

$$\begin{aligned} 1.) E[(x - E[x])^2] &= \int (x - E[x])^2 \rho(x) dx \\ &= \int (x^2 - 2x E[x] + (E[x])^2) \rho(x) dx \\ &= \int x^2 \rho(x) dx + \int (-2x E[x] + (E[x])^2) \rho(x) dx \\ &= E[x^2] + \int E[x](-2x + E[x]) \rho(x) dx \\ &= E[x^2] + E[x](-2E[x] + E[x]) \\ &= E[x^2] - (E[x])^2 \end{aligned}$$