

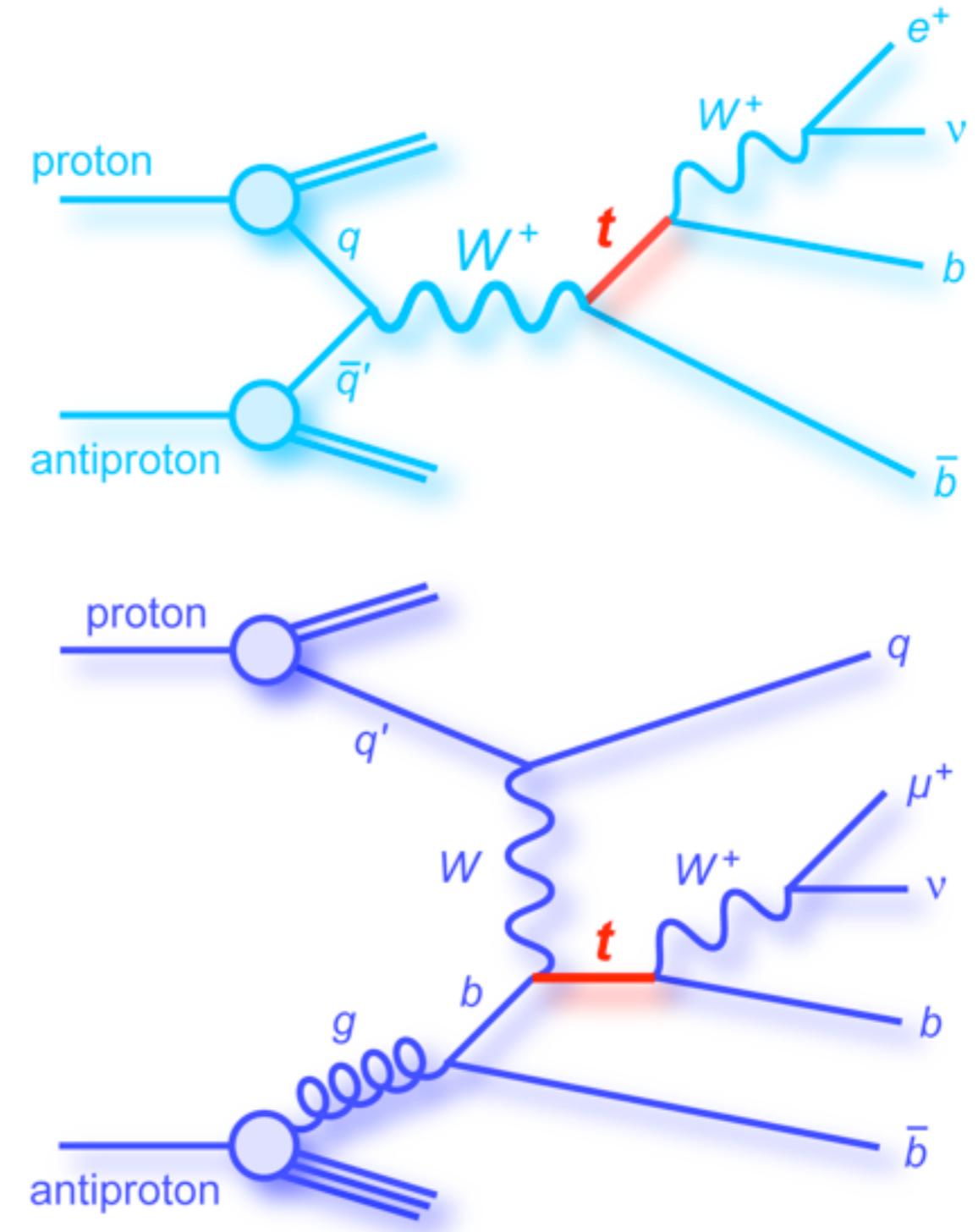
# **Uncovering The Single Top: Observation of the Electroweak Top Quark Production**

**Jorge Armando Benitez  
Ph.D. Dissertation Defense  
Michigan State University**

**August 21st, 2009**

# Outline

- Theoretical motivation
- Single Top quark production
- Experimental Facilities
- Signal and Background
- Boosted Decision Trees
- Analysis
- Conclusions

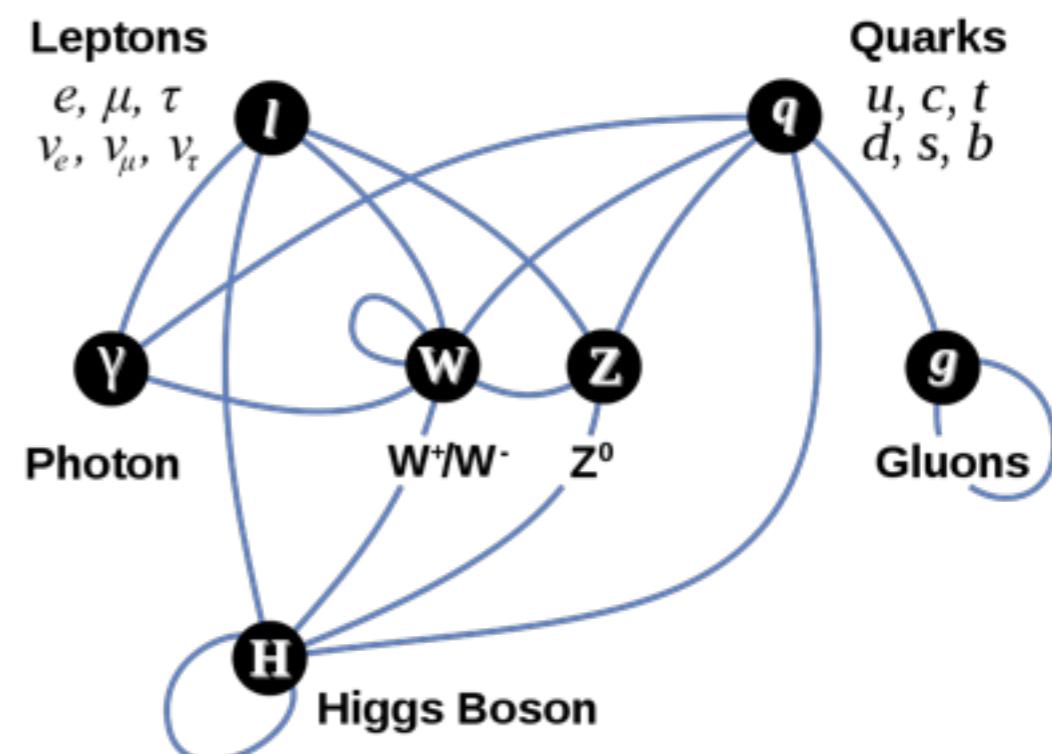


# Standard Model (SM)

- The SM describes the world around us
- Components:
  - 24 particles of matter
  - 4 mediators
- Interactions of the particles explained by the mediators
- Does not include: gravity, dark matter and dark energy

	I	II	III	
Quarks	$u$	$c$	$t$	$\gamma$
	$d$	$s$	$b$	$g$
Leptons	$\nu_e$	$\nu_\mu$	$\nu_\tau$	$Z$
	$e$	$\mu$	$\tau$	$W$

Three Generations of Matter



# Top Quark

- Heaviest SM particle, mass close a gold's atom

$$m_t = 173.1 \pm 1.3 \text{ GeV}/c^2$$

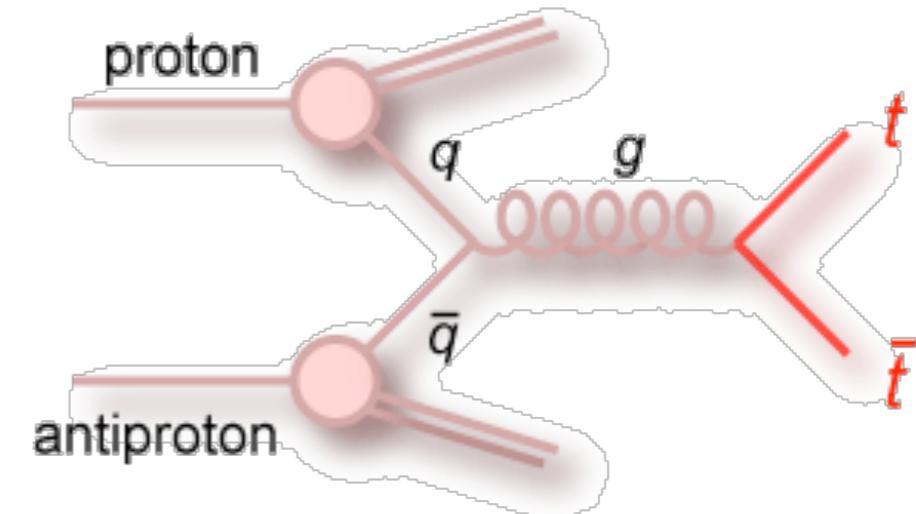
- Discovered in 1995 at Fermilab

- Spin: 1/2, Charge: + 2/3

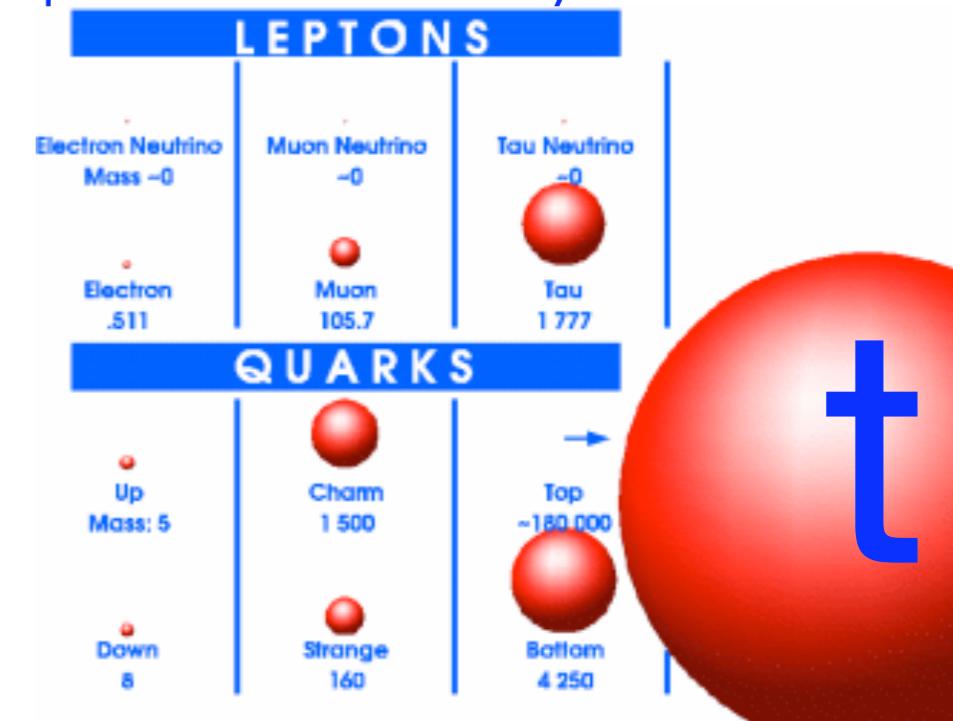
- Mostly produced in quark-antiquark pairs

$$\sigma_{t\bar{t}}(\text{Tevatron}) = 7.62 \pm 0.85 \text{ pb}$$

- Short lifetime  $\sim 10^{-25} \text{ s}$ , it decays before having a chance to hadronize, unique opportunity to study a bare quark



Comparison of the Elementary Particle masses

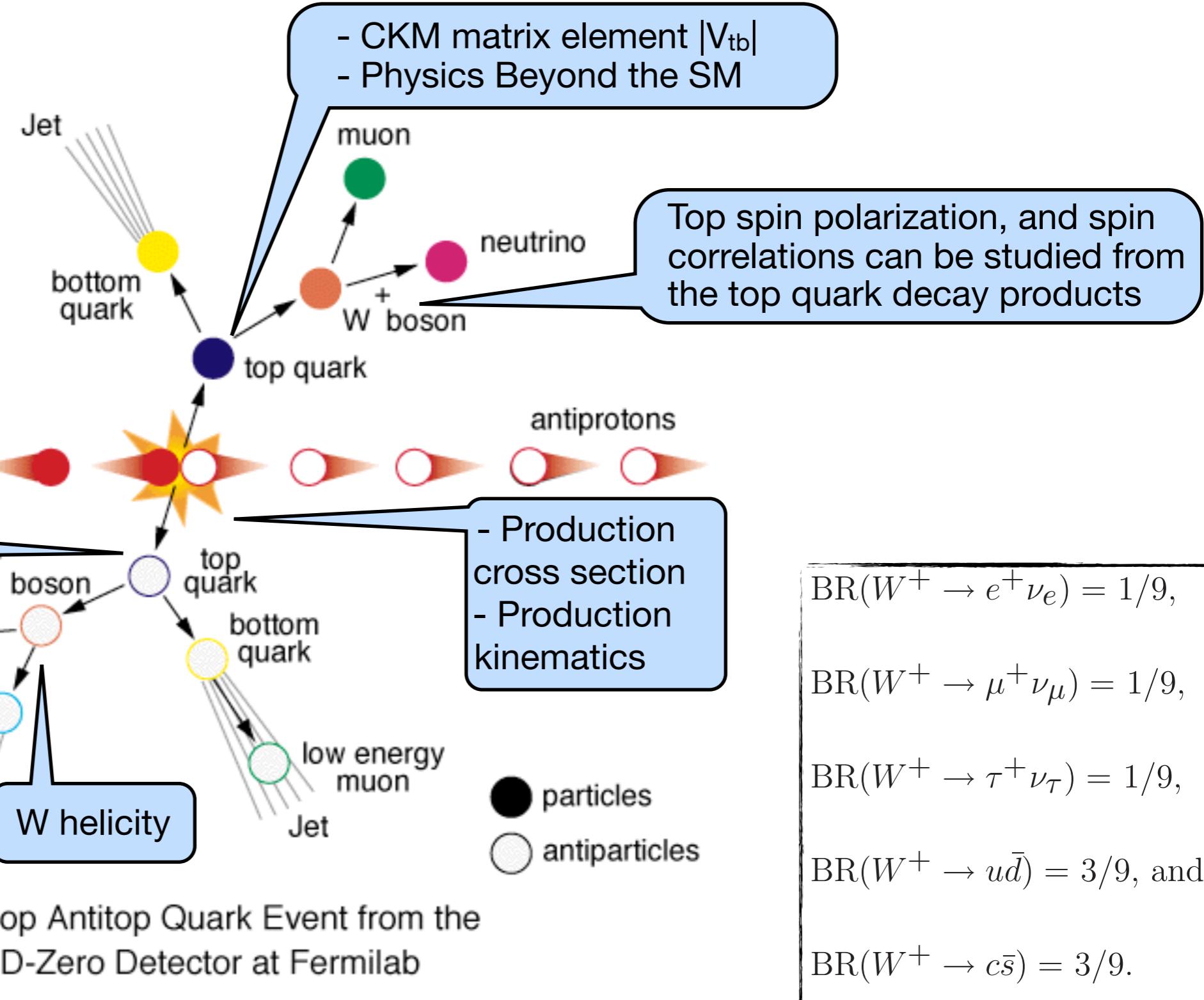


# Top Quark Decay

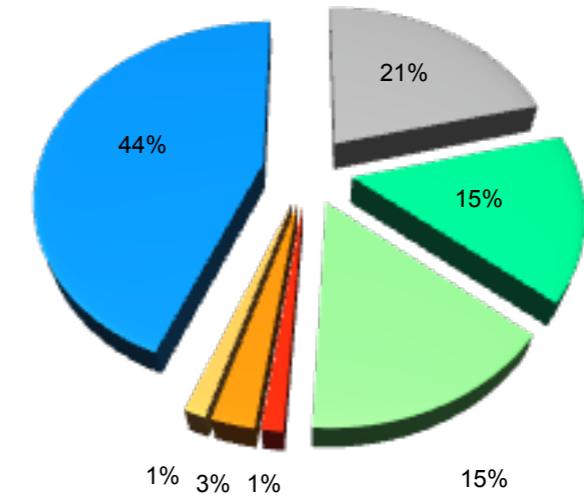
$$B(t \rightarrow W + d) \approx 0.006\%,$$

$$B(t \rightarrow W + s) \approx 0.17\%,$$

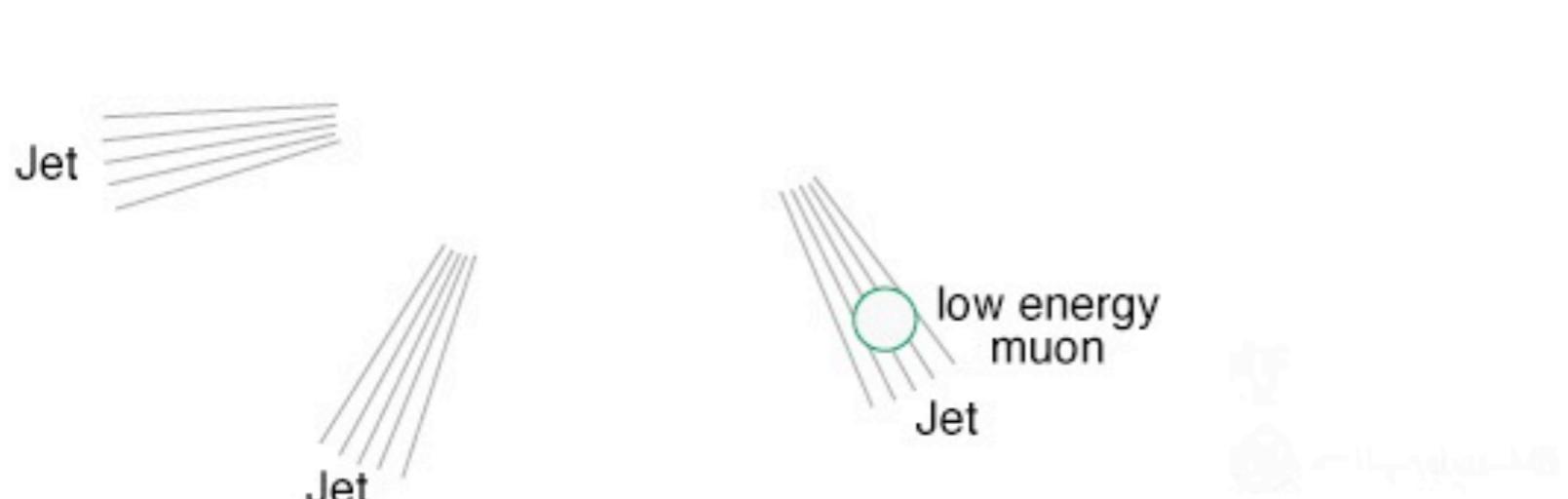
$$B(t \rightarrow W + b) \approx 99.8\%;$$



# Top Quark Decay



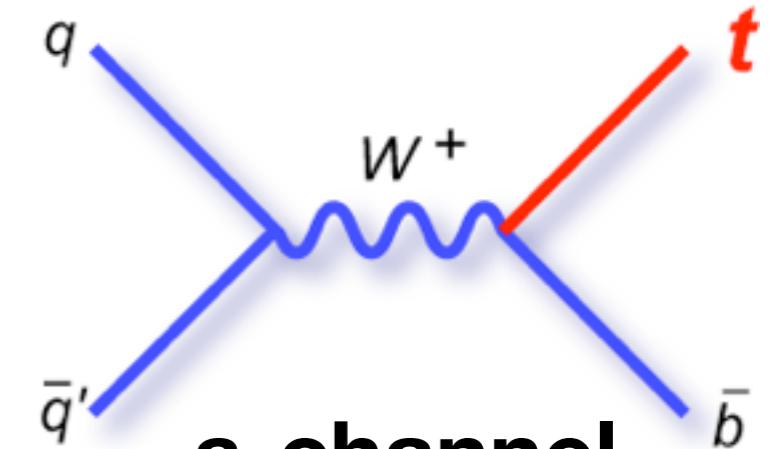
We only see the final states



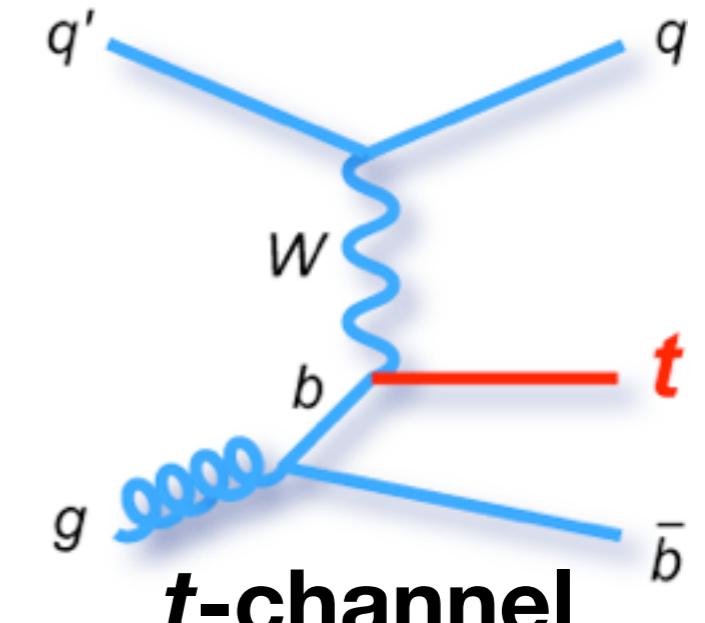
Particles Seen by the D-Zero Detector at Fermilab  
in a Top Antitop Quark Event.

# Single Top

- The Standard Model predicts the production of top quark by means of the electroweak interaction
- Only one top quark is produced! hence the name
- Had not been observed until now
- At the Tevatron Collider, there are two dominant Single Top channels:
  - s-channel
  - t-channel



$$\sigma_s = 1.12 \pm 0.05 \text{ pb}$$

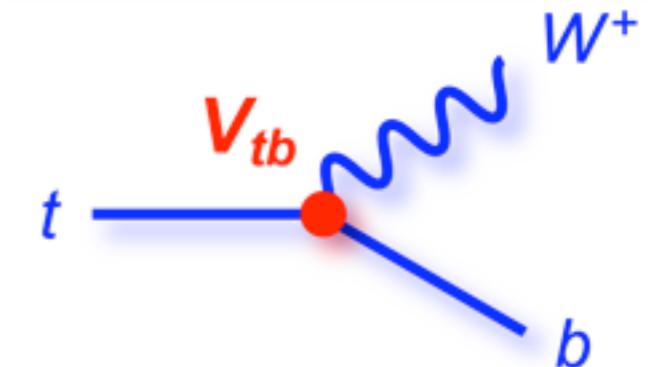


$$\sigma_t = 2.34 \pm 0.12 \text{ pb}$$

PRD 74, 114012 (2006),  $m_t = 170 \text{ GeV}$

# Single Top

- Study the  $Wtb$  vertex:
  - Direct way to measure  $|V_{tb}|$  of the CKM matrix element
  - Test unitarity of CKM matrix
  - Anomalous  $Wtb$  couplings
- Study top quark properties:
  - decay width, lifetime, mass
  - polarization: through the top quark decay products
- Use advance analysis techniques
  - Separate small signal from overwhelming background

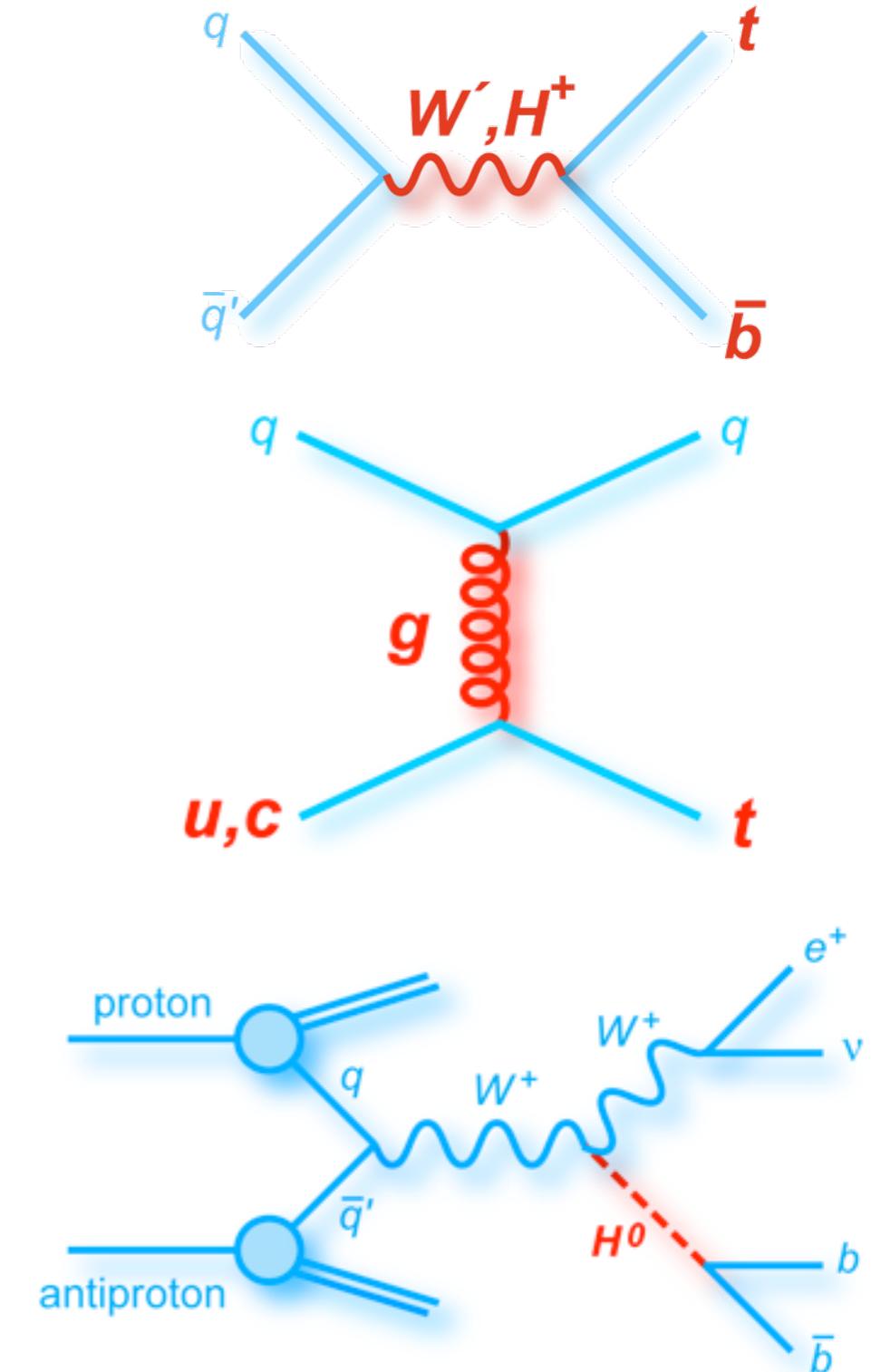


$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & \mathbf{V}_{tb} \end{pmatrix}$$

$V_{CKM}$  Relates weak interaction eigenstates to the mass eigenstates

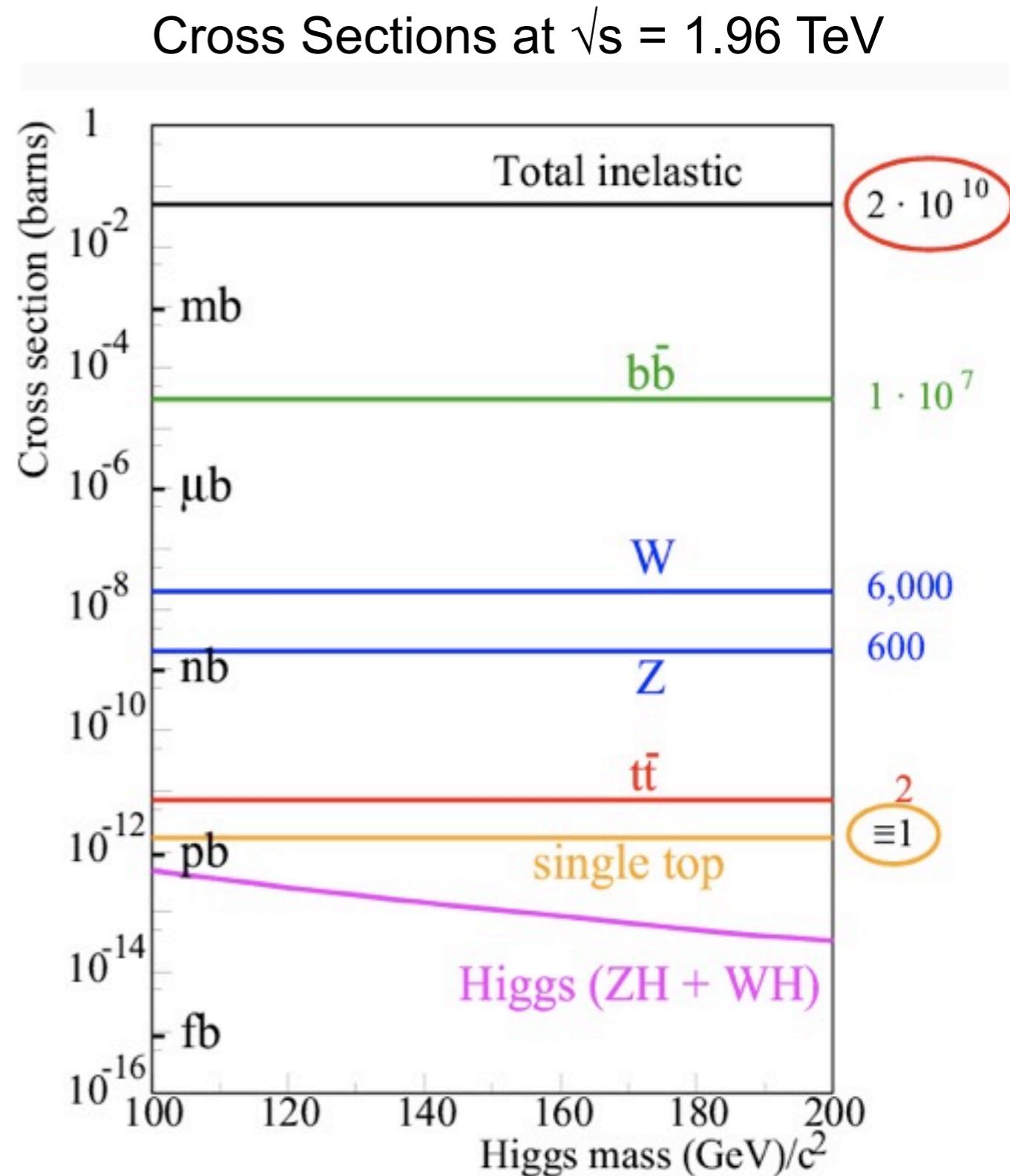
# Single Top

- Sensitive to new physics
  - $W'$  boson of topflavor model
  - Charged Higgs boson
  - Charged top pion of technicolor
  - 4<sup>th</sup> quark generation
  - Flavor changing neutral currents
- Same final state as  $WH$  associated Higgs production



