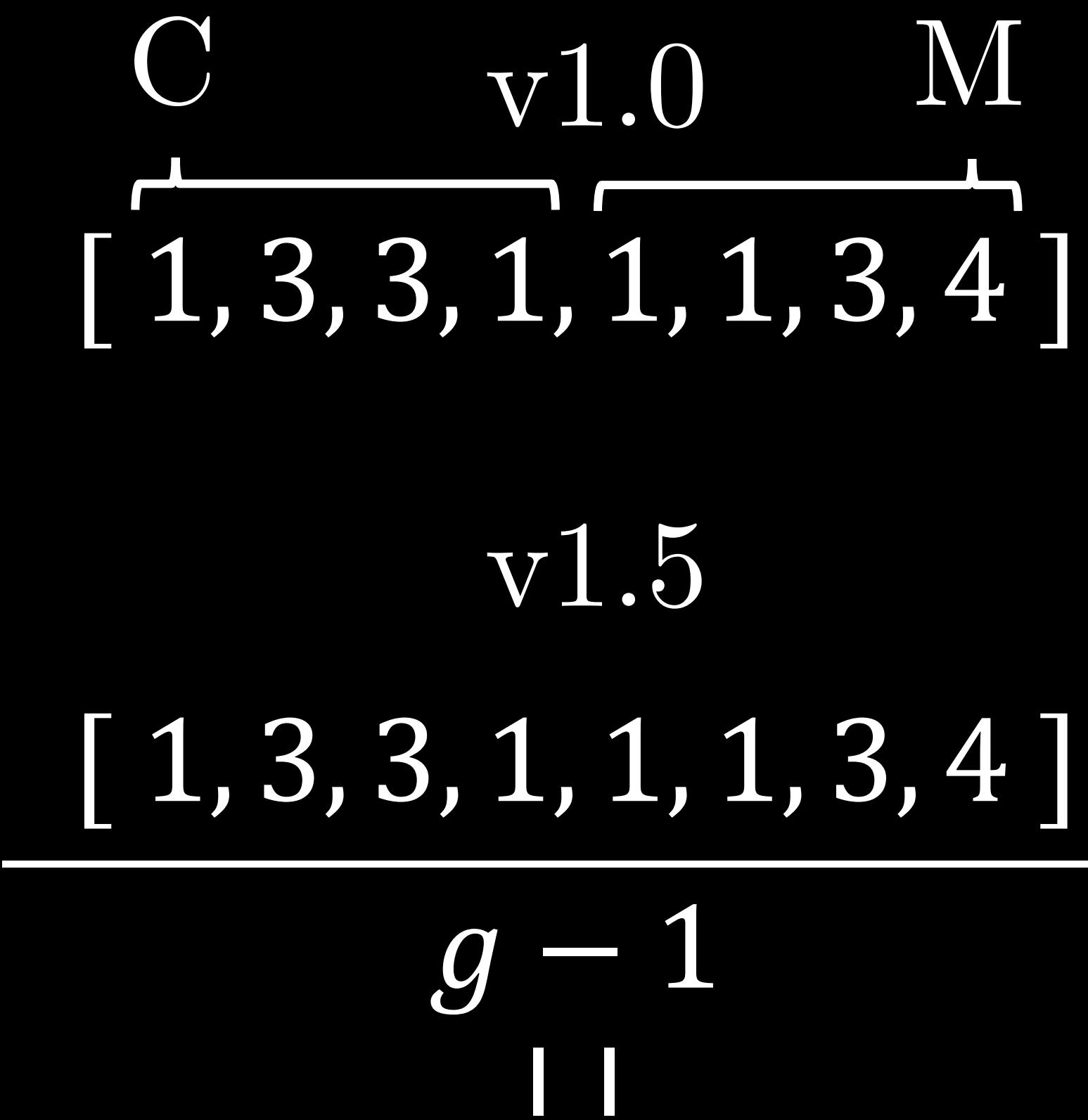
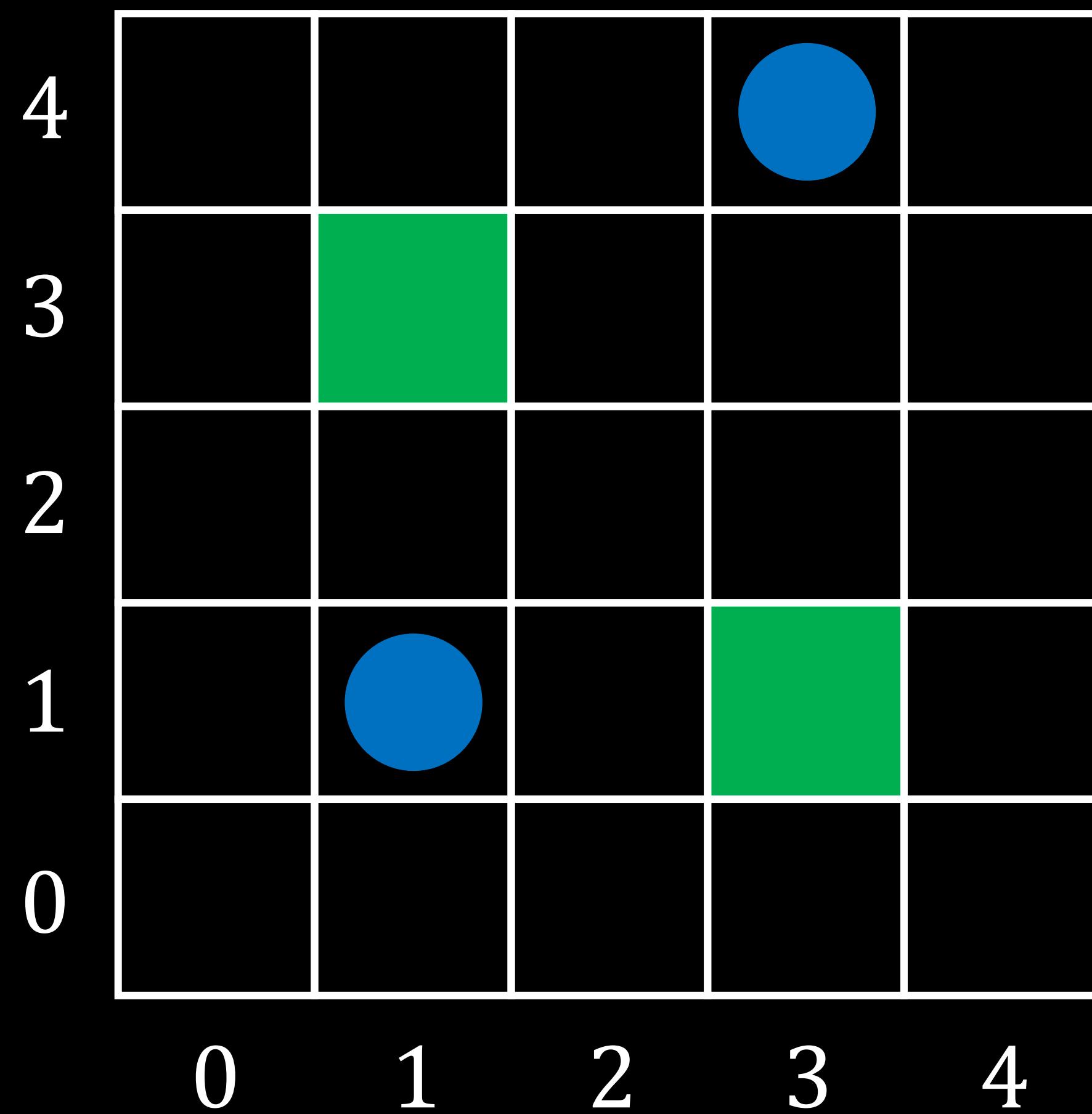
$A = [(0, 0), (0, 1), (0, 2), \dots]$   
 $\text{size}(A) = 5^2 = 25$



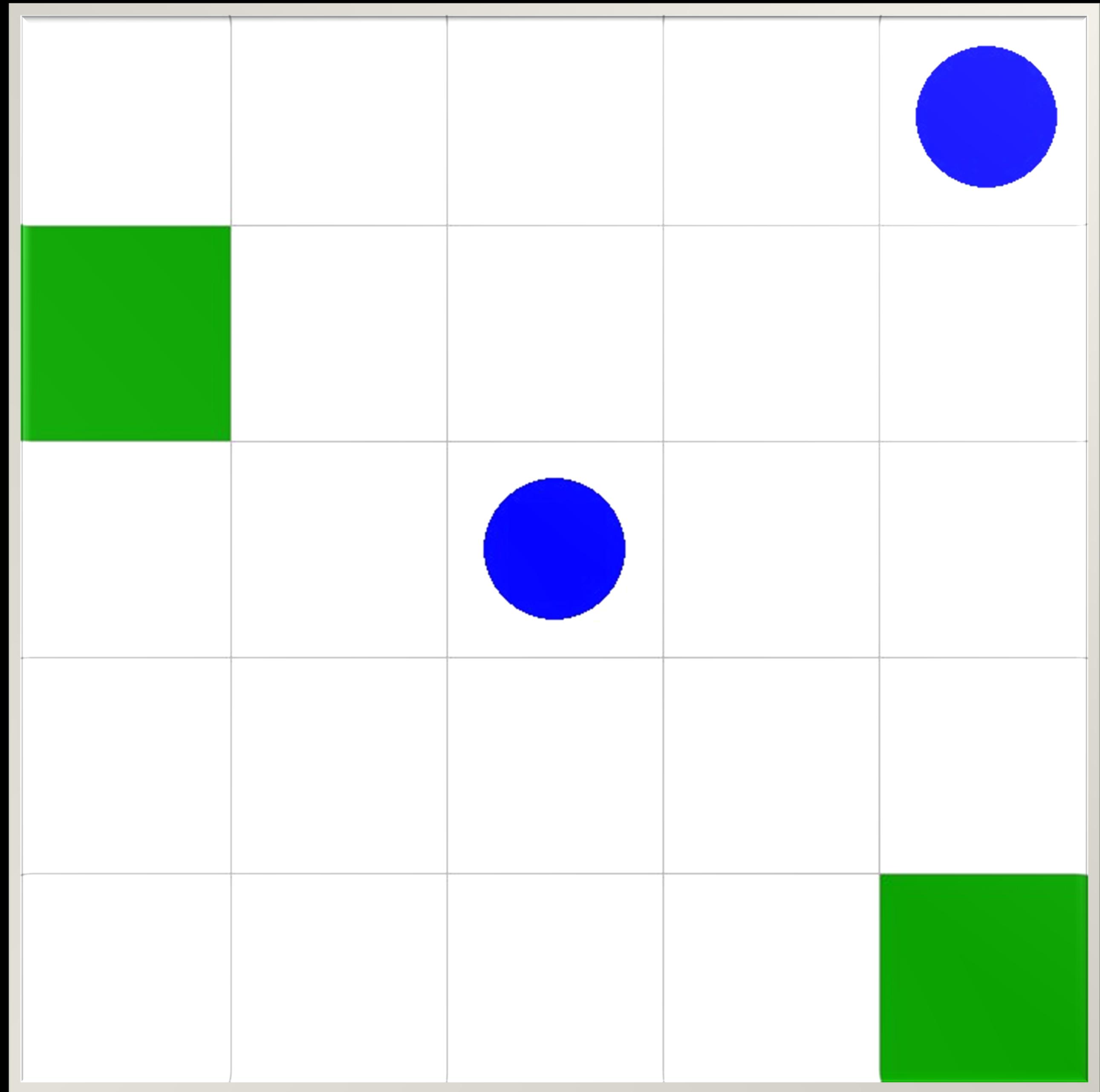
$A = [(0, 0, 0), (0, 0, 1), \dots]$   
 $\text{size}(A) = 5^3 = 125$

