## **Bus-Route Optimization**

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## Why should we care?

- ▶ Transportation accounts for 5% of the GDP of Europe ("Transport Sector Economic Analysis - European Commission")
- Estimated 30 percent of national greenhouse gases are generated by transportation
- People spent significant amounts of time in public transportation. For example in France more than 60 minutes daily. ("Parisians Spend Total of 23 Days a Year on Transport - the Local")

## How can bus-routes be optimized?

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\begin{aligned} & \underset{x}{\text{minimize}} & & f(x) \\ & \text{subject to} & & g_i(x) \leq 0, \quad i = 1, \dots, m \\ & & h_i(x) = 0, \quad i = 1, \dots, p \end{aligned}
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- Mathematical optimization methods can be used for the creation of efficient bus networks
- ▶ Requires formulating the bus routing problem mathematically
- Choose the best numerical method for optimization

### Main Points of the Talk

- 1. How to formulate the bus-routing problem
- 2. How the optimization process works
- 3. The benefits of bus-route optimization

#### **Formulation**

- 1. **Objective**: Minimize the *cost function*, which can include
  - Monetary cost to operate the network
  - ▶ Total travel time
- Constraints: What kinda of features we want to avoid in our network
  - Avoid too long or inconvenient routes
- 3. Real life data to obtain numerical estimates for the parameters
  - Common travel routes
  - Distribution of the population in the city

("Route Optimization Algorithm."), ("Vehicle Routing Problem - Wikipedia"),

## Example Network

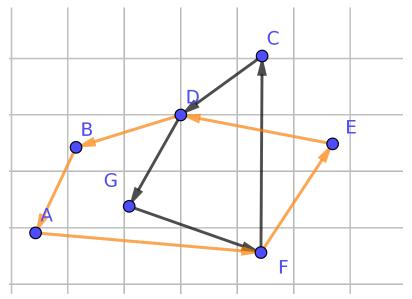


Figure 1: Letters are bus stops and connected arrows are bus-routes

#### Methods

# **Genetic optimization algorithm** ("Genetic Algorithm - Wikipedia")

- 1. Initializing a *population* which is set of possible *routing* candidates (individual bus network)
- 2. Computing the *fitness* of each of the individual routings in the population which measure how good each routing is
- 3. Selecting a percentage of the best performing individuals and using them to *reproduce* new individuals
- 4. We also apply a random mutation on randomly selected individuals to avoid getting stuck in the local optimum
- 5. Use process recursively

Existing solvers, such as Gurobi, can be to perform the optimization. ("Gurobi Optimization - the State-of-the-Art Mathematical Programming Solver")

#### **Benefits**

- ► Savings in transportation time
- ▶ Economical impact, saving money
- ▶ Positive environmental impact, less greenhouse gases

#### Conclusion

- We learned
  - What bus-routing probelm consists of
  - ▶ How it is solved
  - About the positive effects of good bus-routing
- ▶ Proper bus-routing is important for functioning public transportation
- Well designed bus network can impact your daily life by saving time!

#### References

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"Genetic Algorithm - Wikipedia."
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