# Single Top Challenges

- Very small production rate
  - ~1:20 billion collisions
- Very large backgrounds
  - Processes with the same final state as Single Top, but with a much larger production rate
- Search is like looking for a needle in a haystack
- An exceptional machine and many extraordinary ideas are needed

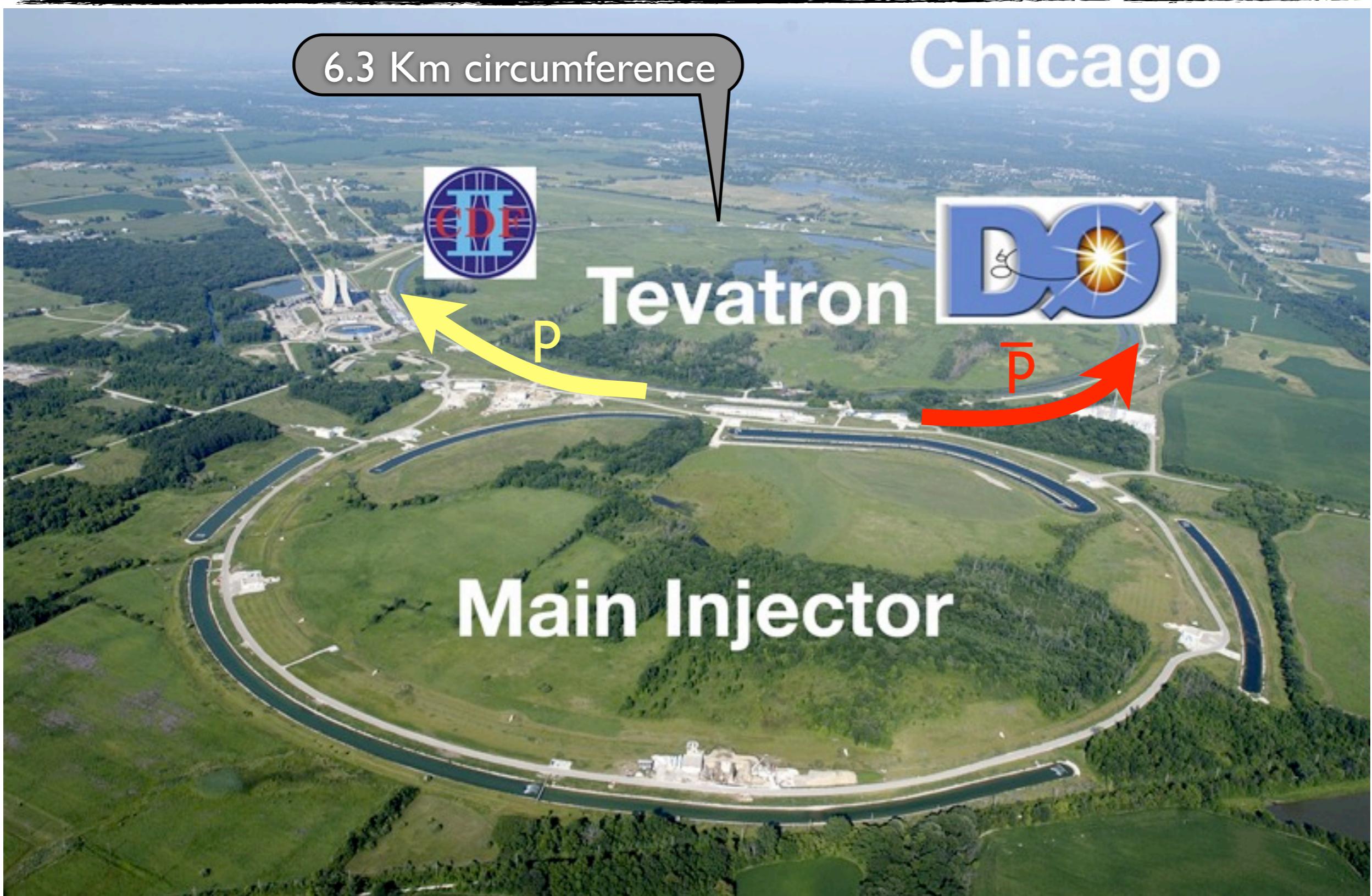


# Single Top Challenges

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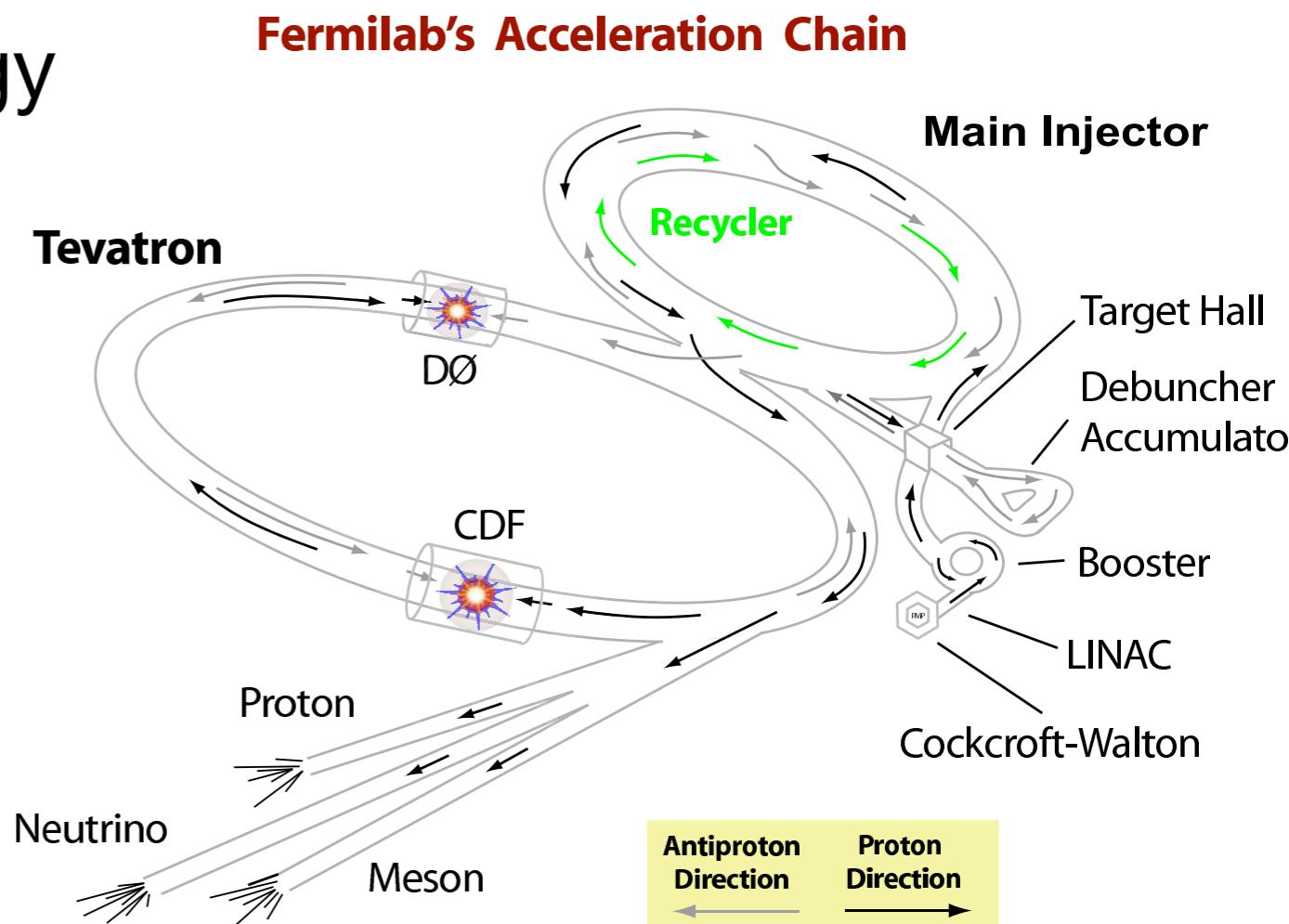


# Fermilab



# Fermilab Tevatron

- Proton-antiproton collider
- Currently highest CM energy  
 $\sqrt{s} = 1.96 \text{ TeV}$
- Instantaneous luminosity:  
 $4.0 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1}$
- The only top quark factory in the world
- 2 main interaction points:  
CDF and D $\emptyset$

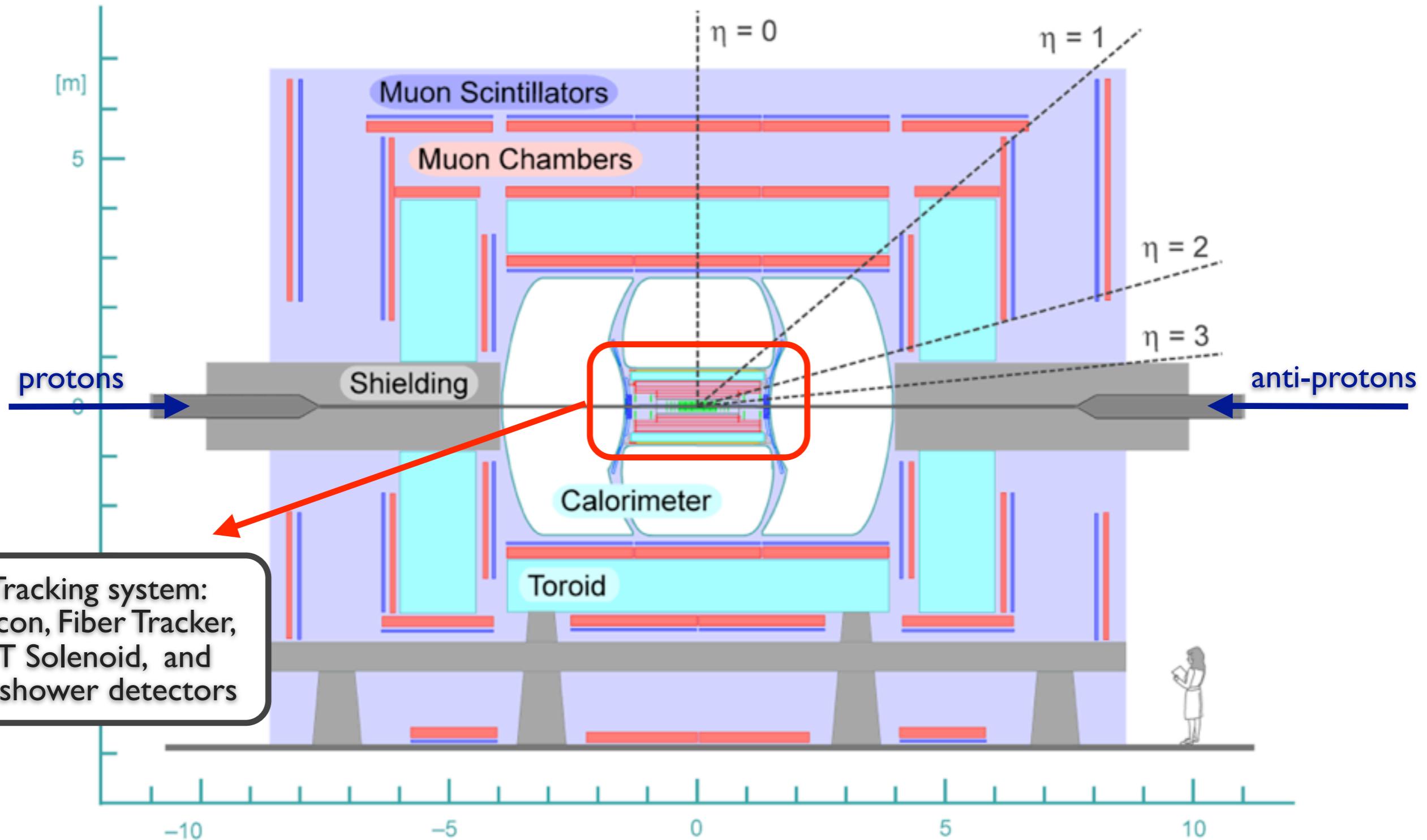


- DØ is a large (5000 tons) experiment on the Tevatron collider at Fermilab
- Run by a collaboration of ~ 500 physicists.

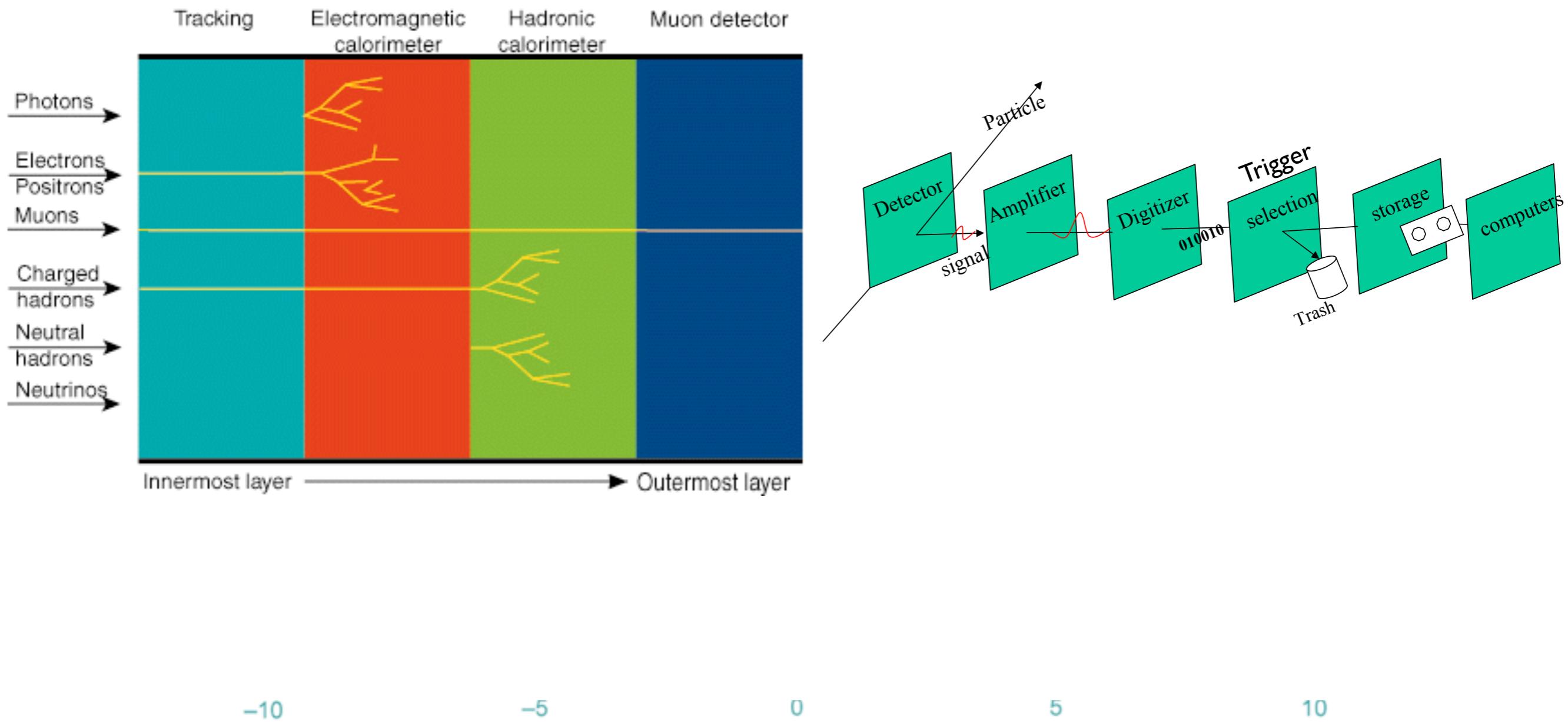


Me

# DØ Experiment

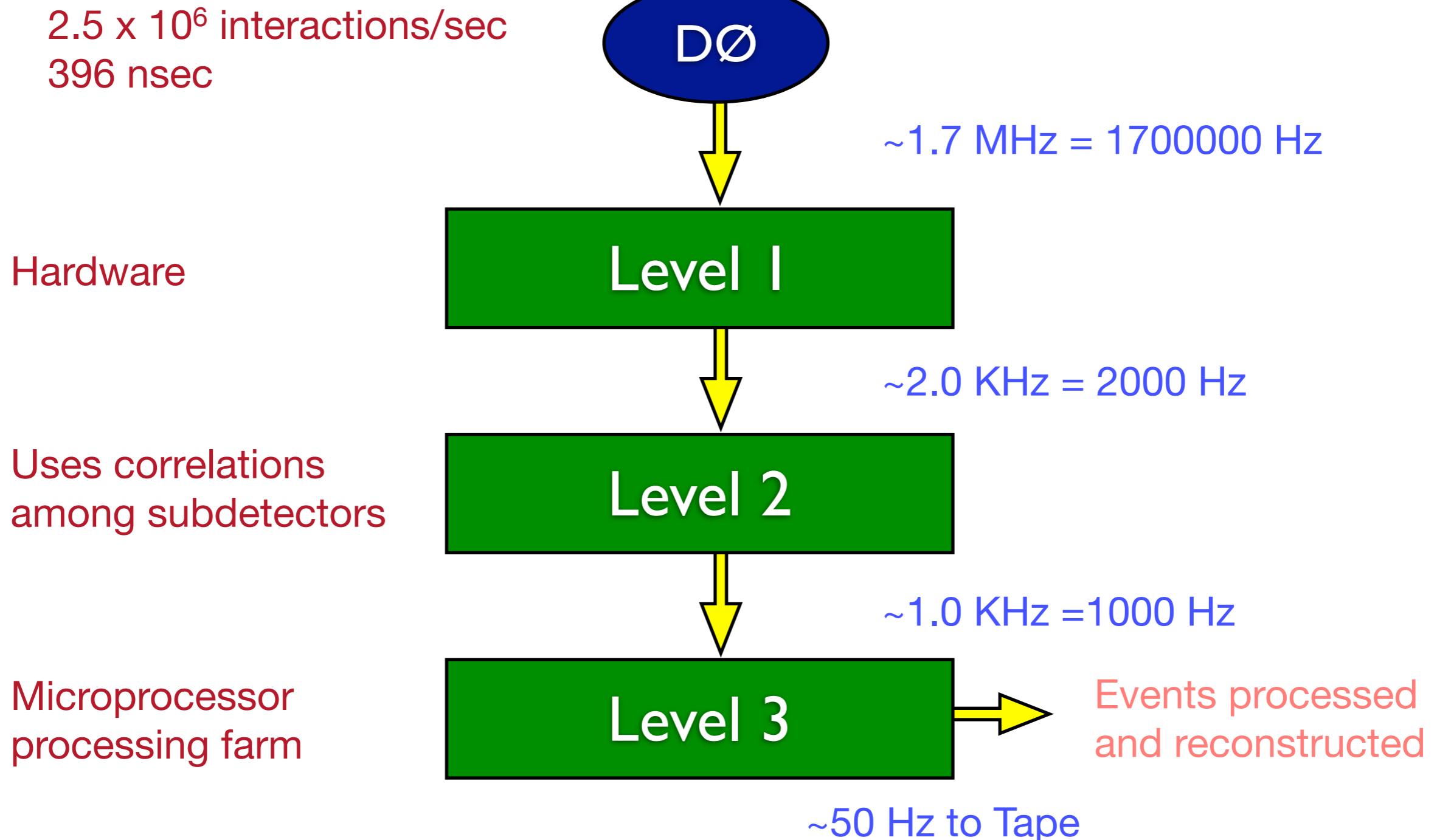


# DØ Experiment



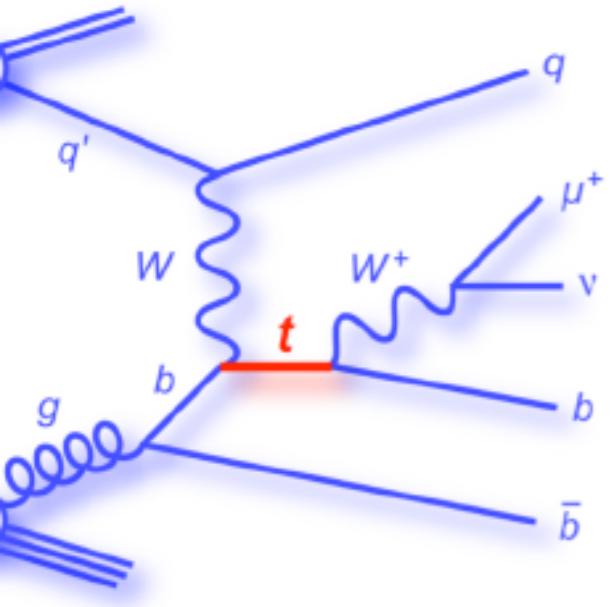
# DØ Trigger

- Main Purpose: to remove non-interesting events.

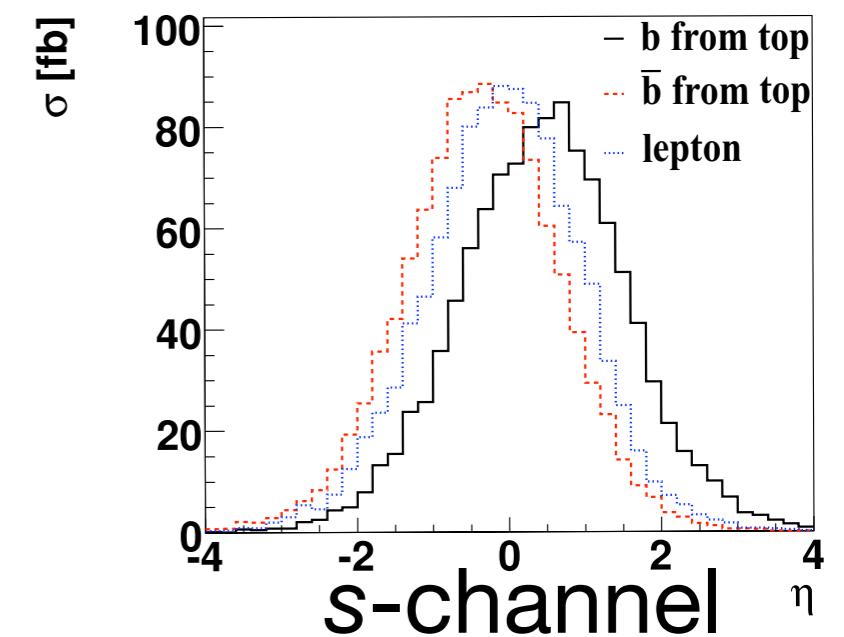


# How does DØ see Single Top?

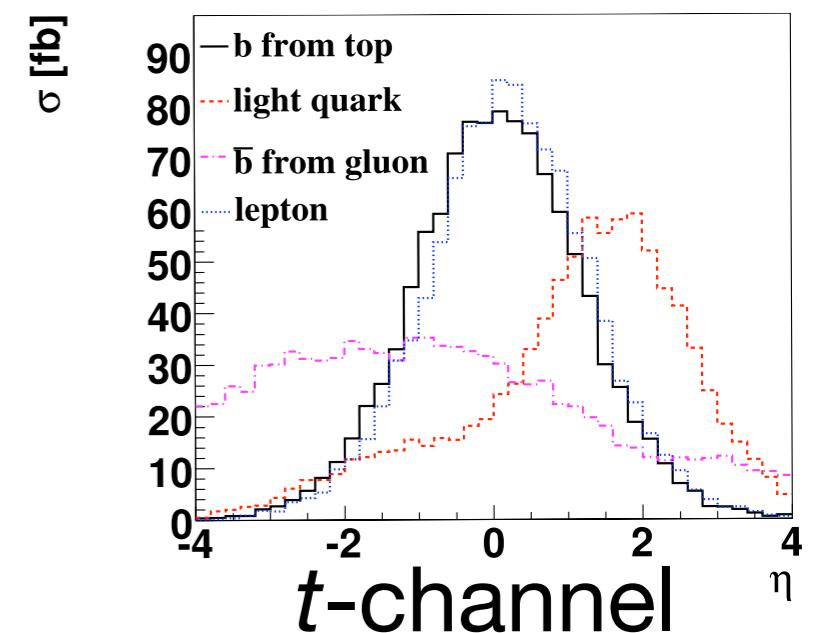
- Events Signature:



- High  $p_T$  jet
- High  $p_T$  lepton
- Missing transverse energy
- High  $p_T$  jet ("b-tagged")
- High  $p_T$  jet ("b-tagged")



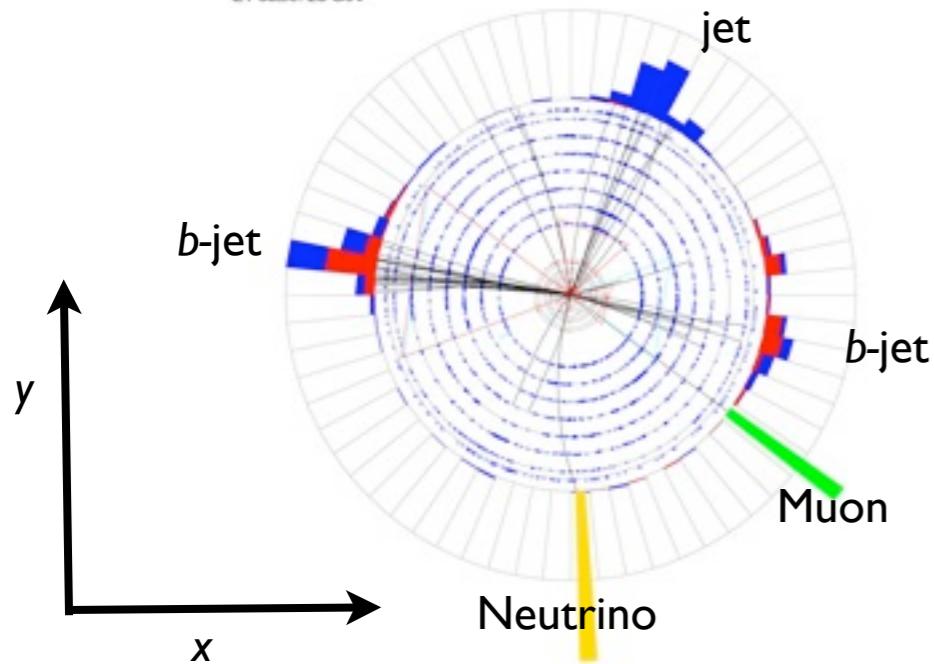
- One high transverse momentum isolated lepton (electron or muon from the  $W$ )
- Missing Transverse Energy (neutrino from the  $W$ )
- Two to four high transverse momentum jets:
  - One or two jets associated with a  $b$ -quark