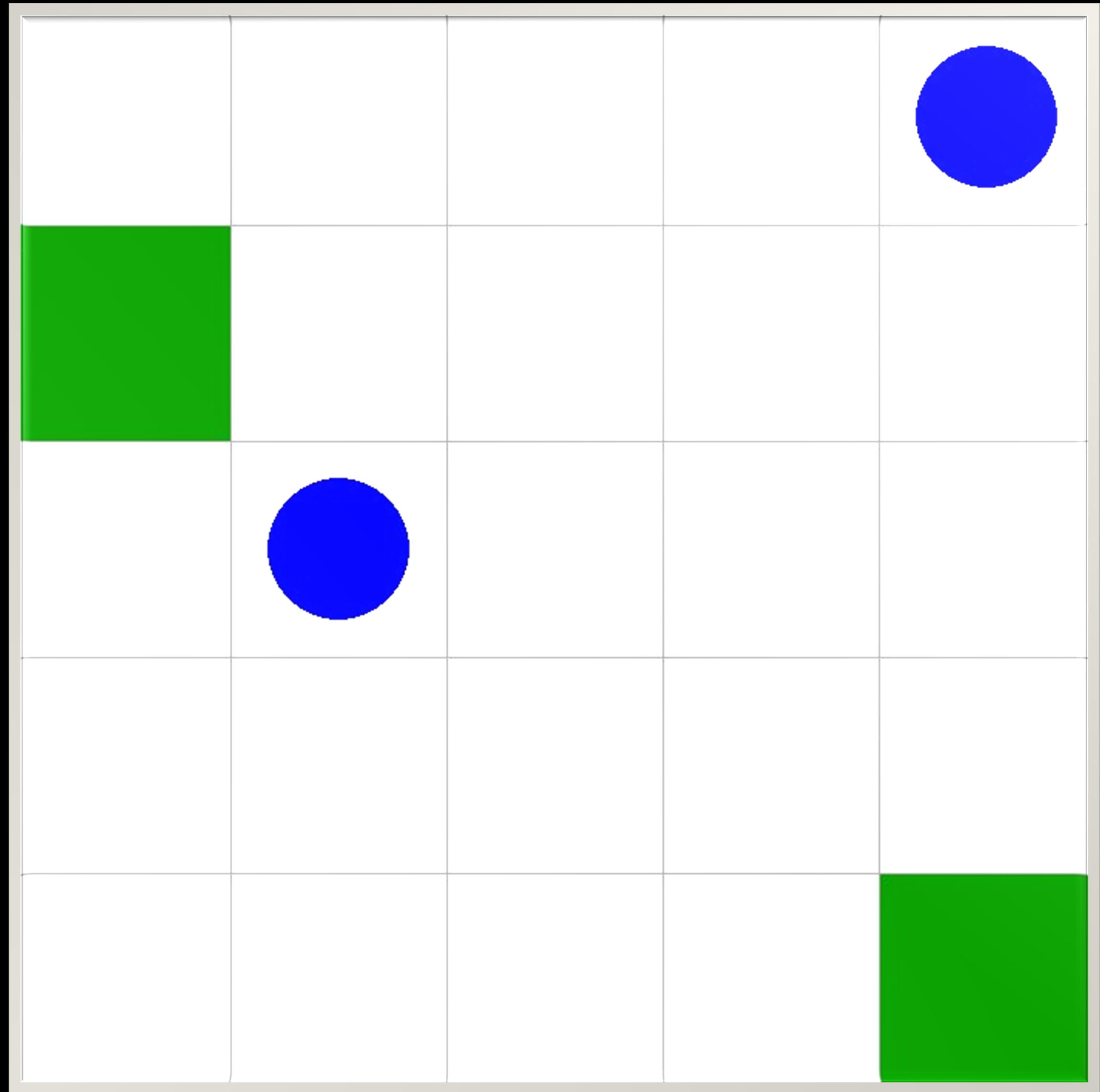
v1.0 & v1.5

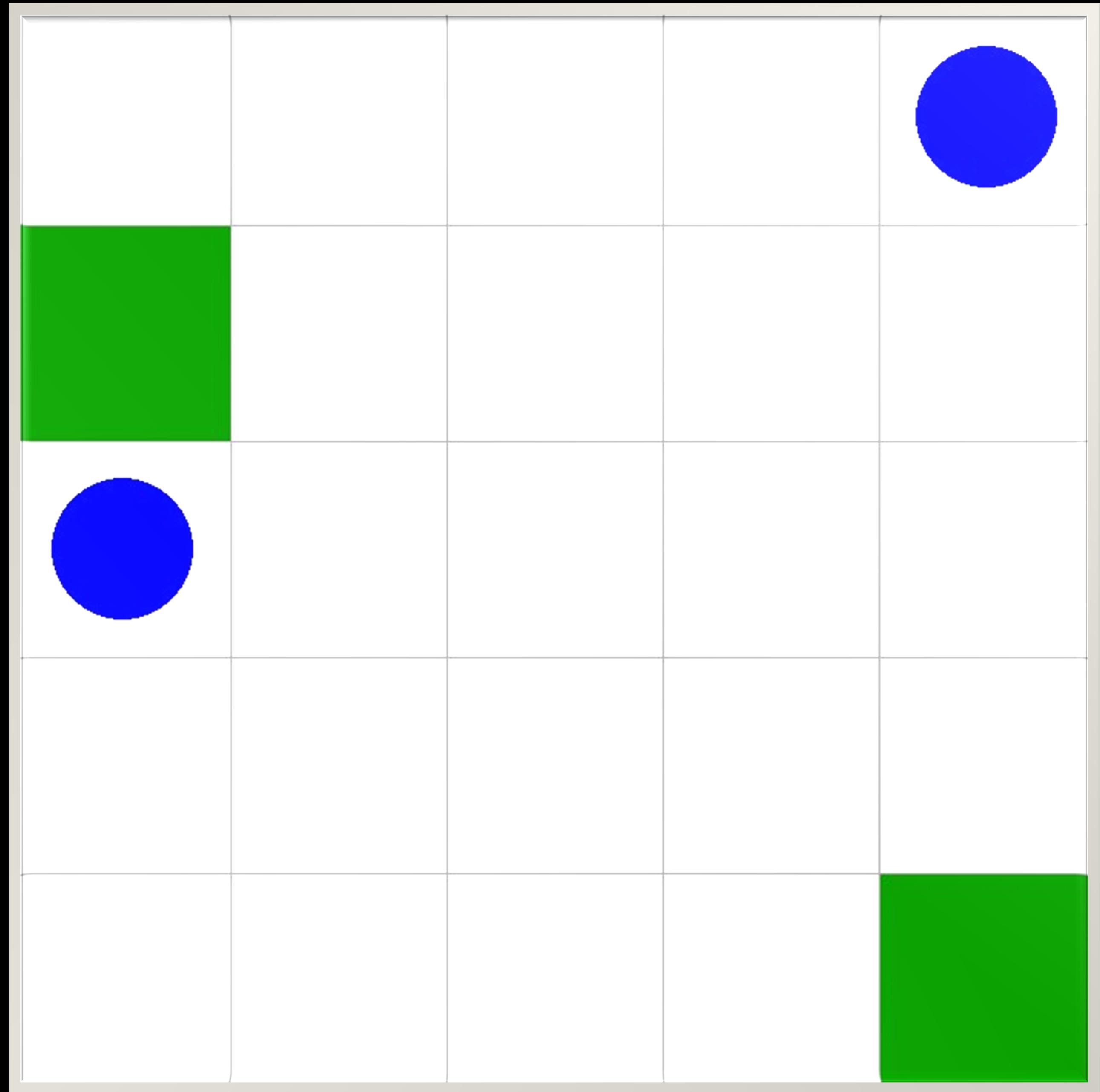
$g = 5$

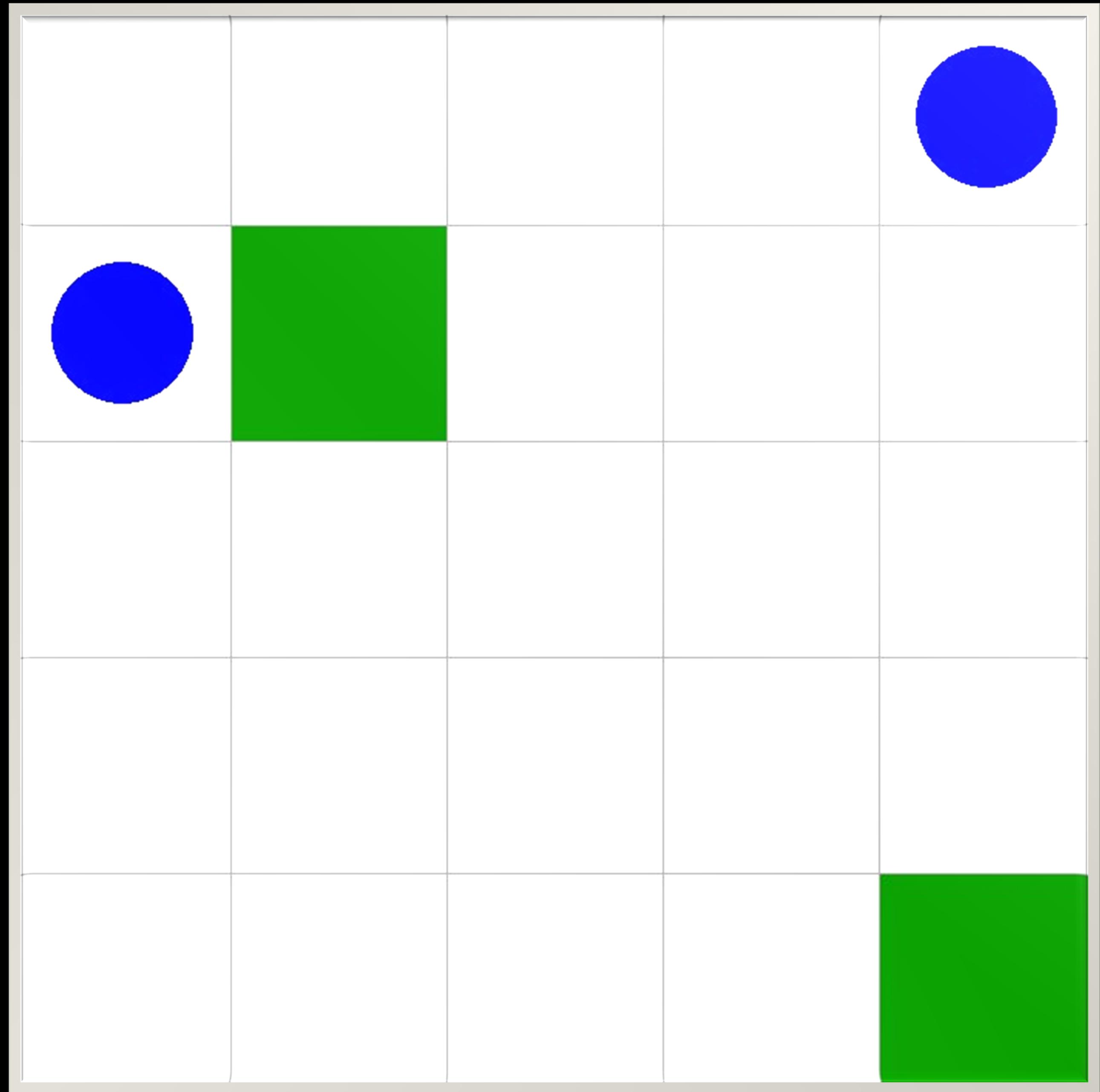


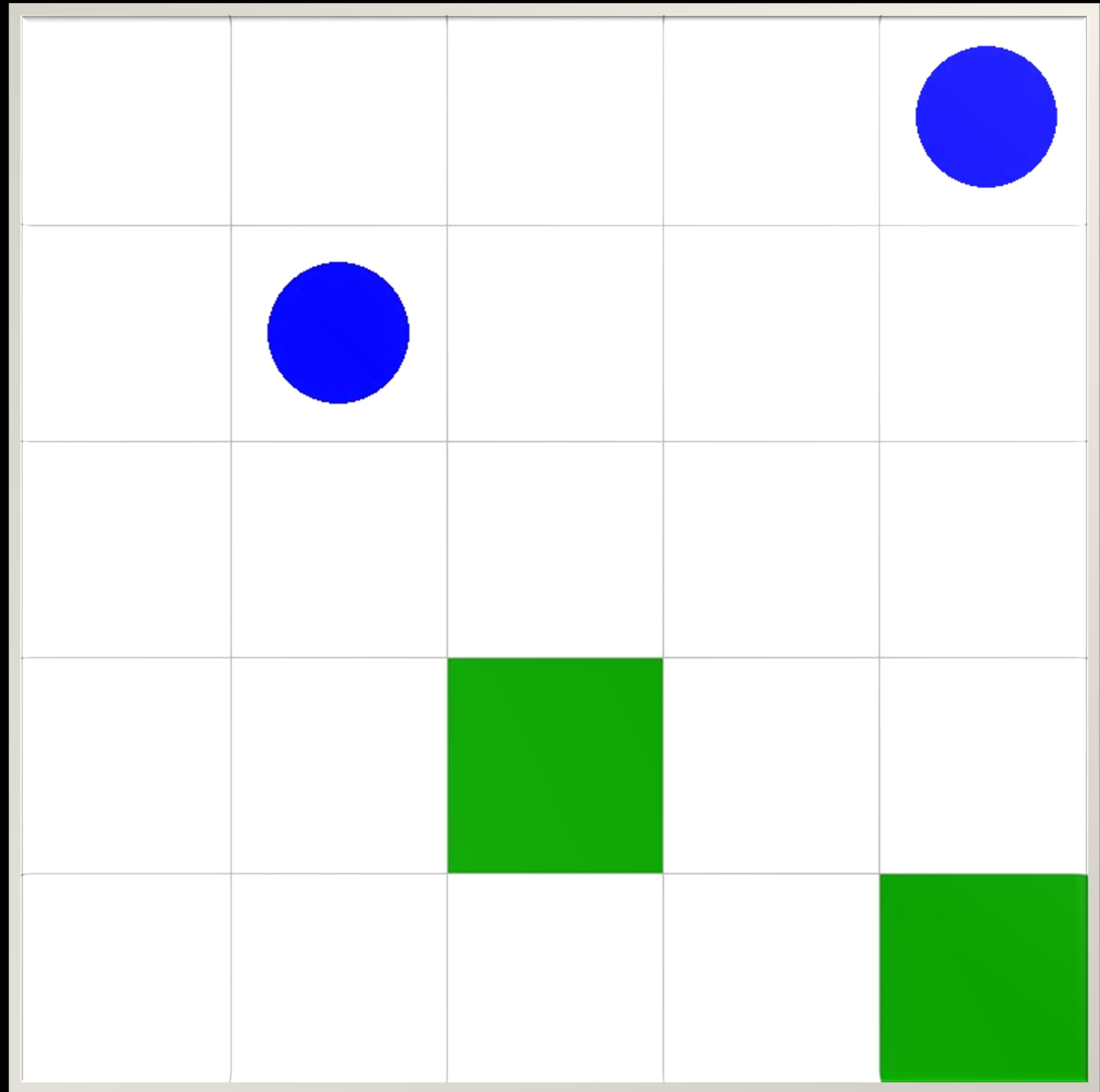
[ 0.25, 0.75, 0.75, 0.25, 0.25, 0.25, 0.75, 1 ]

