

Homework #5

Math 201-003

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Due: August 7, 2023 (in class)

1. If a matrix A is  $5 \times 3$  and the product AB is  $5 \times 7$ , What is the size of B?
2. How many rows does B have if BC is a  $3 \times 4$  matrix?
3. Let  $A = \begin{bmatrix} 2 & 5 \\ -3 & 1 \end{bmatrix}$  and  $B = \begin{bmatrix} 4 & -5 \\ 3 & k \end{bmatrix}$ . What the value of K that will make  $AB = BA$ .

4. Find  $x_1, x_2, x_3, x_4$  in the following product:  $\begin{bmatrix} 1 & -2 \\ -2 & 5 \end{bmatrix} \begin{bmatrix} x_1 & x_2 & * \\ x_3 & x_4 & * \end{bmatrix} = \begin{bmatrix} -1 & 2 & -1 \\ 6 & -9 & 3 \end{bmatrix}$ .

(Hint: First, compute the first two columns of the left-hand side matrix product. Next, compare the resulting matrix with the one on the right-hand side. By doing this, you will have a system of four equations with four unknowns  $x_1, x_2, x_3, x_4$ . Solve this system to determine the values of  $x_1, x_2, x_3, x_4$ .)

5. Find the inverse of the matrix  $\begin{bmatrix} 1 & -2 & 0 \\ 4 & -7 & 3 \\ -2 & 6 & -4 \end{bmatrix}$

6. Find the LU factorization of  $\begin{bmatrix} 2 & -4 & 2 \\ 1 & 5 & -4 \\ -6 & -2 & 4 \end{bmatrix}$