# Candidate Event

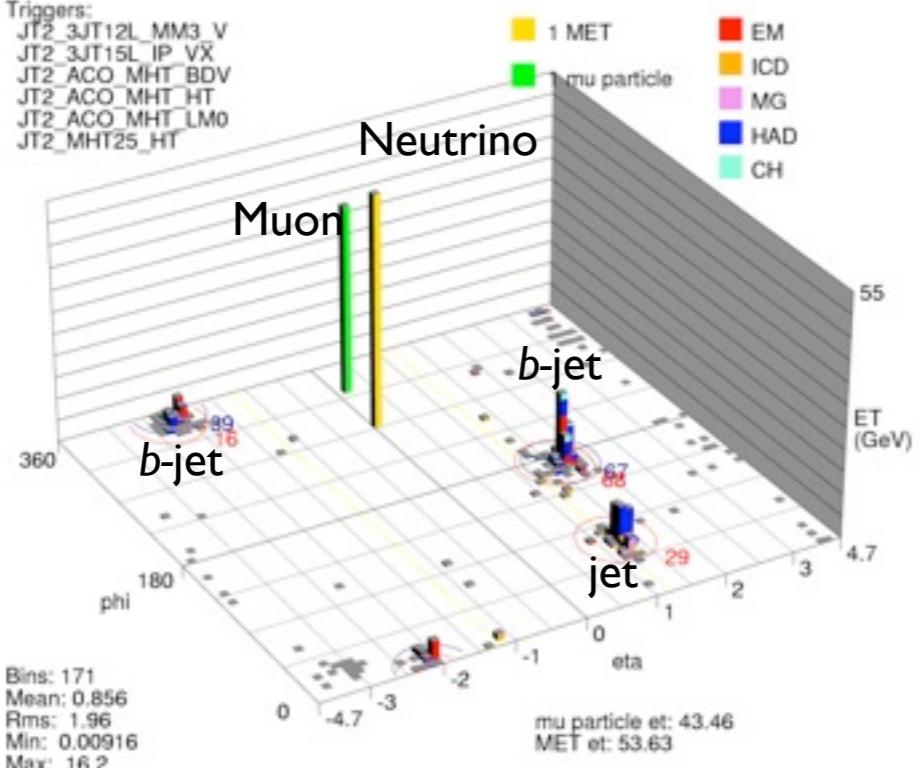
Run 223473 Evt 27278544 Sun Jul 23 19:21:41 2006

ET scale: 28 GeV

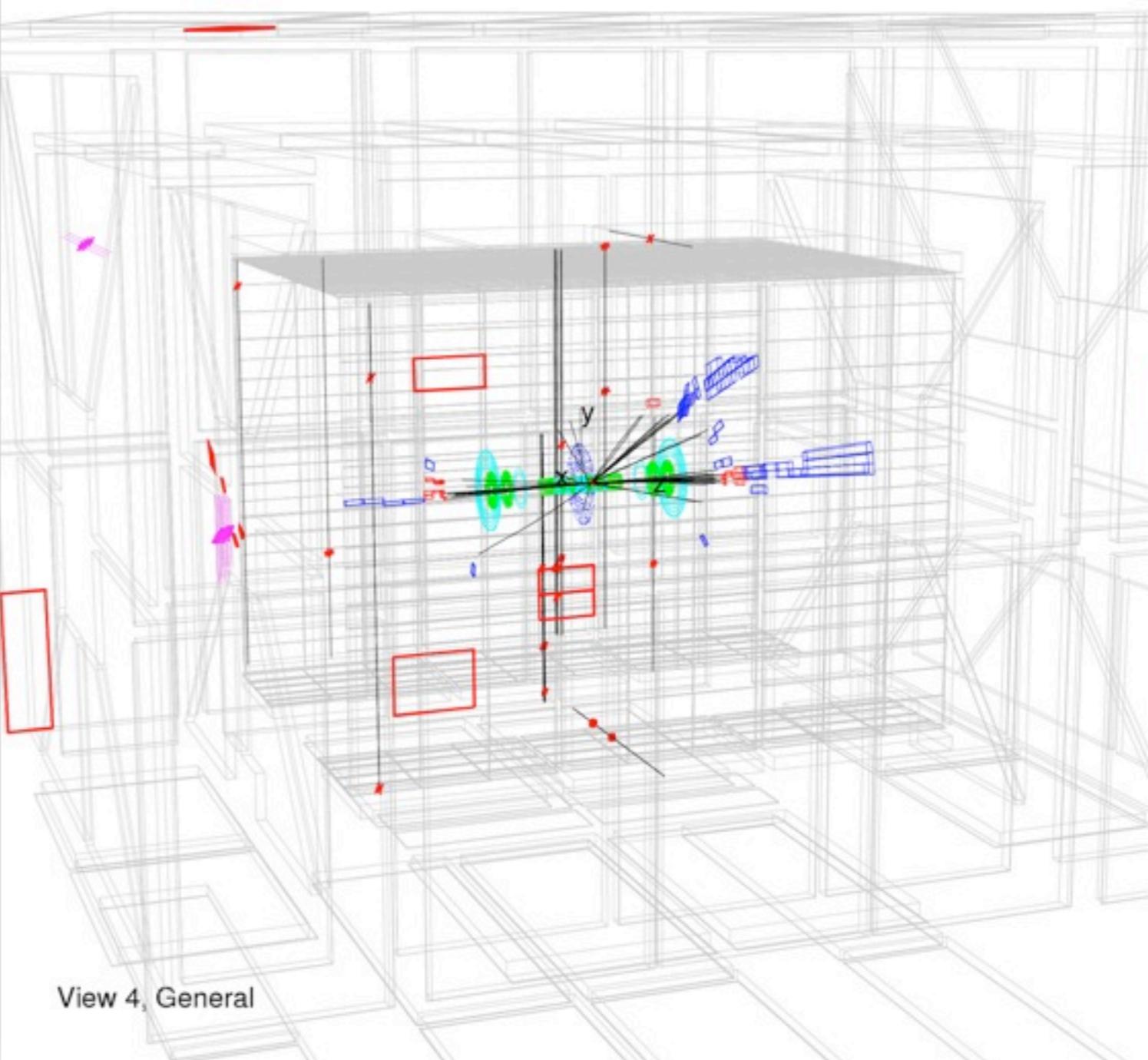


Run 223473 Evt 27278544 Sun Jul 23 19:21:41 2006

Triggers:  
 JT2\_3JT12L\_MM3\_V  
 JT2\_3JT15L\_IP\_VX  
 JT2\_ACO\_MHT\_BDV  
 JT2\_ACO\_MHT\_HT  
 JT2\_ACO\_MHT\_LM0  
 JT2\_MHT25\_HT

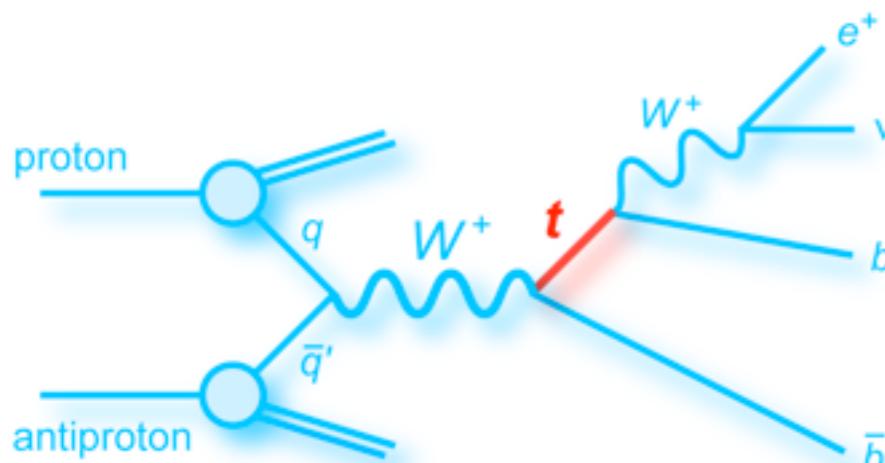


Run 223473 Evt 27278544 Sun Jul 23 19:21:41 2006

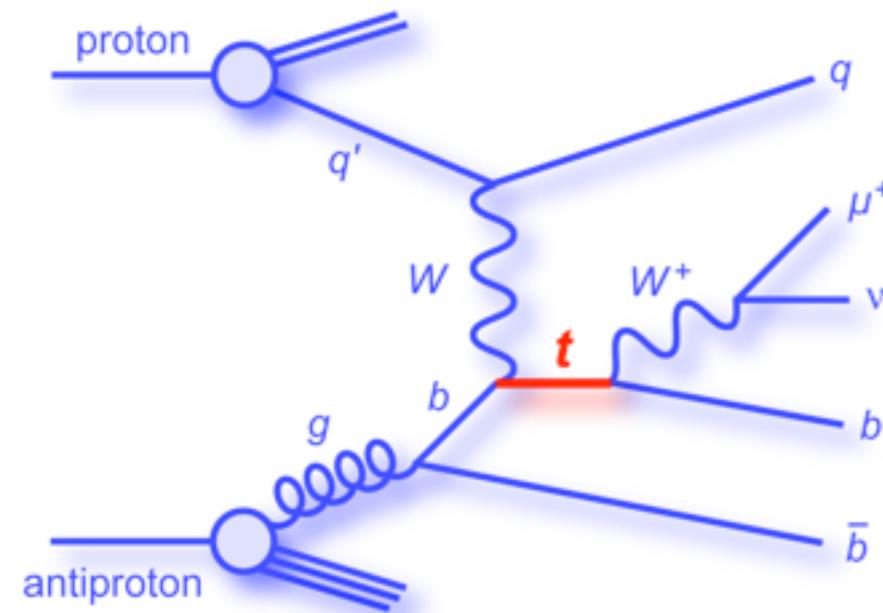


# Backgrounds

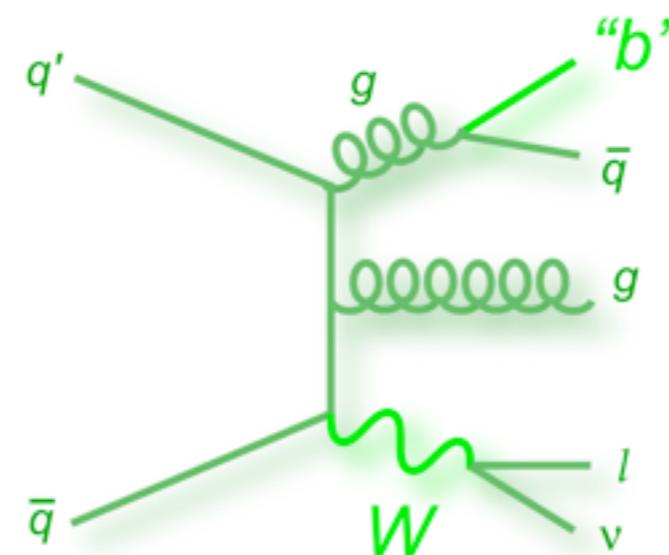
- Same final state as Single Top



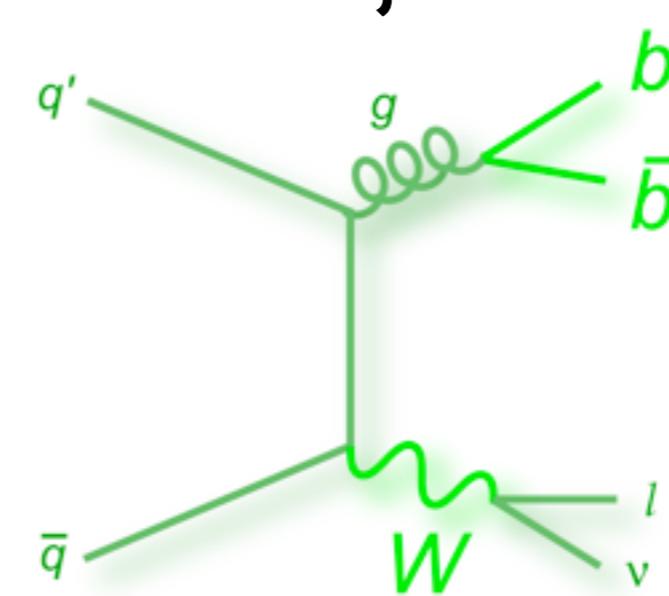
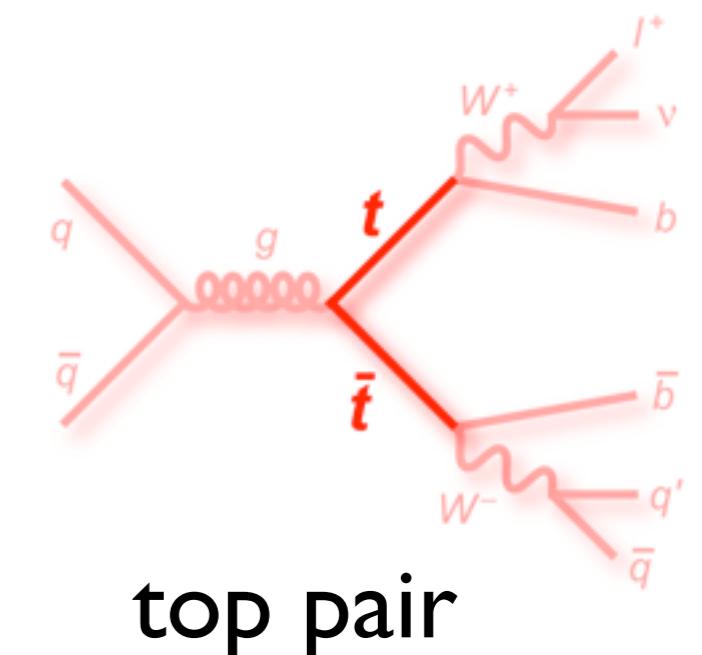
Single Top s-channel



Single Top t-channel



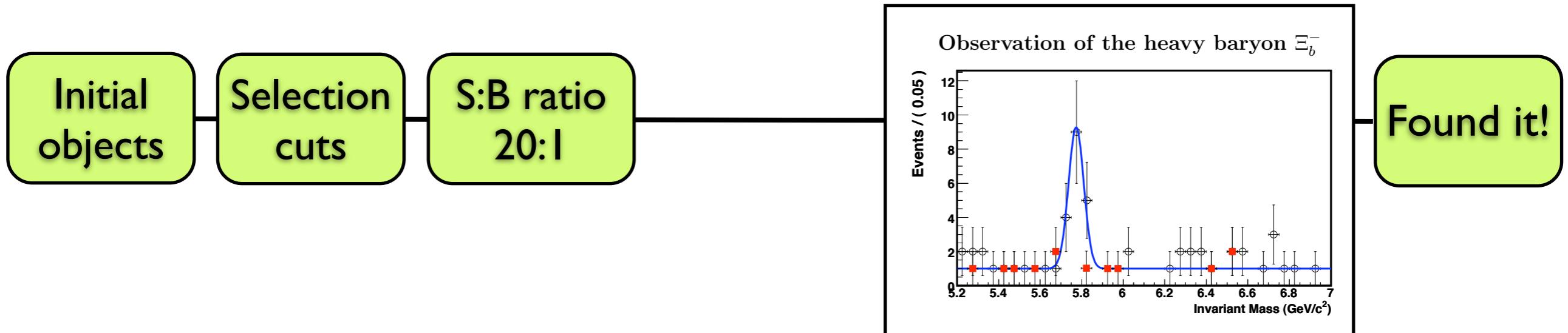
W+jets



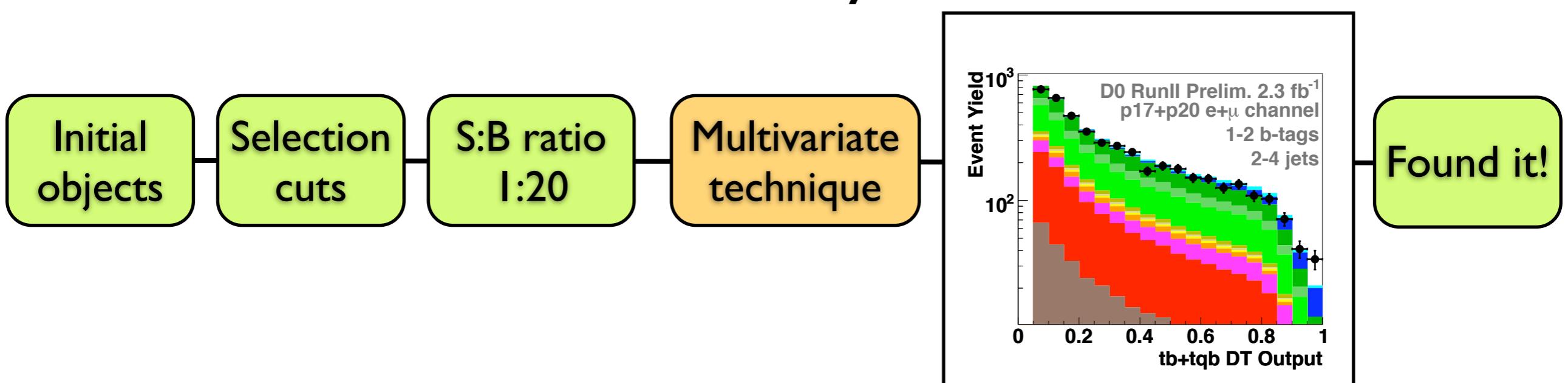
multijets - QCD

# Finding The Signal

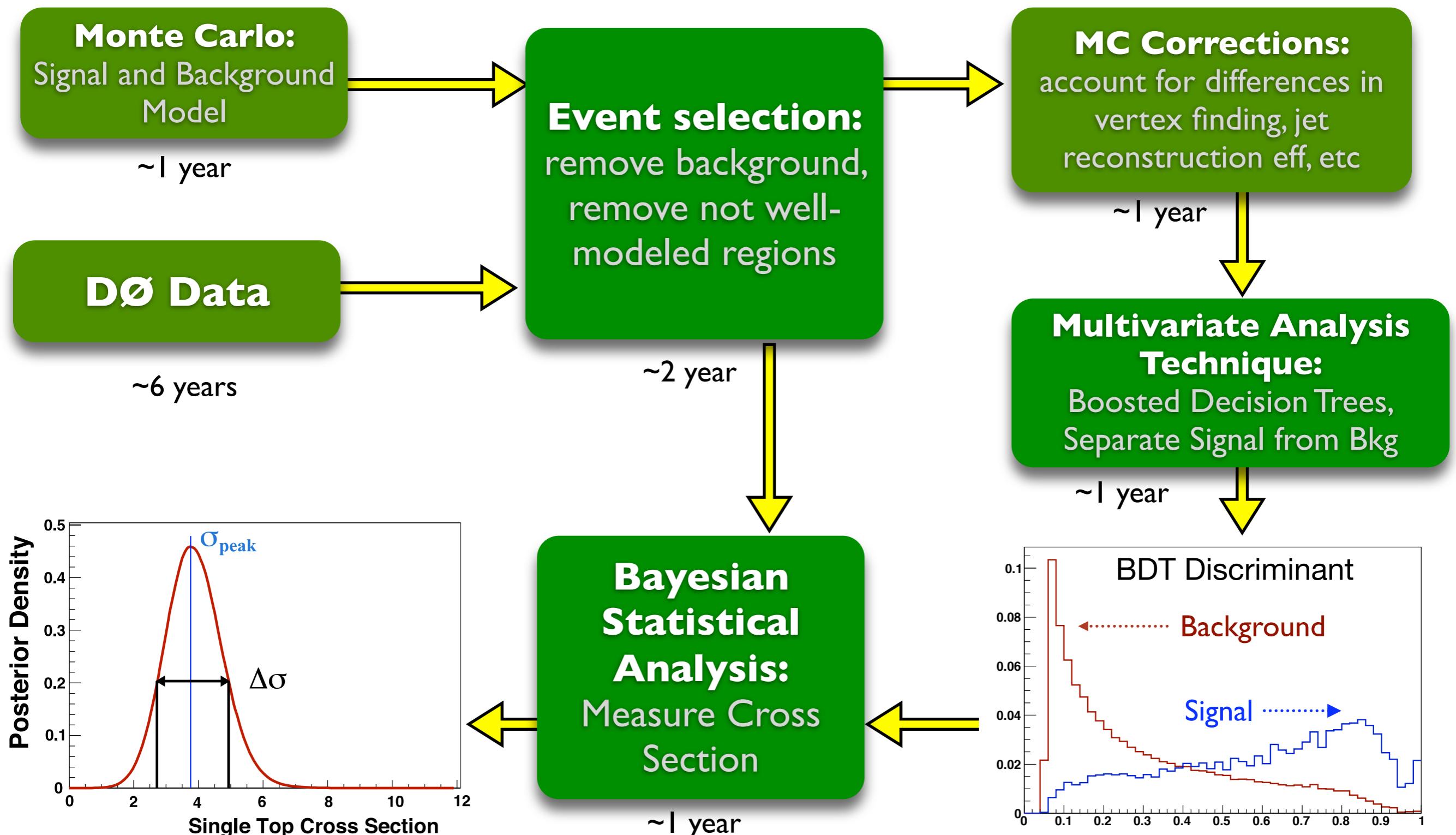
## Traditional cut-based analysis



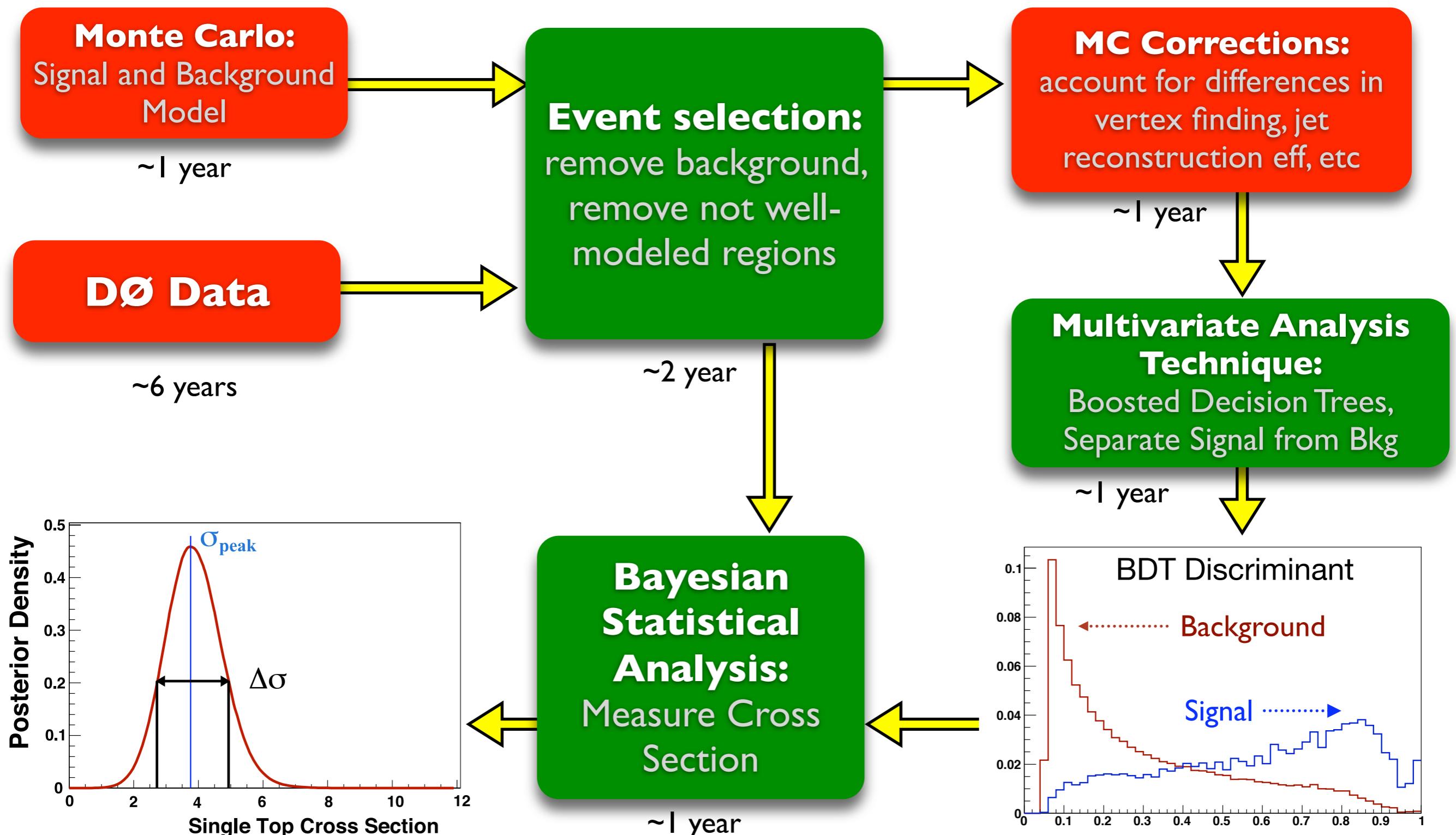
## This analysis



# Single Top Search

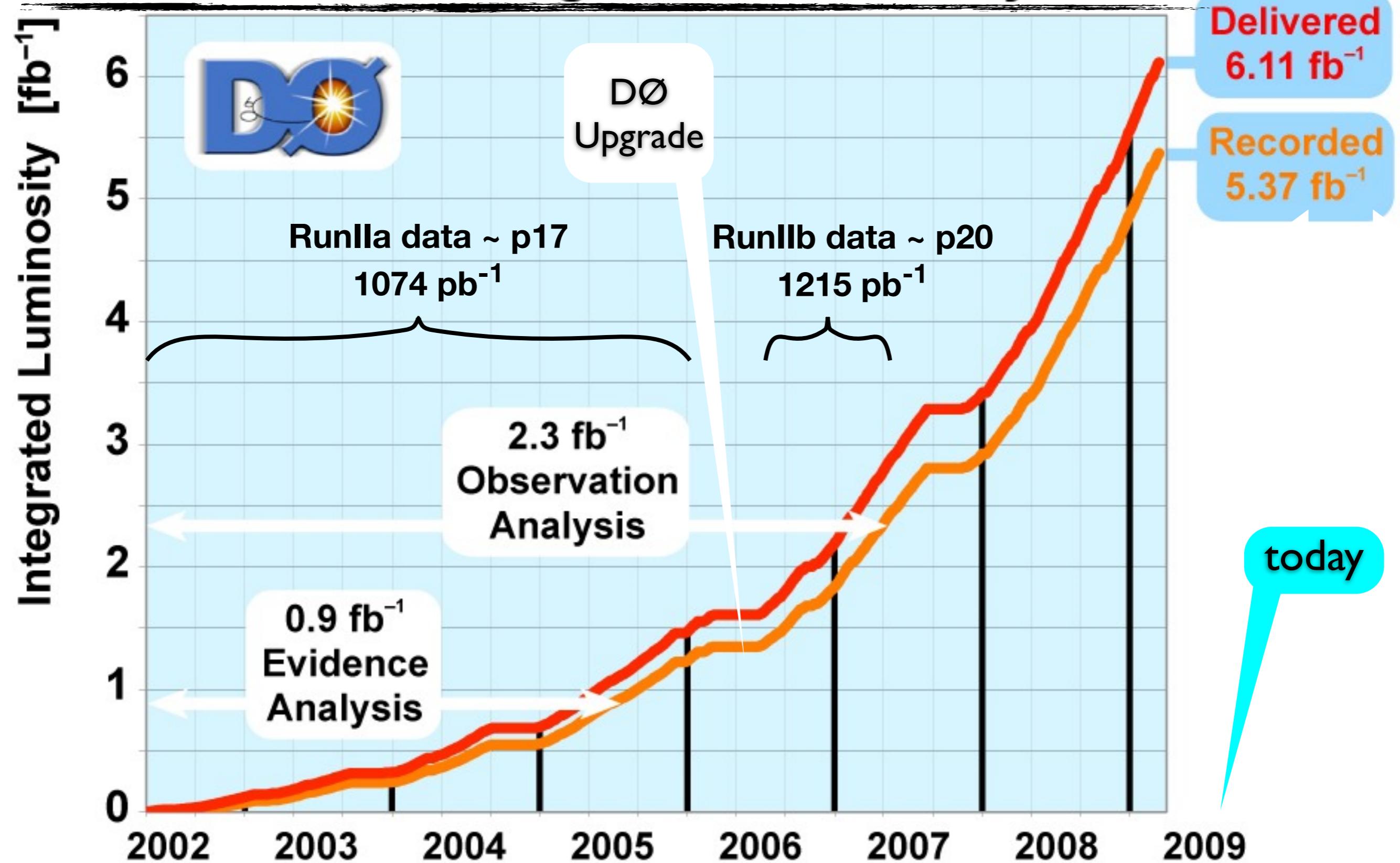


# Single Top Search



# Fermilab Tevatron

## Run II Integrated Luminosity



# Signal and Bkg. Modeling

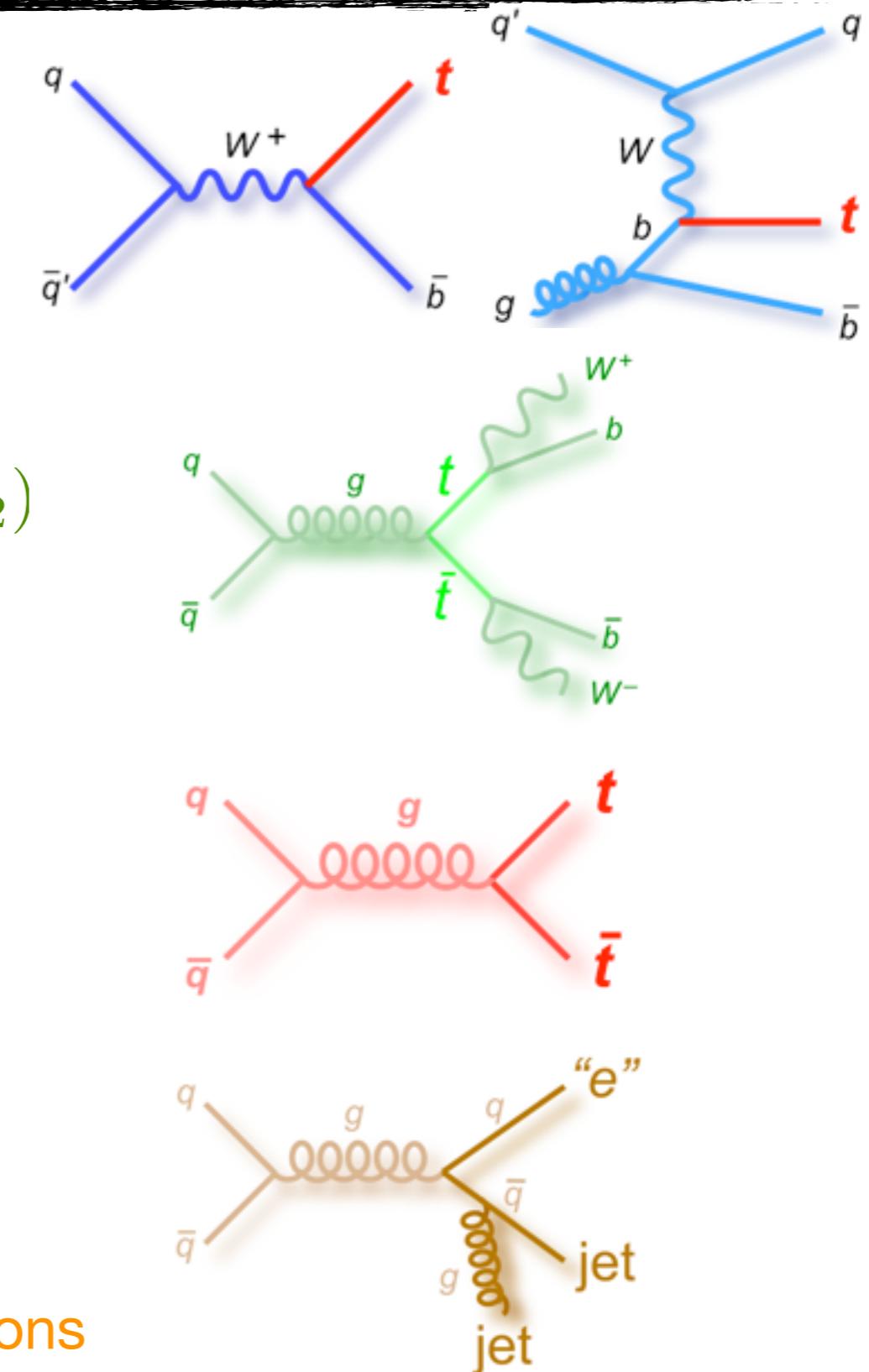
- Single Top →
  - SINGLETOP MC (Based on COMHEP)
  - PYTHIA for parton hadronization