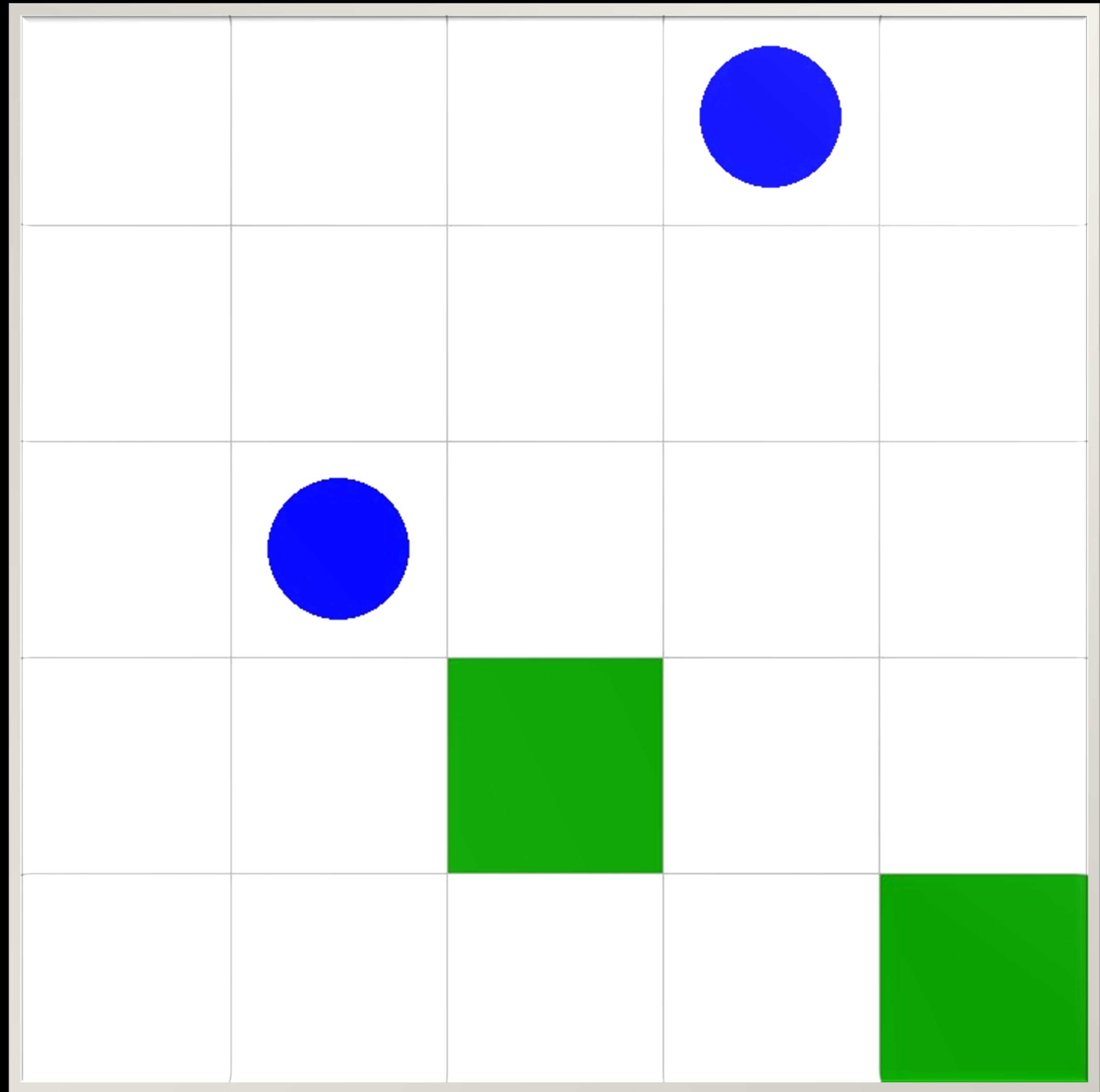


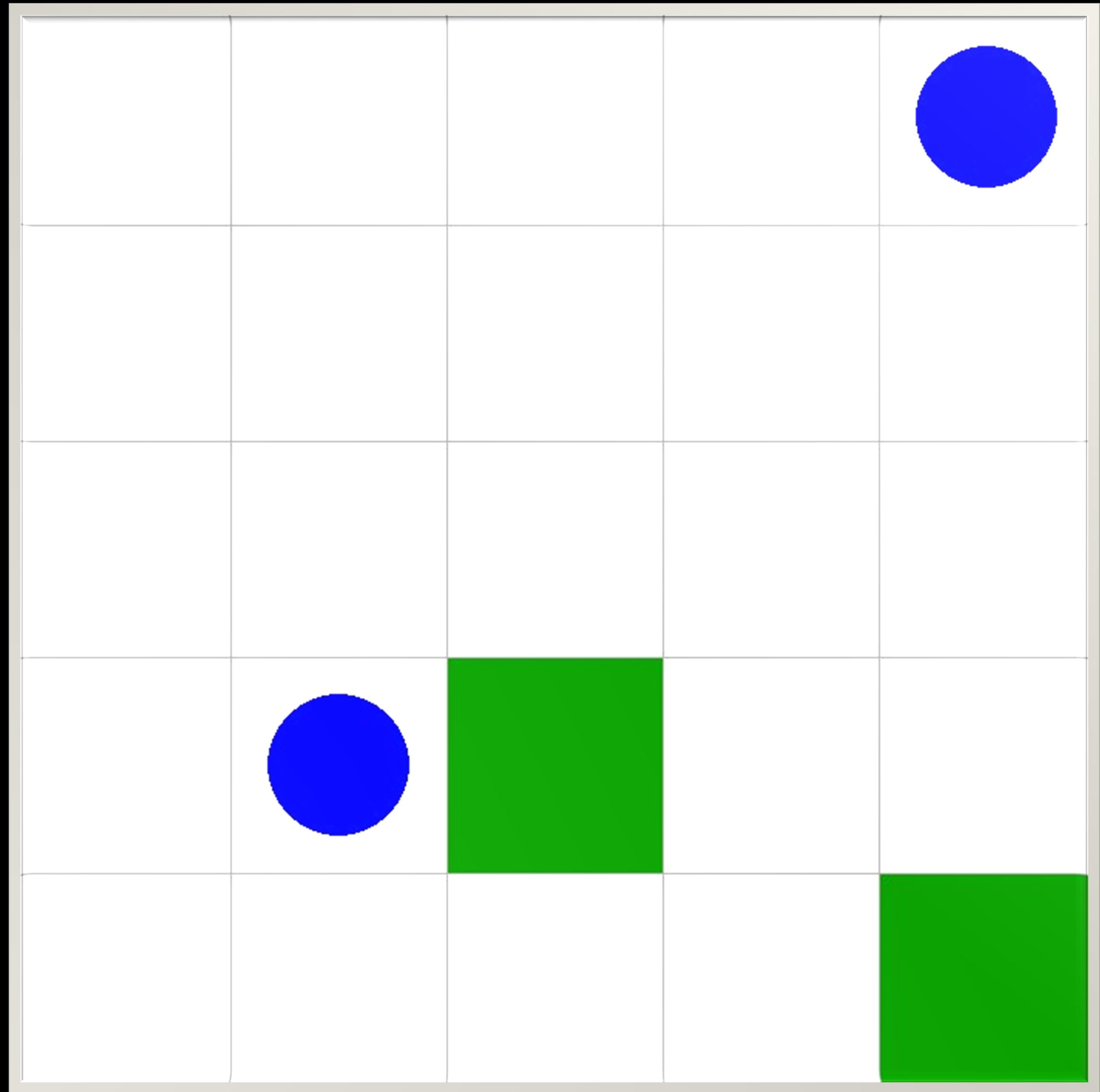


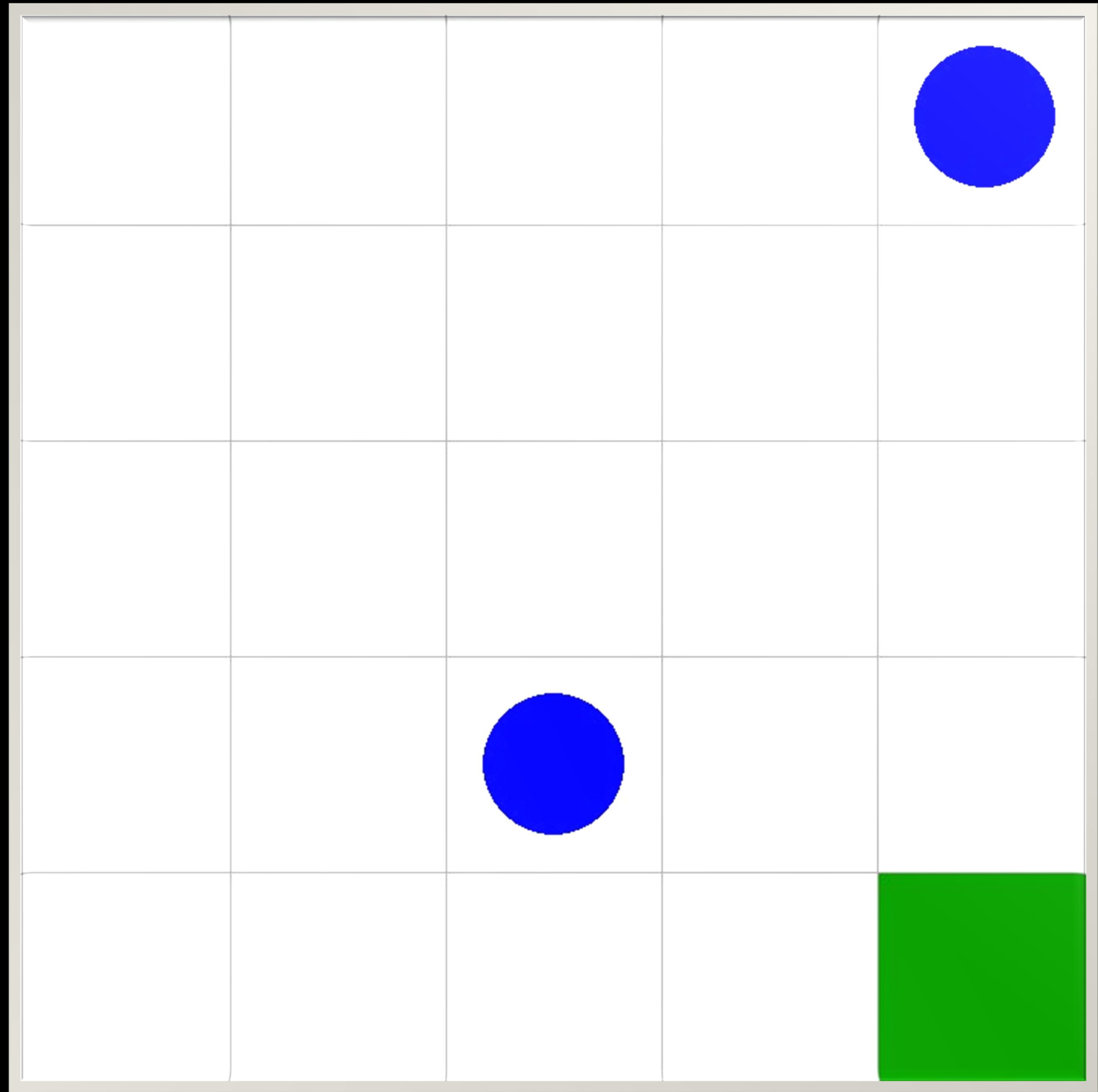


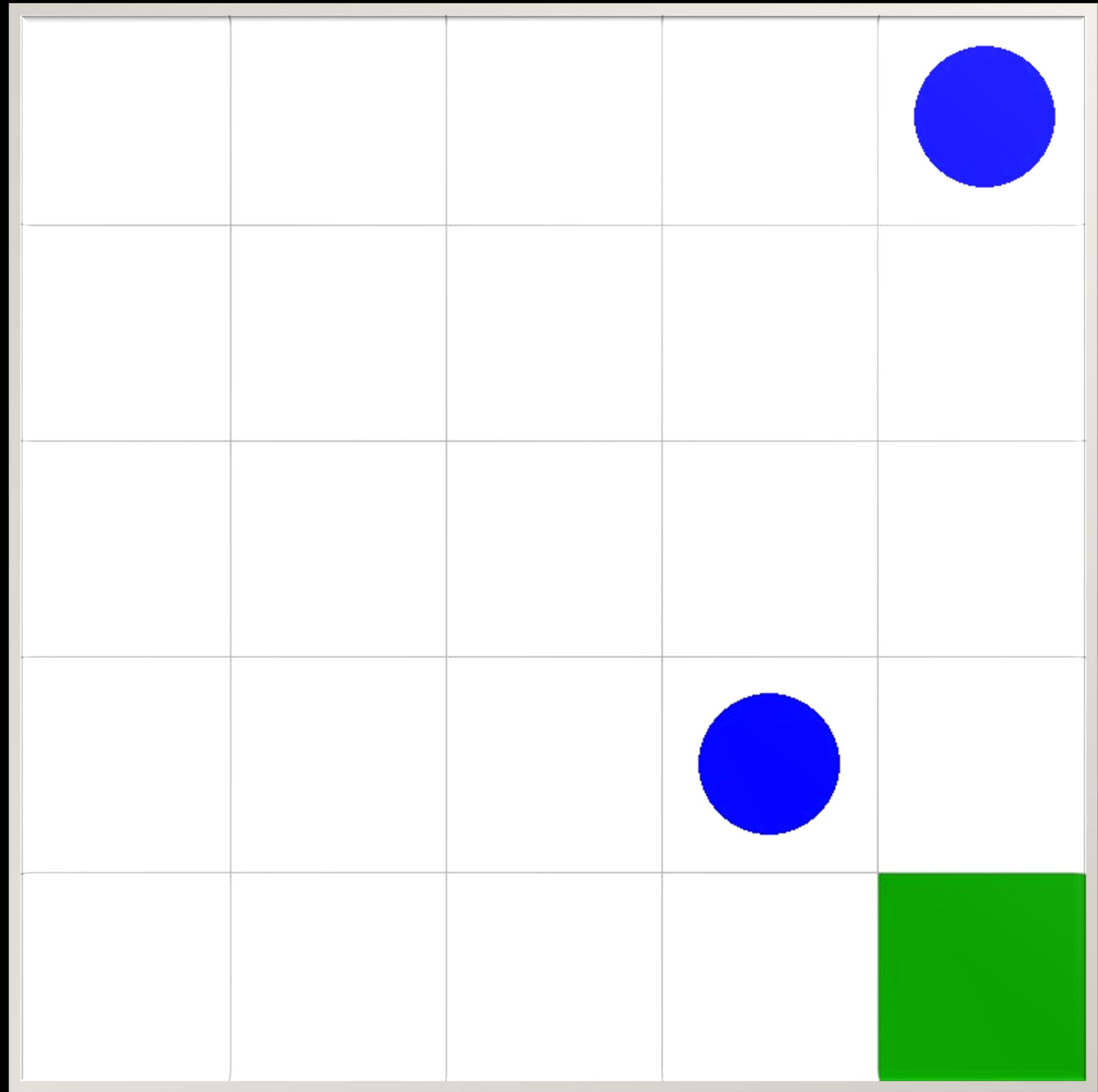


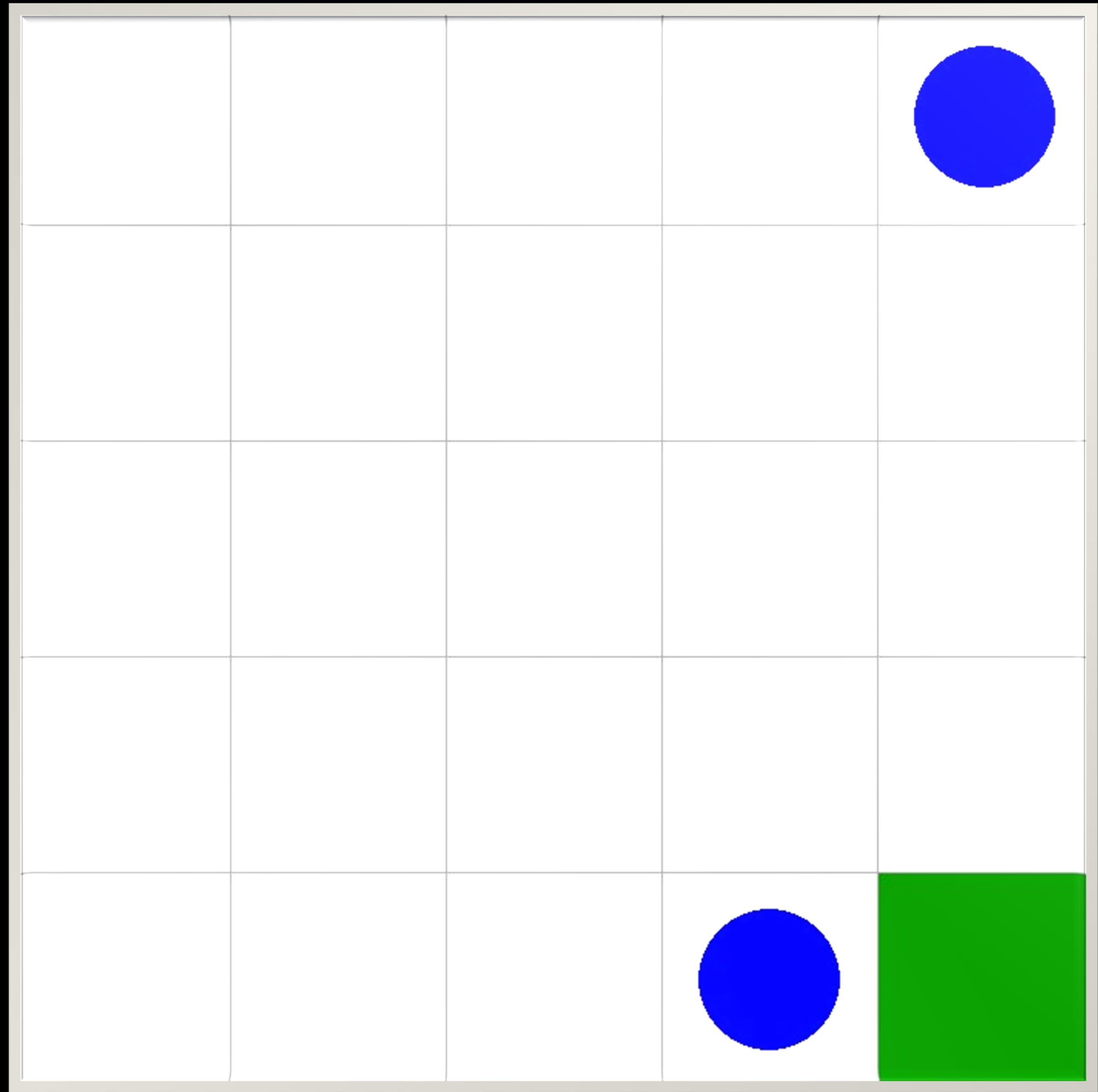






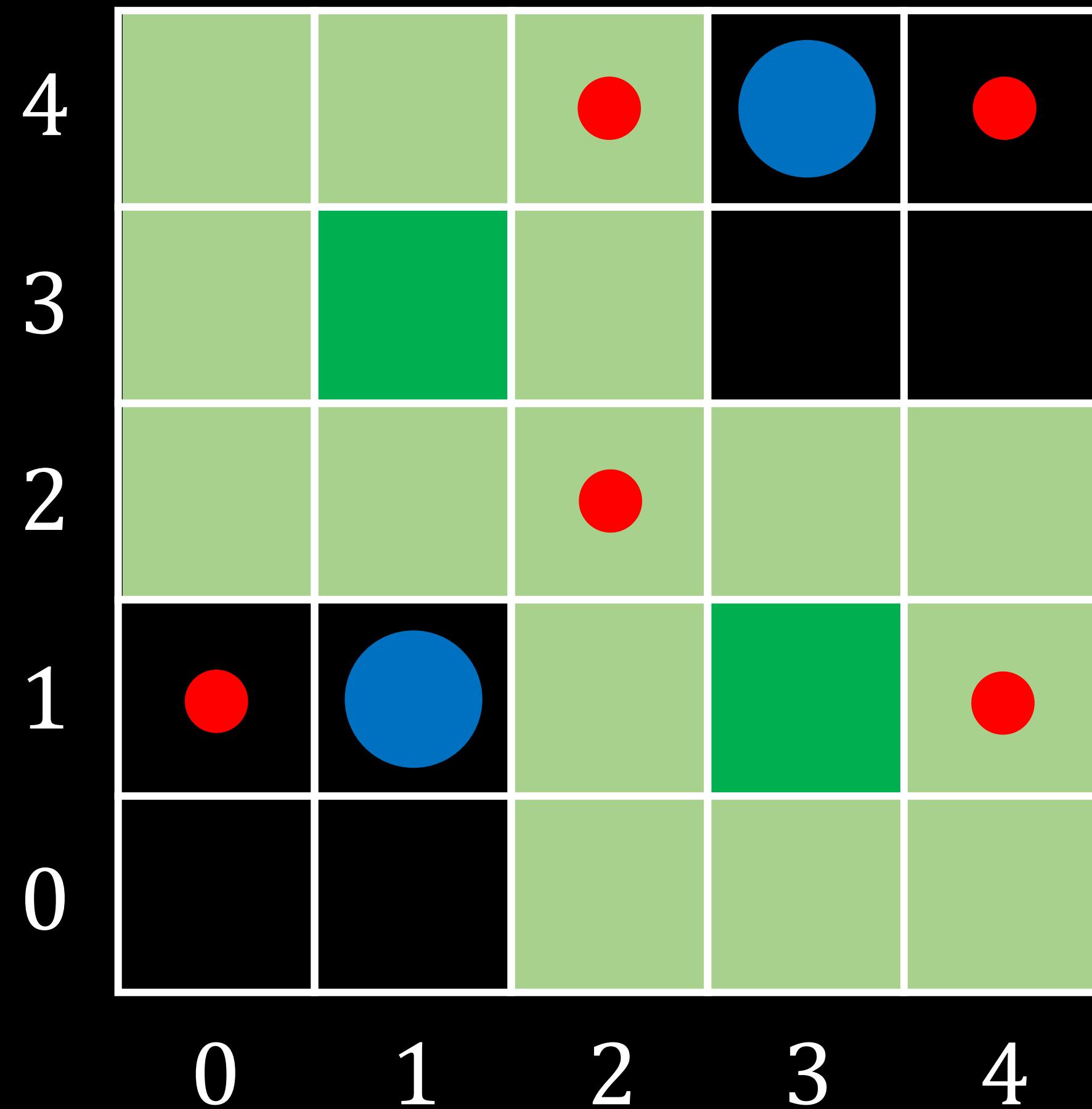






v2.0 & v2.5

$g = 5$   
 $I = 1$   
 $p = 1$

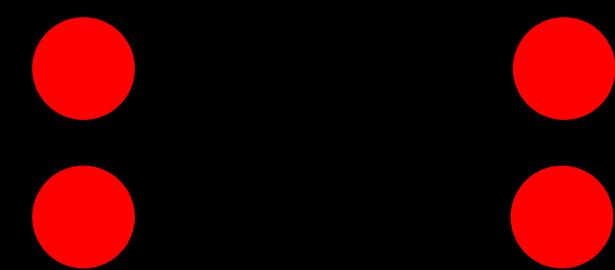


v2.0

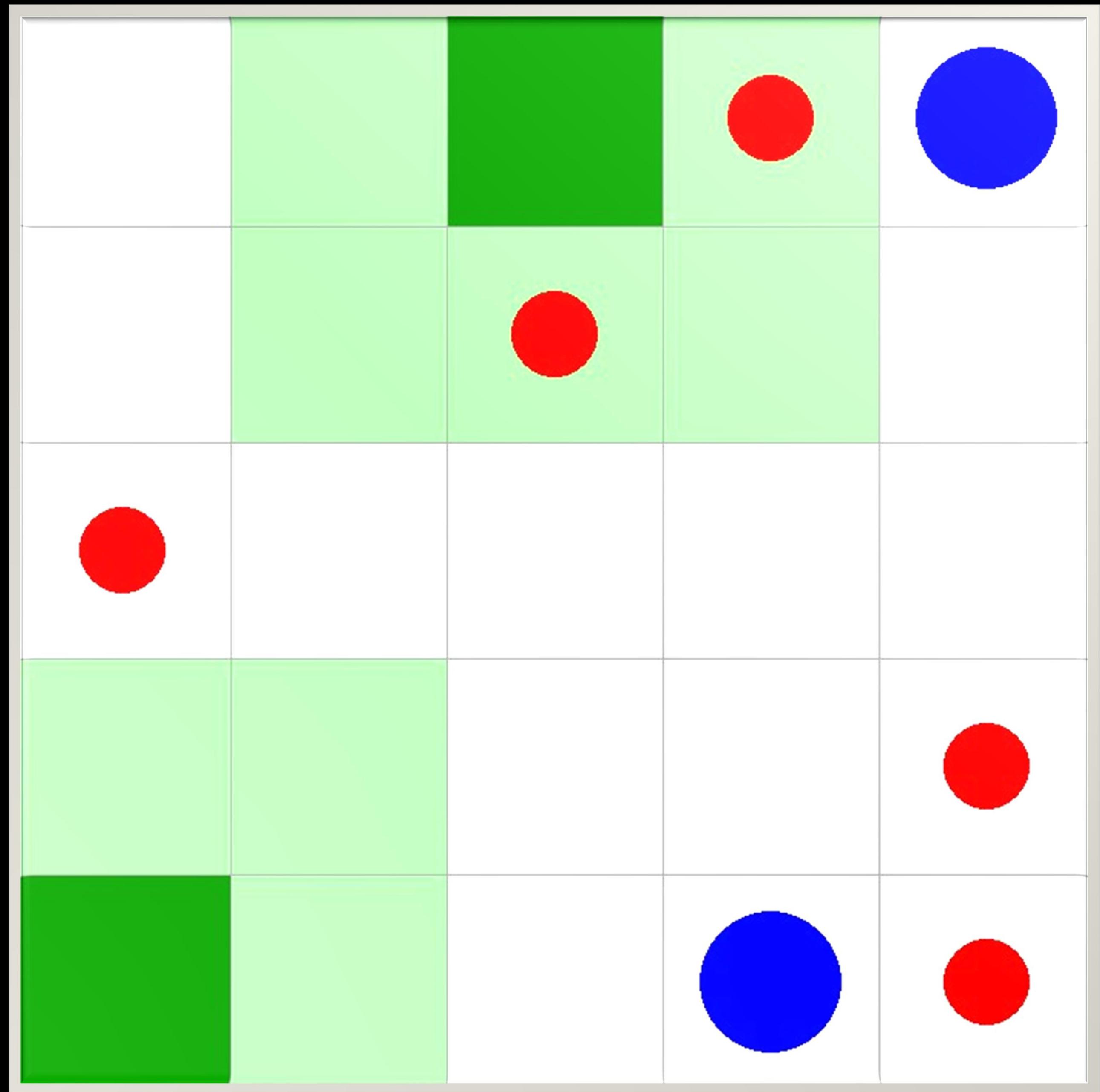
[  $C, M, N$  ]

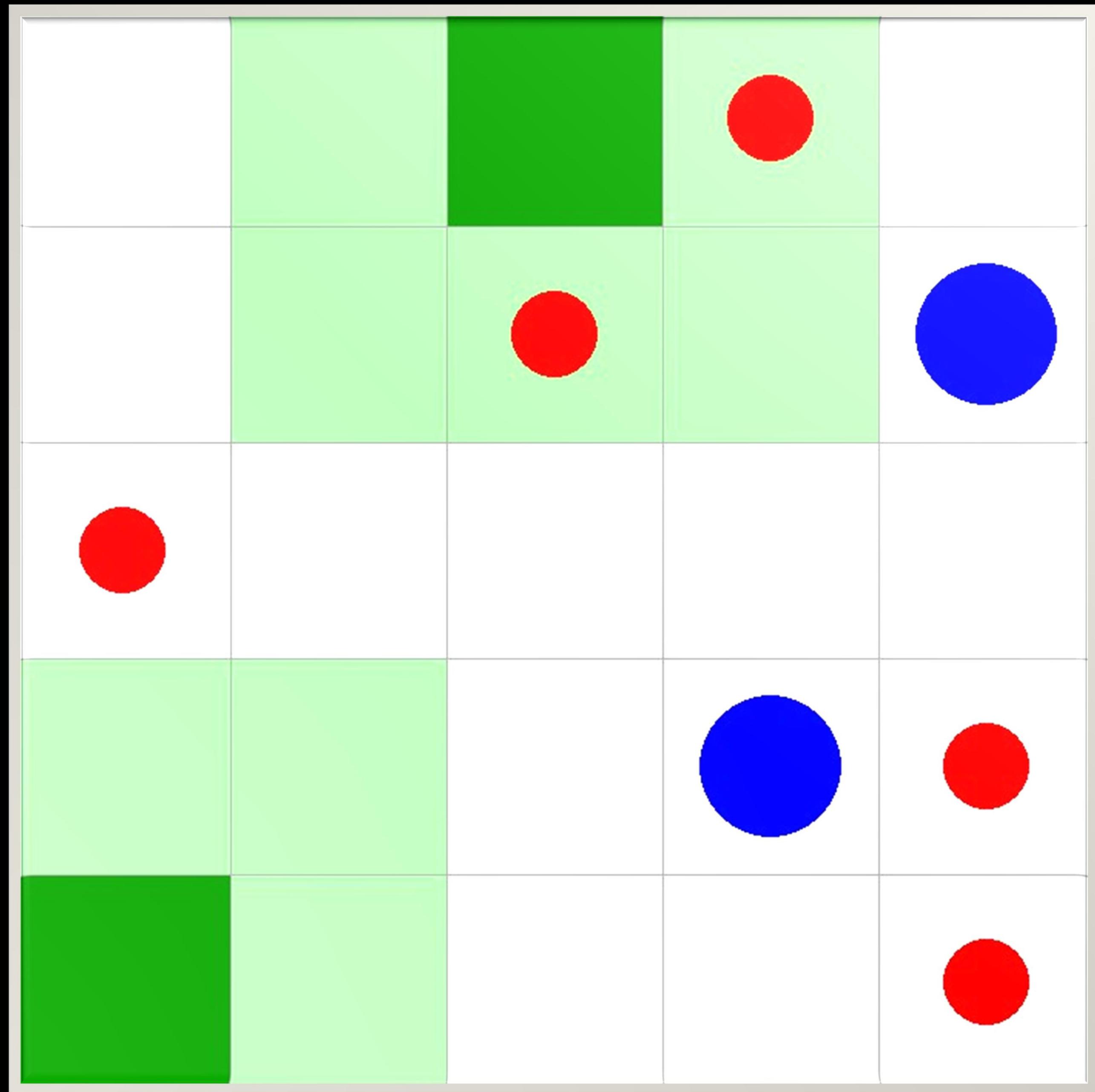
v2.5

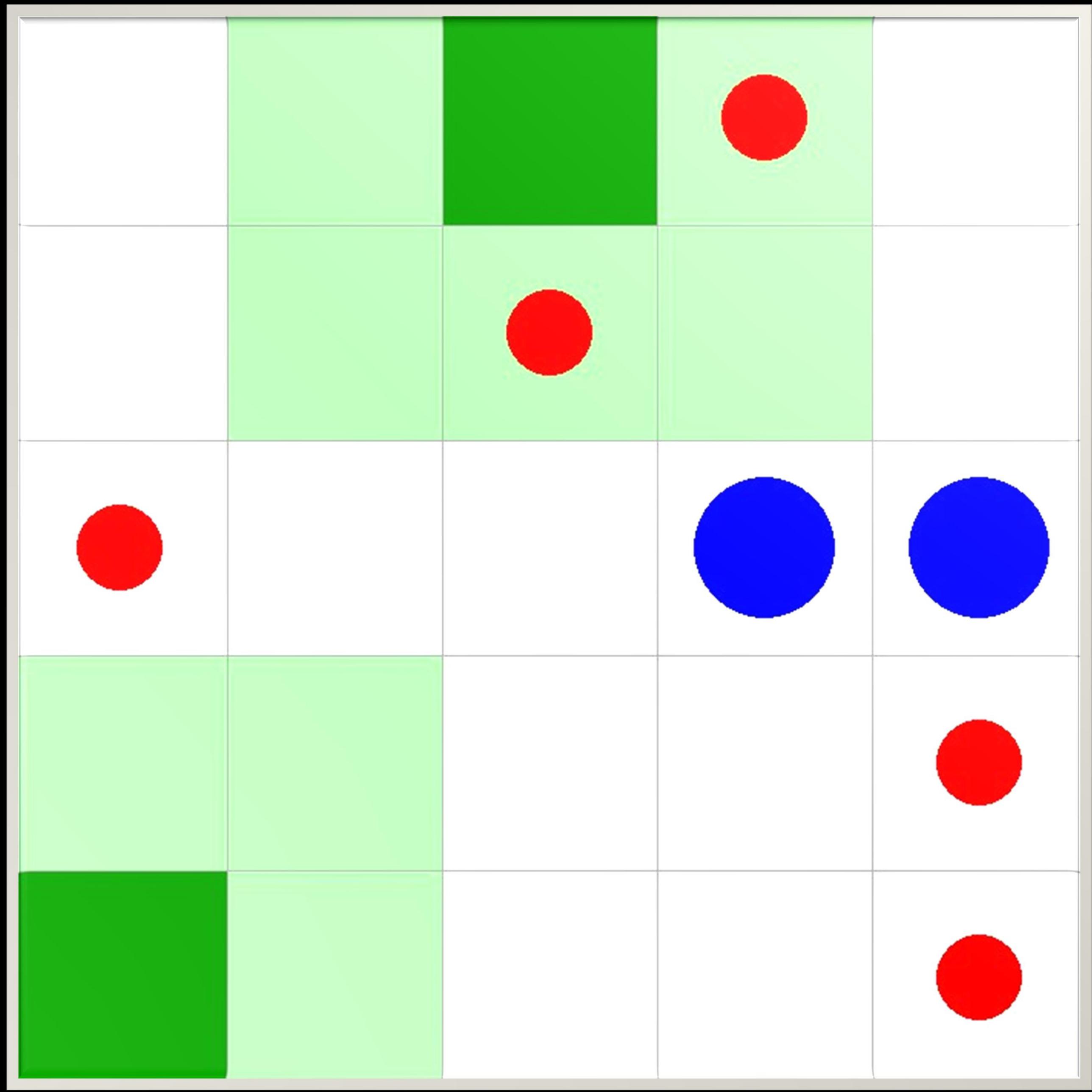
[ 1, 3, 2, 3, 1, 2, 1, 1, 3, 4 ]

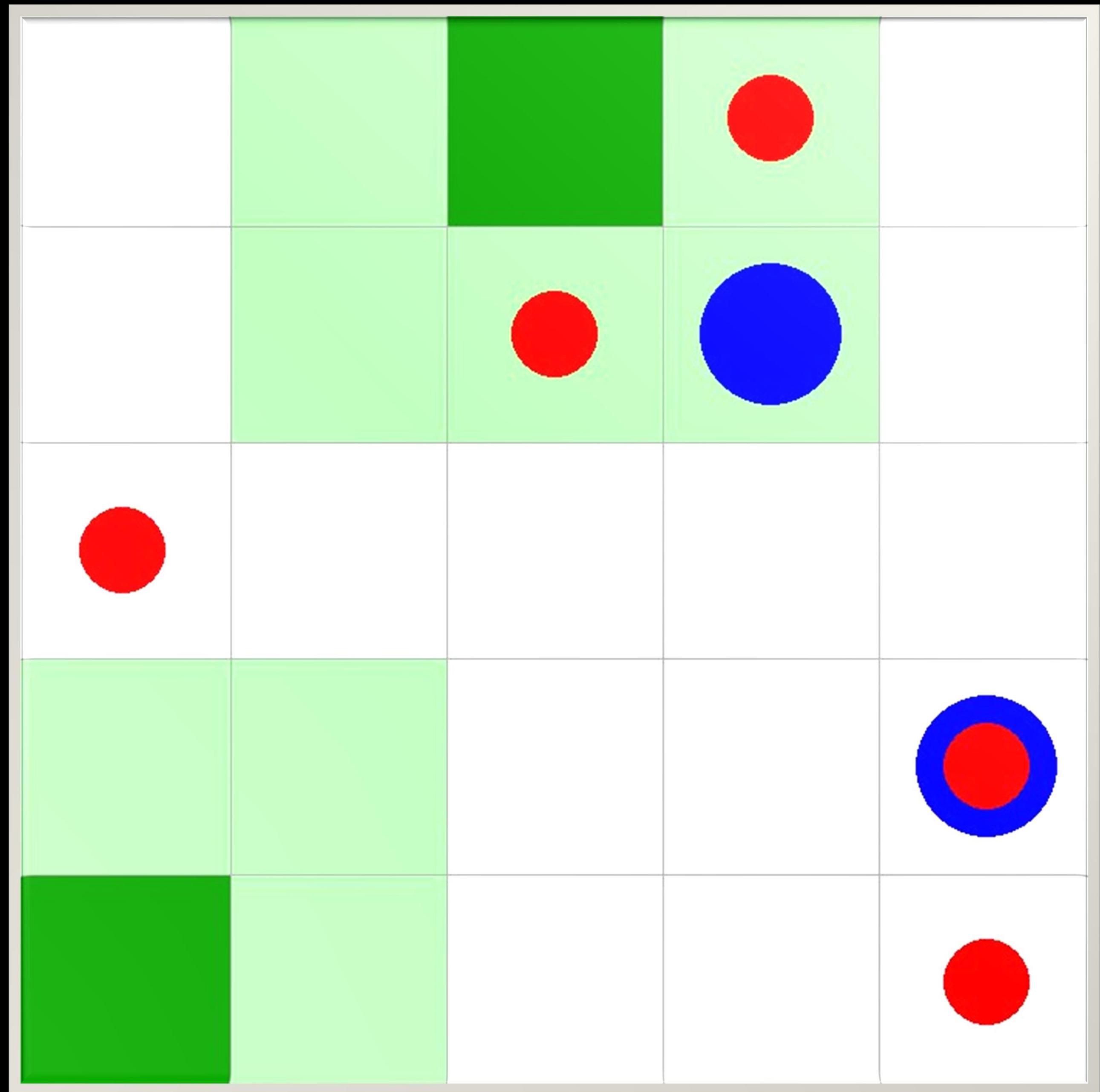


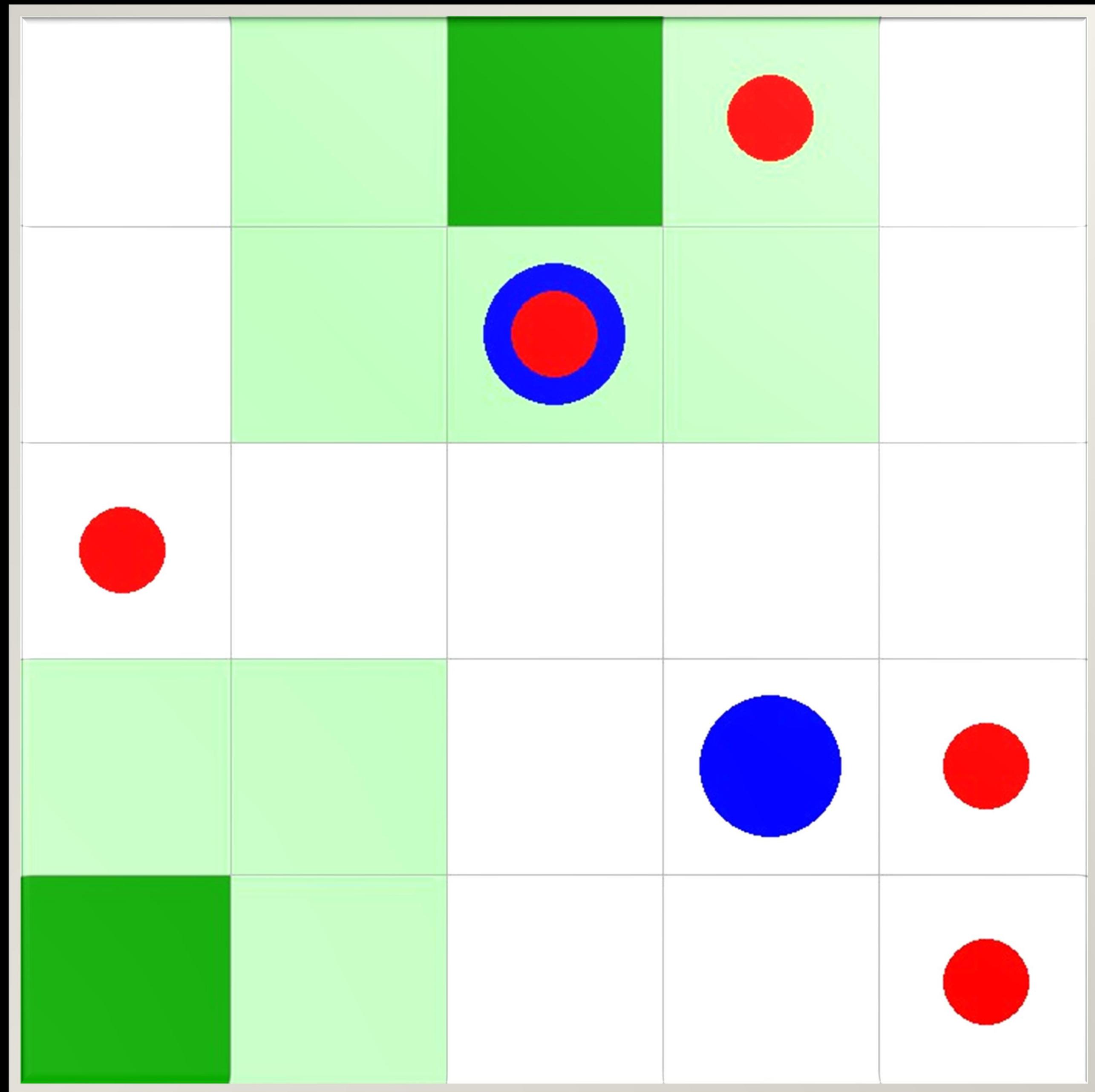
Normalize!