- W+jets →
  - ALPGEN + PYTHIA
  - $\eta(jets)$ ,  $\Delta\phi(jet_1, jet_2)$ ,  $\Delta\eta(jet_1, jet_2)$  corrected to match data
  - normalized to data
  - W+heavy flavor corrections

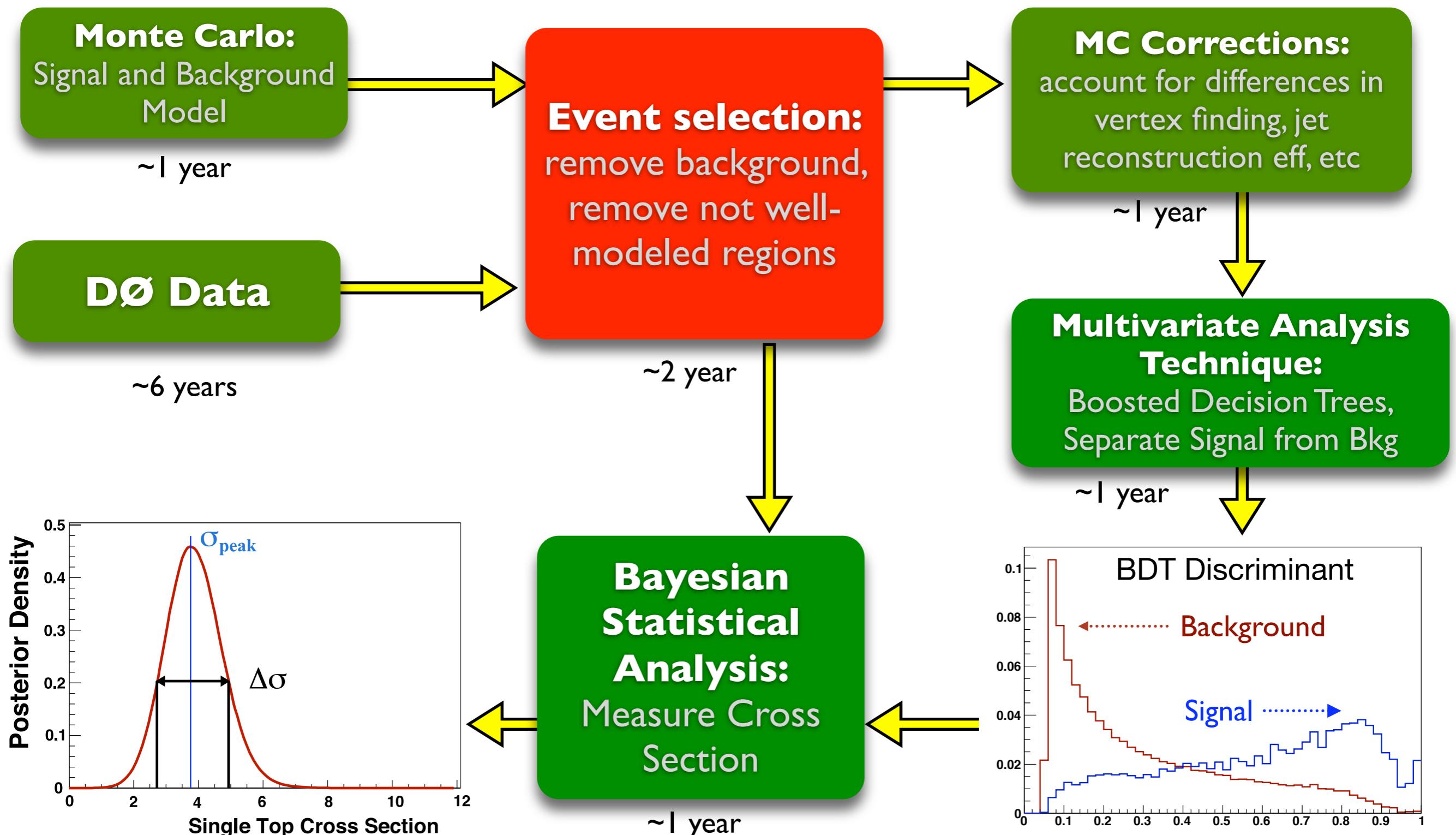
- Top Pair →
  - ALPGEN + PYTHIA
  - normalized to theory cross section

- Multijets (QCD) →
  - data with non-isolated leptons

- Additional backgrounds:
  - Z+jets
  - Dibosons

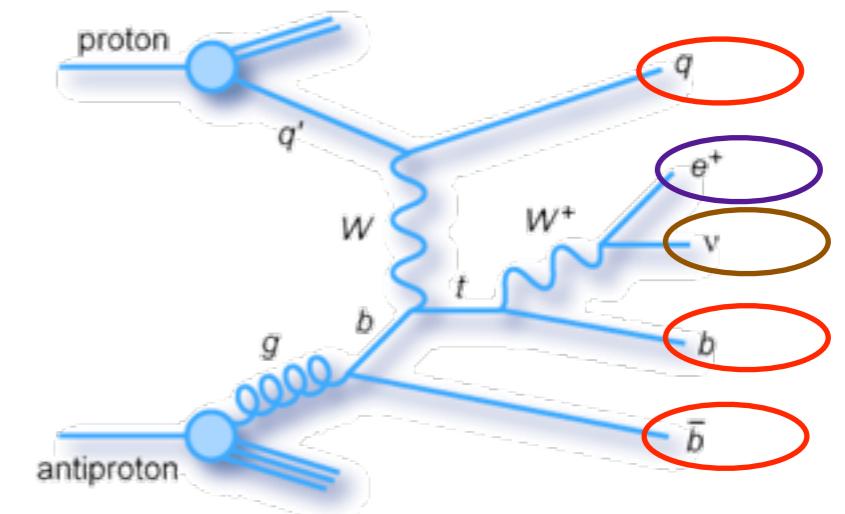
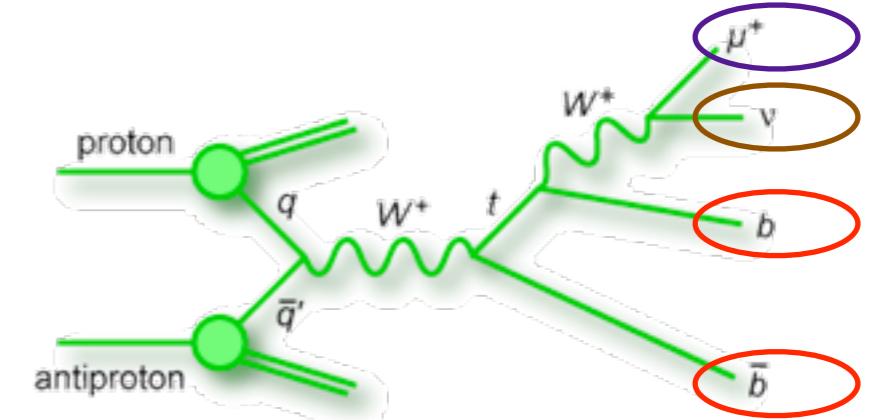


# Single Top Search



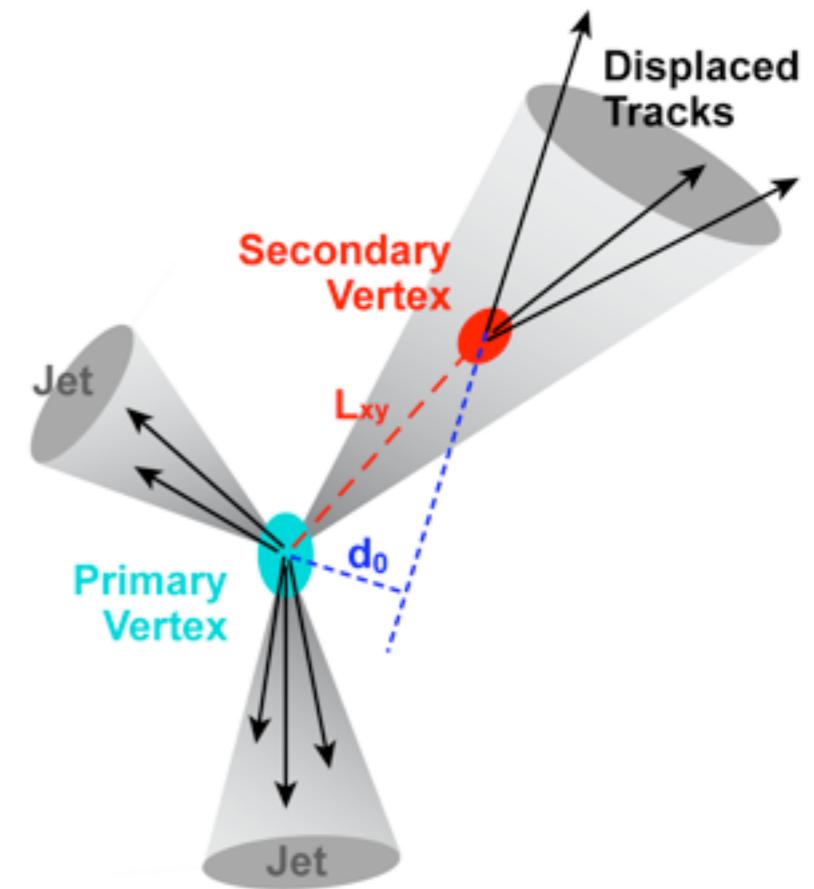
# Event Selection

- Many triggers
- One Isolated Lepton:
  - Electron  $p_T > 15 \text{ GeV}$ ,  $|n| < 1.1$
  - Muon  $p_T > 15 \text{ GeV}$ ,  $|n| < 2.0$
- $20 \text{ GeV} > \text{MET} > 200 \text{ GeV}$
- One  $b$ -tagged jet and at least one more jet
  - 2-4 jets with  $p_T > 15 \text{ GeV}$ ,  $|n| < 3.4$
  - Leading jet  $p_T > 25 \text{ GeV}$
- Cut on scalar sum of transverse energies (alljets, lepton, MET)
- Triangular Cuts:  
 $\Delta\phi(\text{Leading jet}, \text{MET})$  vs MET and  $\Delta\phi(\text{lepton}, \text{MET})$  vs MET



# Event Selection (cont.)

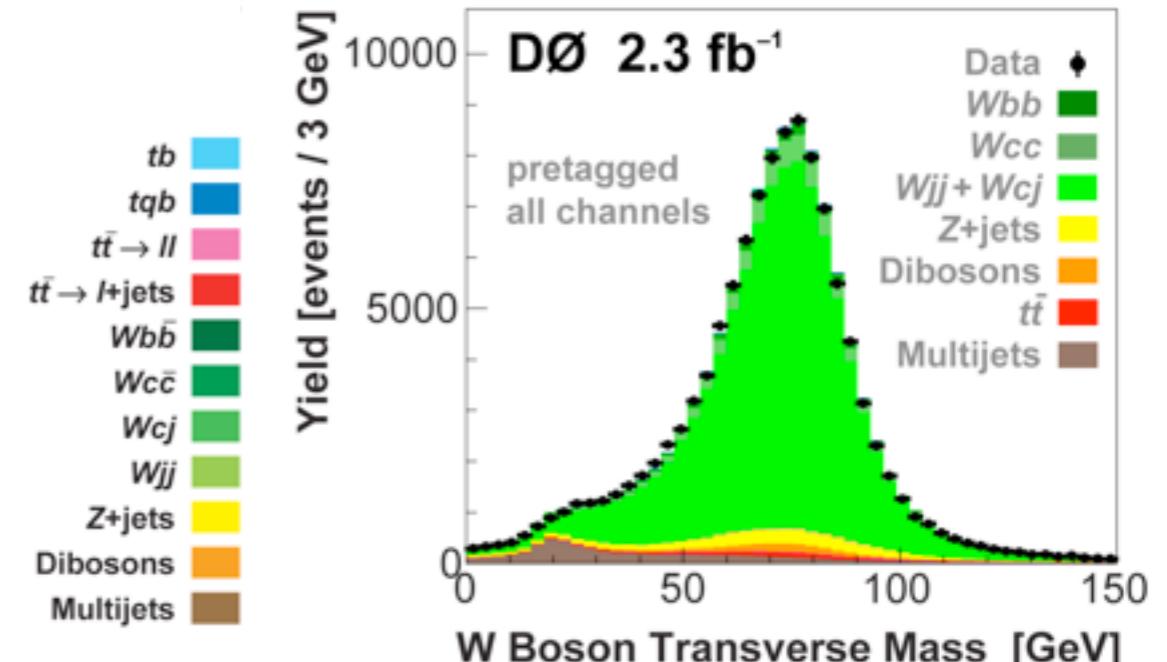
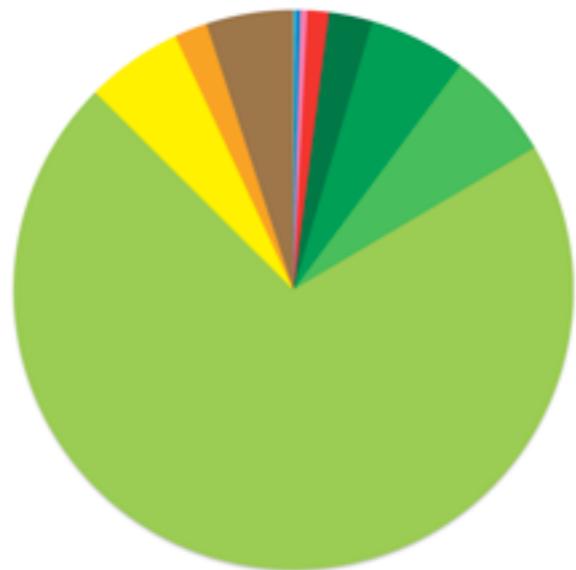
- *b*-tagging:
  - Greatly reduces w+jets bkg!
  - Identifies jets coming from a *b*-quark
    - *b*-hadron travel ~ 3 mm before decaying, which creates a secondary vertex
    - The identification uses a neural network algorithm based on the vertex reco variables.
- The selection process results in a total of 24 channels!  
[ 2 Data Run periods (IIa,IIb) ] x [ 2 lepton types ( $\mu, e^-$ ) ] x  
[ 3 jet multiplicities (2,3,4 jets) ] x [ 2 *b*-jet multiplicities (1,2 *b*-jets) ]



# Good DATA/MC Agreement!

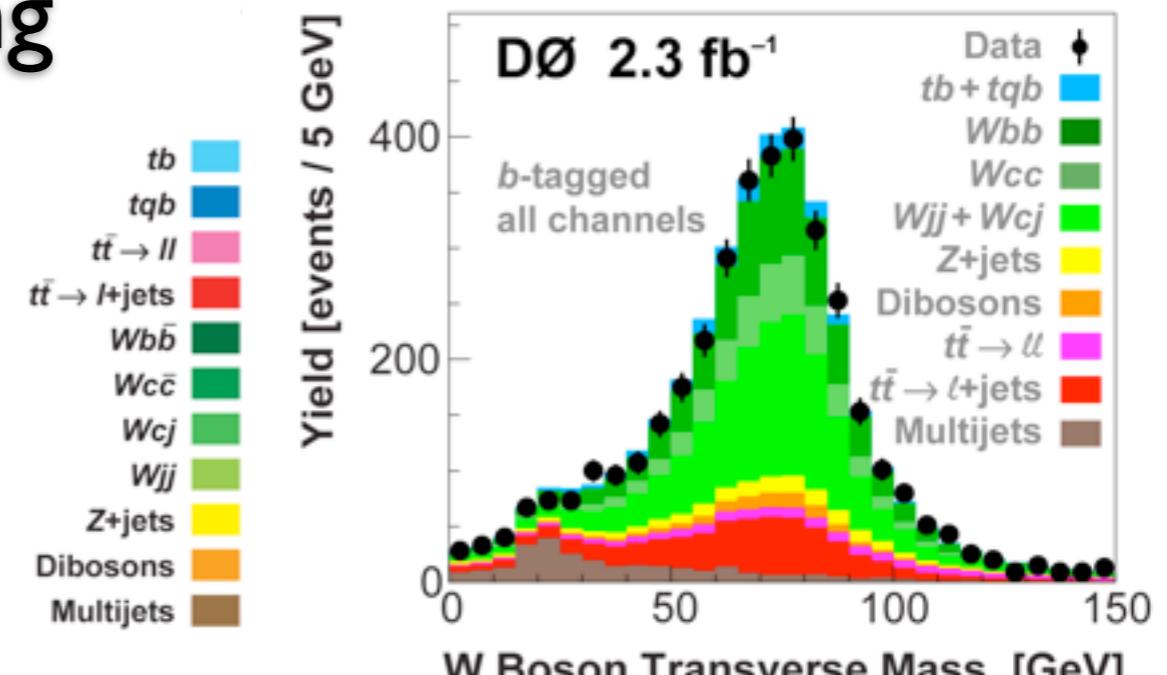
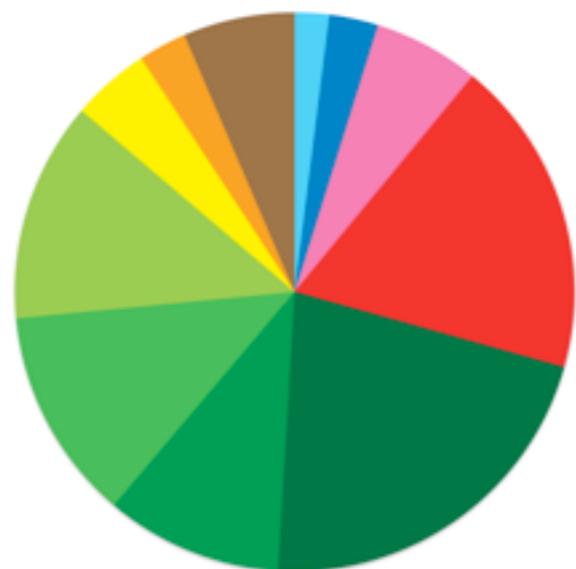
Event Yields in $2.3 \text{ fb}^{-1}$ of DØ Data	
e, $\mu$ , 2,3,4-jets, pretag	
$t b + t q b$	444
$W + \text{jets}$	98,444
$Z + \text{jets, dibosons}$	8,631
$t\bar{t}$ pairs	1,895
Multijets	5,798
Total background	114,777
Data	114,777

Pre b-tagging



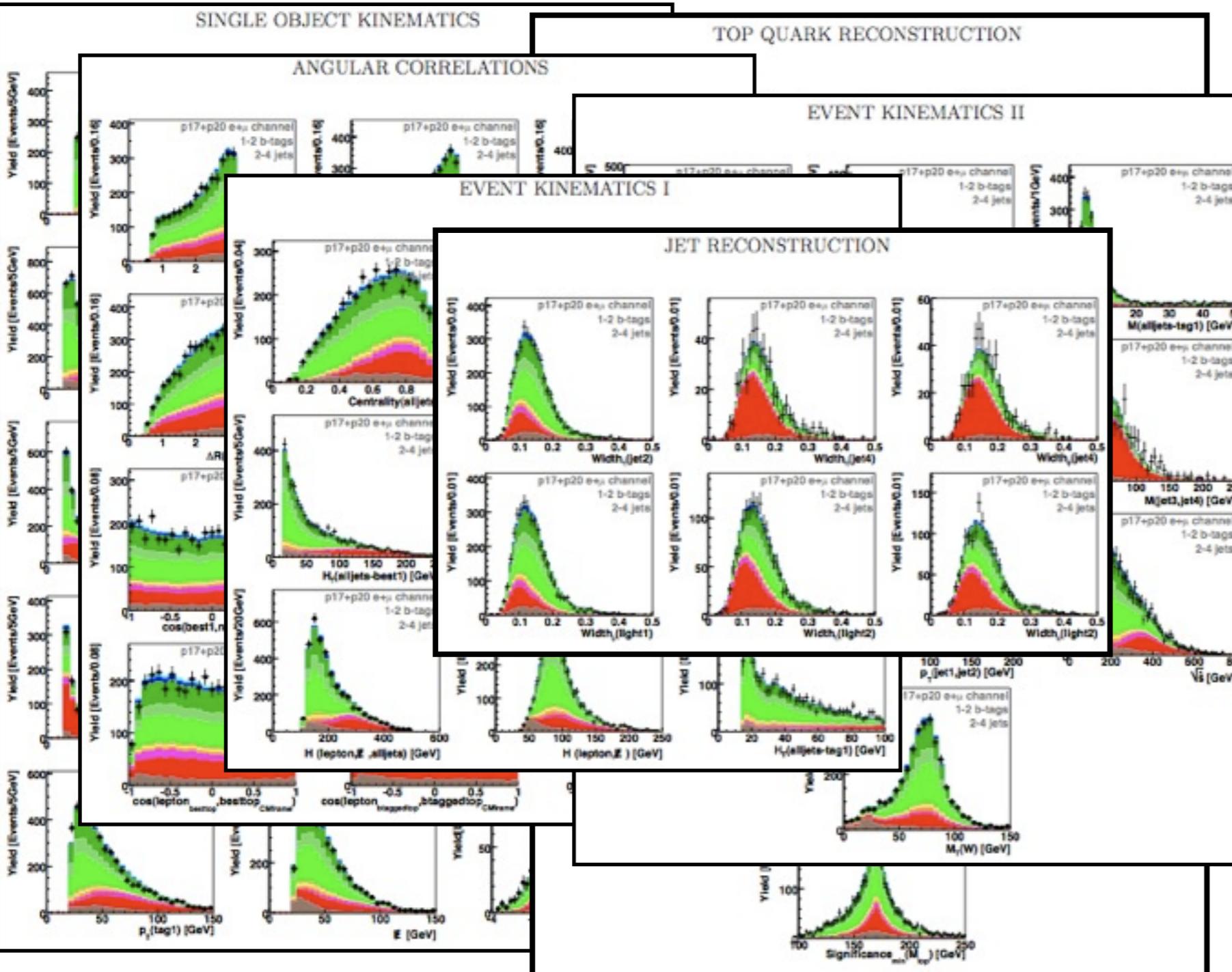
Event Yields in $2.3 \text{ fb}^{-1}$ of DØ Data	
e, $\mu$ , 2,3,4-jets, 1,2-tags combined	
$t b + t q b$	$223 \pm 30$
$W + \text{jets}$	$2,647 \pm 241$
$Z + \text{jets, dibosons}$	$340 \pm 61$
$t\bar{t}$ pairs	$1,142 \pm 168$
Multijets	$300 \pm 52$
Total prediction	$4,652 \pm 352$
Data	4,519

After b-tagging

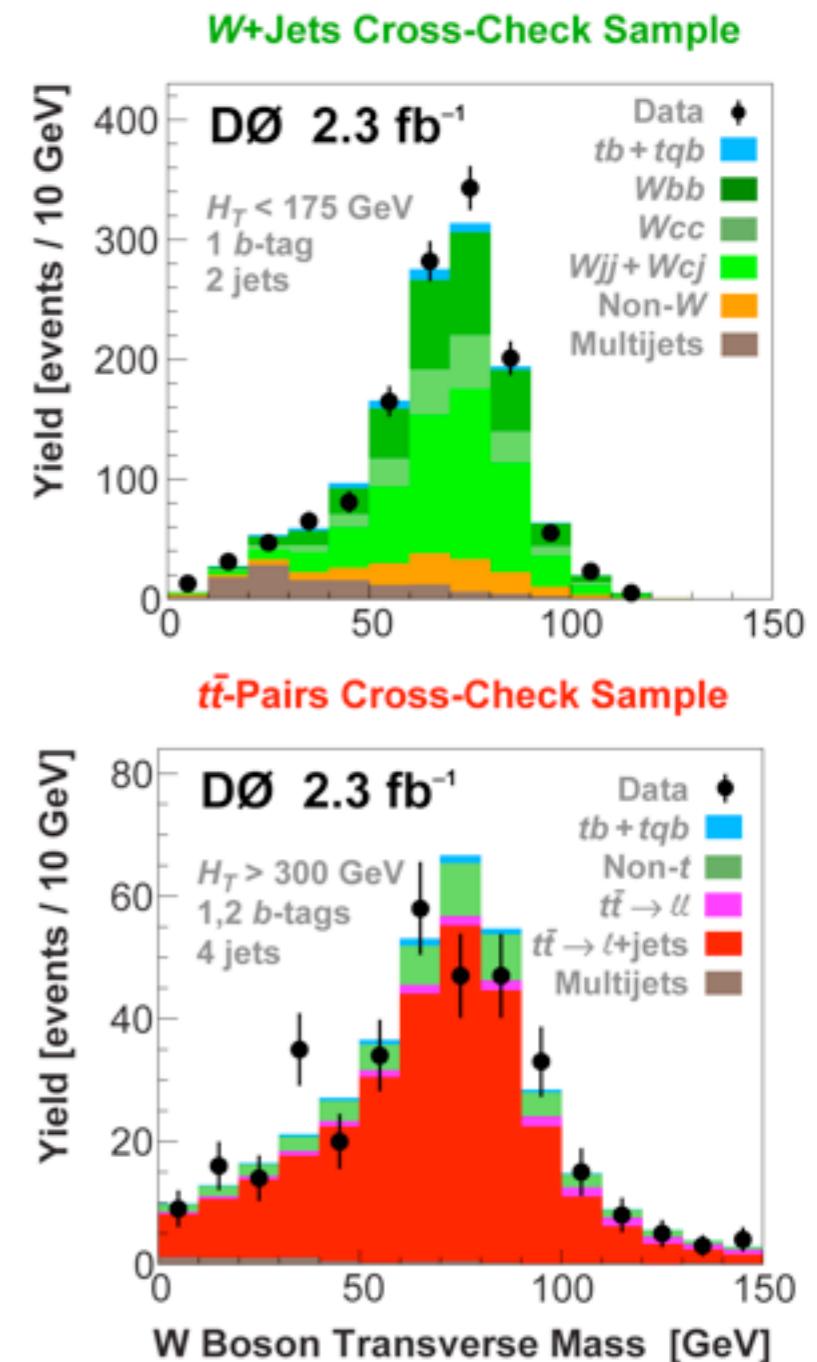


# Cross Checks

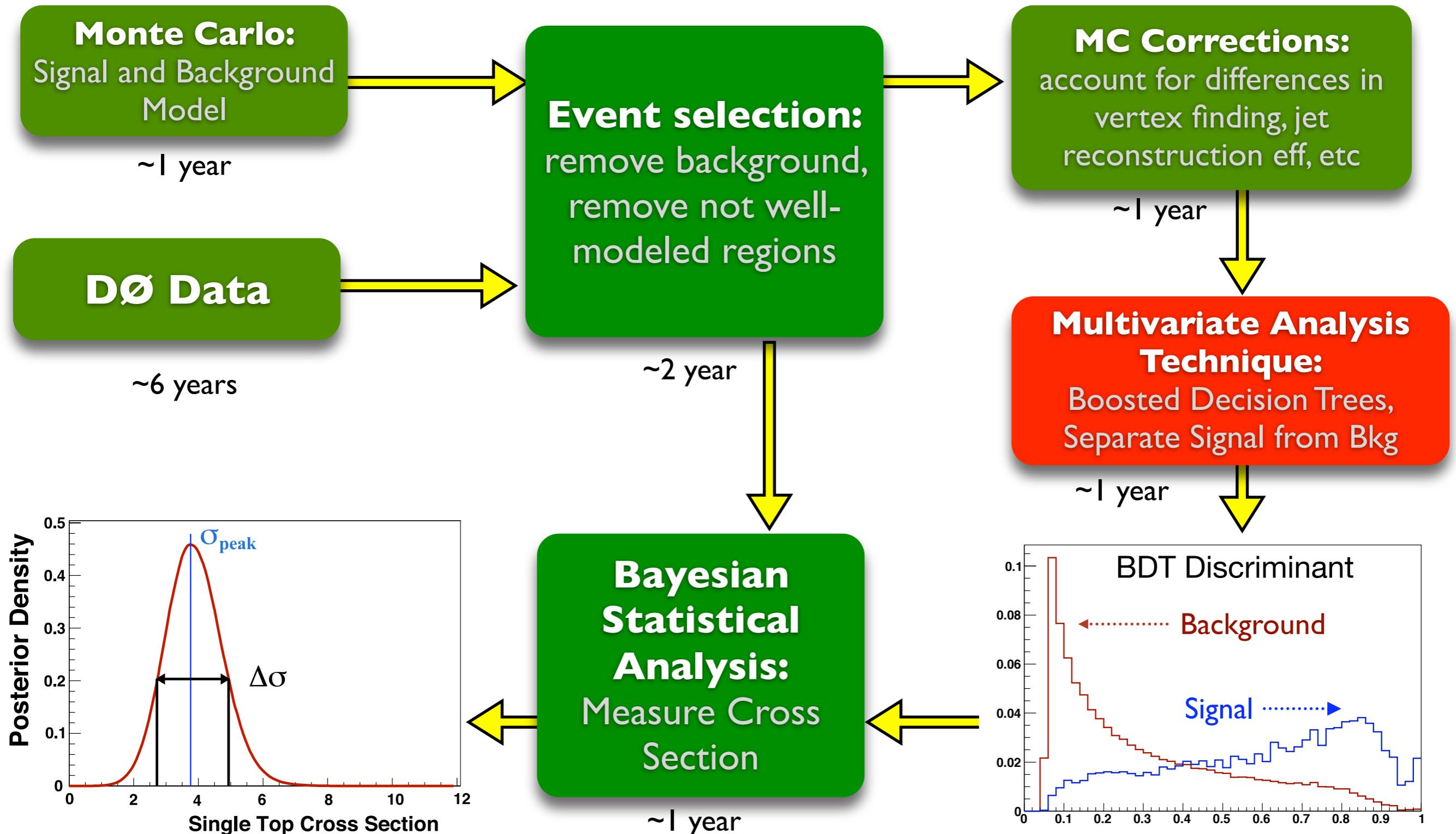
- Checked good data/mc agreement over 500 distributions on each of the 24 analyses channels!