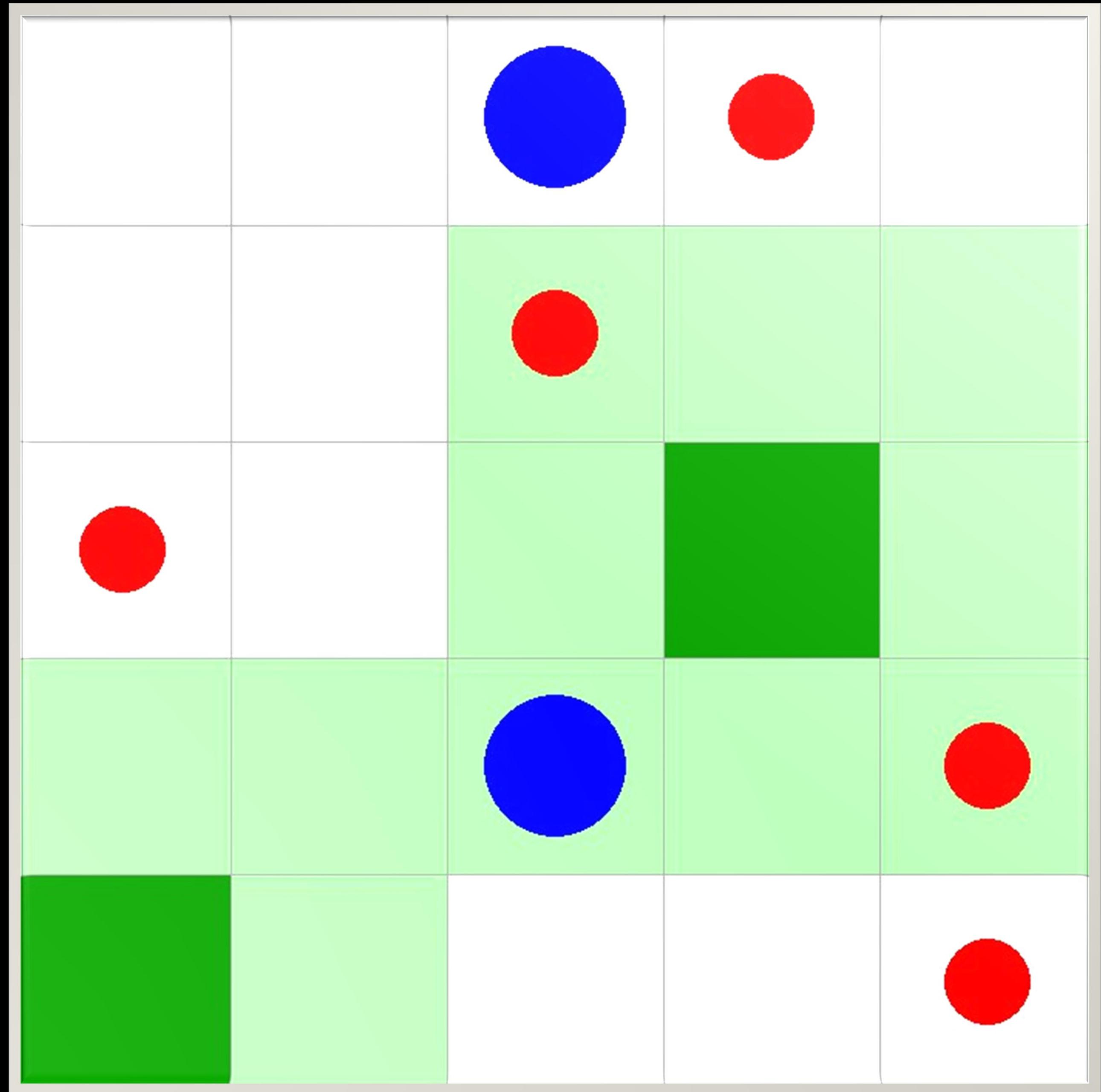


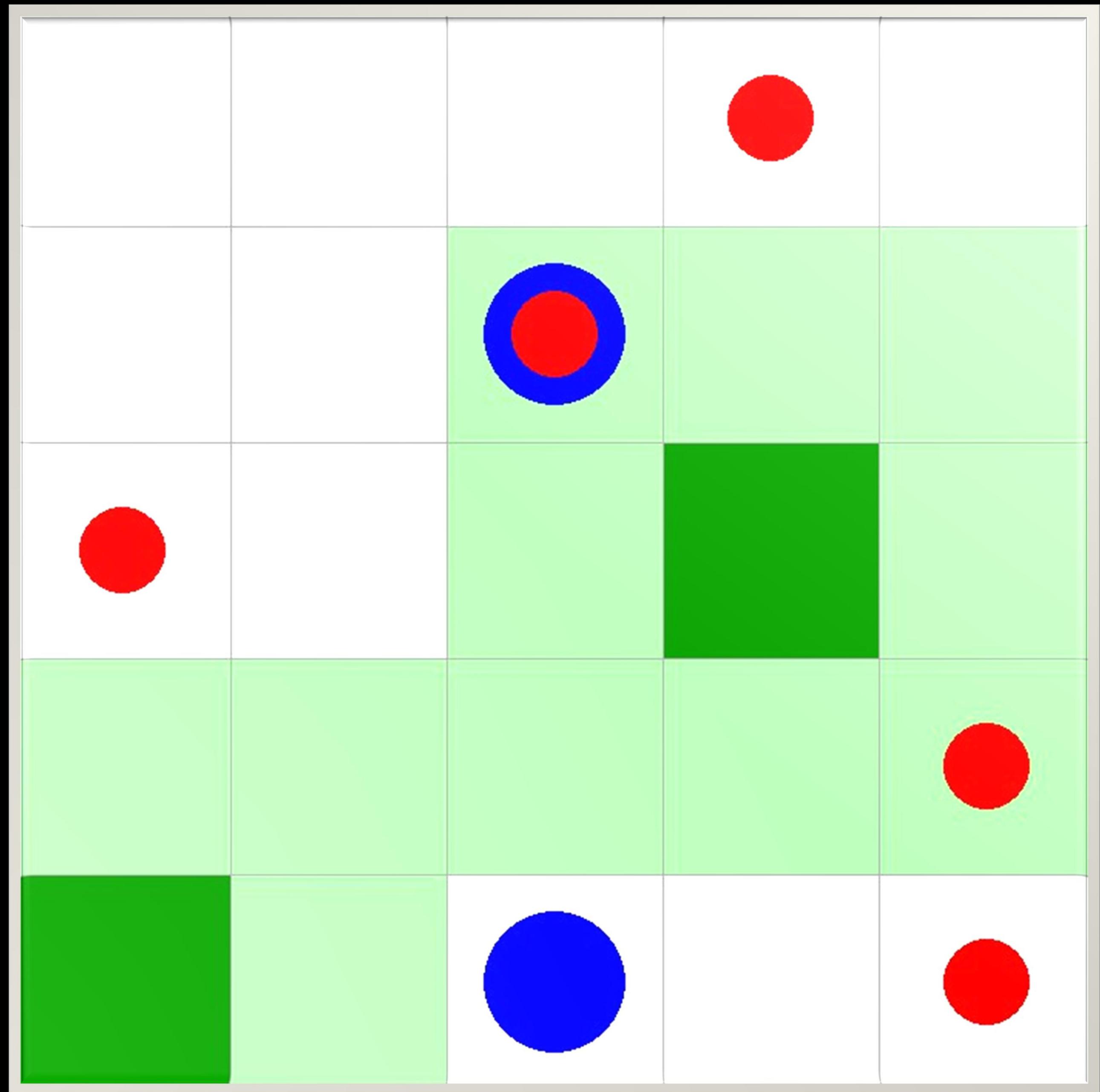


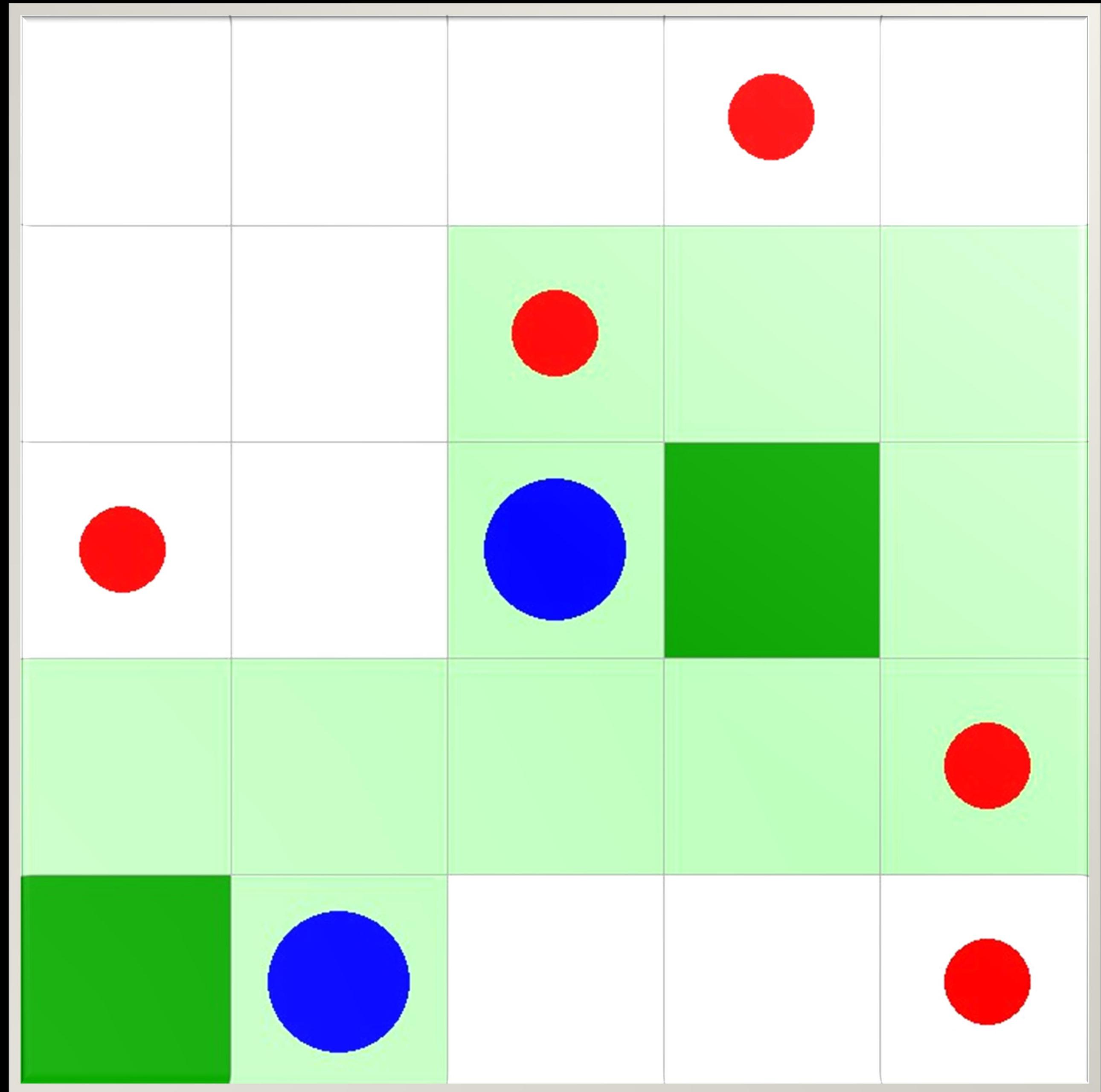


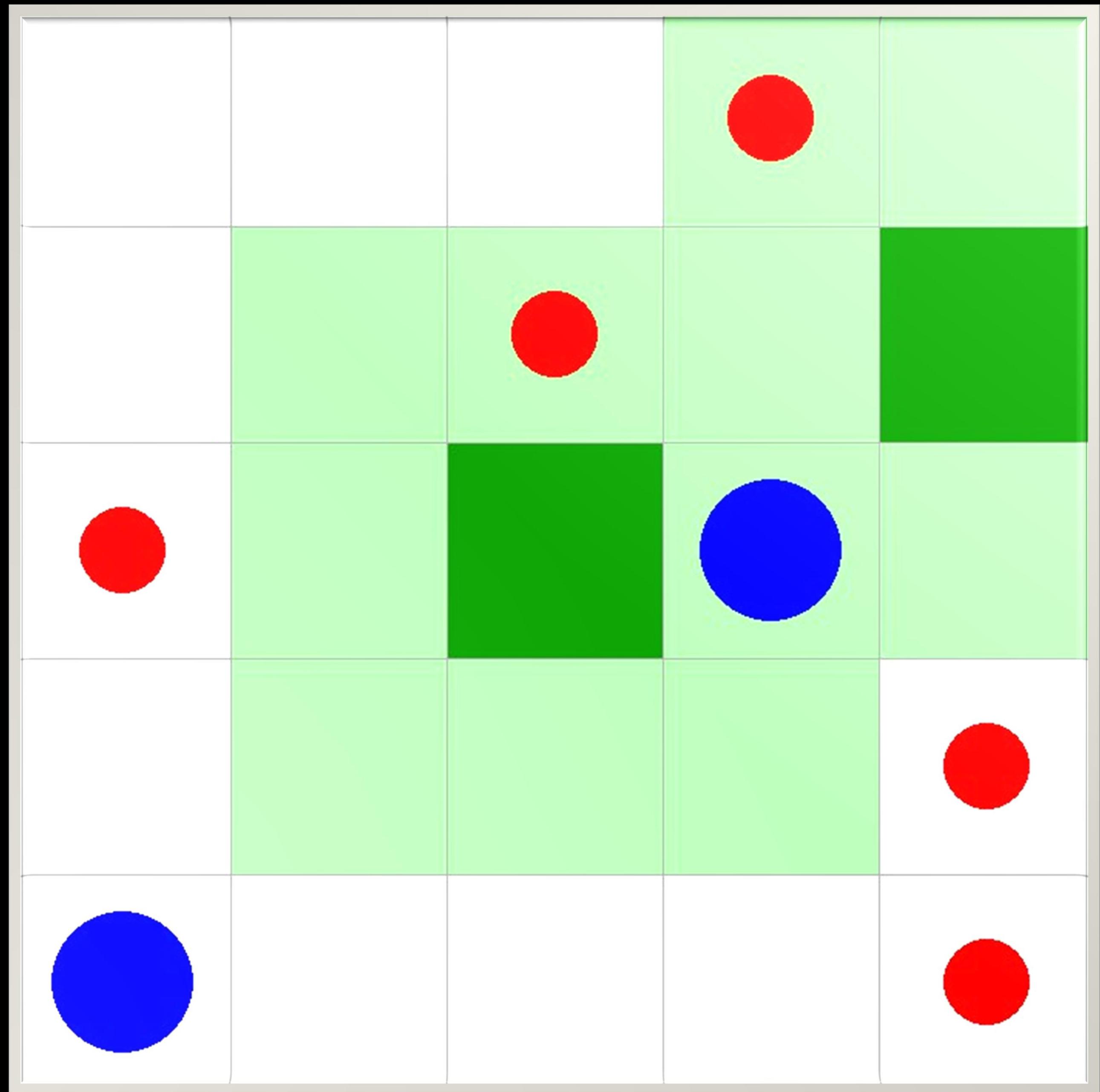


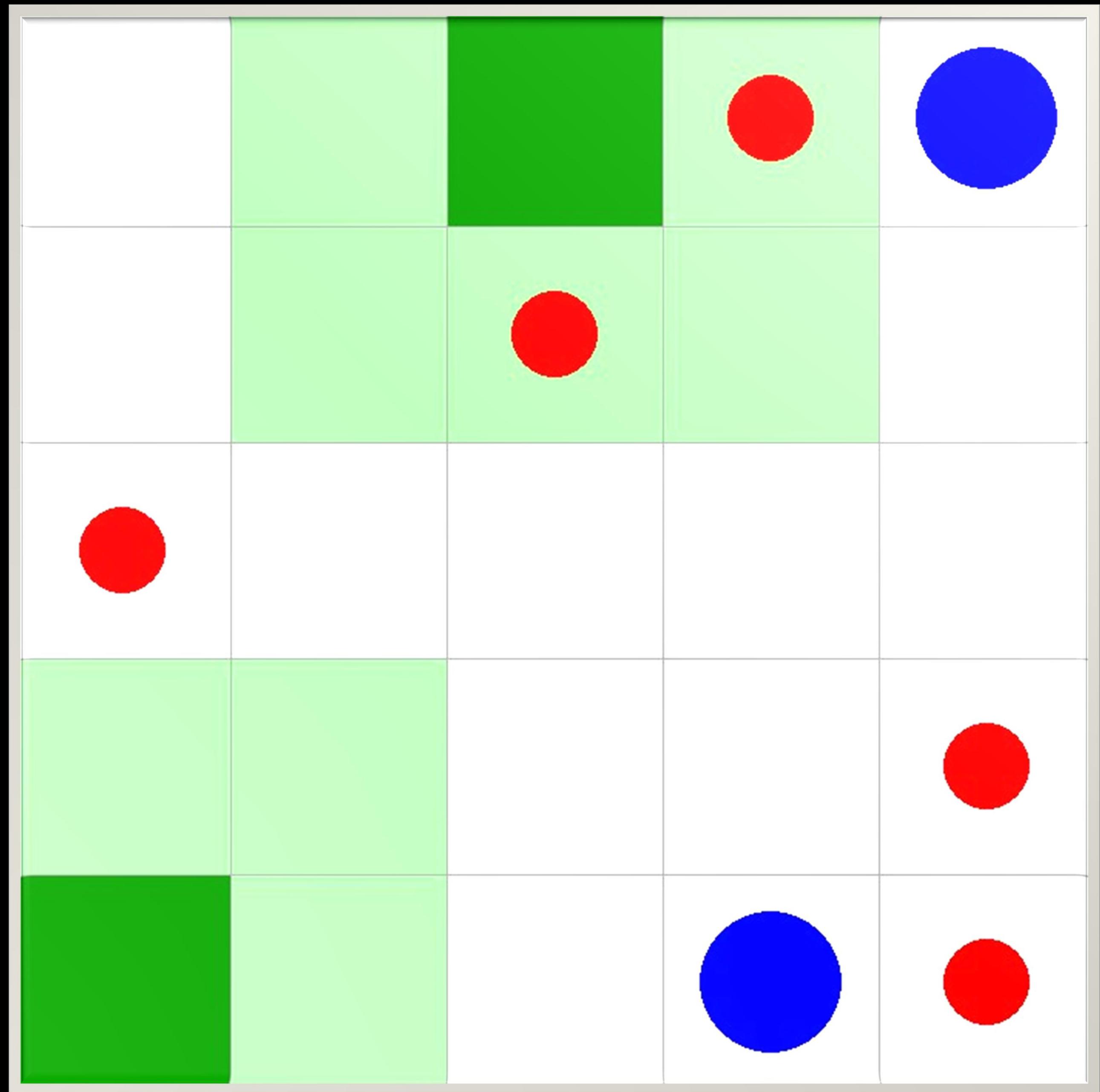


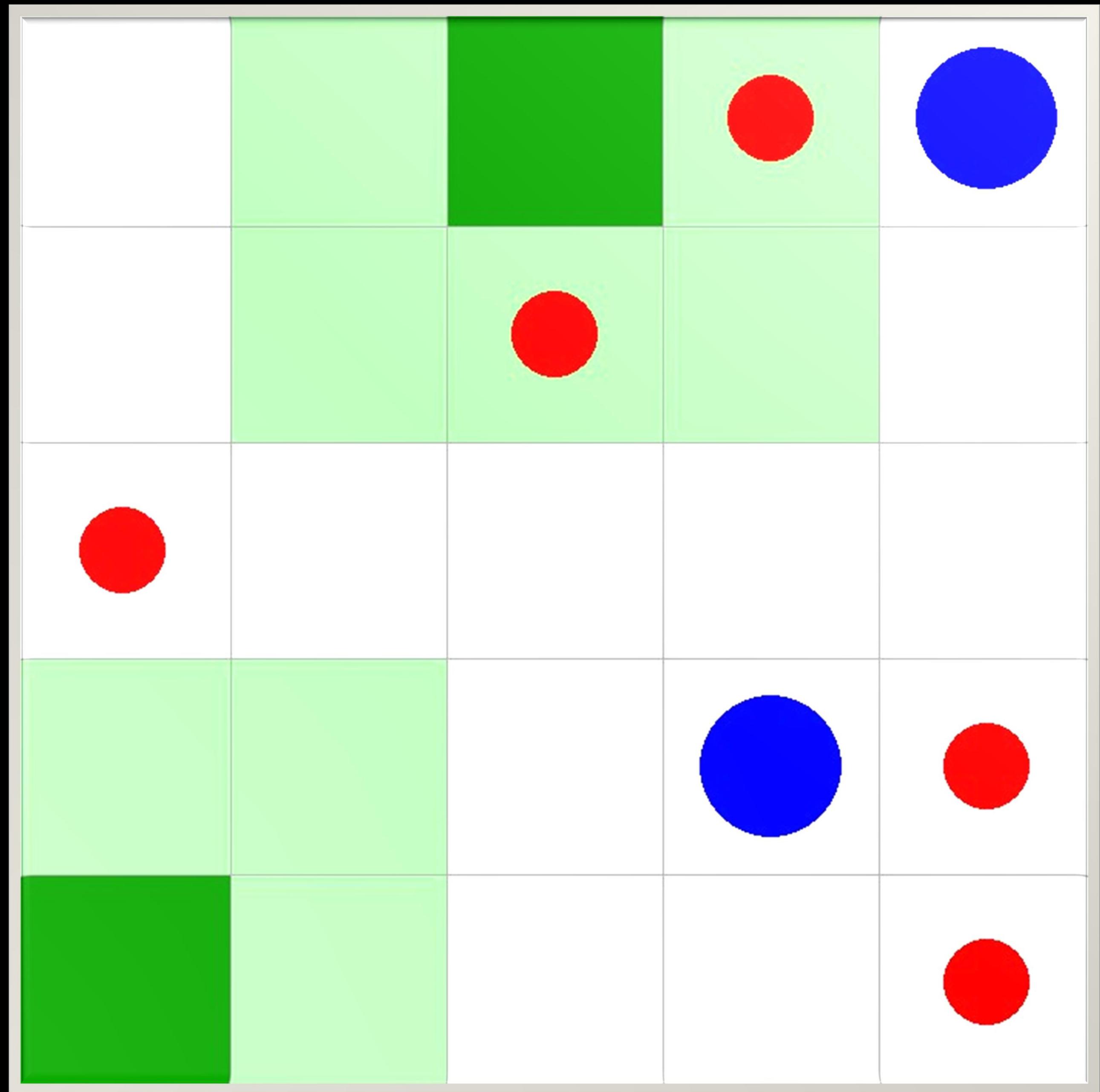


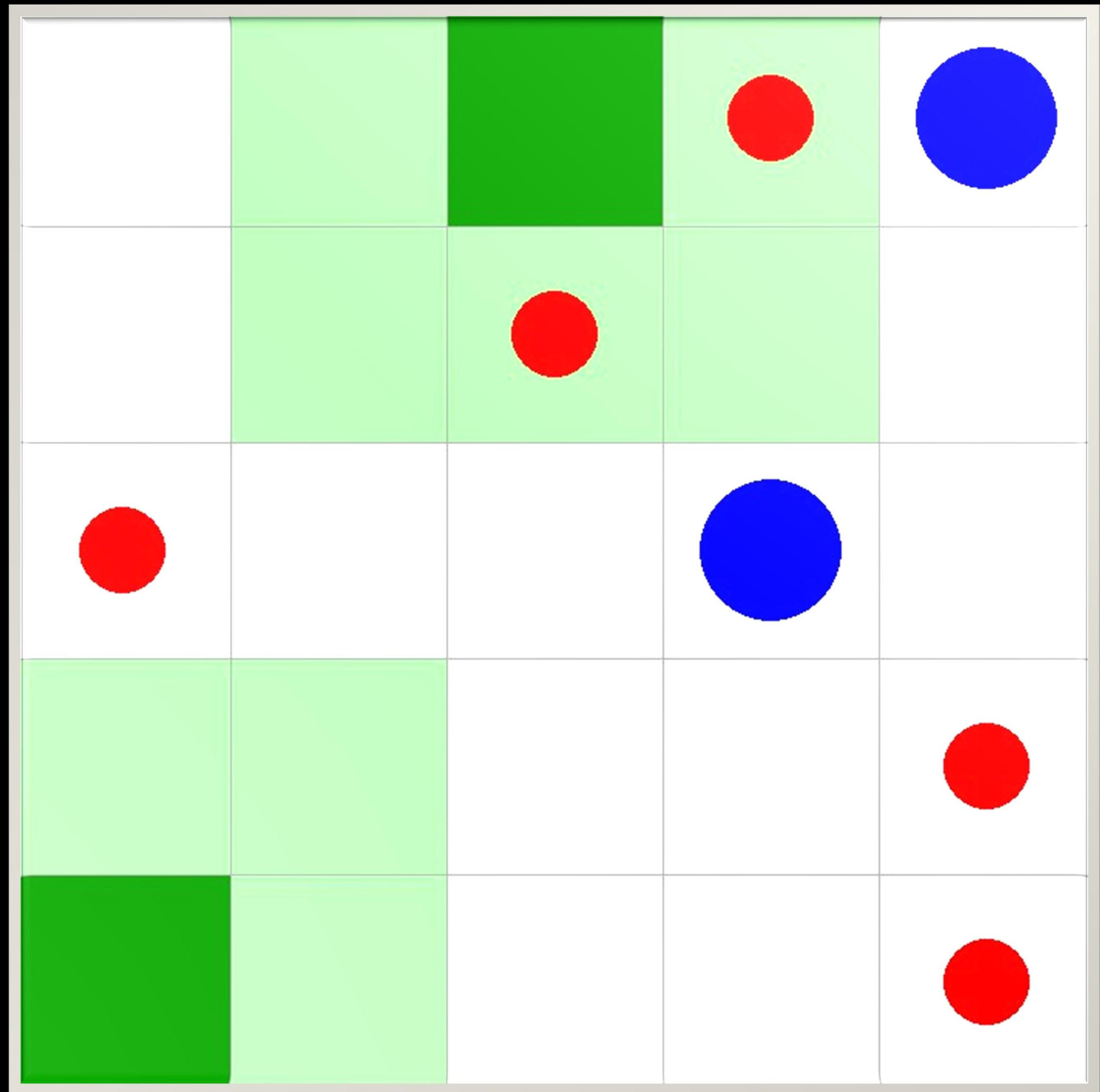


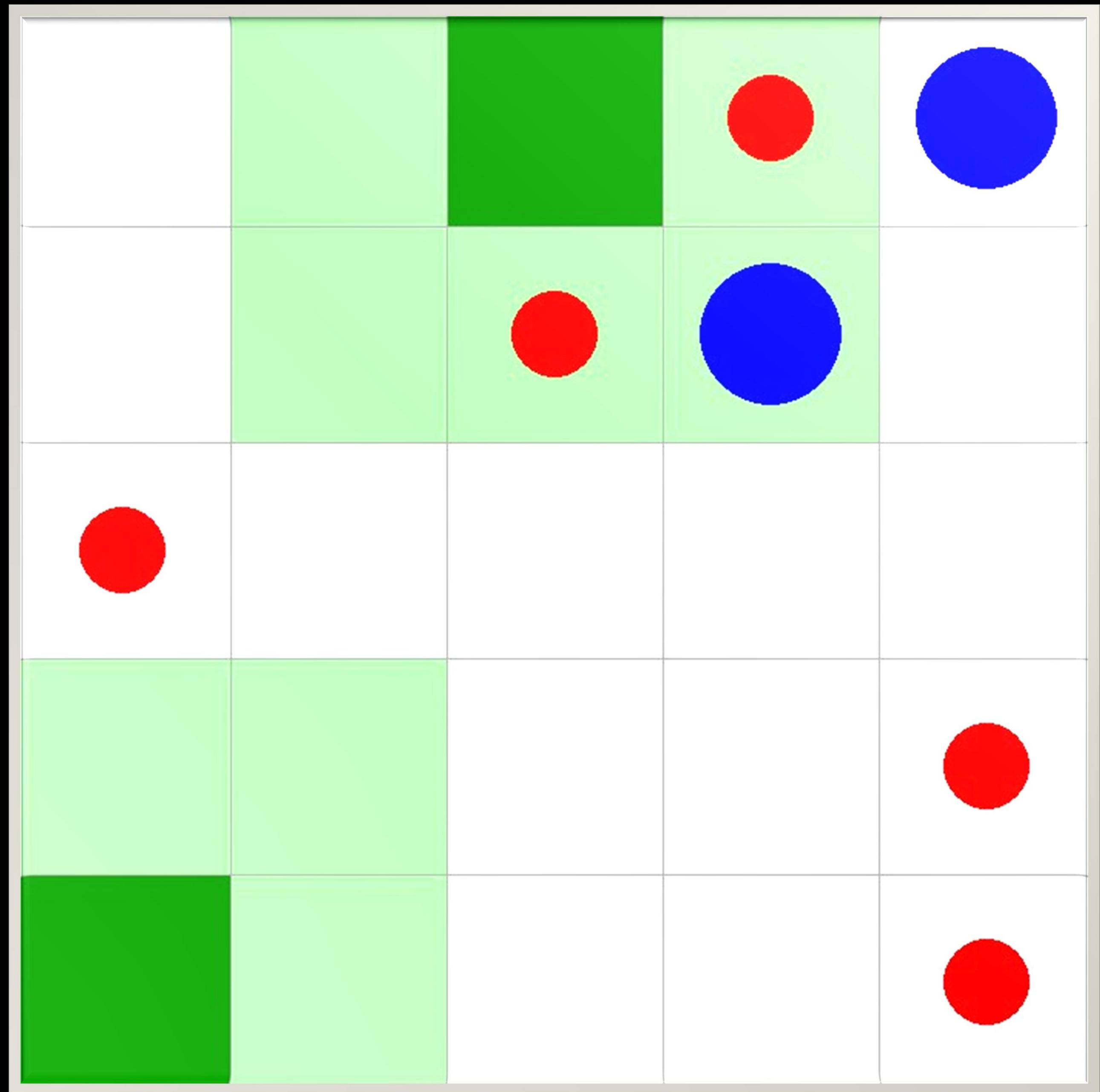


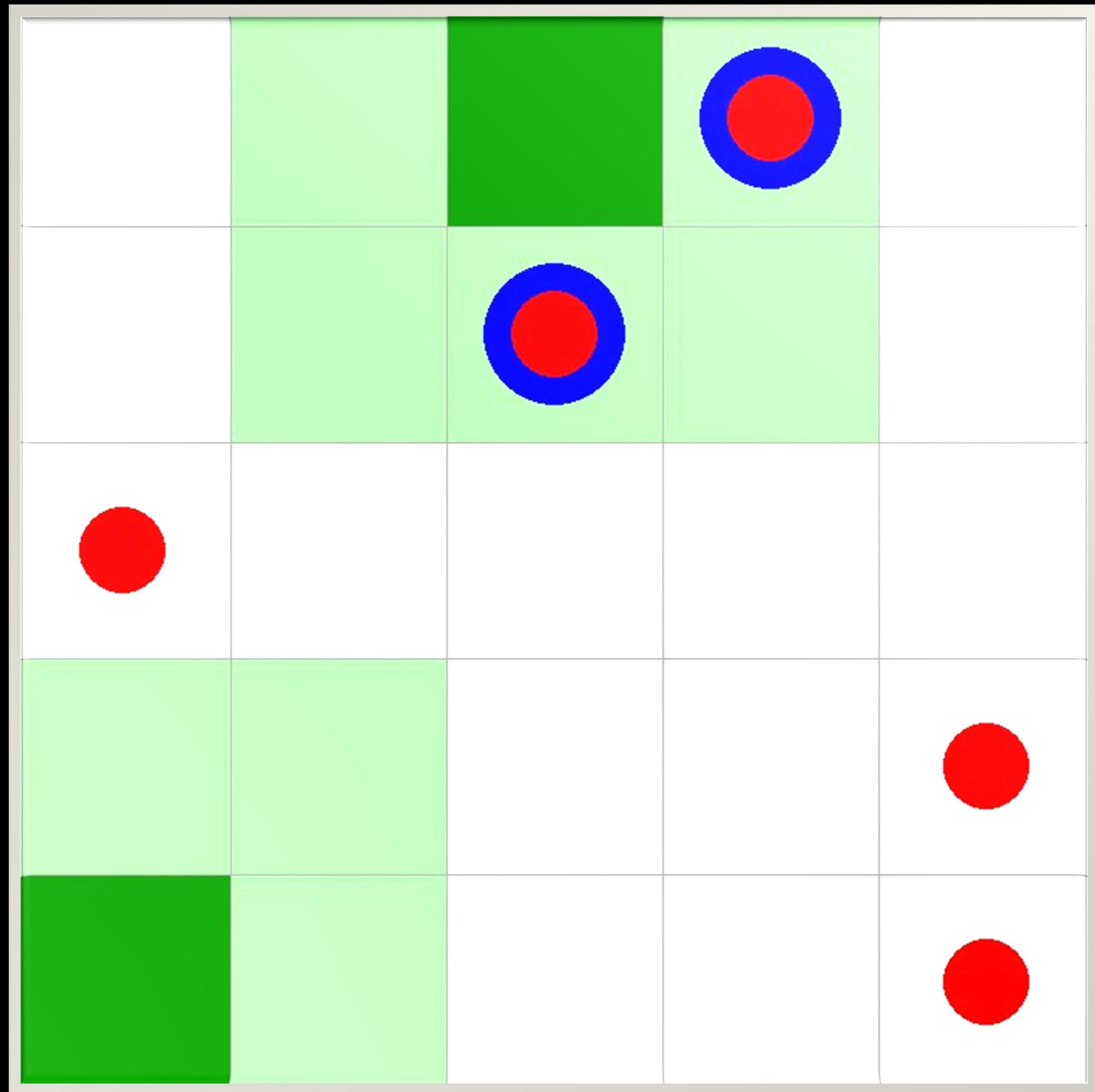


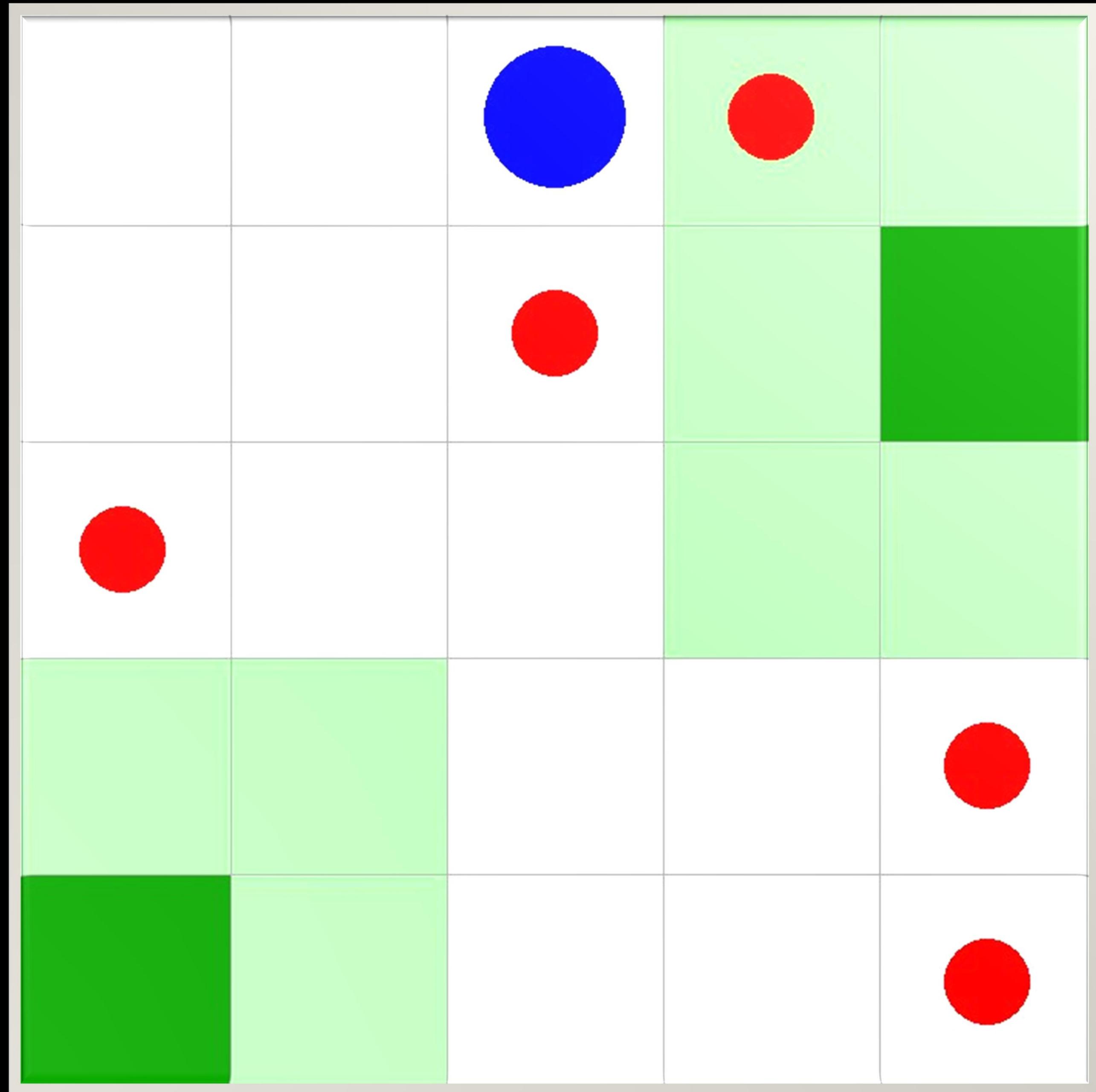


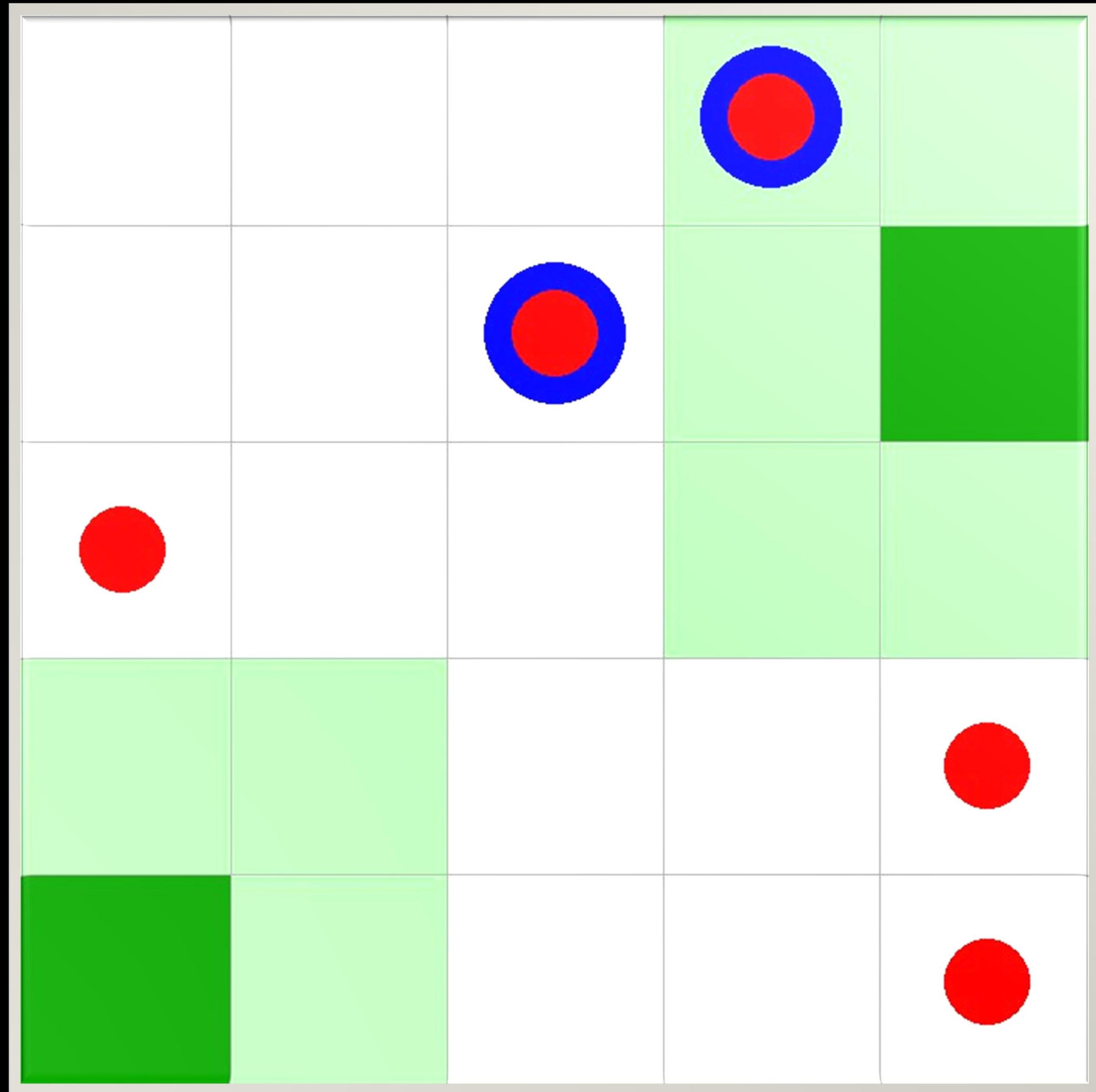


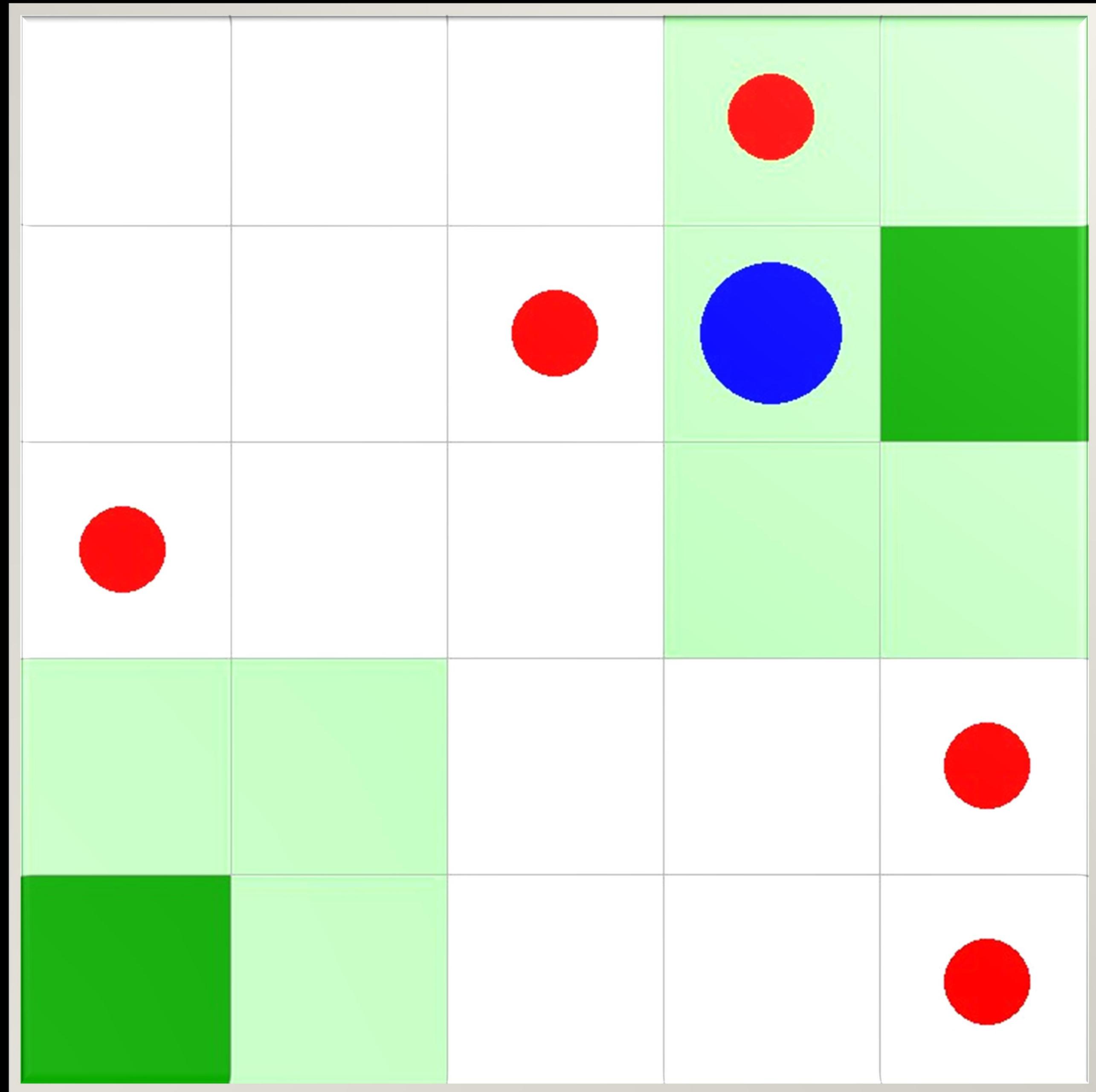


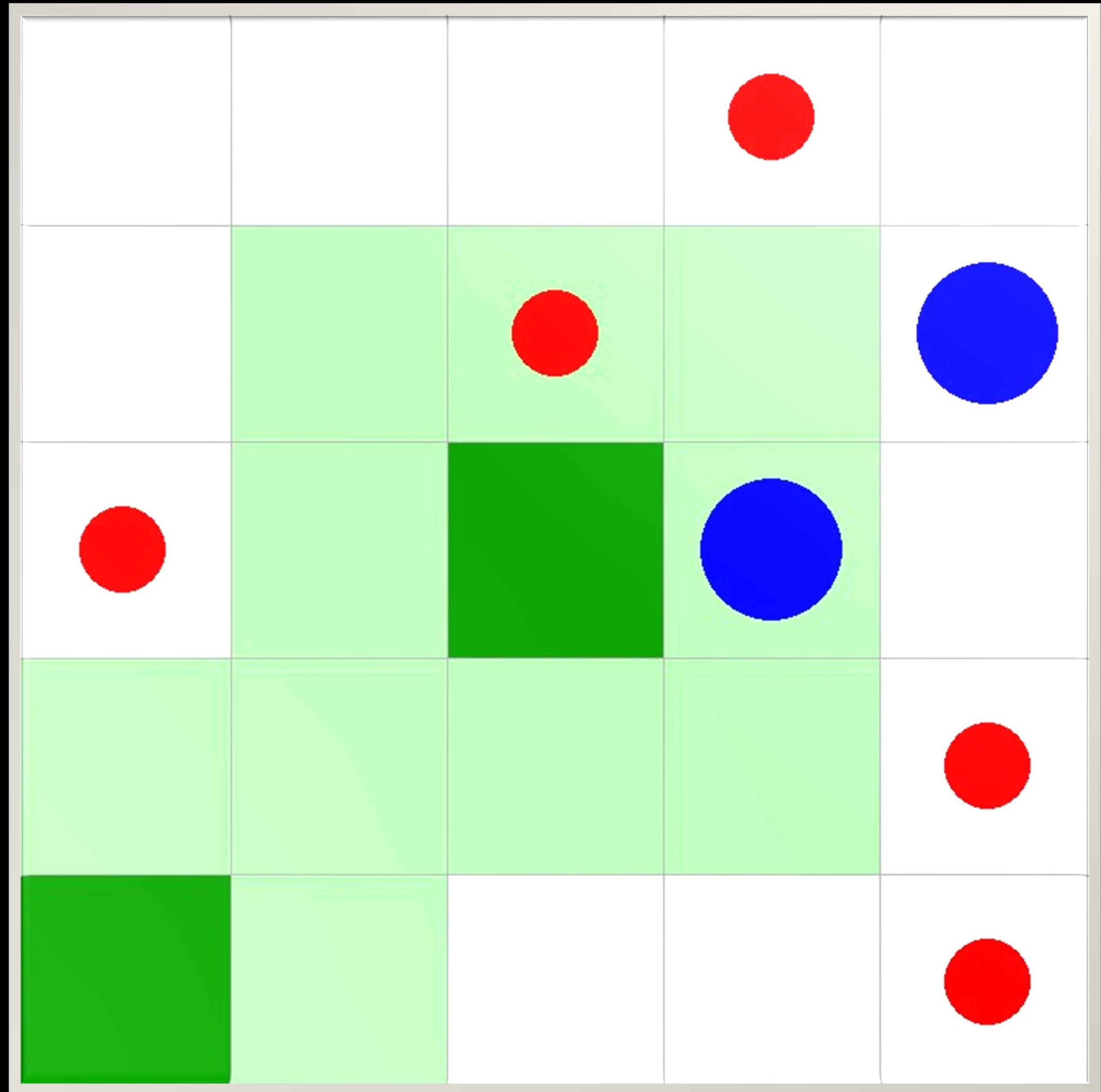






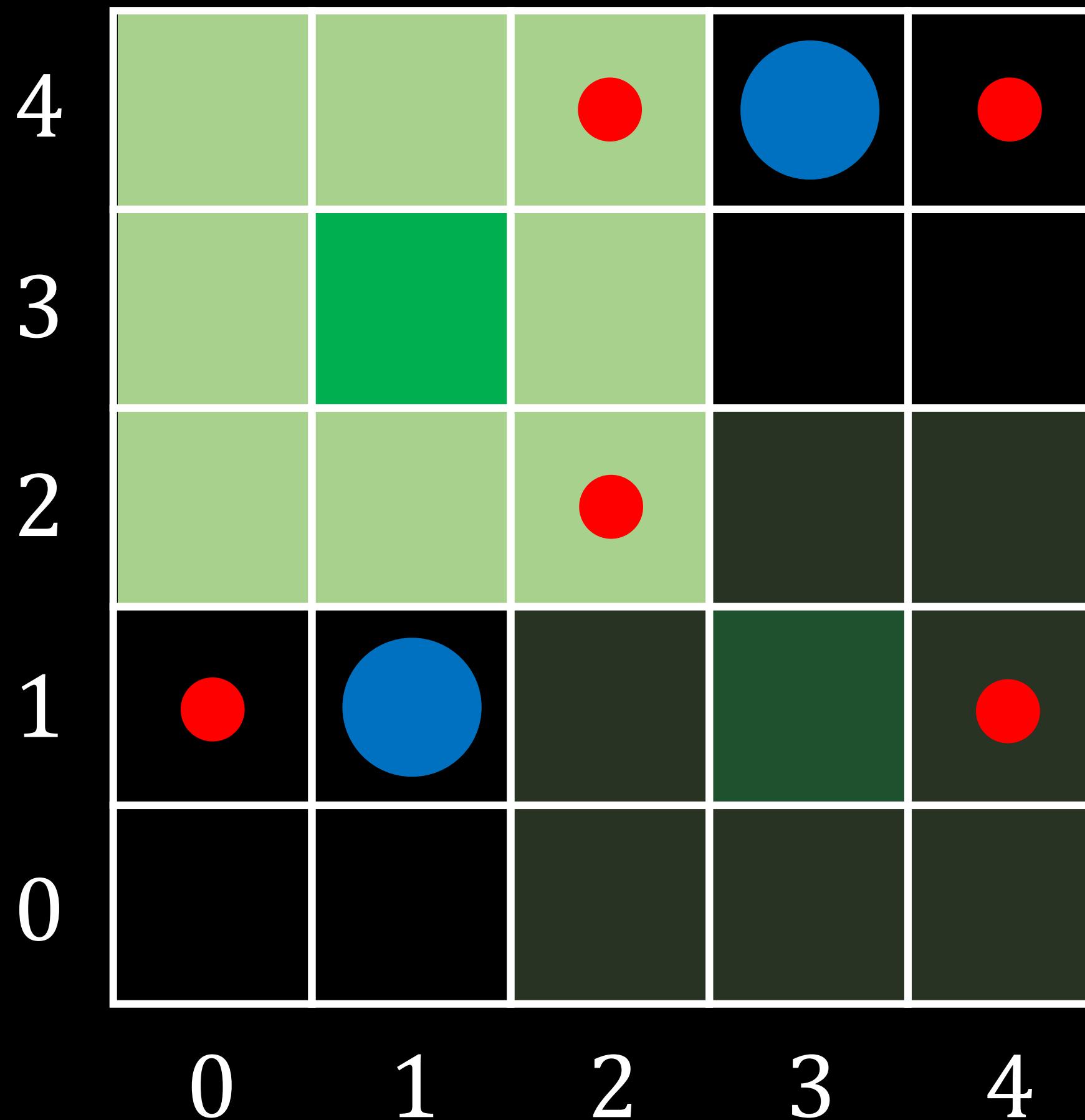






v3.0 & v3.5

$g = 5$   
 $I = 1$   
 $p = 1$

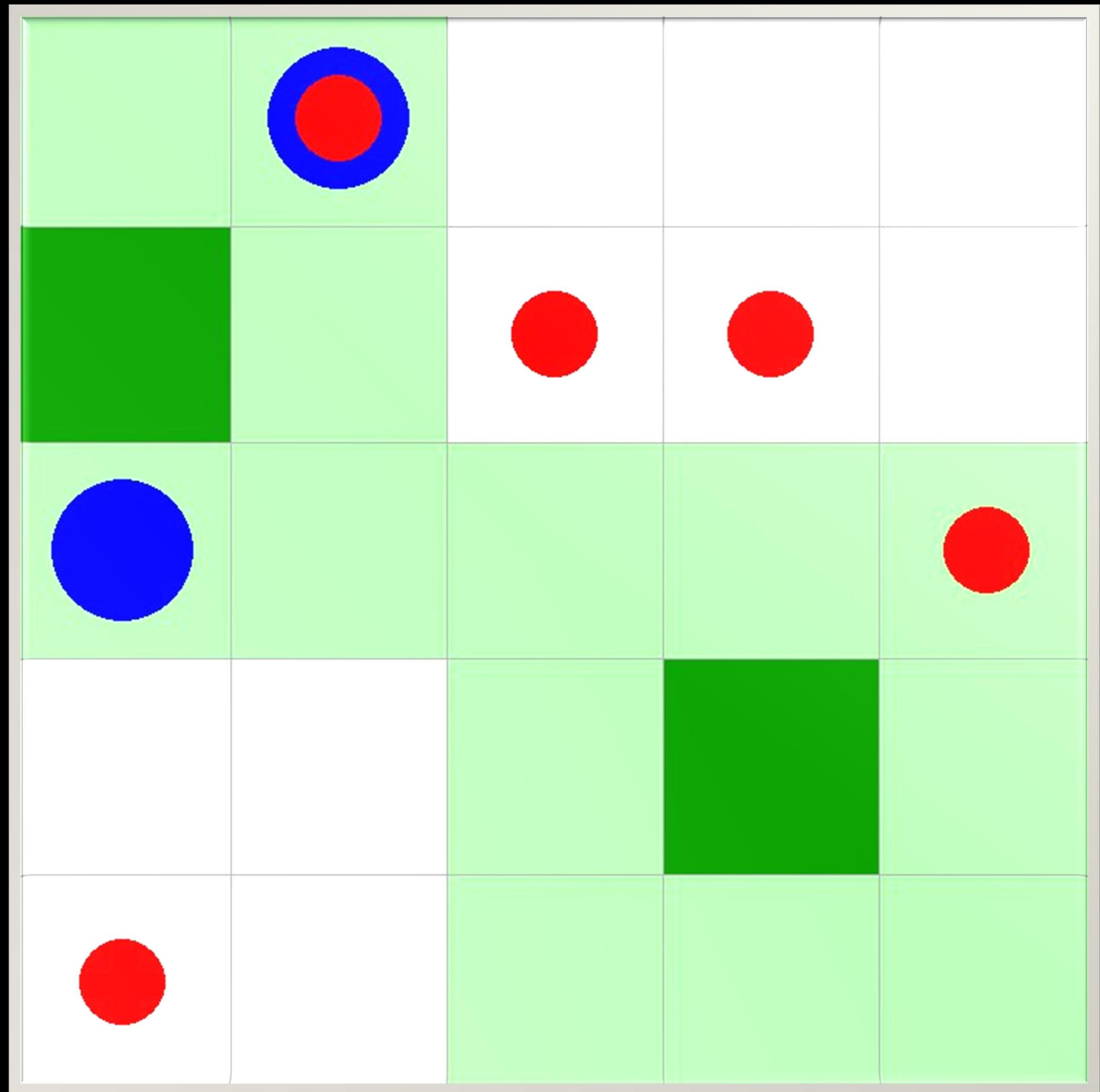


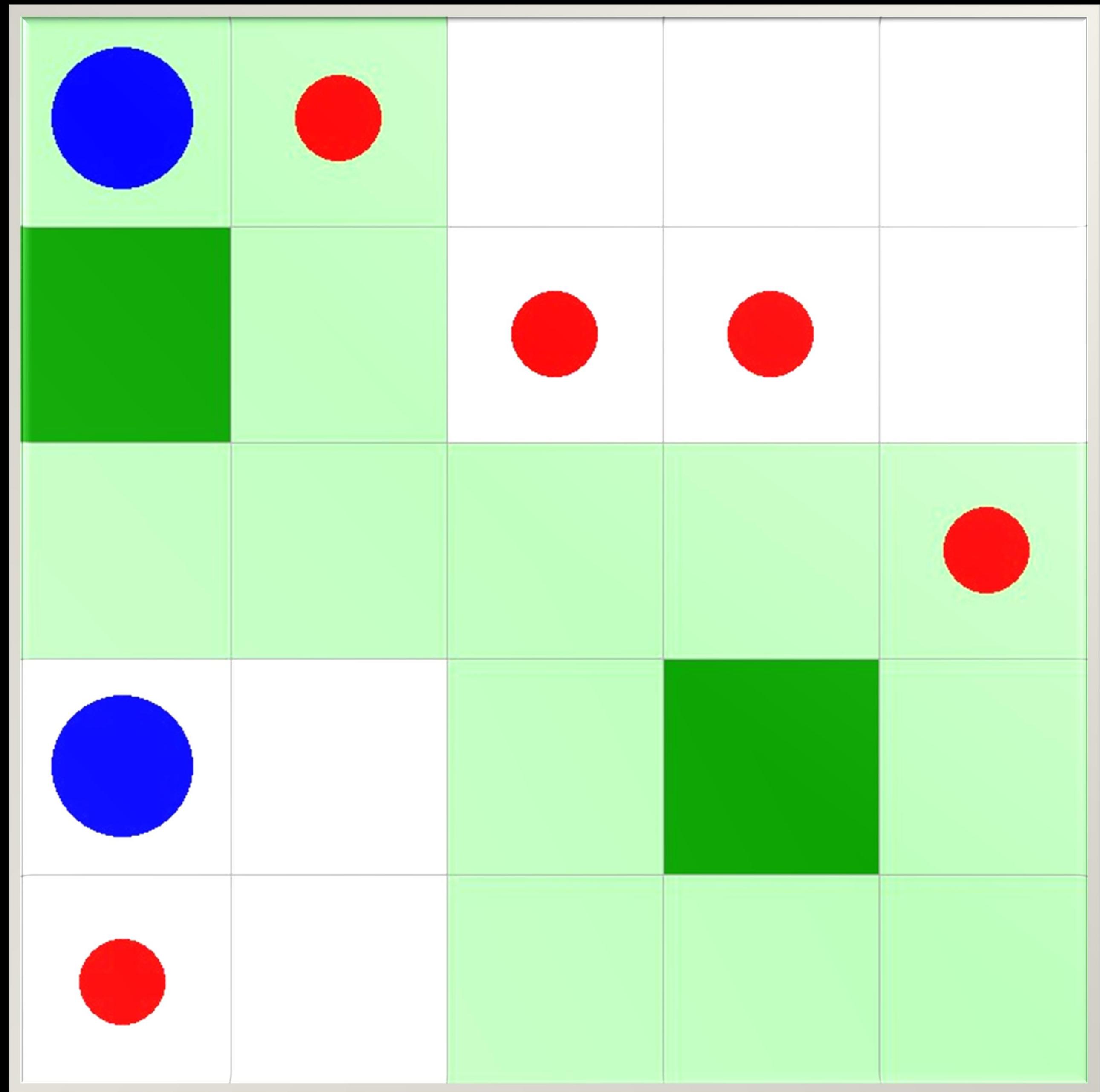
v3.0  
[ 1, 3, 2, -1, -1, 0, 1, 1, 3, 4 ]

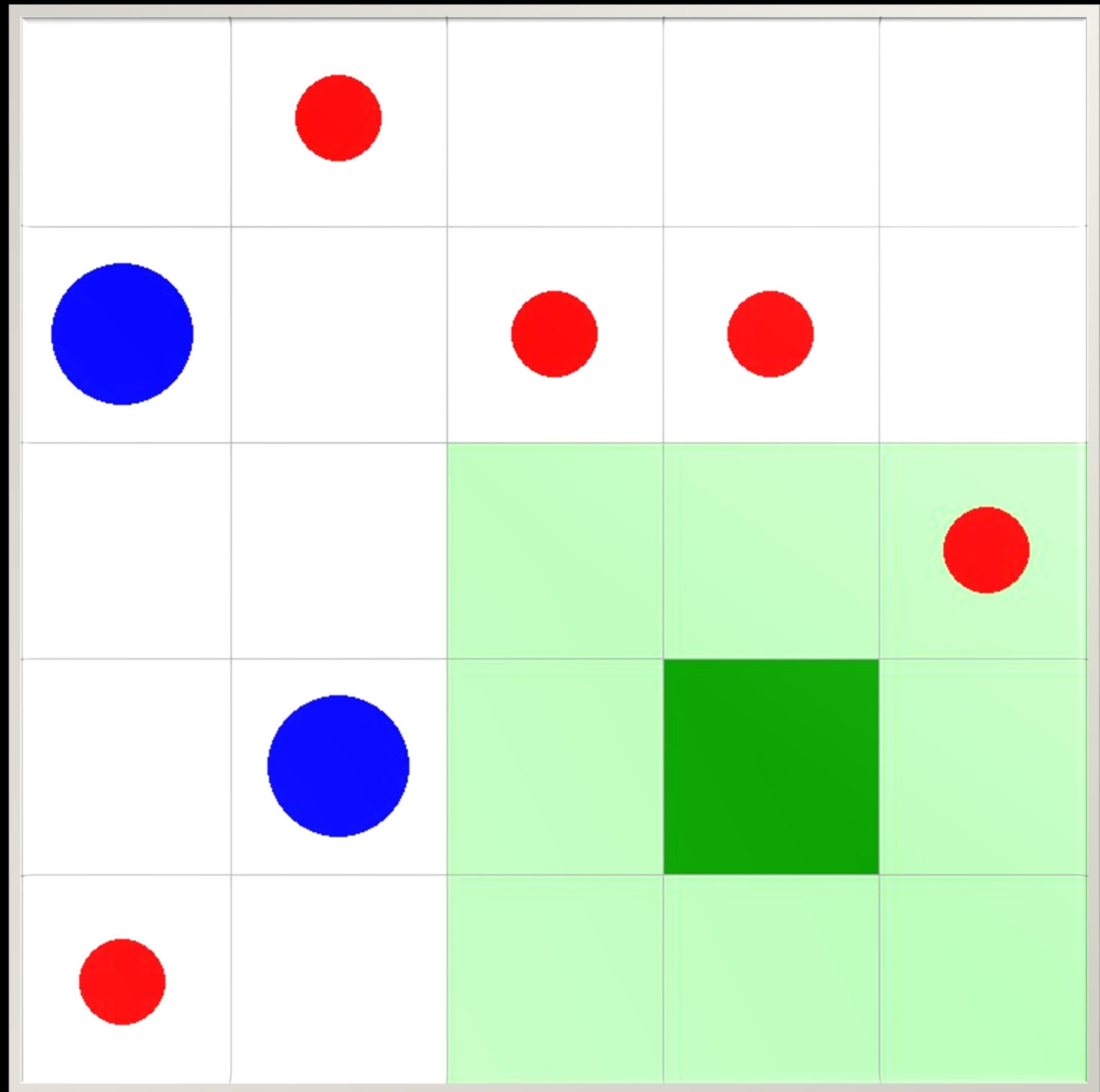
Normalize!