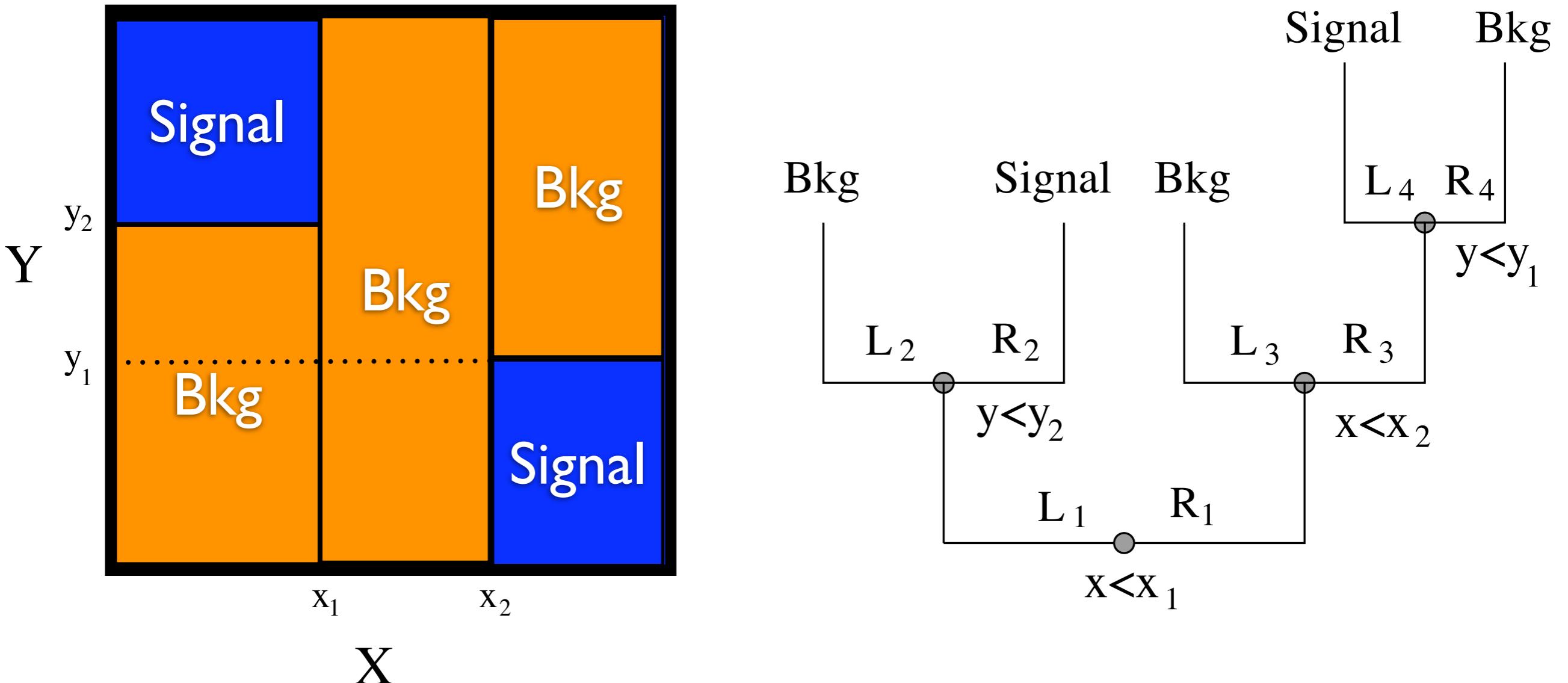
- data/mc agreement holds on regions dominated by the backgrounds:



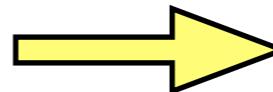
# Single Top Search



# Toy Decision Tree

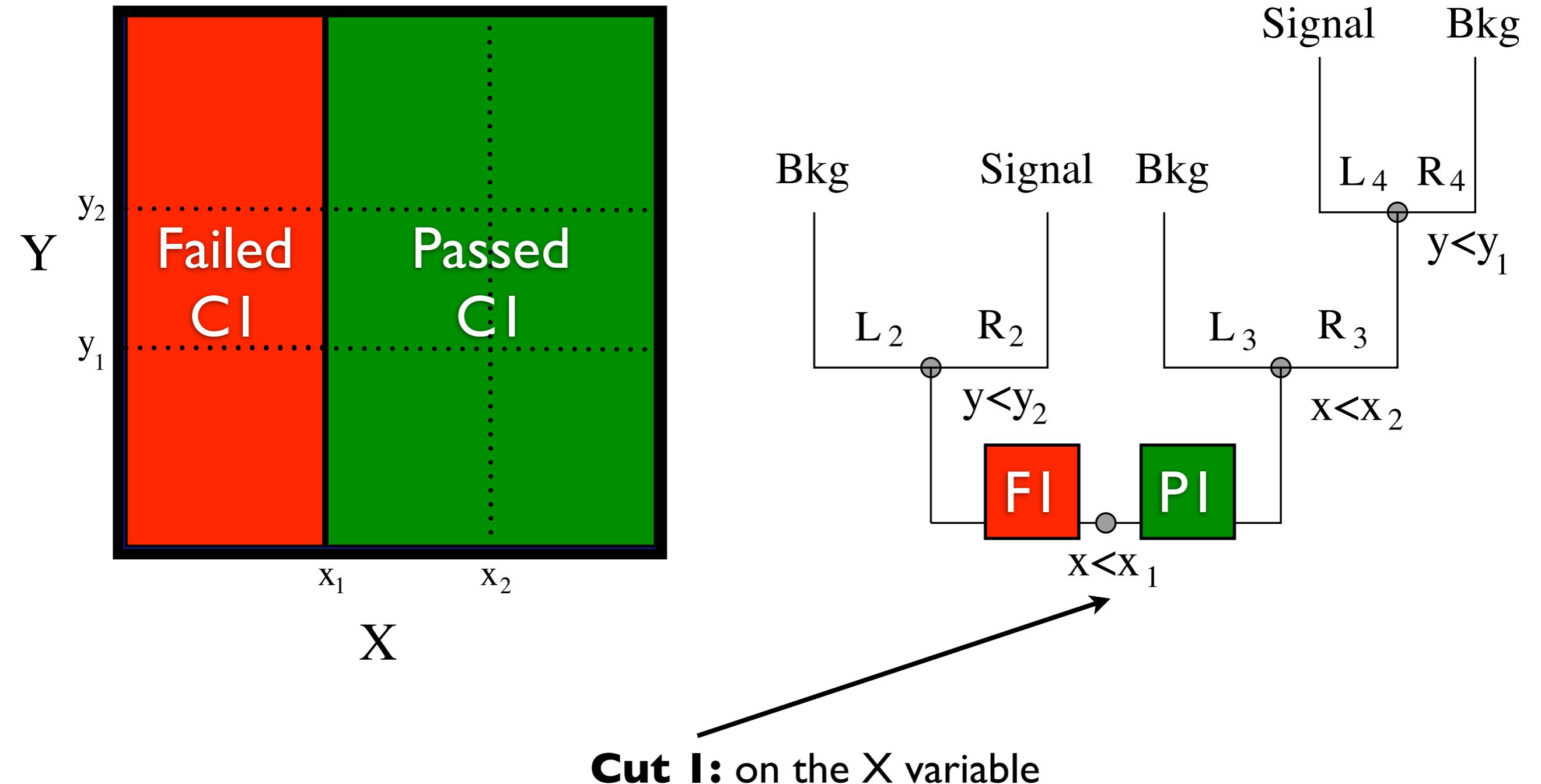


**Task:** separate signal from background  
**Issue:** A single cut on X or Y does not work!

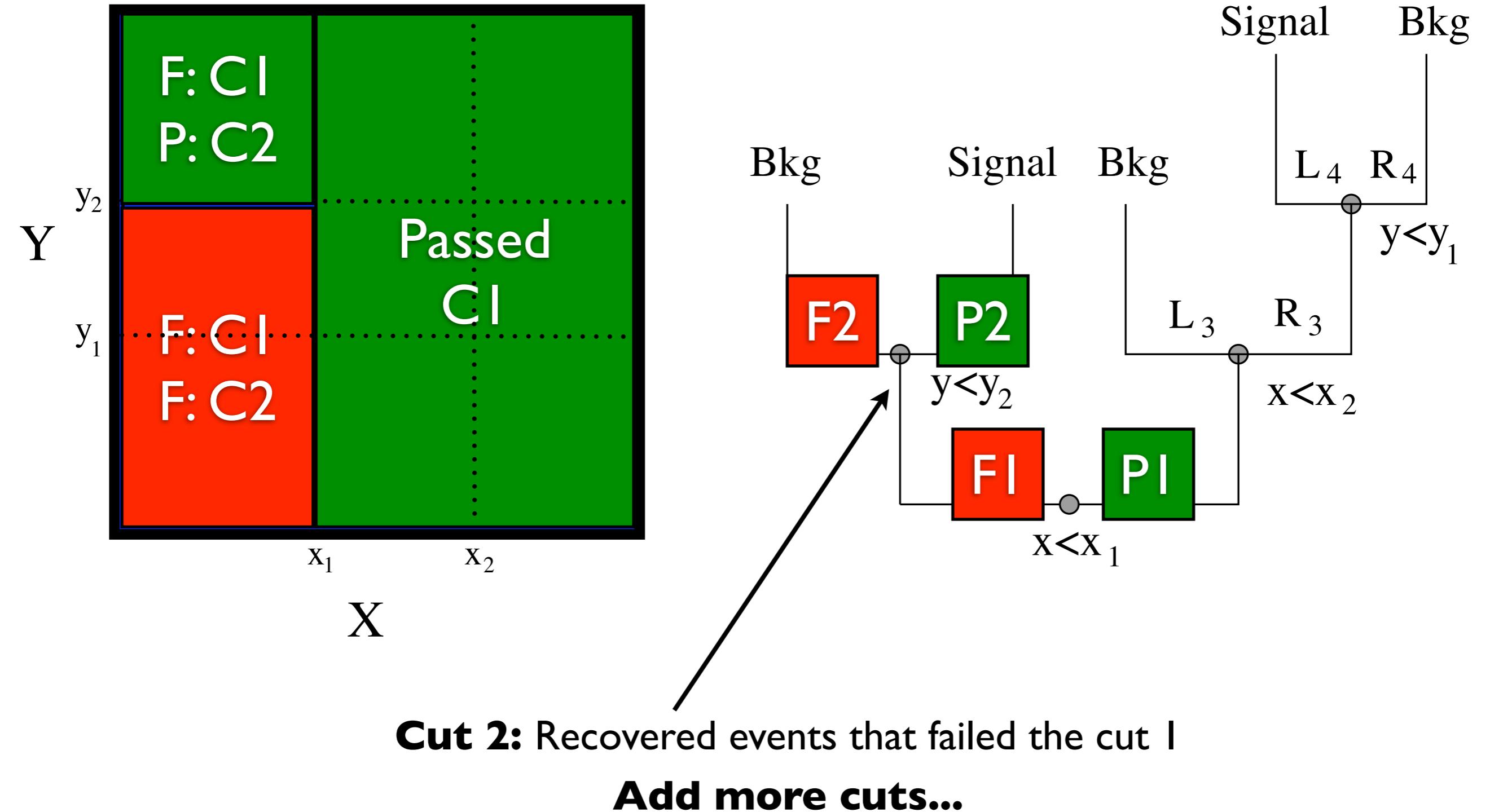


**Solution:** Use a series of consecutive cuts, generating a tree structure

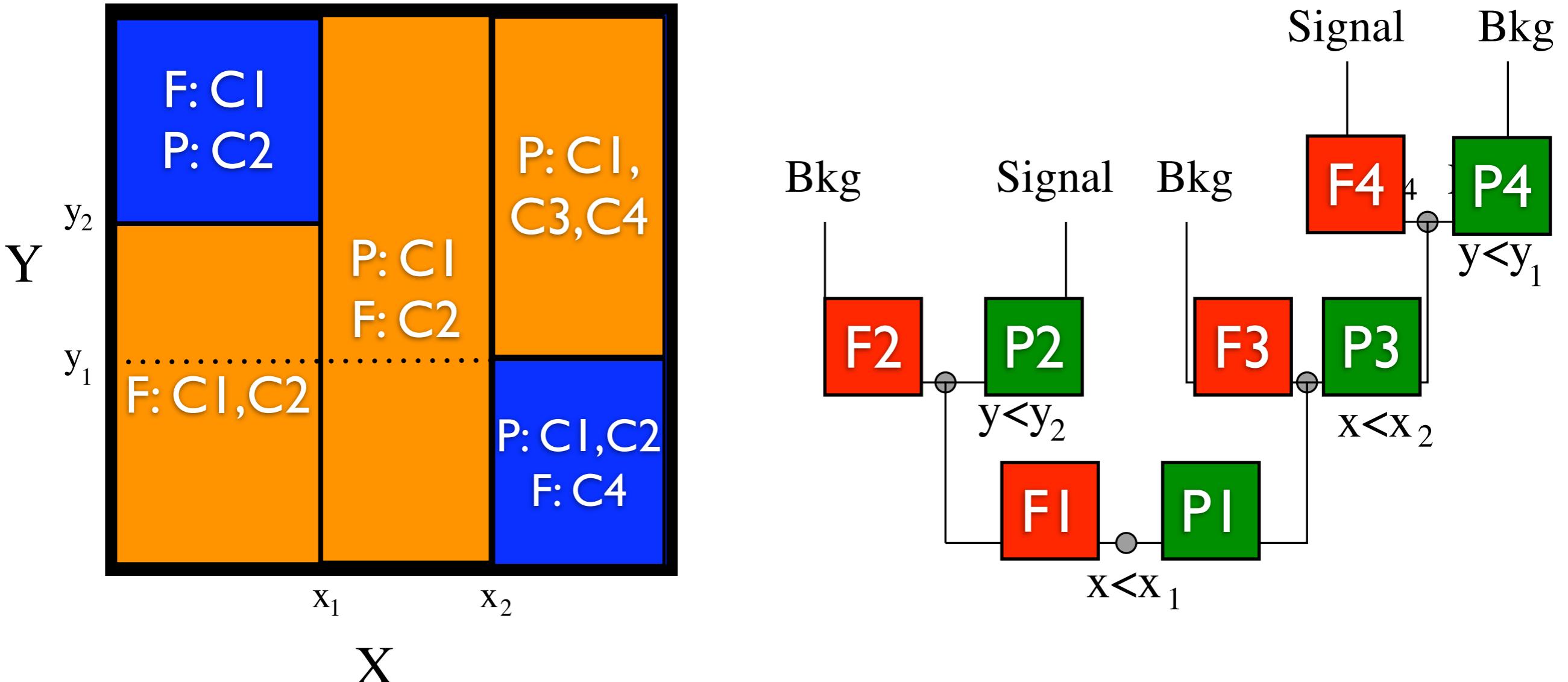
# Toy Decision Tree



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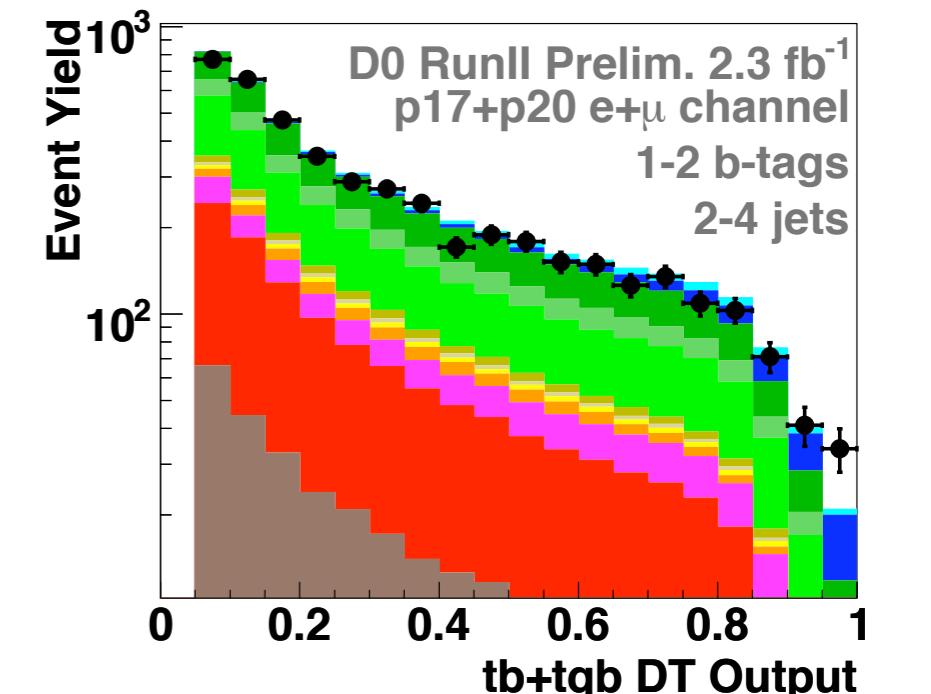
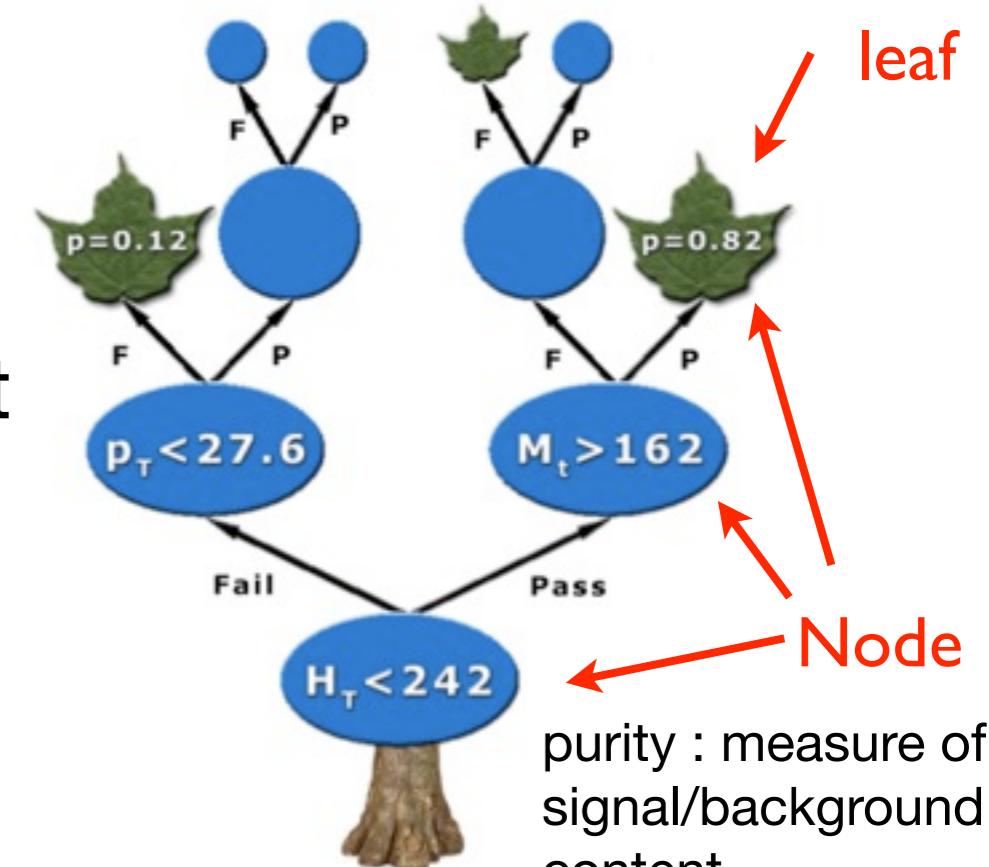


**After 4 cuts:** Signal and Background regions are separated! Done!

**Toy model:** only 2 variables, easy to determine cut values

# Boosted Decision Trees

- Starting from a list of ~ 500 variables, select only well-modeled variables, and those with the highest discriminating power. This procedure results in a final list of **64 variables**
- **Goal:** Recover events that fail a simple cut-based analysis
- Each event will follow a particular path through the DT and will end up in a “leaf”. The associated purity of the “leaf” corresponds to the discriminant output
- **Boosting:** Retrain 50 times to improve separation power, giving increasing importance to hard to classify events



# BDTs: Training and Boosting

## Training: (MC only!)

1. Signal and Background are normalized to the same value
2. Create the first node
3. Sort all events according to each variable
4. Select the variable and variable value that best split the sample. The splitting results into two child nodes
5. If no split possible, node becomes a leaf
6. Apply steps 3 to 6 recursively

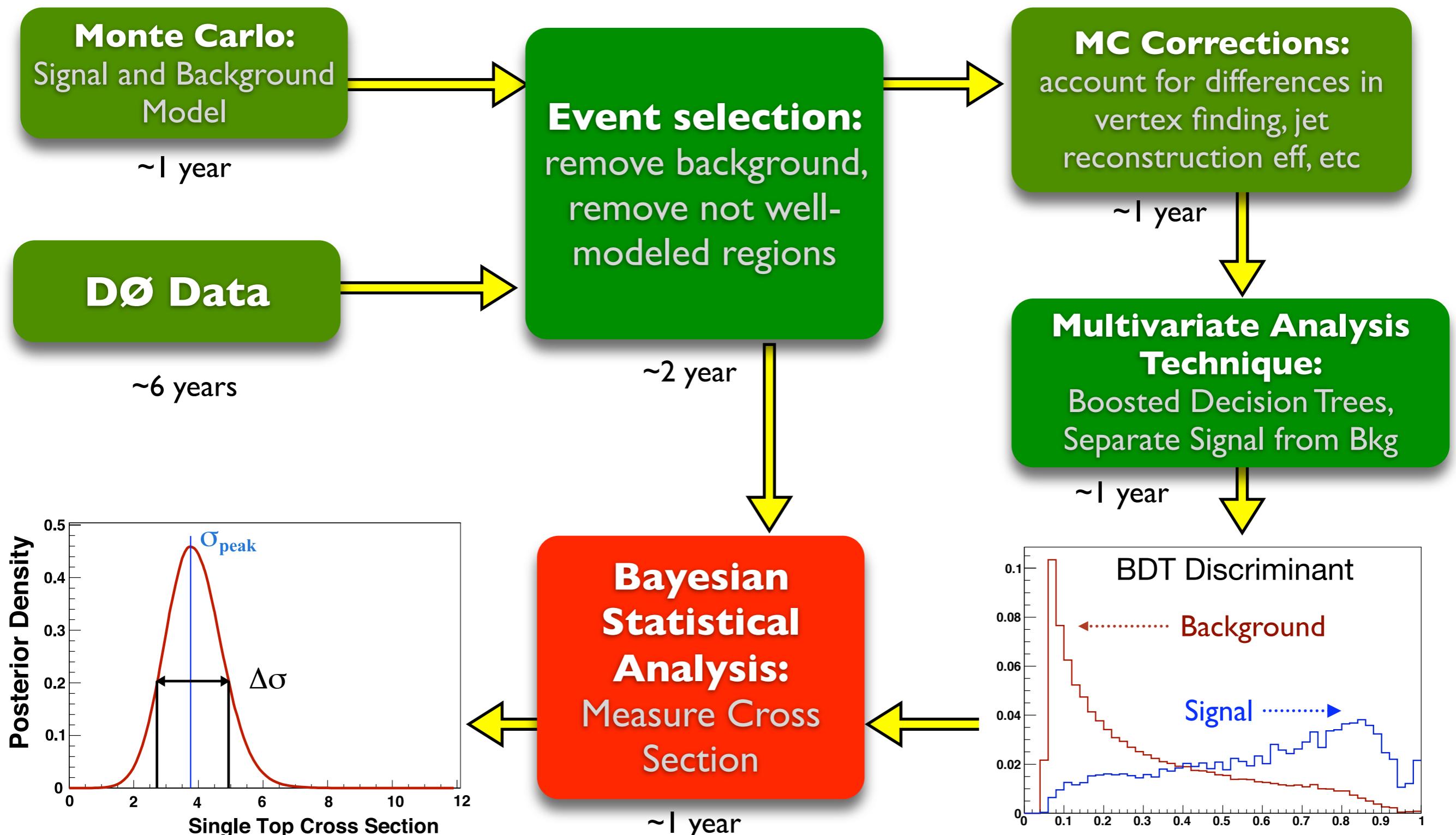
## Boosting:

1. Tree  $T_n$  is trained
2. Calculate the Tree weight  $a_n$ , based on the Tree missclassification rate
3. Events are reweighted according to  $a_n$ , such that misidentified events are assigned a higher weight
4. Tree  $T_{n+1}$  is built from the reweighted events

Final boosted result is

$$\sum(a_n T_n)$$

# Single Top Search

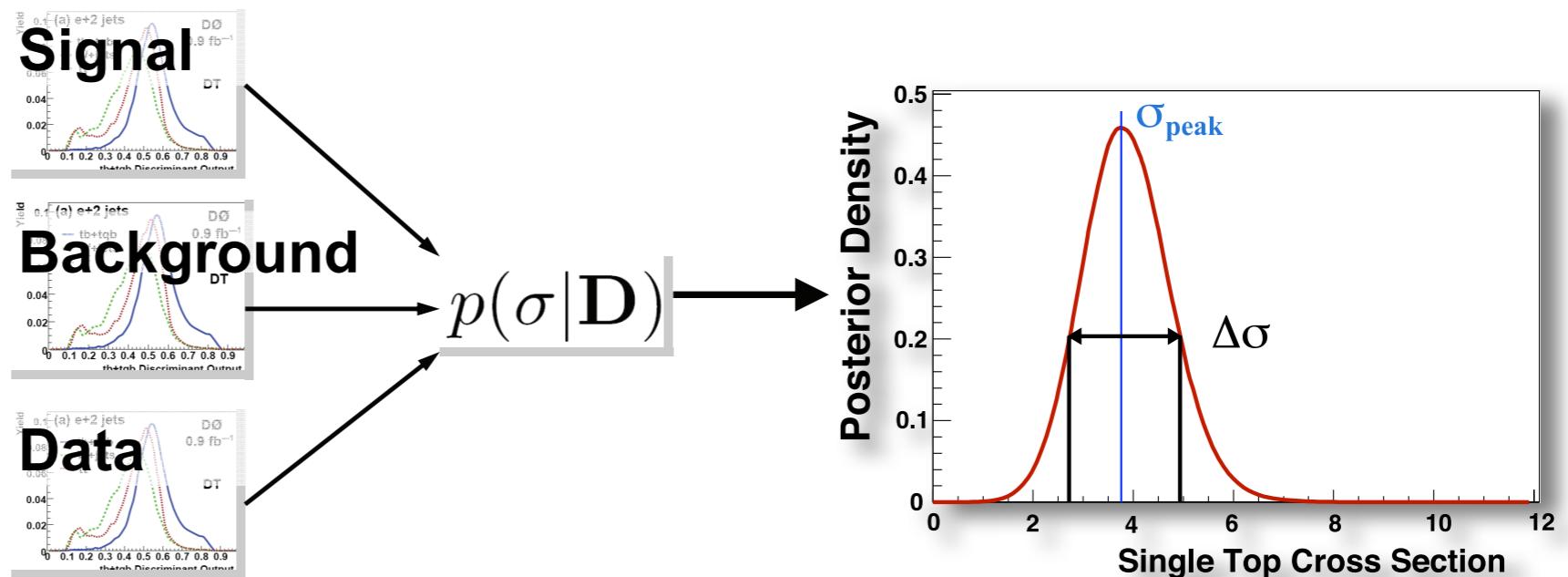


# Measuring Cross Section

A binned likelihood is used to measure the cross section from the observed binned discriminant distribution.