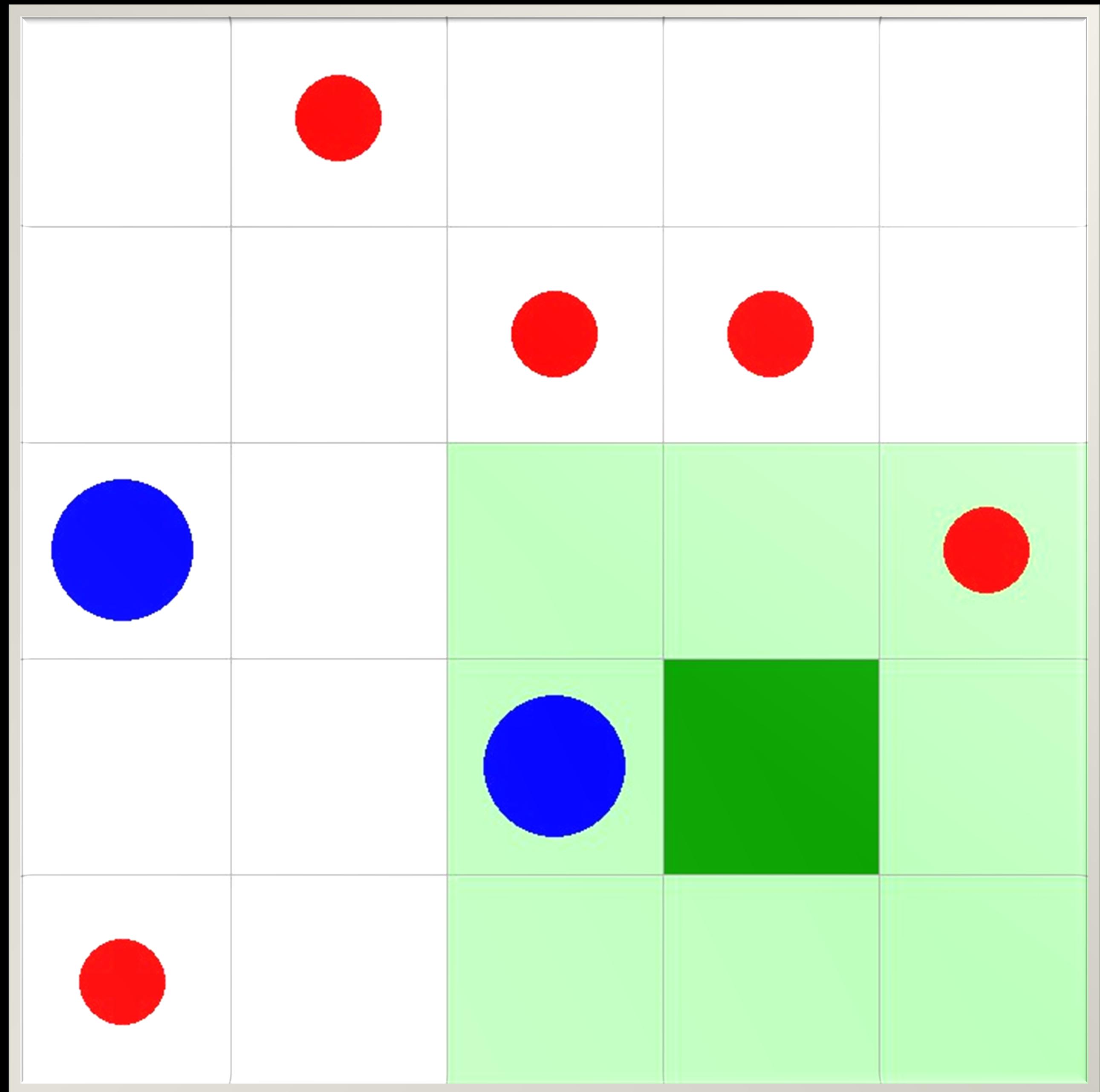
v3.5  
[ 1, 3, 0, 2, 3, 1, 1, 0, 1, 1, 3, 4 ]

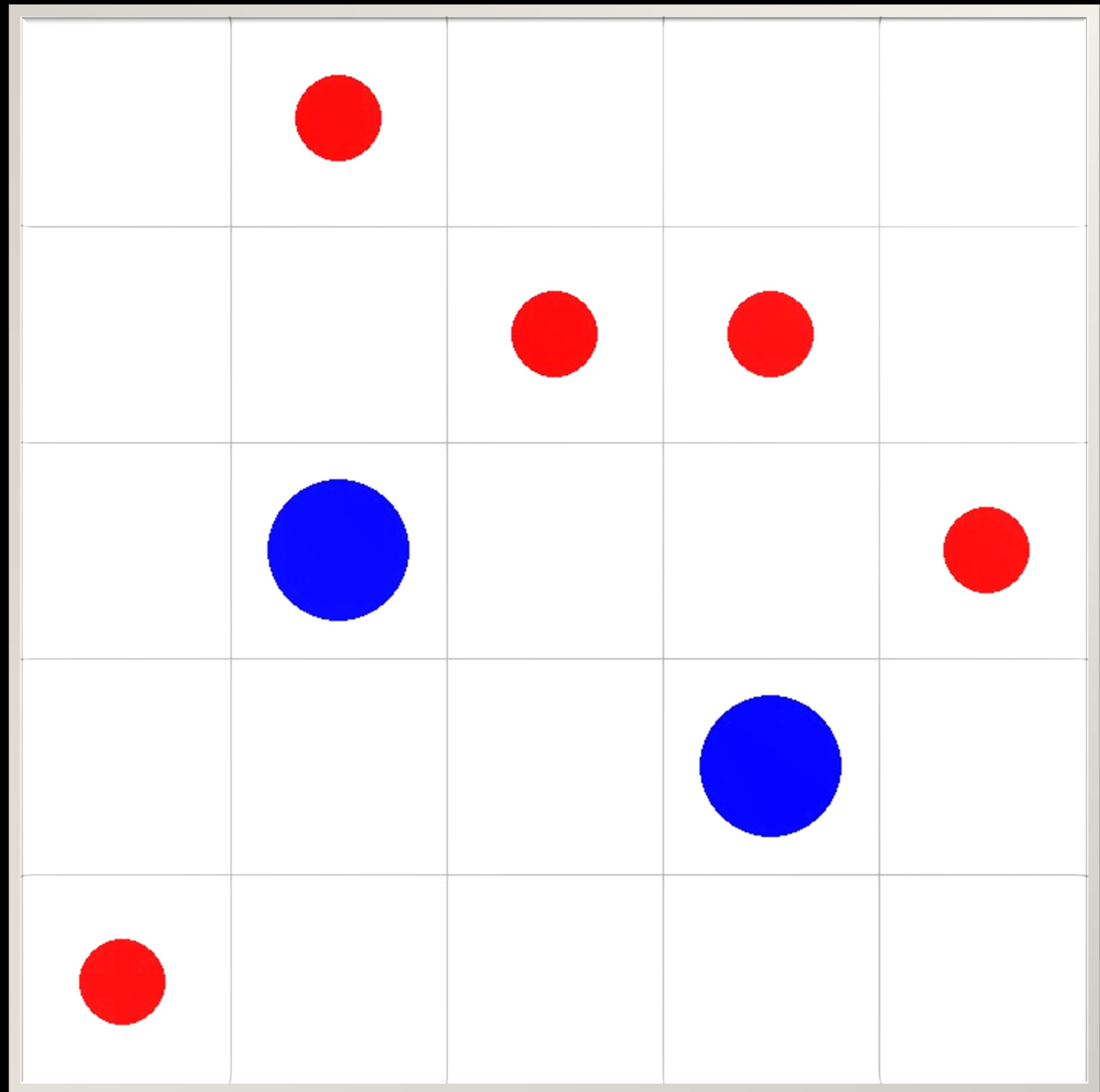
Normalize!