For a particular bin, the probability to observe  $D$  events, given  $d$  expected events is given by the Poisson distribution:

$$p(D|d) = \frac{e^{-d} d^D}{\Gamma(D+1)}$$



The likelihood for  $M$  bins, corresponds to the product of all bins likelihoods

$$\begin{aligned} L(D|d) &\equiv L(D|\sigma, a, b) \\ &= \prod_{j=1}^M L(D_j|d_j) \end{aligned}$$

From Bayes' Theorem the cross section posterior probability:

$$p(\sigma|D) = \frac{1}{N\sigma_{\max}} \iint L(D|\sigma, a, b) \pi(a, b) da db$$

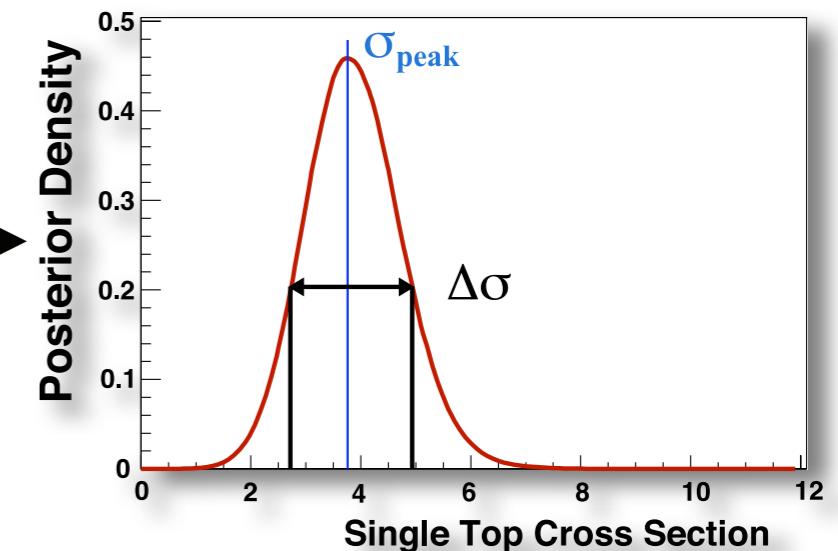
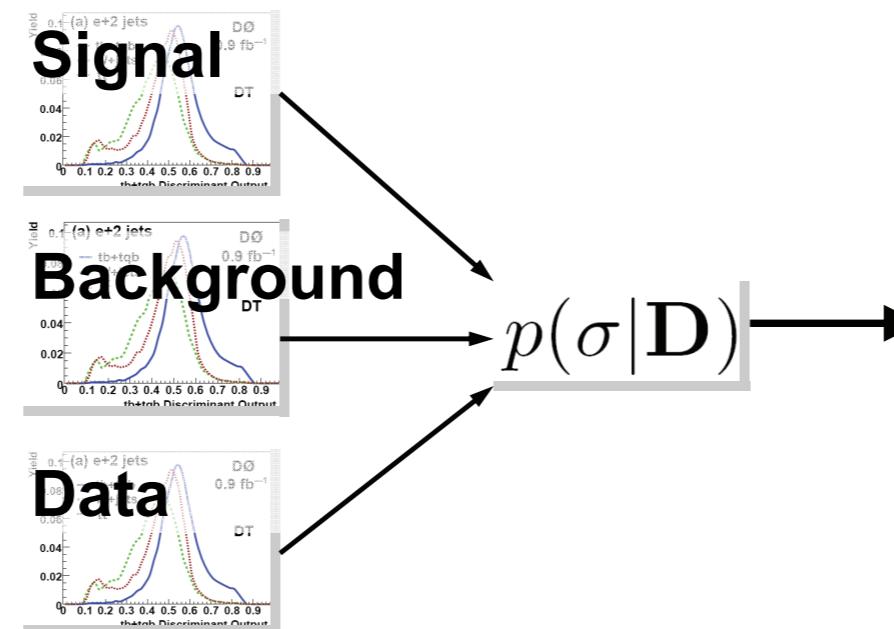
Cross Section    
 Observed Data    
 Signal Acceptance    
 Background    
 Probability of the Signal or Bkg

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$$p(D|d) = \frac{e^{-d} d^D}{\Gamma(D+1)}$$



The likelihood for  $M$  bins, corresponds to the product of all bins likelihoods

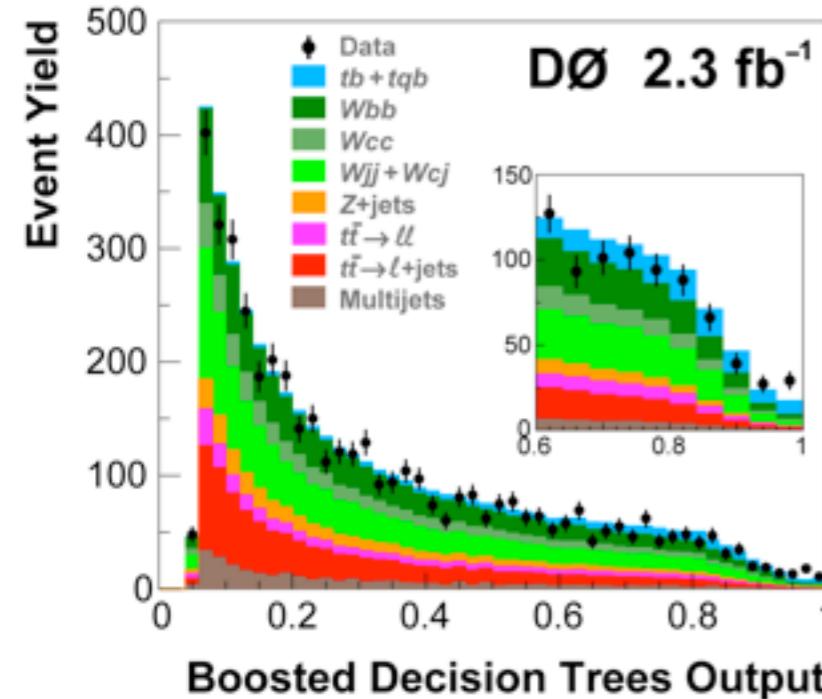
$$\mathcal{L}(D|d) \equiv \mathcal{L}(D|\sigma, a, b)$$

$$= \prod_{j=1}^M \mathcal{L}(D_j|d_j)$$

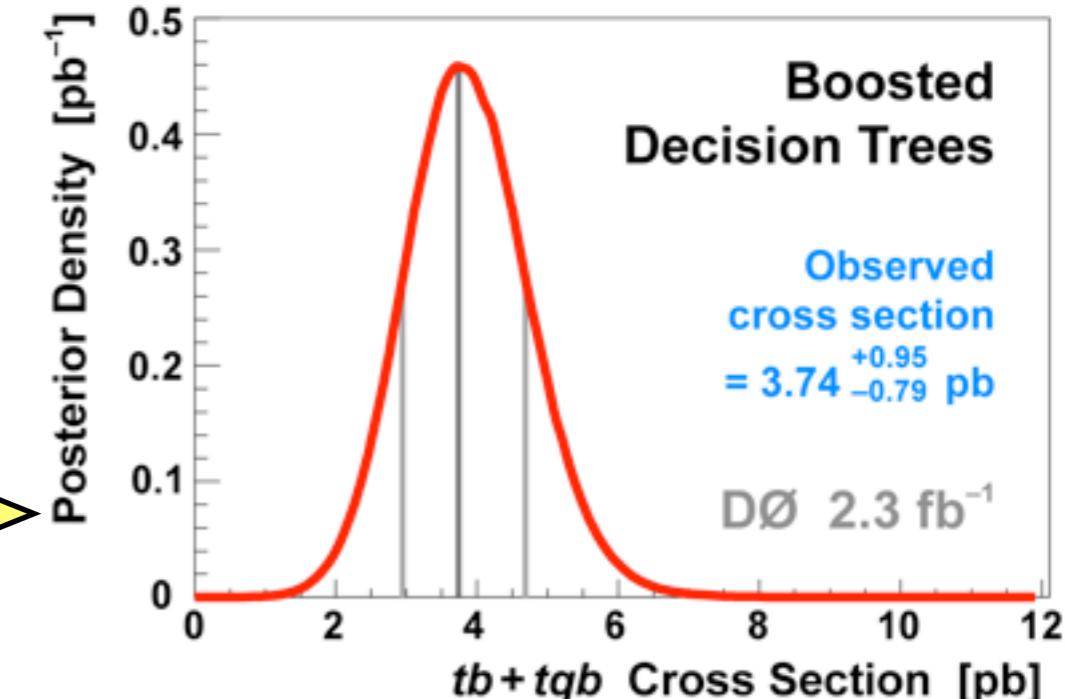
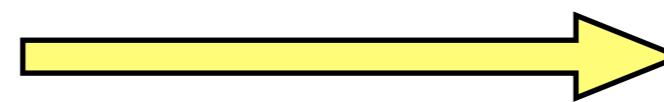
which can be estimated numerically by sampling the prior  $\pi(a, b)$

$$p(\sigma|D) \sim \frac{1}{N\sigma_{max}} \frac{1}{K} \sum_{k=1}^K L(D|\sigma, a_k, b_k)$$

# Cross Section Measurement

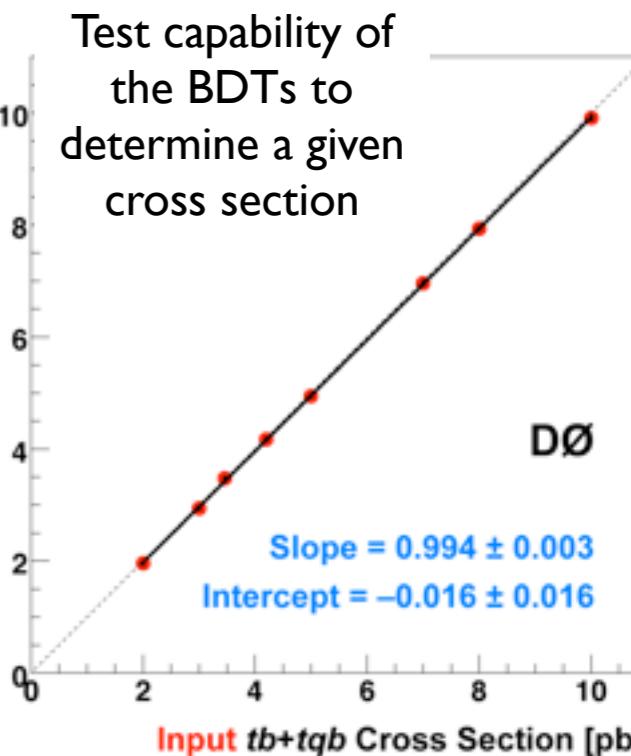
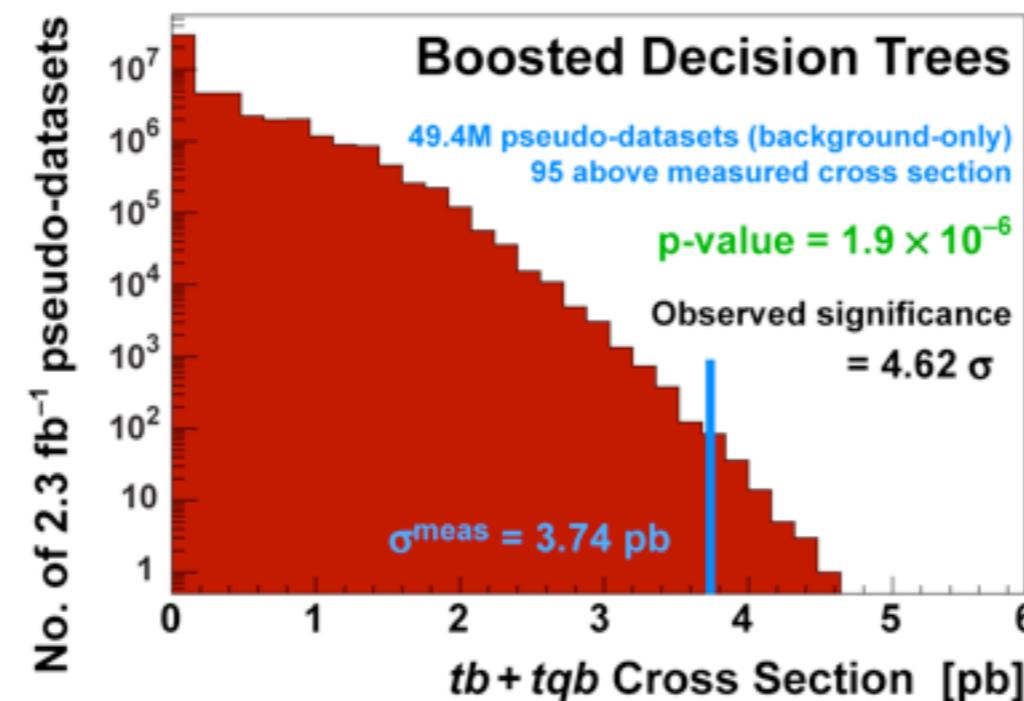


Using Bayesian  
Statistical analysis,  
including all  
systematics and  
their correlations

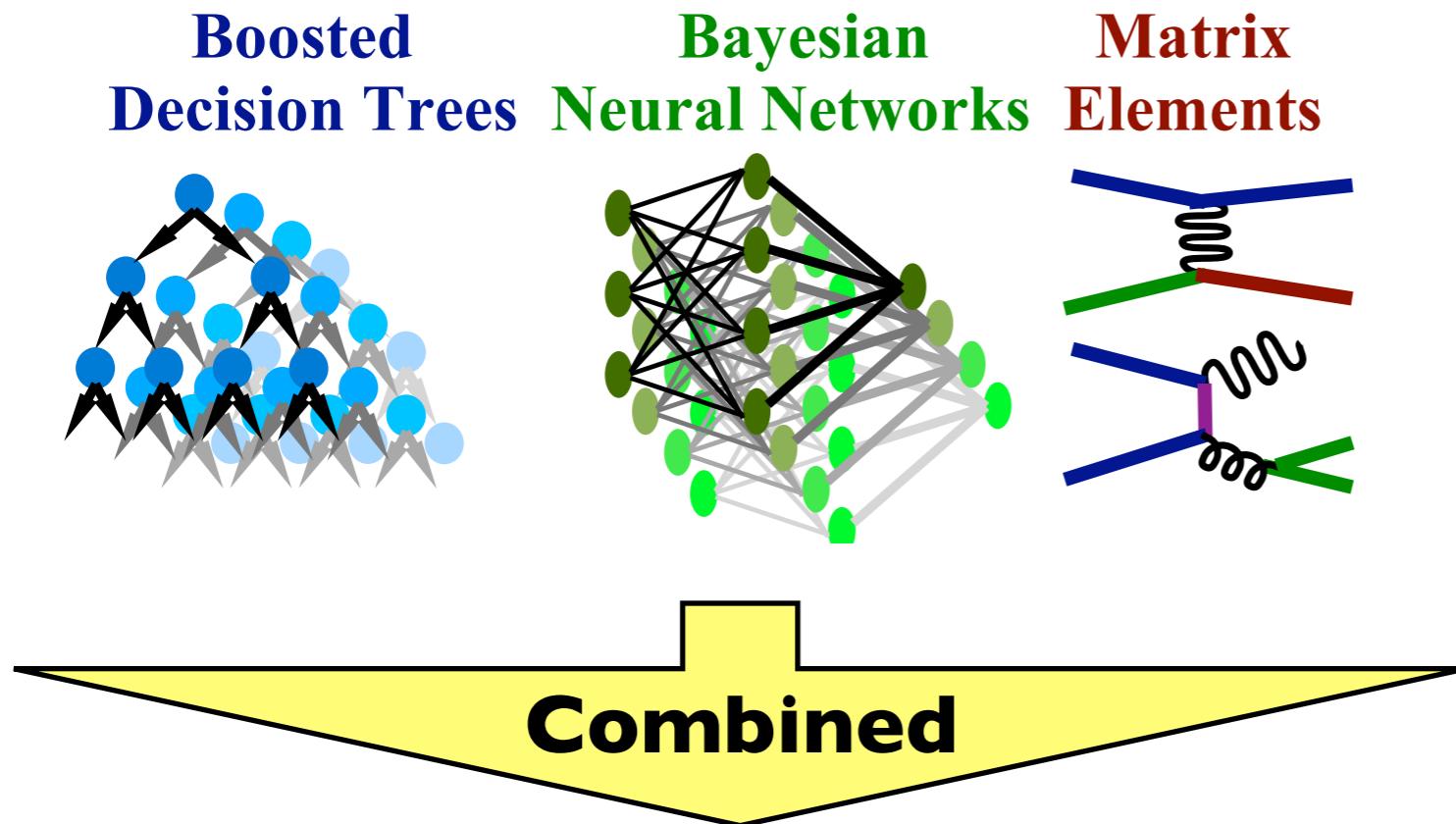


Significance of the measurement is estimated using psuedo-datasets that contain only the background model and all systematic uncertainties.

Count how many psuedo-datasets have a cross section higher than the observed measurement

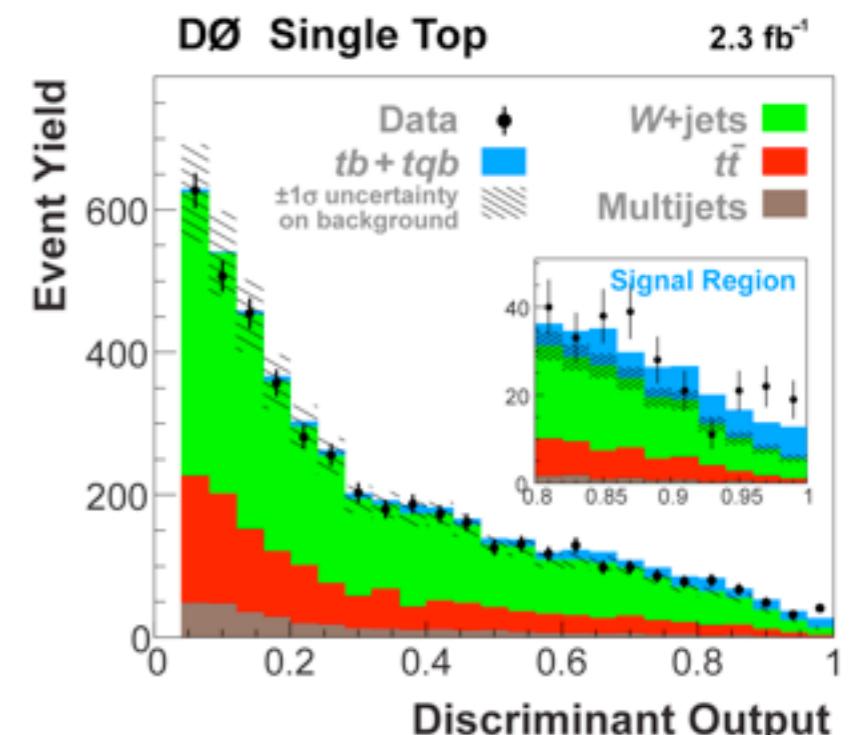


# Additional Multivariate Analyses



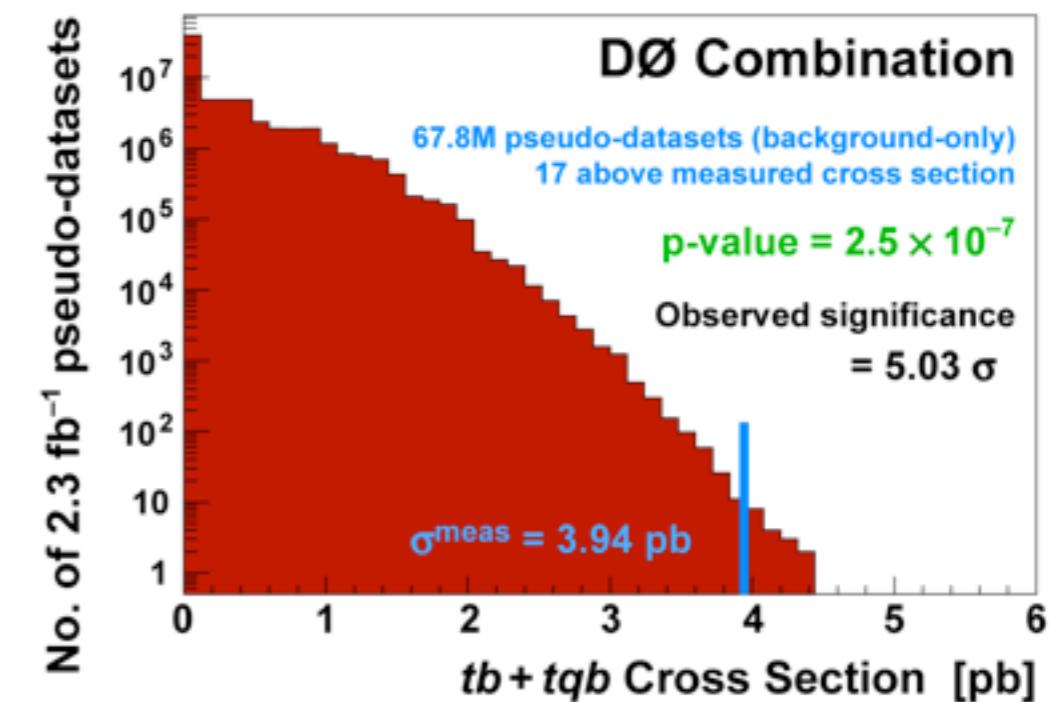
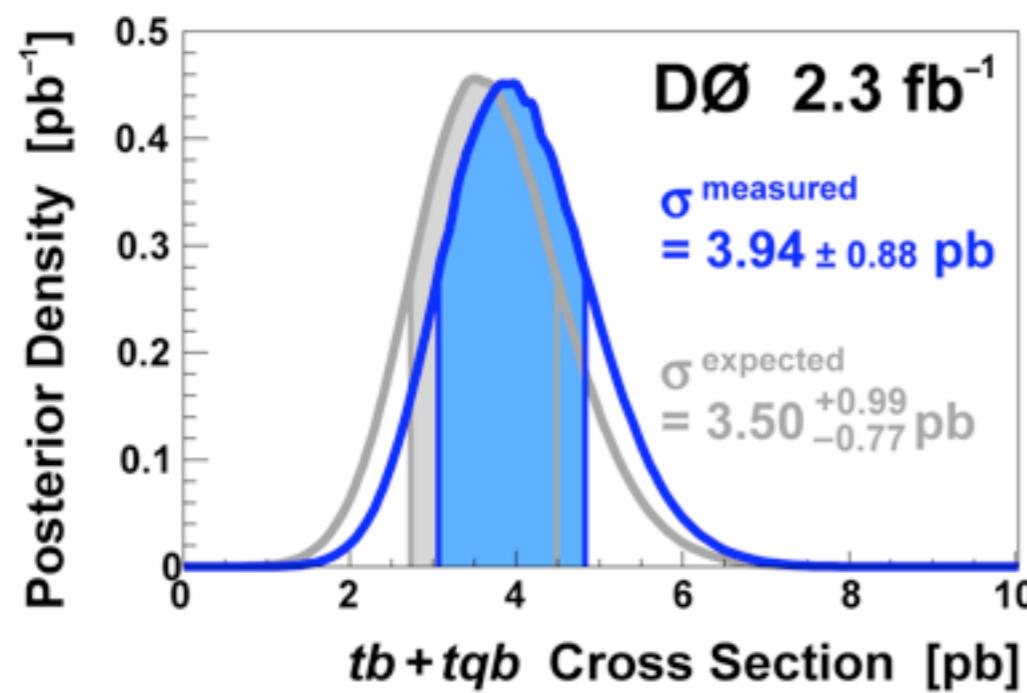
Using a Bayesian Neural Network that considers the individual analyses discriminant outputs as inputs to the Network. Purpose is to extract all possible information from the DØ data set.