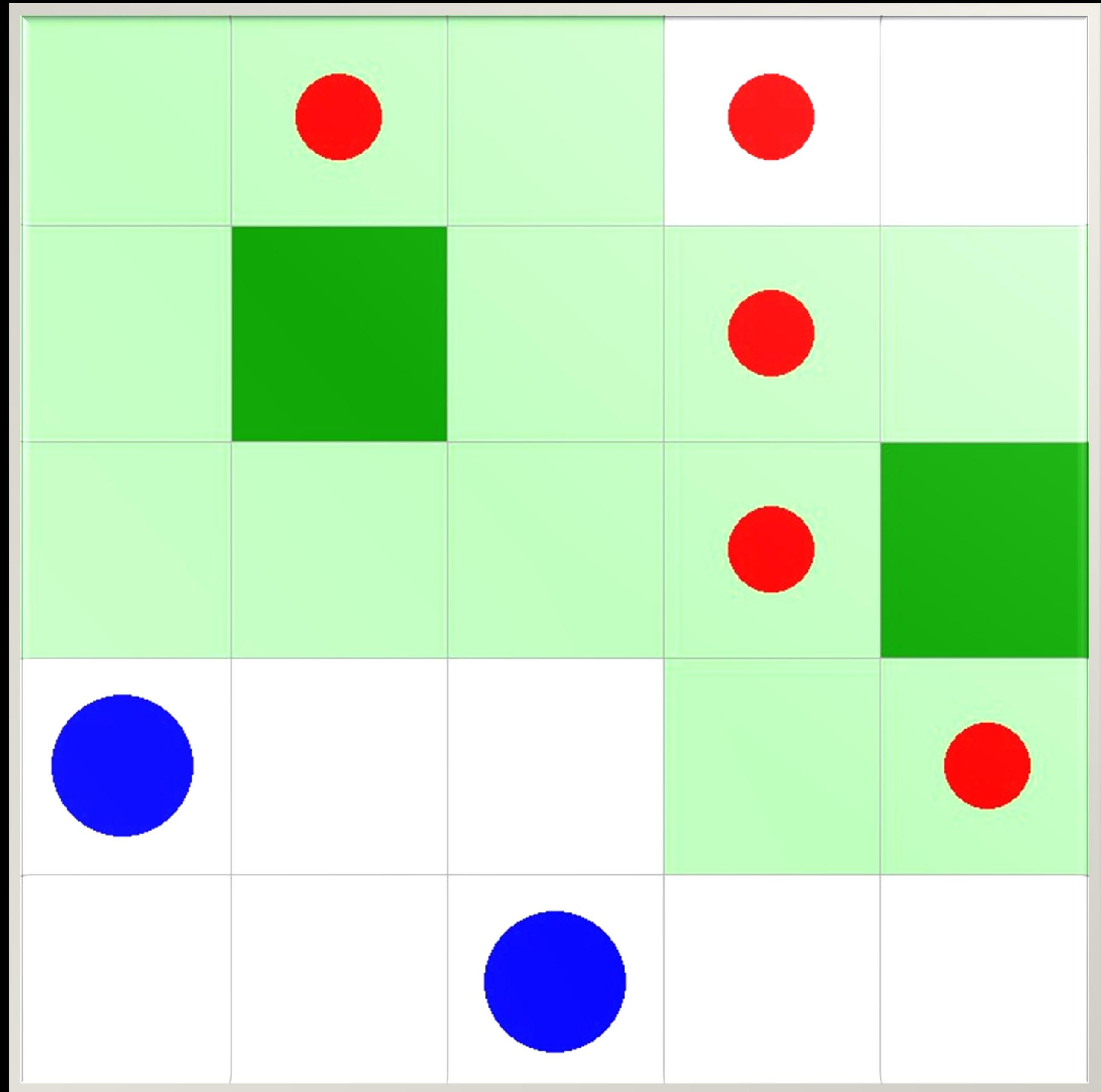


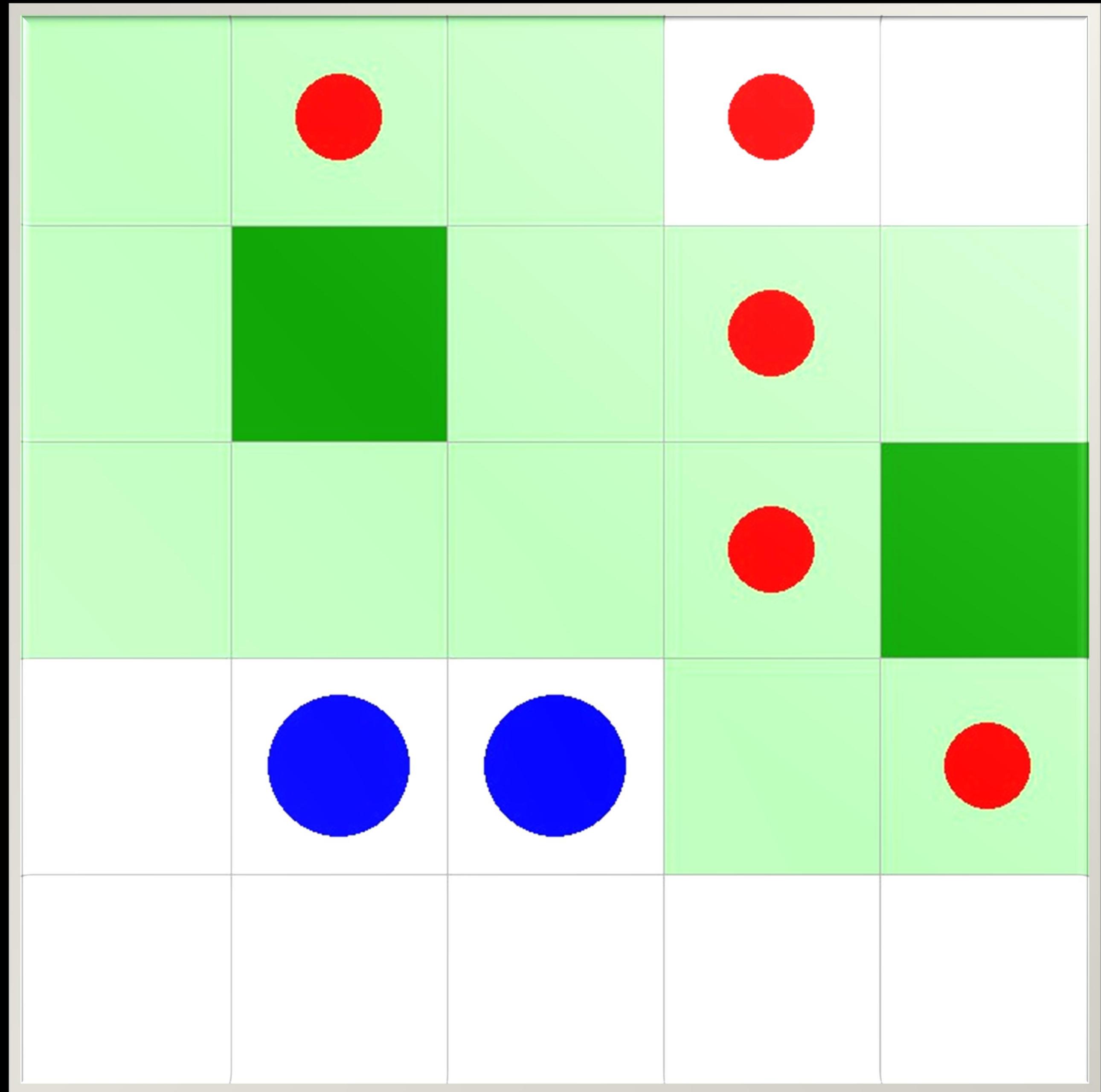


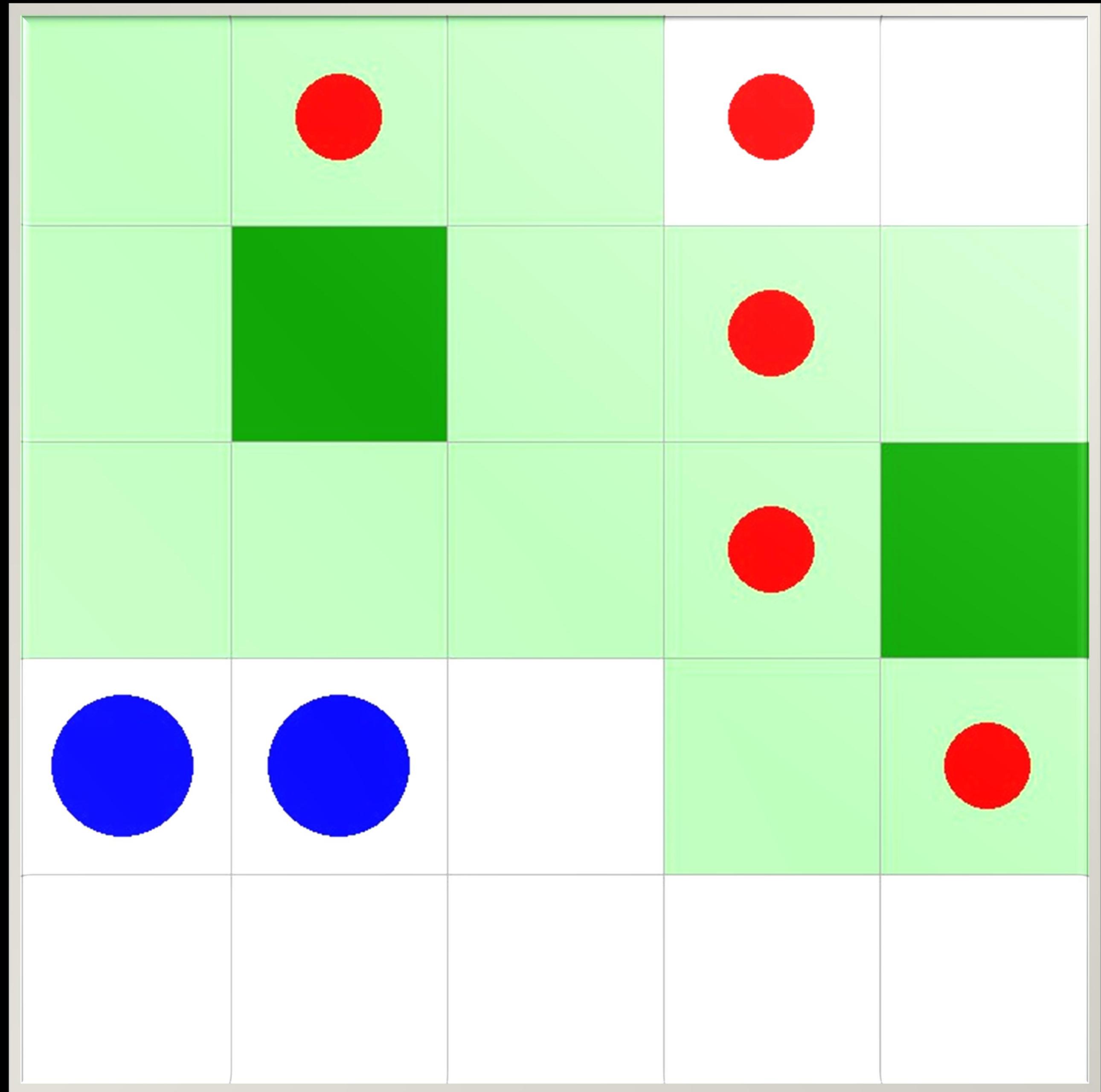


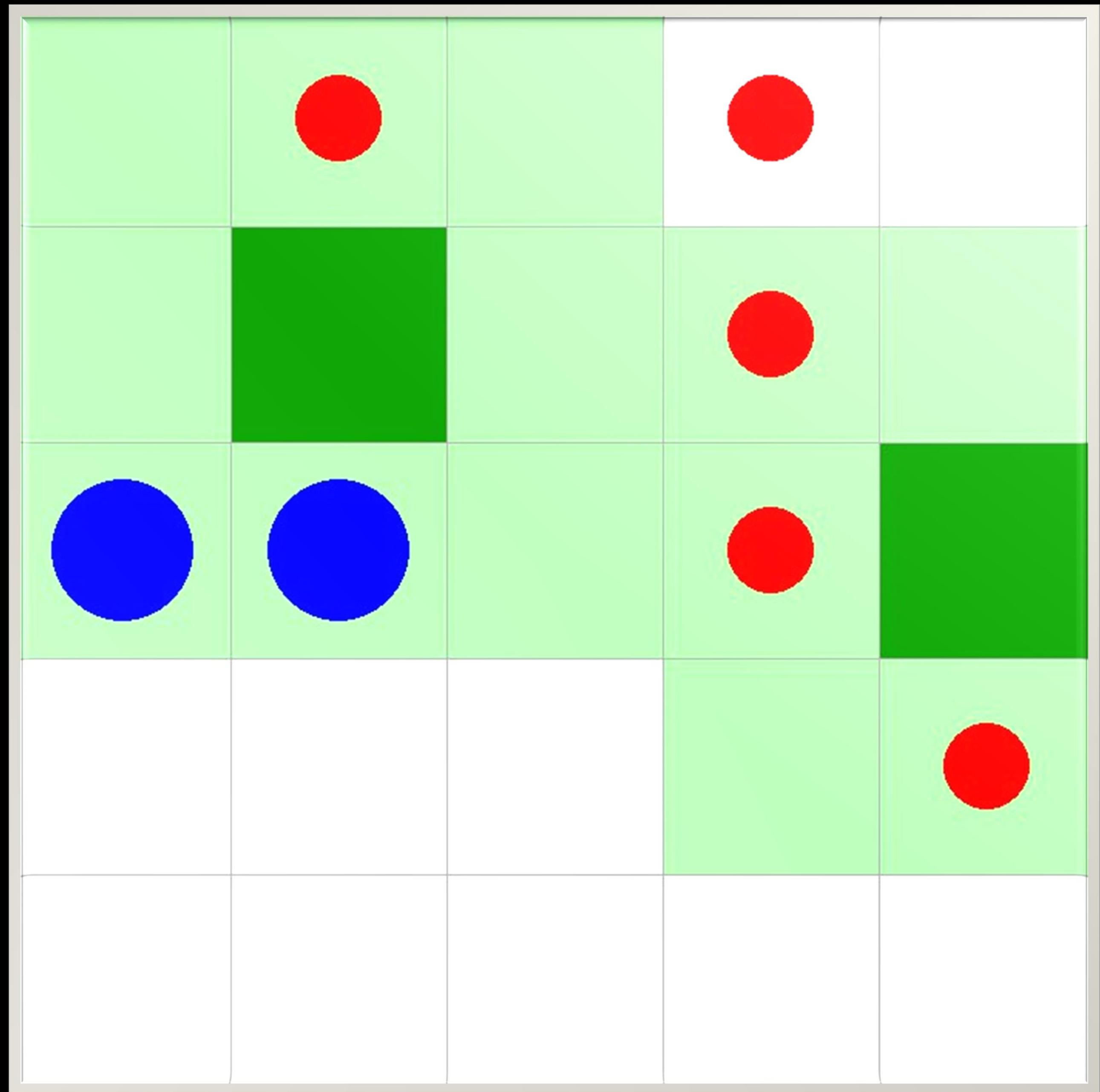


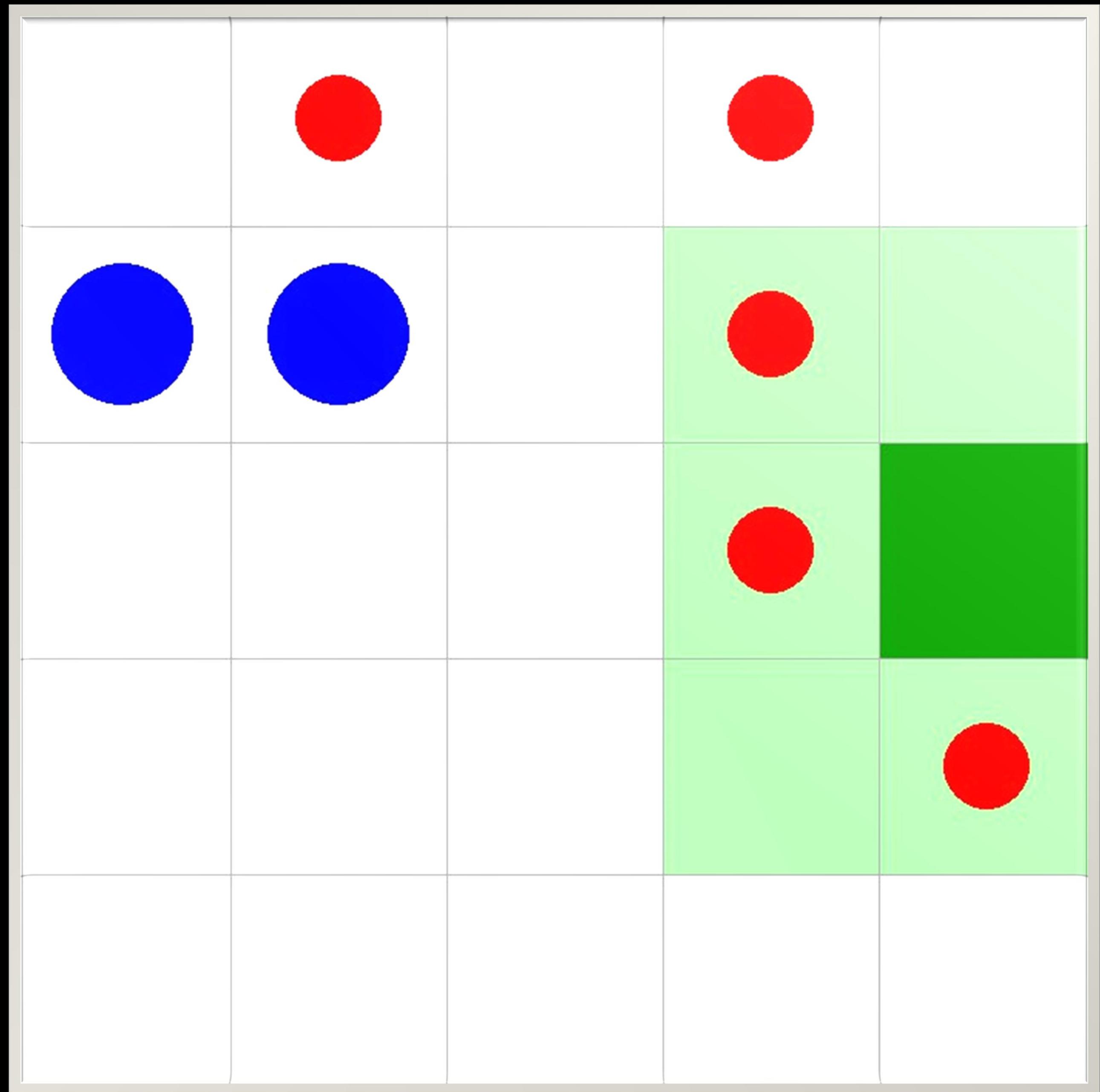


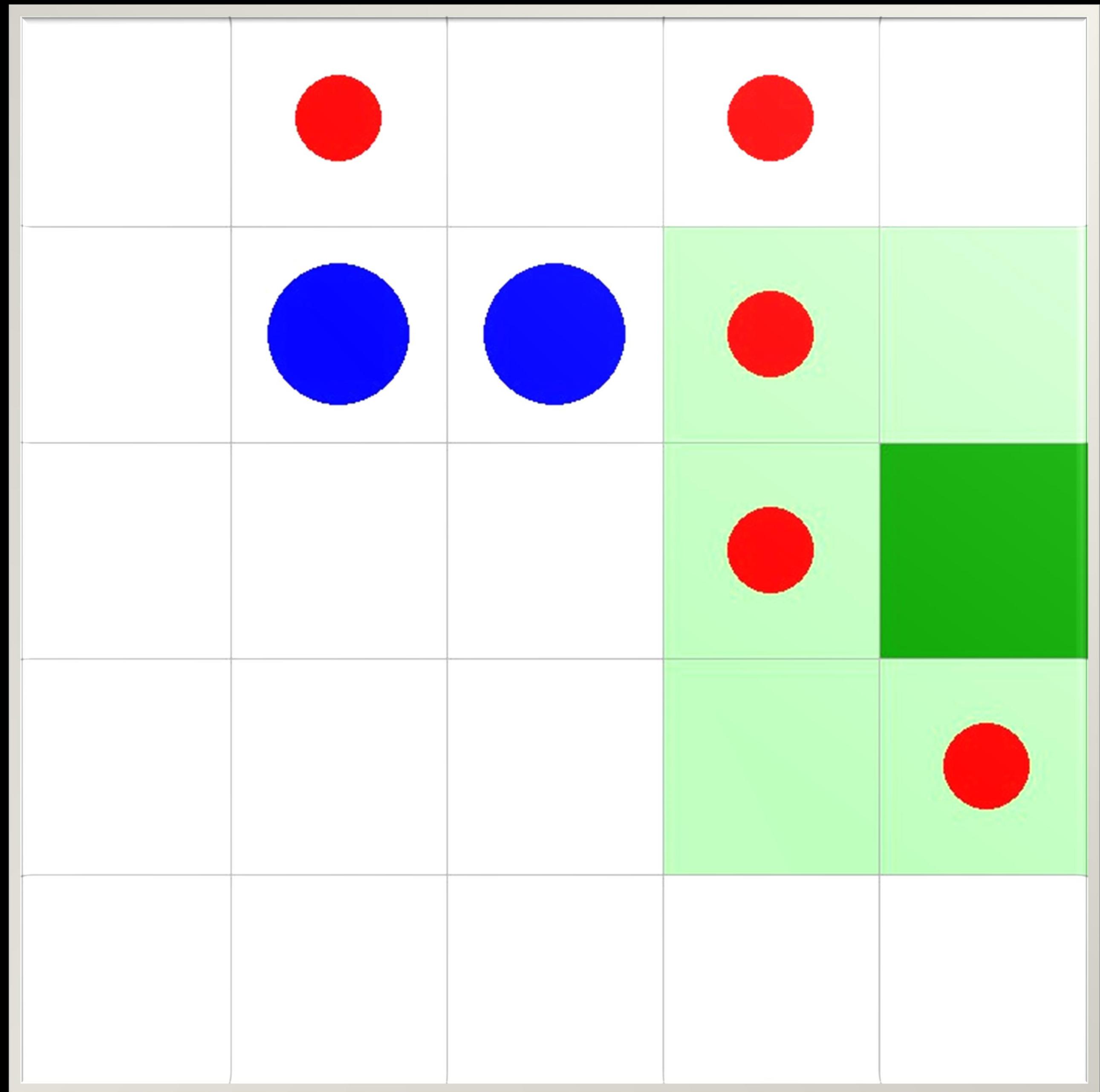


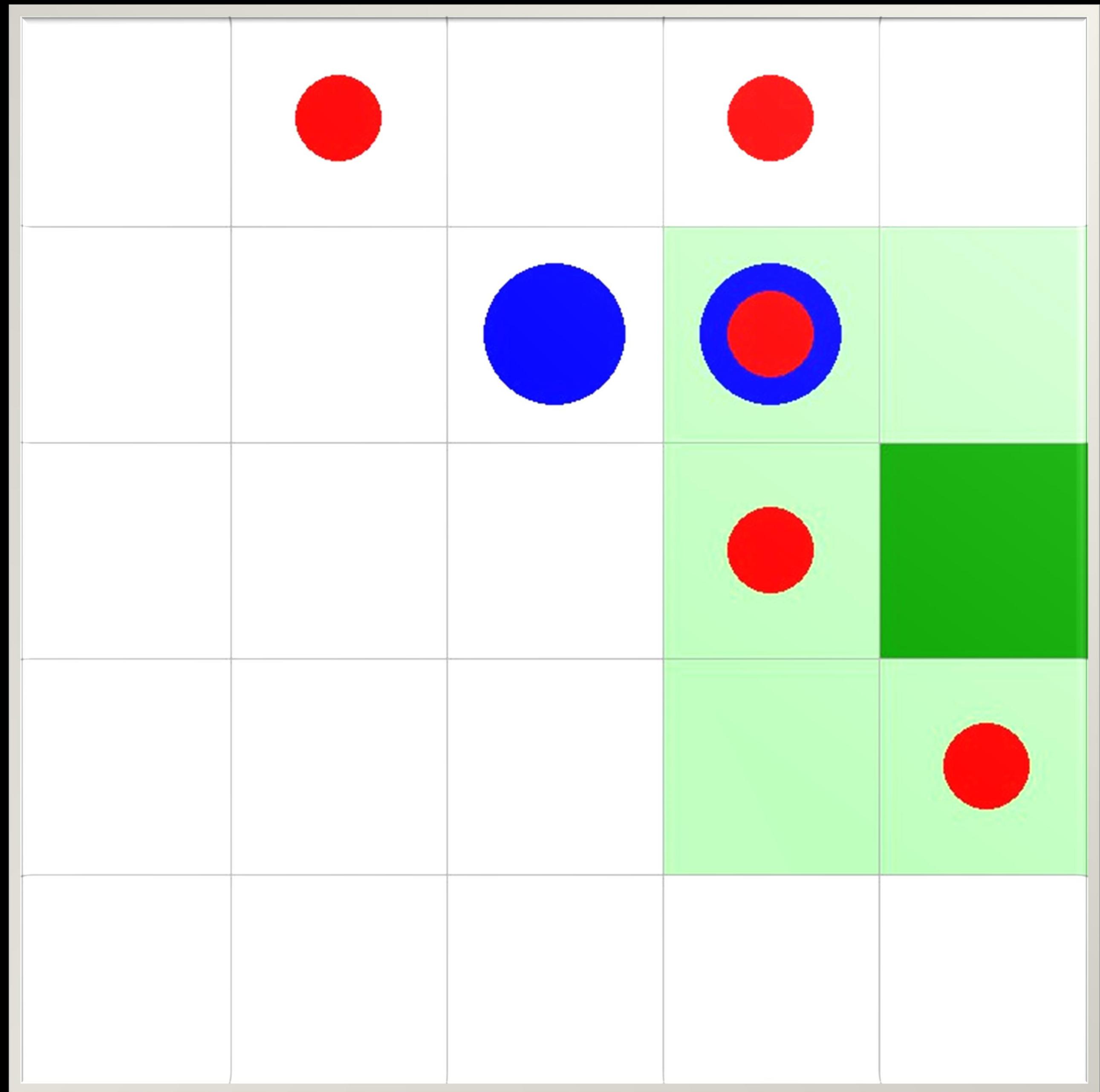


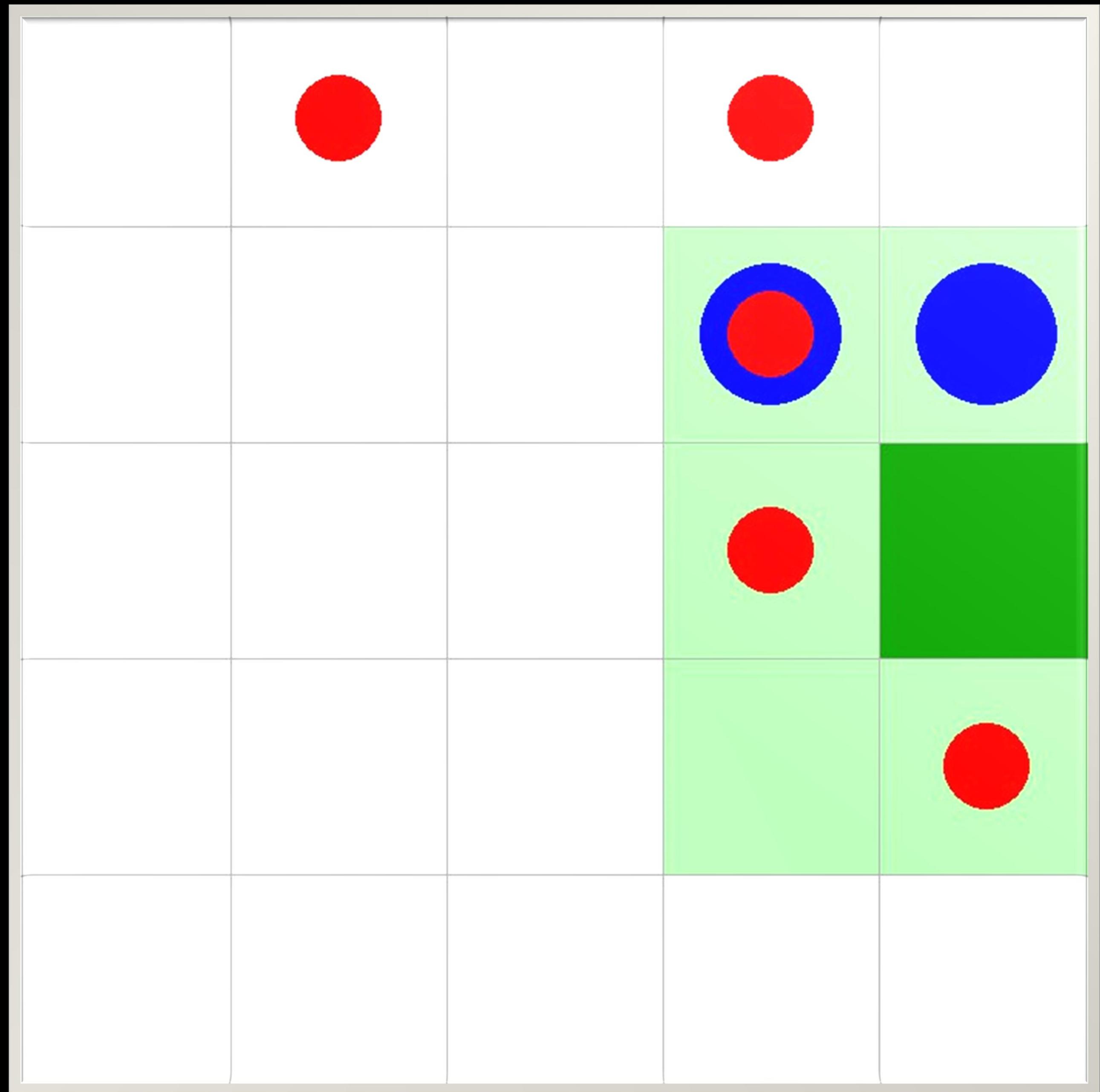


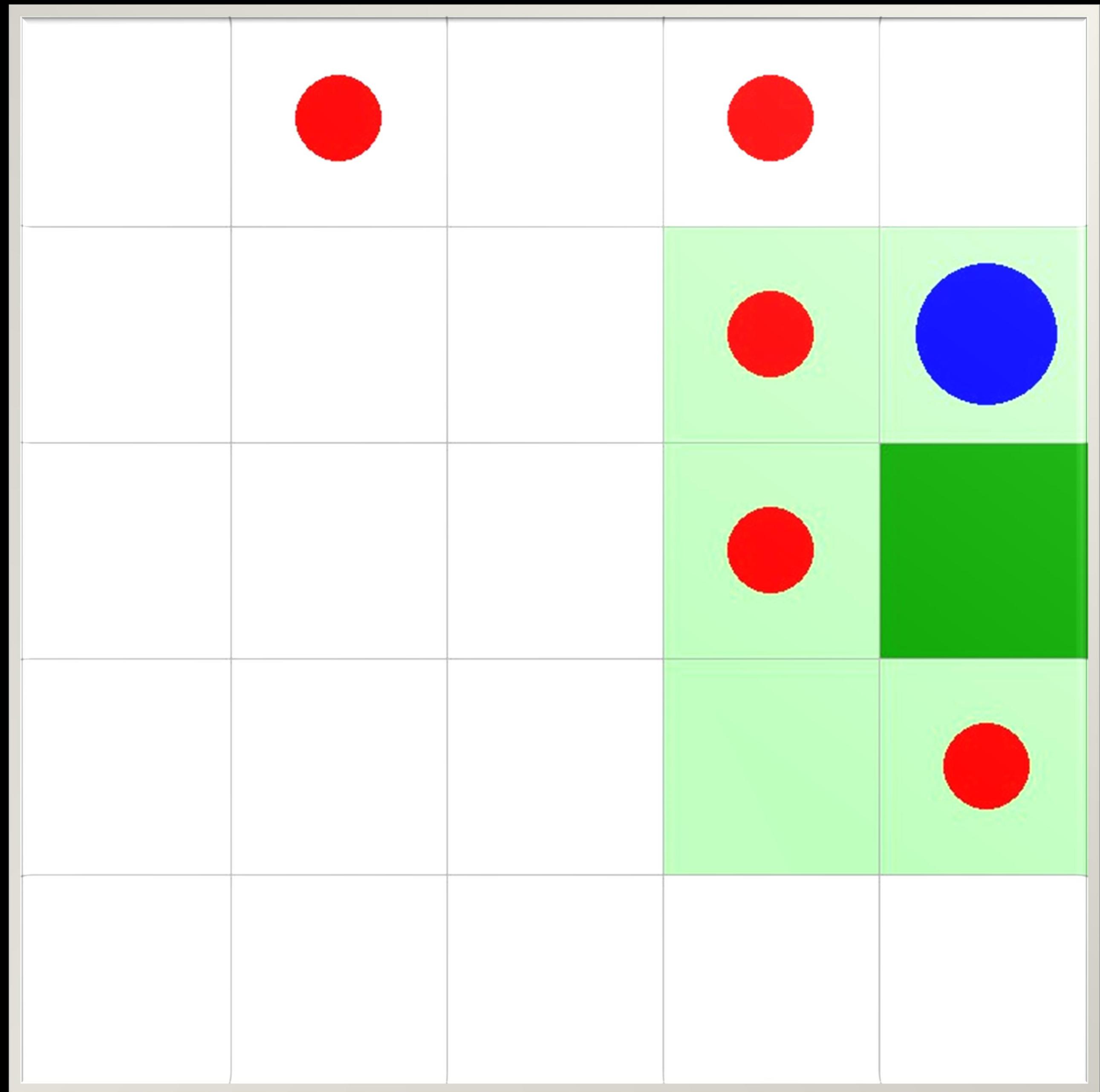


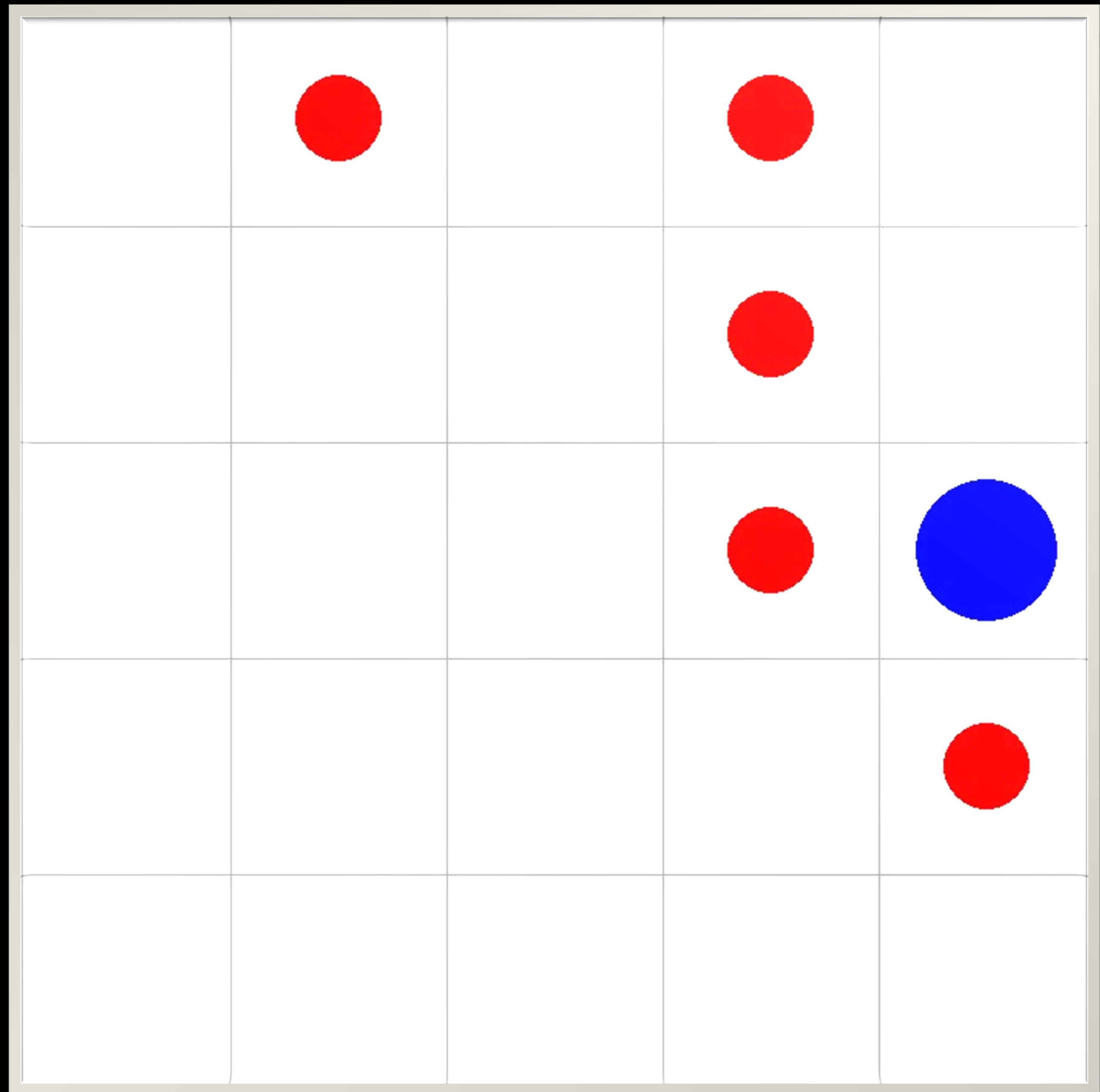












# In a nutshell

- Resource extraction game
- MARL to SARL
- DQNs
- Normalization
- Lazy agents
- Exploits
- Beyond 5-by-5 grids?
- Distributed learning & execution

Questions?