The Combination BNN produces a discriminant output, from where a cross section measurement is obtained



# Cross Section Measurements

DØ 2.3 fb <sup>-1</sup> Single Top Results			
Analysis Method	Single Top Cross Section	Significance	
		Expected	Measured
Boosted Decision Trees	3.74 $^{+0.95}_{-0.79}$ pb	4.3 $\sigma$	4.6 $\sigma$
Bayesian Neural Networks	4.70 $^{+1.18}_{-0.93}$ pb	4.1 $\sigma$	5.4 $\sigma$
Matrix Elements	4.30 $^{+0.99}_{-1.20}$ pb	4.1 $\sigma$	4.9 $\sigma$
Combination	$3.94 \pm 0.88$ pb	4.5 $\sigma$	5.0 $\sigma$



# $|V_{tb}|$ measurement

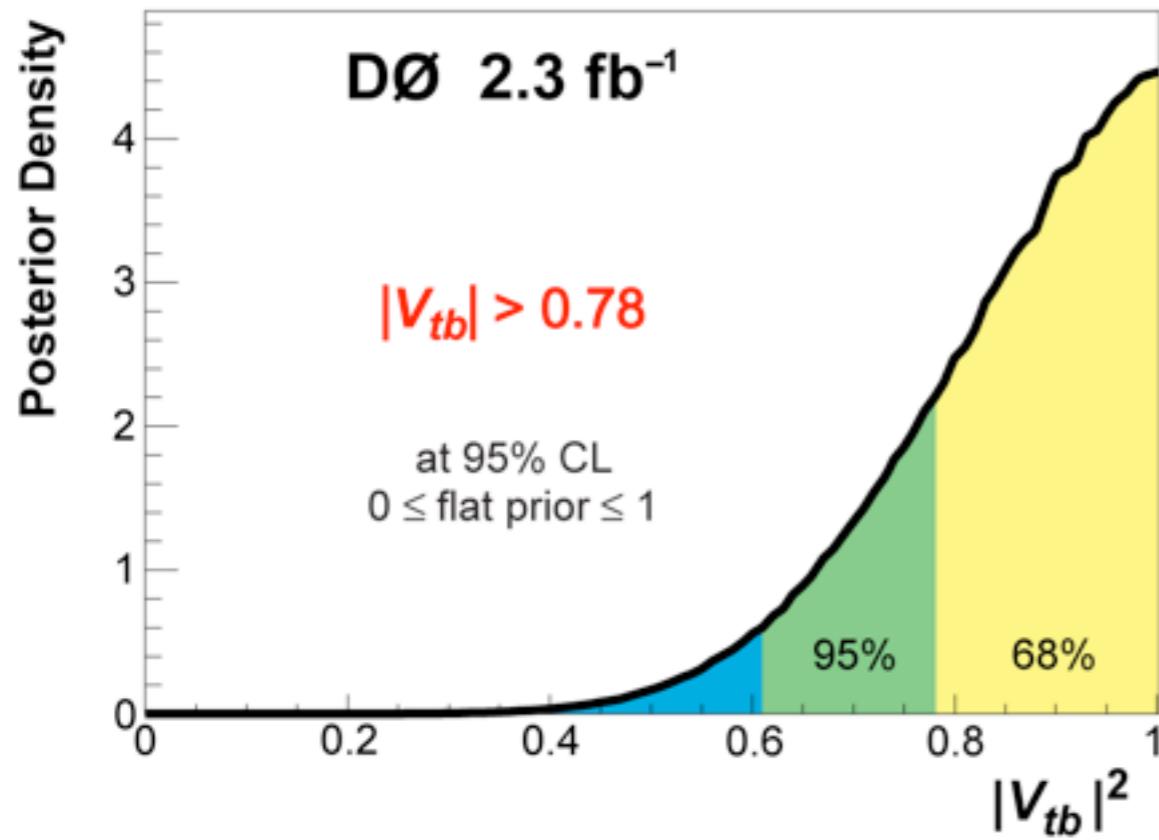
General form of the  $|V_{tb}|$  vertex:

$$\Gamma_{Wtb}^\mu = -\frac{g}{\sqrt{2}} \textcolor{red}{V_{tb}} \left\{ \gamma^\mu [f_1^L P_L + f_1^R P_R] - \frac{i\sigma^{\mu\nu}}{M_W} (p_t - p_b)_\nu [f_2^L P_L + f_2^R P_R] \right\}$$

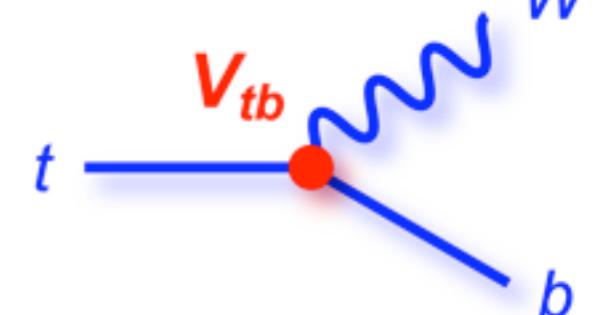
$|f_1^L V_{tb}|$  proportional to the Single Top cross section

within the SM :

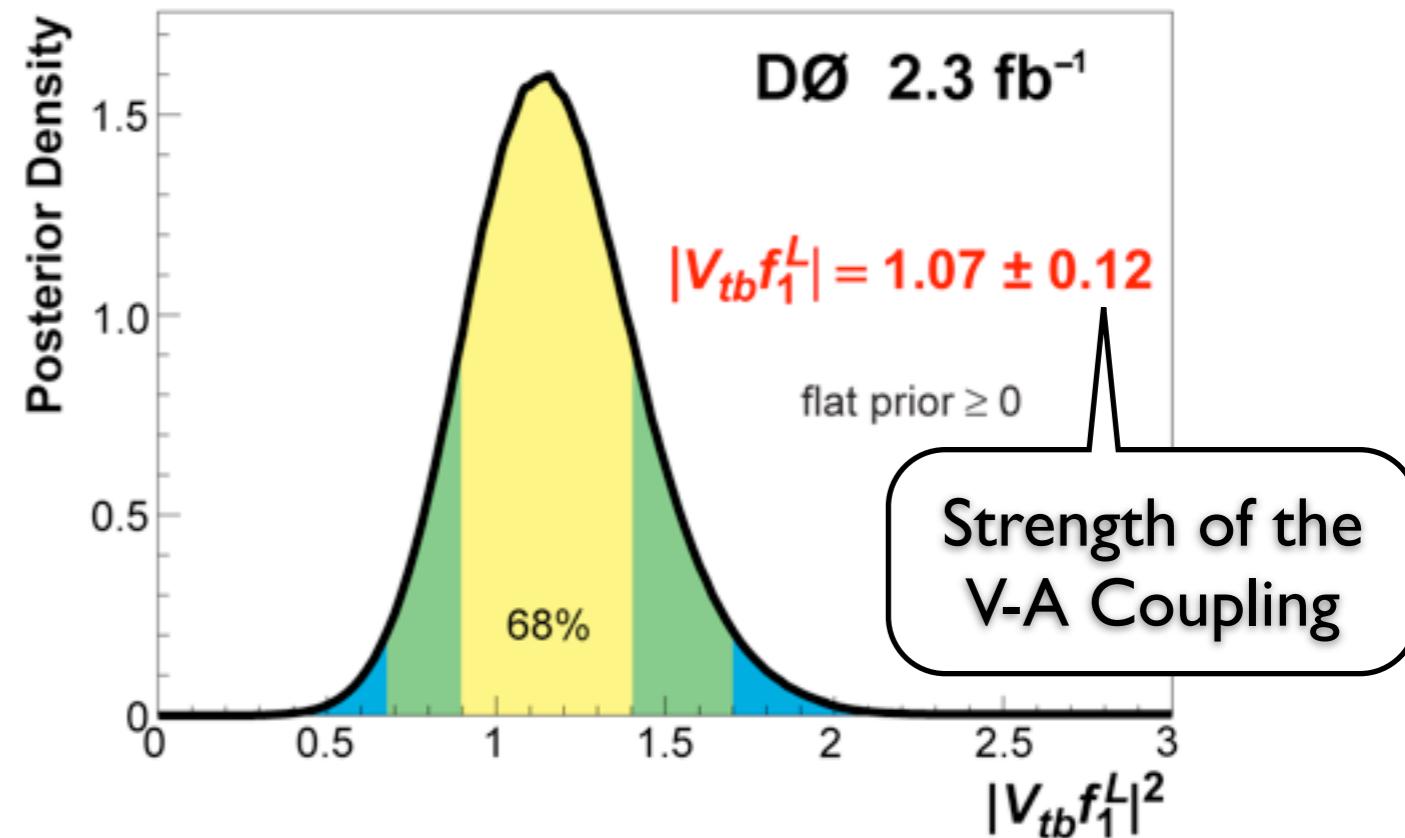
$$f_1^L = 1, f_1^R = f_2^L = f_2^R = 0$$



$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & \textcolor{red}{V_{tb}} \end{pmatrix}$$



removing the constrain  $[0, 1]$  :



# Conclusion

- Using  $2.3 \text{ fb}^{-1}$  of data collected with the DØ detector at the Fermilab Tevatron Collider and Boosted Decision Trees to separate the Single Top signal from the background, the Single Top cross section is measured to be:

$$\sigma(p\bar{p} \rightarrow tb + X, tqb + X) = 3.74^{+0.95}_{-0.74} \text{ pb},$$

where the errors include both systematic and statistical uncertainties

- Combining three Single Top analysis the corresponding Single Top cross section is measured to be:

$$\sigma(p\bar{p} \rightarrow tb + X, tqb + X) = 3.94 \pm 0.88 \text{ pb},$$

- The probability to measure a cross section at this value or higher in the absence of signal is  $p = 1.9 \times 10^{-6}$ . This corresponds to a significance of **5.03 standard deviations**
- A PRL paper containing the result has been accepted for publication. [arXiv:0903.0850](https://arxiv.org/abs/0903.0850)
- DØ has more than  $5 \text{ fb}^{-1}$  of data to analyze from where new physics can be studied, and more precise single top measurements can be done

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### Calendar

Wednesday, March 11  
3:30 p.m.  
DIRECTOR'S COFFEE  
BREAK - 2nd Flr X-Over  
4 p.m.  
[Fermilab Colloquium](#) - One  
West  
Speaker: R. Sekhar  
Chivukula, Michigan State  
University



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**Fermilab collider experiments discover rare single top quark**

March 9th, 2009

### Special Result of the Week

**Single and loving it!**

CERN COURIER



**symmetrybreaking**  
extra dimensions of particle physics

A joint Fermilab/SLAC publication

Fermilab collider experiments discover rare single top quark

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**SINGLE TOP QUARK DISCOVERY**

Same technique used to find the Higgs boson

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**MSU scientists help lead teams in detection of fundamental component of matter**



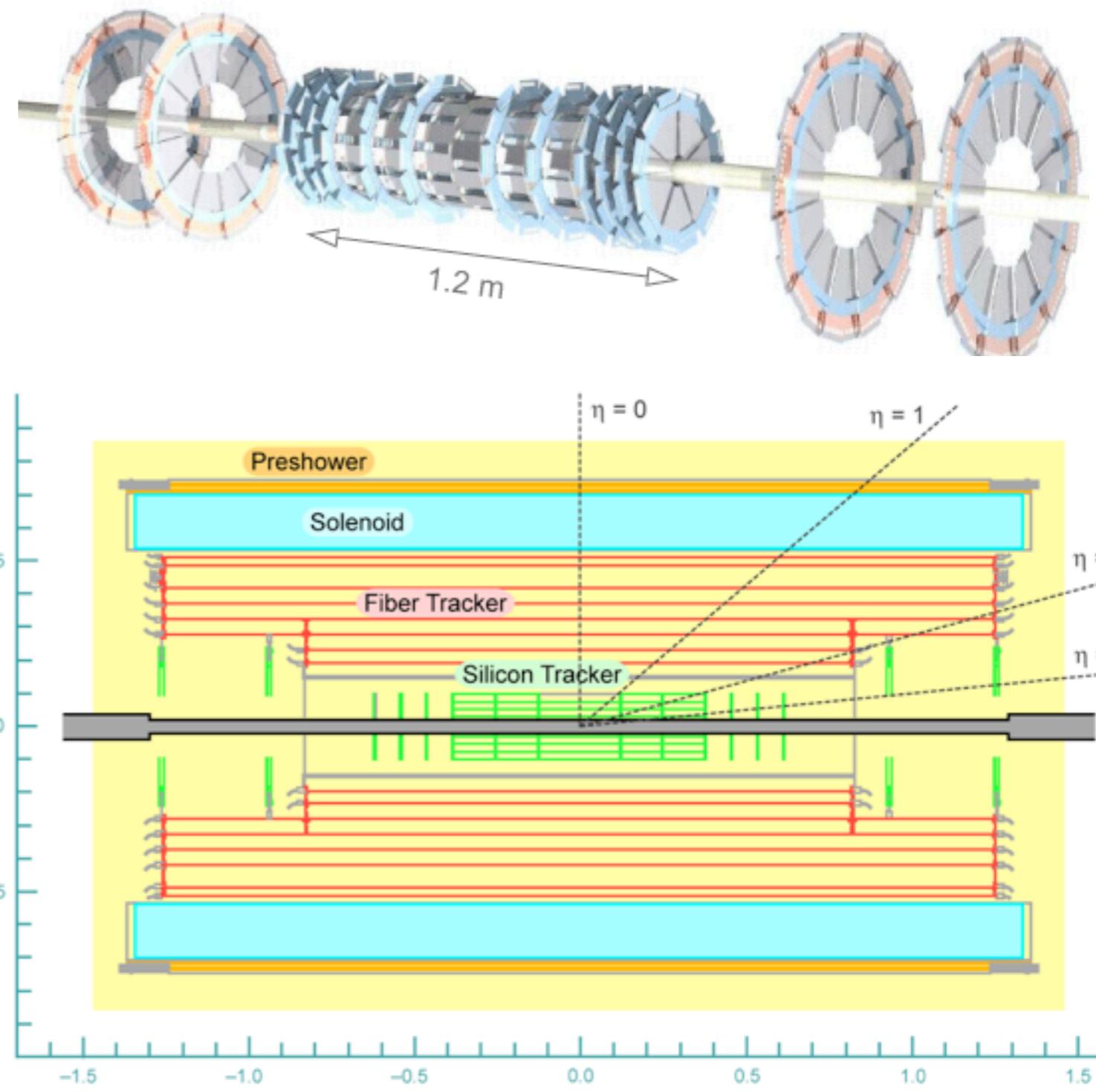
# Thank You

---

- Chip for his support and words of wisdom that guided me through graduate school.
- Reinhard for getting me into Single Top, leading the way to the discovery, and incredible motivational techniques
- Committee members for reviewing my dissertation
- The DØ Single Top group and the BDT team.  
Specially to Dag, Dugan, Monica, Andres, Liang, Ernest, Ann, Cecilia.
- Friends and Family for their support and good company
- Catherine for her patience and for being my tower of strength

# Extra Slides

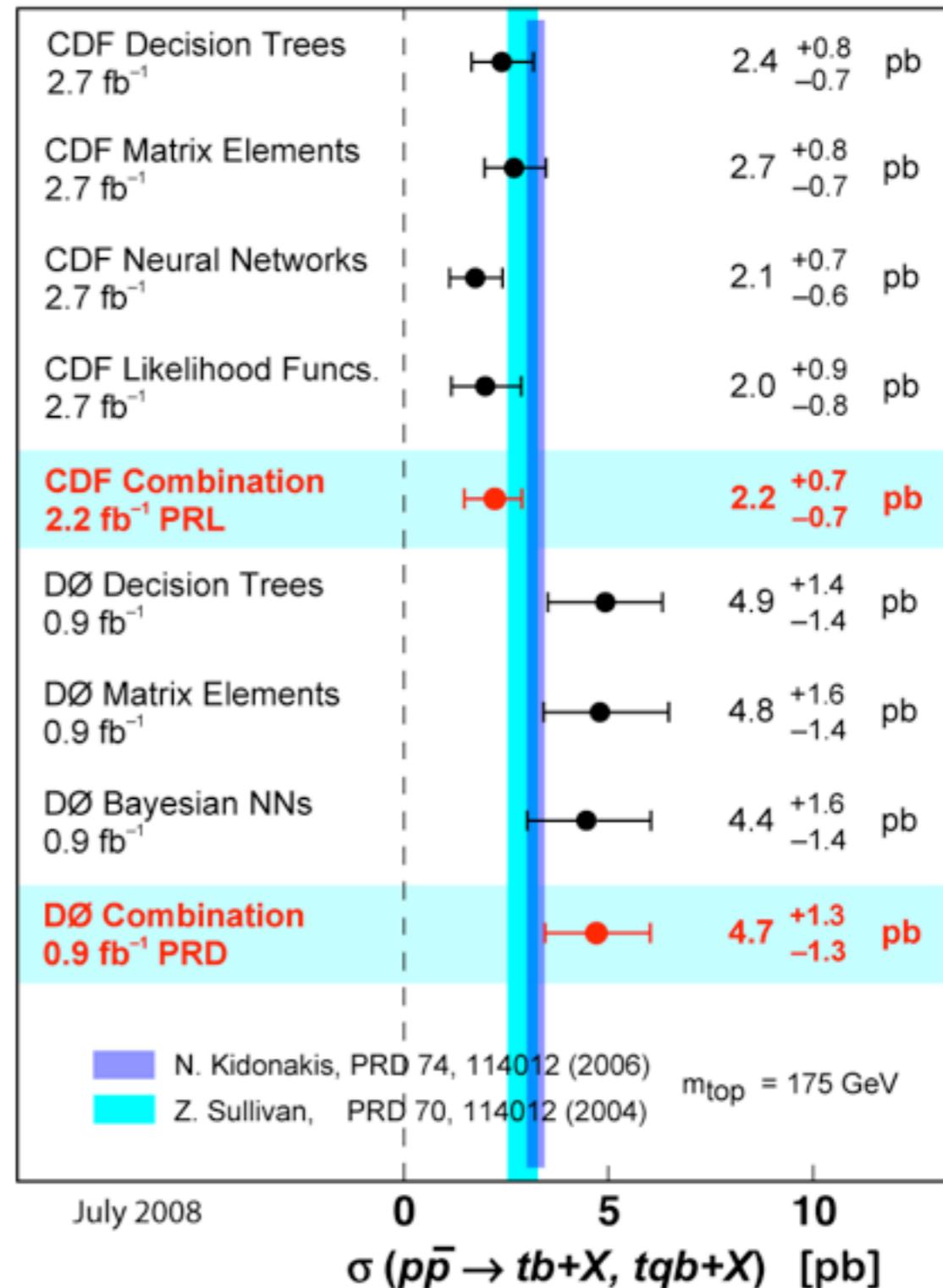
# DØ Detector



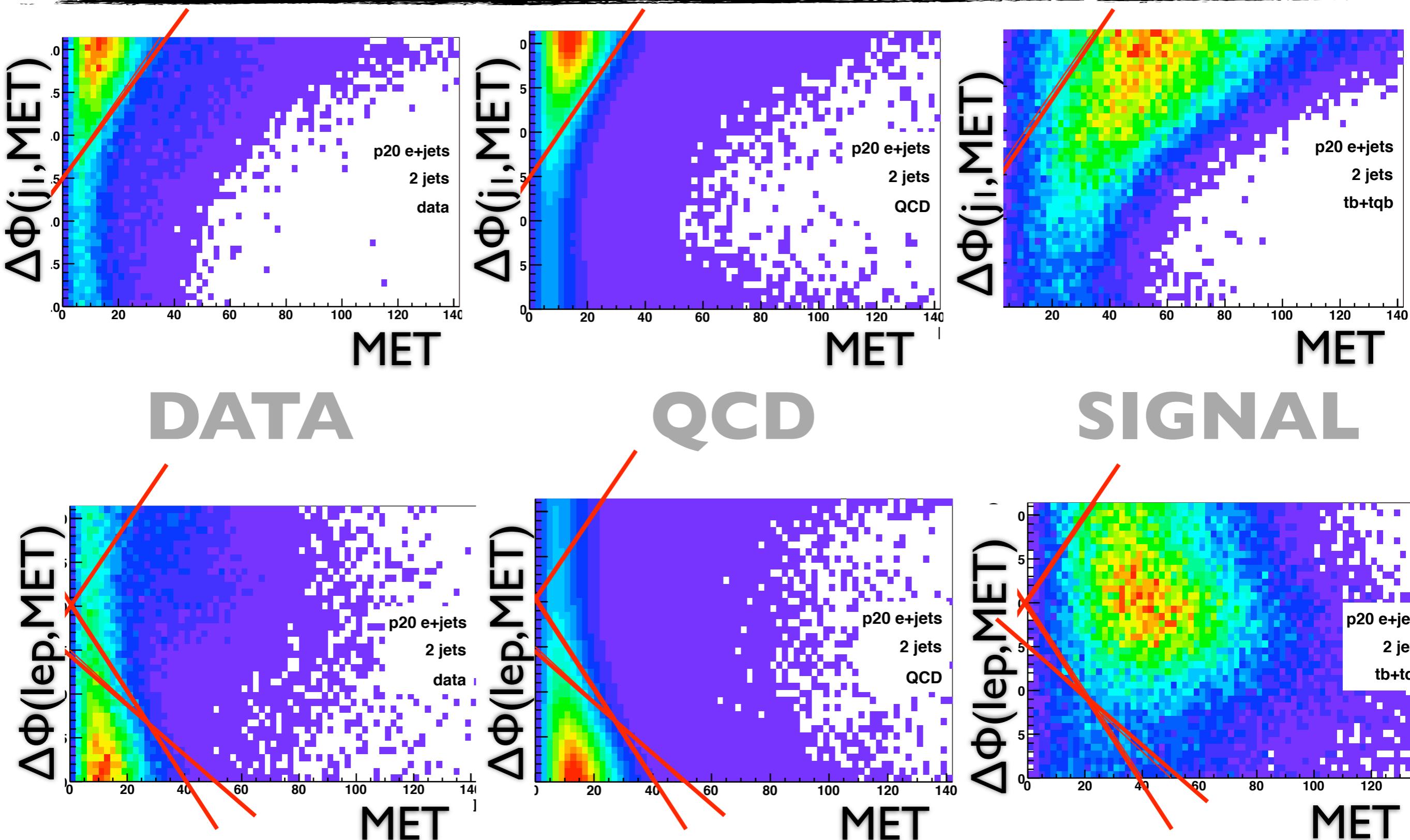
# Previous Single Top Results

Single Top Cross Section	Signal Significance		CKM Matrix Element $V_{tb}$
	Expected	Observed	
<b>December 2006 DØ (0.9 fb<sup>-1</sup>)</b>		PRL 98, 181802 (2007)	
$4.7 \pm 1.3$ pb	$2.3\sigma$	$3.6\sigma$	$ V_{tb}f_1^L  = 1.31^{+0.25}_{-0.21}$ $ V_{tb}  > 0.68$ at 95% CL
<b>September 2008 CDF (2.2 fb<sup>-1</sup>)</b>		PRL 101, 252001 (2008)	
$2.2 \pm 0.7$ pb	$4.9\sigma$	$3.7\sigma$	$ V_{tb}f_1^L  = 0.88^{+0.13}_{-0.12}$ $ V_{tb}  > 0.66$ at 95% CL

CDF and DØ tb+tqb Cross Section



# Triangular Cuts



# QCD Determination

---

- Using Reverse Isolation sample: (Traditional)

$$\text{QCD} = \text{Loose} - \text{Tight}$$

- Enlarge sample:

- Remove the  $\Delta R$  requirement from the loose sample:

$$\text{QCD} = \text{SuperLoose (no } \Delta R) - \text{Tight}$$

- In addition:

- Correct kinematical distributions by removing jets that are within  $\Delta R < 0.5$  of the muon.
    - Properly account for the removed jet MET
    - Sample statistics increases by a factor of  $\sim 10!$

# W+jet and QCD normalization

- The total number of pre-tagging data events:

$$Y_{\text{pretagged data}} = S_{W+\text{jets}} * Y_{W+\text{jets}}^{\text{before-IKS}} + Y_{\text{all other MC}} + S_{\text{multijets}} * Y_{\text{multijets}}^{\text{before-IKS}}$$

- Using three variable distributions ( $p_T(\text{lep})$ , MET,  $M_T(W)$ ):

- Scan possible values for  $S_{W+\text{jets}}$  and  $S_{\text{multijets}}$  and select those that give the best KS value

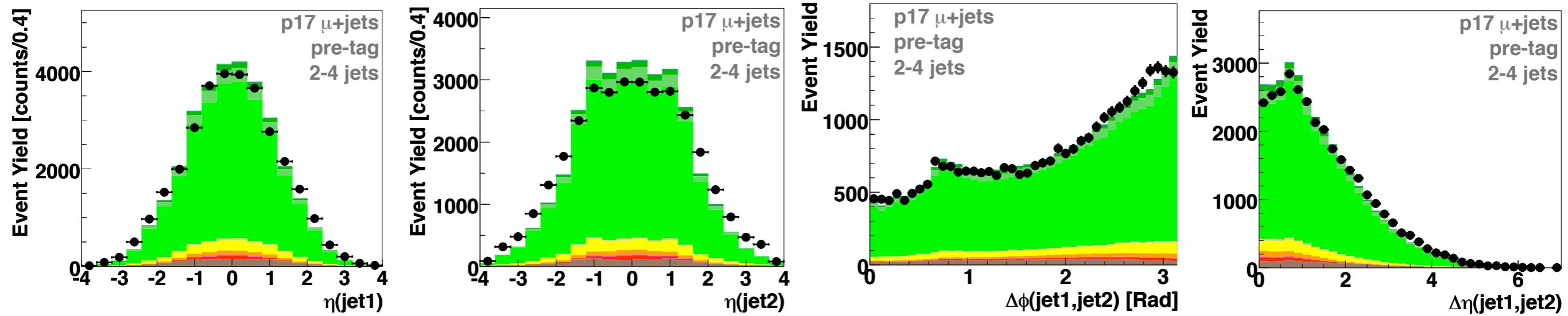
- Average the constant values and scale samples:

$$S_{\text{multijets}} = \frac{\sum_{i=\text{var1}}^{\text{varN}} S_{\text{multijets}}^i * \text{KS}_{\text{max}}^i}{\sum_{i=\text{var1}}^{\text{varN}} \text{KS}_{\text{max}}^i}$$

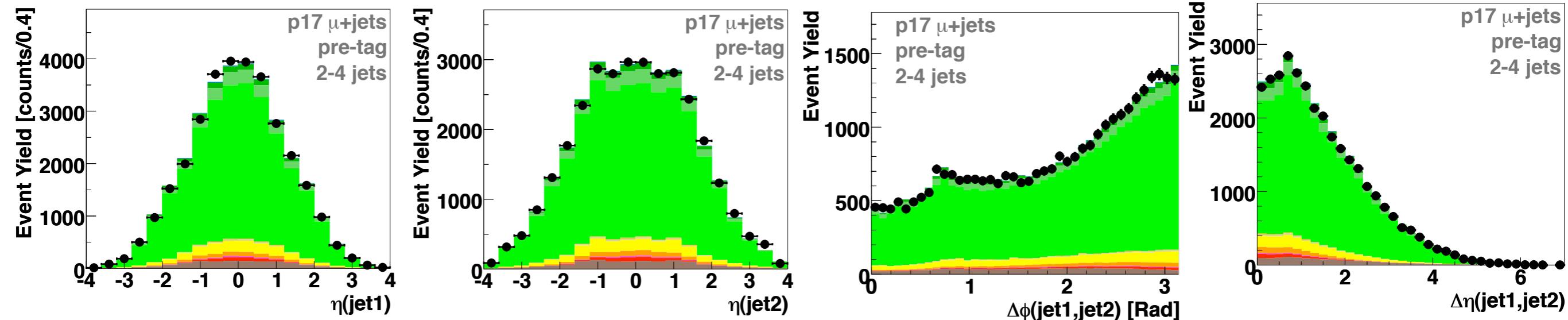
# $W+jets$ re-weighting

- Purpose: correct ALPGEN modeling discrepancies

BEFORE

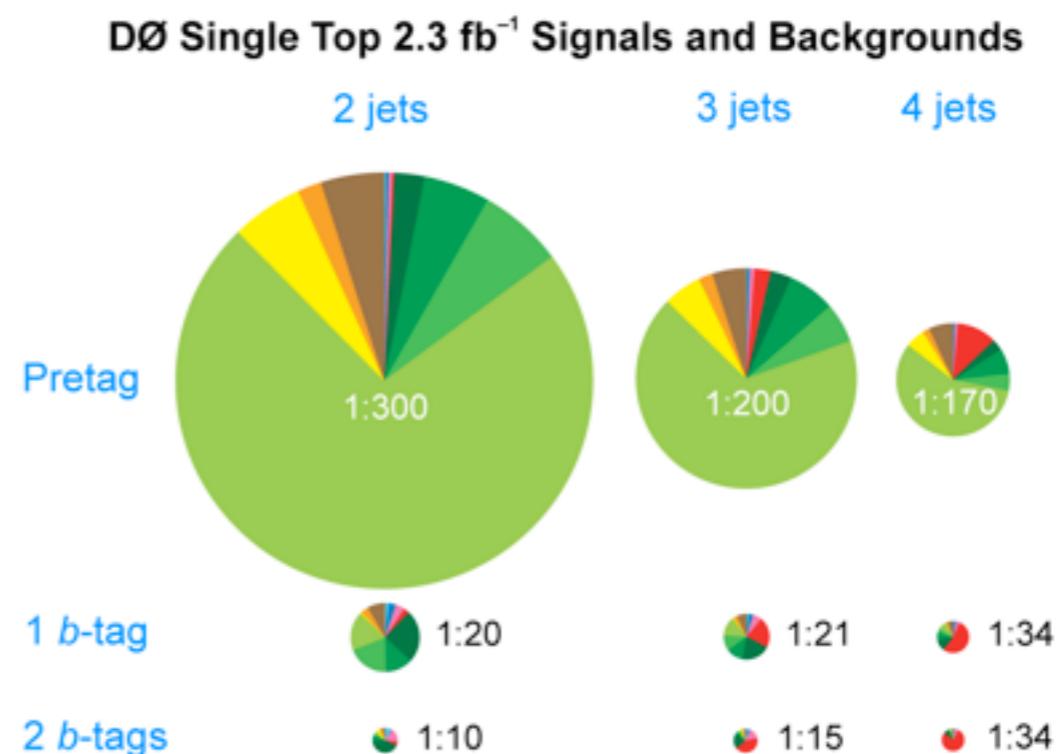


AFTER



# After $b$ -tagging Yields

Event Yields in $2.3 \text{ fb}^{-1}$ of DØ Data			
Source	Electron + muon, 1 tag + 2 tags combined		
	2 jets	3 jets	4 jets
s-channel $tb$	$62 \pm 9$	$24 \pm 4$	$7 \pm 2$
t-channel $tqb$	$77 \pm 10$	$39 \pm 6$	$14 \pm 3$
$W+b\bar{b}$	$678 \pm 104$	$254 \pm 39$	$73 \pm 11$
$W+c\bar{c}$	$303 \pm 48$	$130 \pm 21$	$42 \pm 7$
$W+cj$	$435 \pm 27$	$113 \pm 7$	$24 \pm 2$
$W+jj$	$413 \pm 26$	$140 \pm 9$	$41 \pm 3$
$Z+jets$	$141 \pm 33$	$54 \pm 14$	$17 \pm 5$
Dibosons	$89 \pm 11$	$32 \pm 5$	$9 \pm 2$
$t\bar{t} \rightarrow \ell\ell$	$149 \pm 23$	$105 \pm 16$	$32 \pm 6$
$t\bar{t} \rightarrow \ell+jets$	$72 \pm 13$	$331 \pm 51$	$452 \pm 66$
Multijets	$196 \pm 50$	$73 \pm 17$	$30 \pm 6$
<b>Total prediction</b>	$2,615 \pm 192$	$1,294 \pm 107$	$742 \pm 80$
<b>Data</b>	2,579	1,216	724



# Cross Check Samples

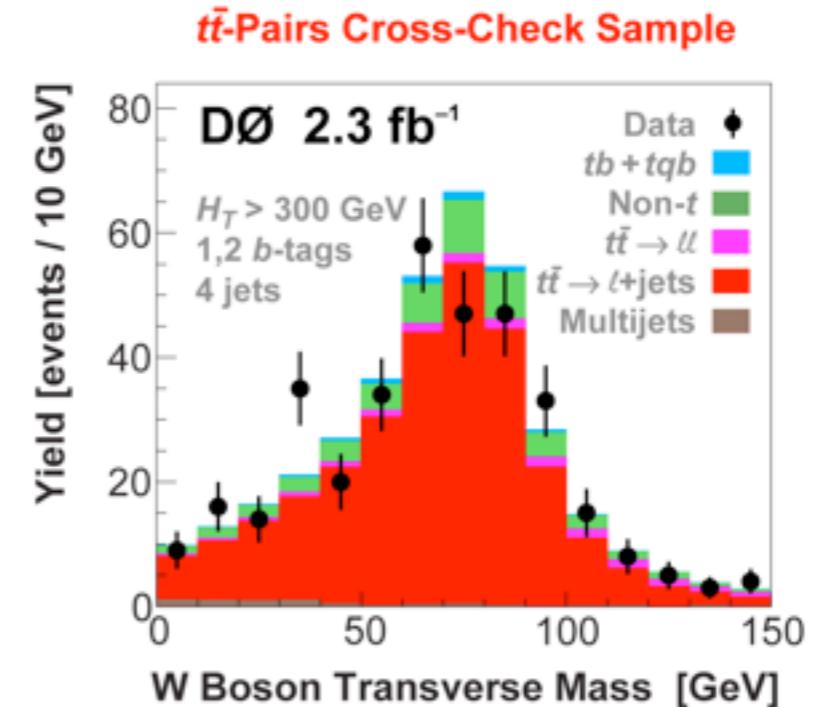
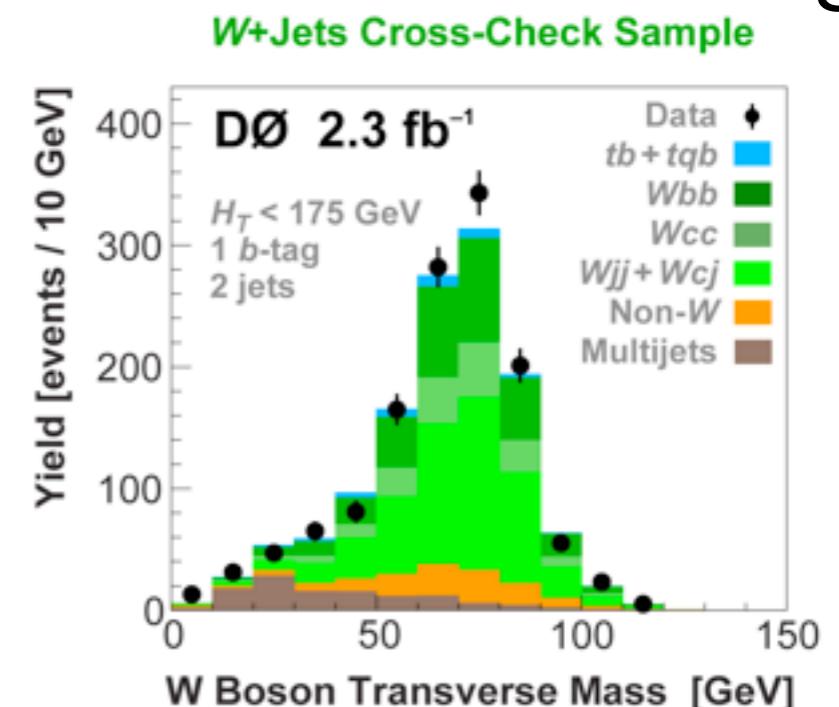
- Background dominated regions used to check modeling
- Same selection cuts as the main samples plus:

“ $W$ +jets” sample

- Exactly two jets
- $H_T(\text{lepton}, \cancel{E}_T, \text{all jets}) < 175 \text{ GeV}$
- One  $b$ -tagged jet

“ $t\bar{t}$ ” sample

- Exactly four jets
- $H_T(\text{lepton}, \cancel{E}_T, \text{all jets}) > 300 \text{ GeV}$
- One or two  $b$ -tagged jets



# Selection of Variables

- Starting from a list of ~ 500 variables, select only well-modeled variables, and those with the highest discriminating power.

Resulting in a final list of **64 variables**

## BDT – Object Kinematics

$p_T(\text{jet}2)$   
 $p_T(\text{jet}3)$   
 $p_T(\text{jet}4)$   
 $p_T(\text{tag}1)$   
 $p_T(\text{light}2)$   
 $p_T(\text{notbest}2)$   
 $p_T(\text{lepton})$   
 $\cancel{E}_T$   
 $Q(\text{lepton}) \times \eta(\text{jet}1)$   
 $Q(\text{lepton}) \times \eta(\text{jet}2)$   
 $Q(\text{lepton}) \times \eta(\text{best})$   
 $Q(\text{lepton}) \times \eta(\text{light}1)$   
 $Q(\text{lepton}) \times \eta(\text{light}2)$

## BDT – Top Quark Reconstruction

$M(W, \text{best}1)$  (“best” top mass)  
 $M(W, \text{tag}1)$  (“ $b$ -tagged” top mass)  
 $M(W, \text{tag}1, S2)$  (with 2<sup>nd</sup> v solution)  
 $M(W, \text{jet}1)$   
 $M(W, \text{jet}1, S2)$   
 $M(W, \text{jet}2)$   
 $M(W, \text{jet}2, S2)$   
 $M(W, \text{notbest}2)$   
 $M(W, \text{notbest}2, S2)$   
 $M_{\text{top}}^{\Delta M^{\min}}$   
 $M_{\text{top}}^{\text{sig}}$   
 $\Delta M_{\text{top}}^{\min}$   
 $\text{Significance}_{\min}(M_{\text{top}})$

## BDT – Angular Correlations

$\Delta R(\text{jet}1, \text{jet}2)$   
 $\Delta R(\text{jet}1, \text{lepton})$   
 $\Delta R(\text{tag}1, \text{lepton})$   
 $\Delta R(\text{light}1, \text{lepton})$   
 $\Delta\phi(\text{lepton}, \cancel{E}_T)$   
 $\cos(\text{best}, \text{lepton})_{\text{besttop}}$   
 $\cos(\text{best}, \text{notbest})_{\text{besttop}}$   
 $\cos(\text{jet}1, \text{lepton})_{\text{btaggedtop}}$   
 $\cos(\text{tag}1, \text{lepton})_{\text{btaggedtop}}$   
 $\cos(\text{lepton}_{\text{besttop}}, \text{besttop}_{\text{CMframe}})$   
 $\cos(\text{lepton}_{\text{btaggedtop}}, \text{btaggedtop}_{\text{CMframe}})$   
 $\cos(\text{tag}1, \text{lepton})_{\text{btaggedtop}}$   
 $\cos(\text{lepton}, Q(\text{lepton}) \times z)_{\text{besttop}}$

## BDT – Jet Reconstruction

$\text{Width}_\eta(\text{jet}2)$   
 $\text{Width}_\eta(\text{jet}4)$   
 $\text{Width}_\phi(\text{jet}4)$   
 $\text{Width}_\eta(\text{tag}1)$   
 $\text{Width}_\eta(\text{light}2)$   
 $\text{Width}_\phi(\text{light}2)$

## BDT – Event Kinematics

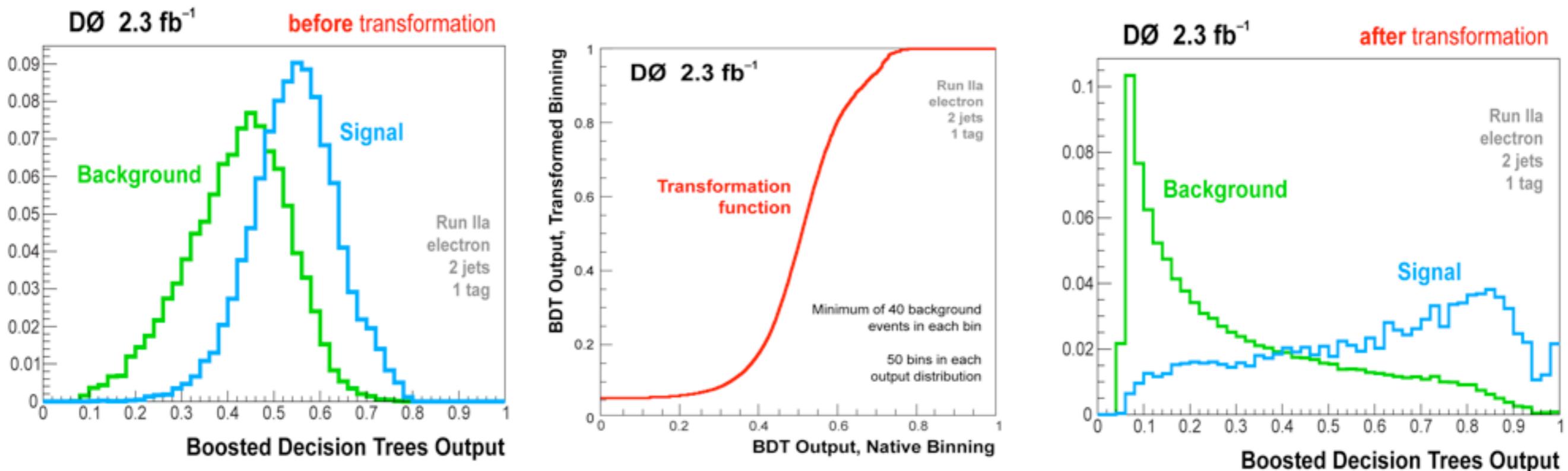
Centrality(alljets)  
 $H_T(\text{alljets})$   
 $H_T(\text{alljets} - \text{tag}1)$   
 $H_T(\text{alljets} - \text{best})$   
 $H_T(\text{jet}1, \text{jet}2)$   
 $H_T(\text{jet}1, \text{jet}2, \text{lepton}, \cancel{E}_T)$   
 $H_T(\text{alljets}, \text{lepton}, \cancel{E}_T)$   
 $H_T(\cancel{E}_T, \text{lepton})$   
 $H(\text{alljets} - \text{tag}1)$   
 $M(\text{alljets})$   
 $M(\text{alljets} - \text{best})$   
 $M(\text{alljets} - \text{tag}1)$   
 $M(\text{jet}1, \text{jet}2)$   
 $M(\text{jet}1, \text{jet}2, W)$   
 $M(\text{jet}3, \text{jet}4)$   
 $M_T(\text{jet}1, \text{jet}2)$   
 $p_T(\text{jet}1, \text{jet}2)$   
 $\sqrt{\hat{s}}$   
 $M_T(W)$

# BDT More Powerful Variables

Best Variables to Separate Single Top from W+Jets	
DØ 2.3 fb <sup>-1</sup> Analysis	
Object kinematics	$\cancel{E}_T$ $p_T(\text{jet2})$ $p_T^{\text{rel}}(\text{jet1}, \text{tag-}\mu)$ $E(\text{light1})$
Event kinematics	$M(\text{jet1,jet2})$ $M_T(W)$ $H_T(\text{lepton}, \cancel{E}_T, \text{jet1,jet2})$ $H_T(\text{jet1,jet2})$ $H_T(\text{lepton}, \cancel{E}_T)$
Jet reconstruction	$\text{Width}_\phi(\text{jet2})$ $\text{Width}_\eta(\text{jet2})$
Top quark reconstruction	$M_{\text{top}}(W, \text{tag1})$ $\Delta M_{\text{top}}^{\text{min}}$ $M_{\text{top}}(W, \text{tag1, S2})$
Angular correlations	$\cos(\text{light1, lepton})_{\text{btaggedtop}}$ $\Delta\phi(\text{lepton}, \cancel{E}_T)$ $Q(\text{lepton}) \times \eta(\text{light1})$

Best Variables to Separate Single Top from Top Pairs	
DØ 2.3 fb <sup>-1</sup> Analysis	
Object kinematics	$pT(\text{notbest2})$ $pT(\text{jet4})$ $pT(\text{light2})$
Event kinematics	$M(\text{all jets} - \text{tag1})$ $\text{Centrality}(\text{all jets})$ $M(\text{all jets} - \text{best1})$ $H_T(\text{all jets} - \text{tag1})$ $H_T(\text{lepton}, \cancel{E}_T, \text{all jets})$ $M(\text{all jets})$
Jet reconstruction	$\text{Width}_\eta(\text{jet4})$ $\text{Width}_\phi(\text{jet4})$ $\text{Width}_\phi(\text{jet2})$
Angular correlations	$\cos(\text{lepton}_{\text{btaggedtop}}, \text{btaggedtop}_{\text{CMframe}})$ $Q(\text{lepton}) \times \eta(\text{light1})$ $\Delta R(\text{jet1,jet2})$

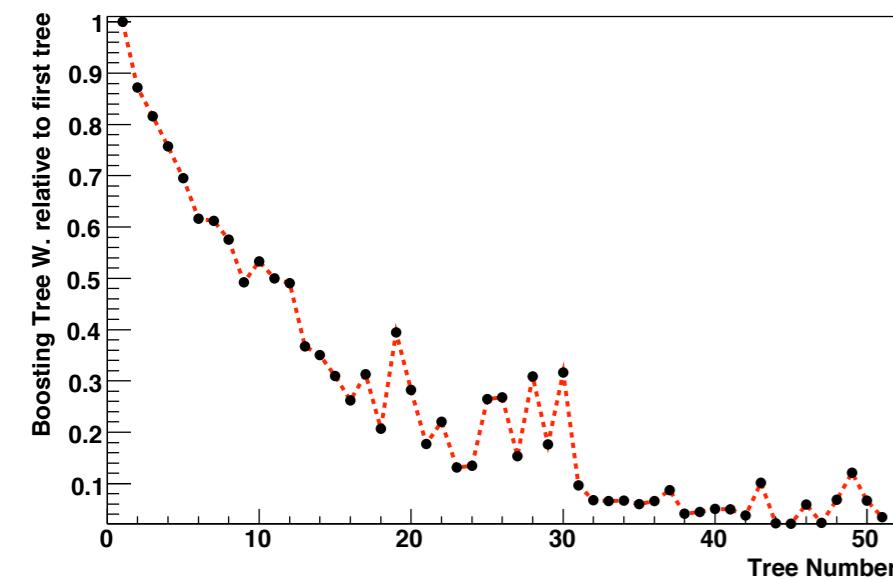
# Discriminant Output Transf



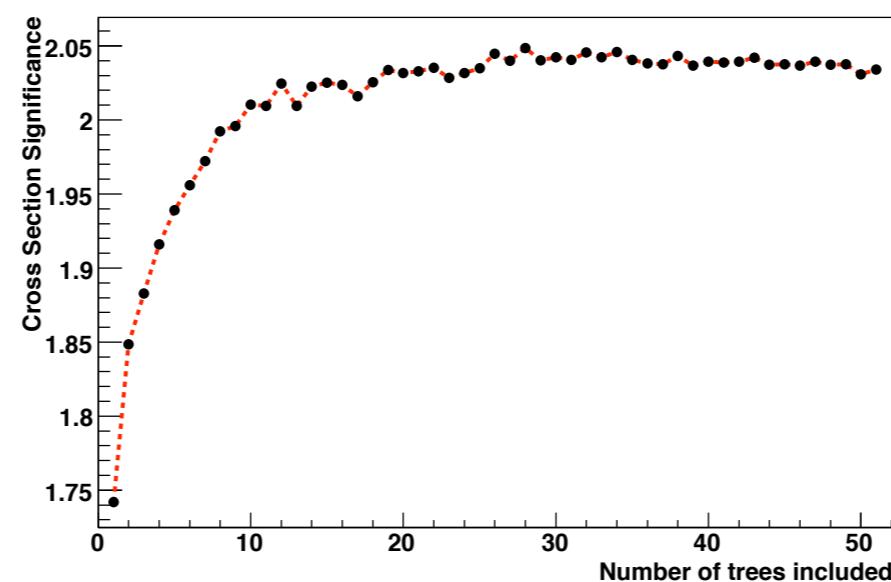
- Purpose: Ensure there are no undefined regions on the output discriminant
- At least, 40 background events are present on each bin

# BDT Performance

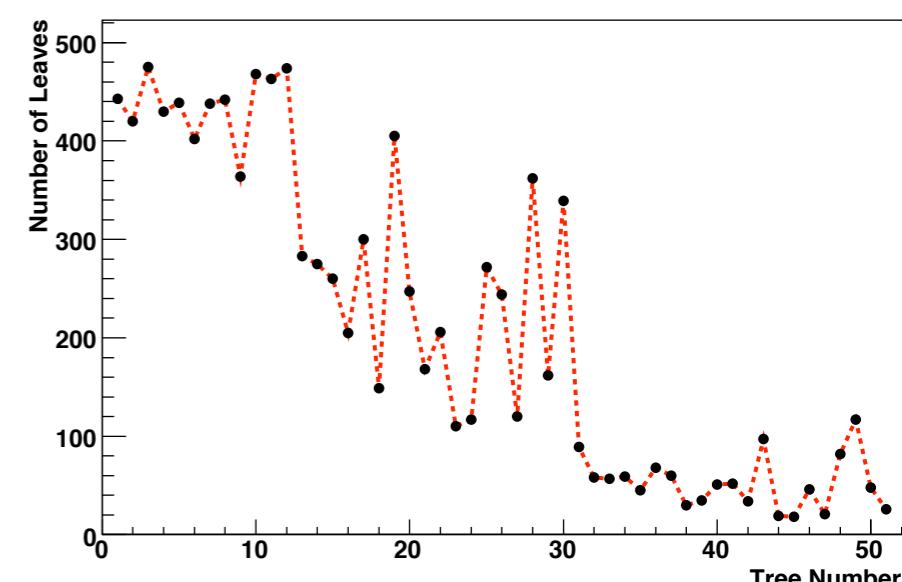
Boosting Tree W. relative to first tree for each tree



Cross Section Significance vs number of trees included

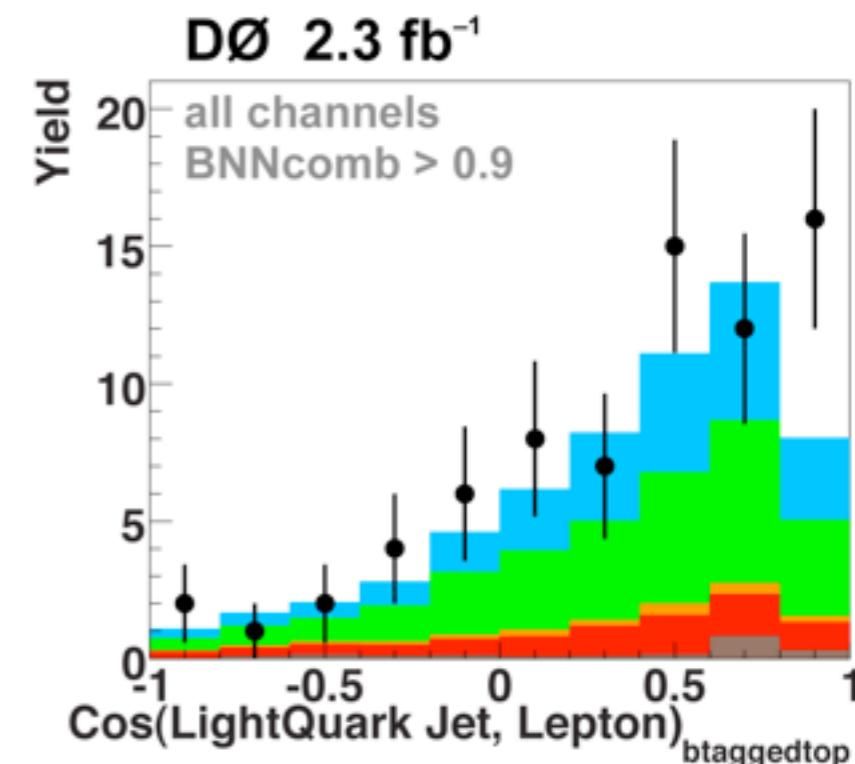
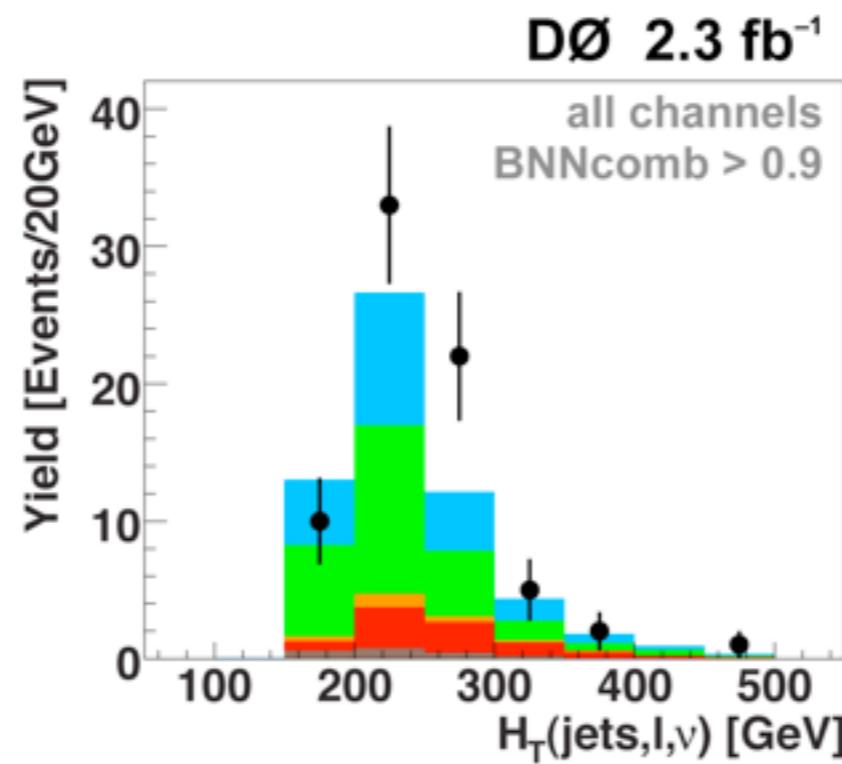
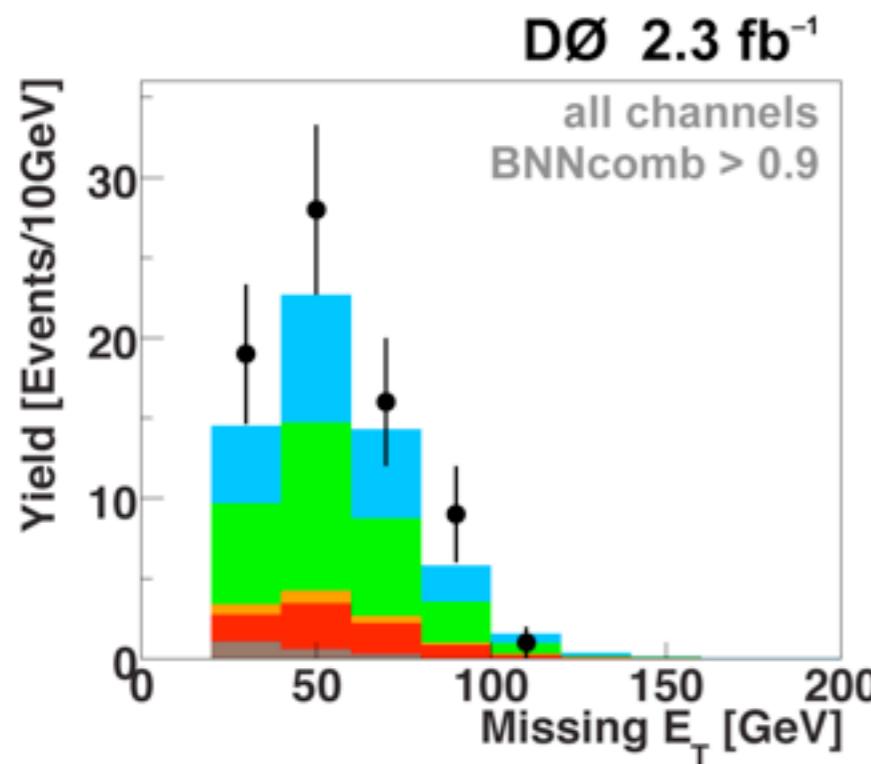


Number of Leaves for each tree



# High Discriminant Region

- Data / Monte Carlo agreement holds in the high discriminant region



# Systematics

## Systematic Uncertainties

Ranked from Largest to Smallest Effect  
on Single Top Cross Section

DØ 2.3 fb<sup>-1</sup>

### Larger terms

<i>b</i> -ID tag-rate functions (includes shape variations)	(2.1–7.0)% (1-tag) (9.0–11.4)% (2-tags)
Jet energy scale (includes shape variations)	(1.1–13.1)% (signal) (0.1–2.1)% (bkgd)
<i>W+jets</i> heavy-flavor correction	13.7%
Integrated luminosity	6.1%
Jet energy resolution	4.0%
Initial- and final-state radiation	(0.6–12.6)%
<i>b</i> -jet fragmentation	2.0%
<i>t</i> <i>t̄</i> pairs theory cross section	12.7%
Lepton identification	2.5%
<i>Wbb/Wcc</i> correction ratio	5%
Primary vertex selection	1.4%

## Systematic Uncertainties

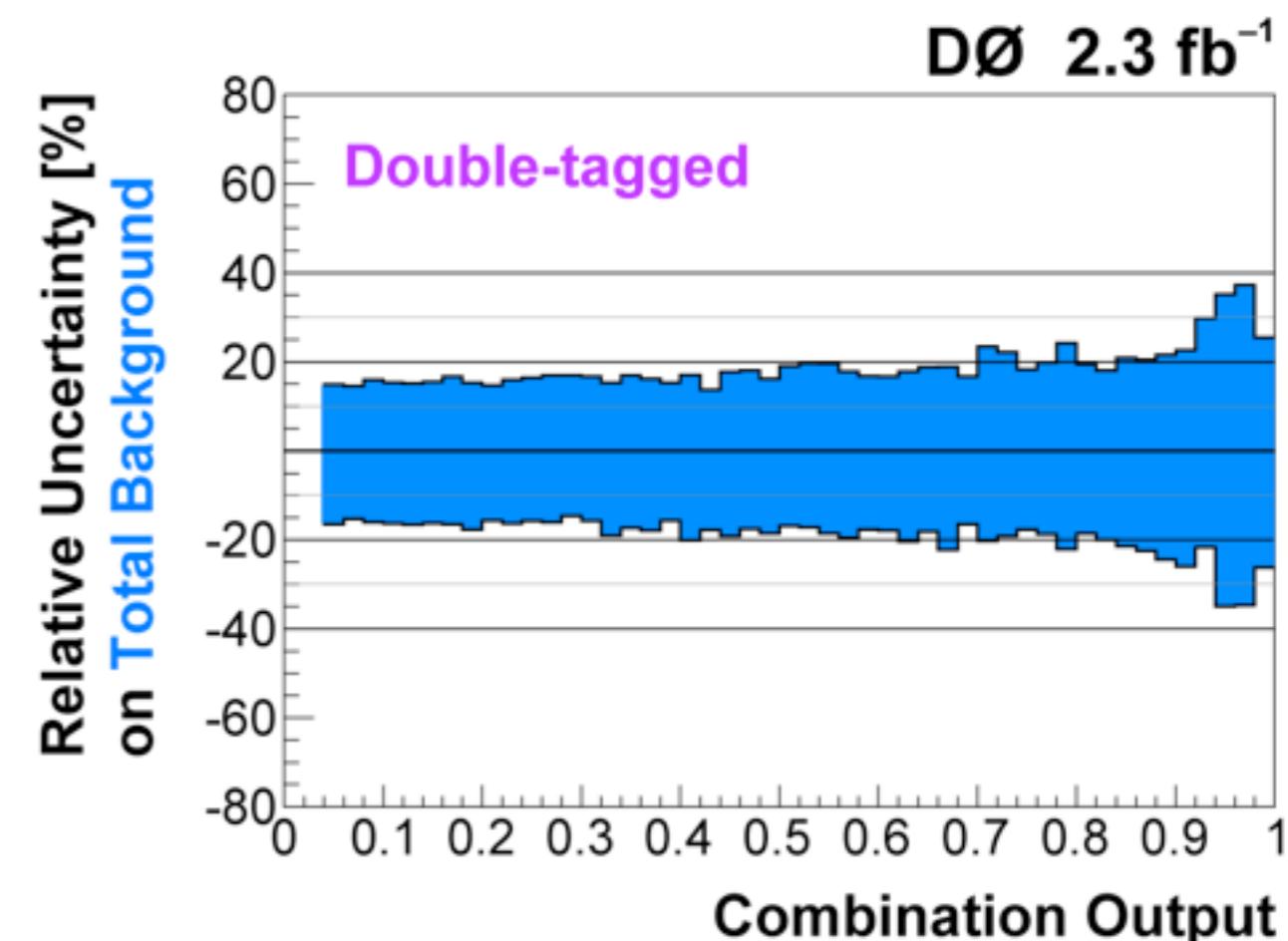
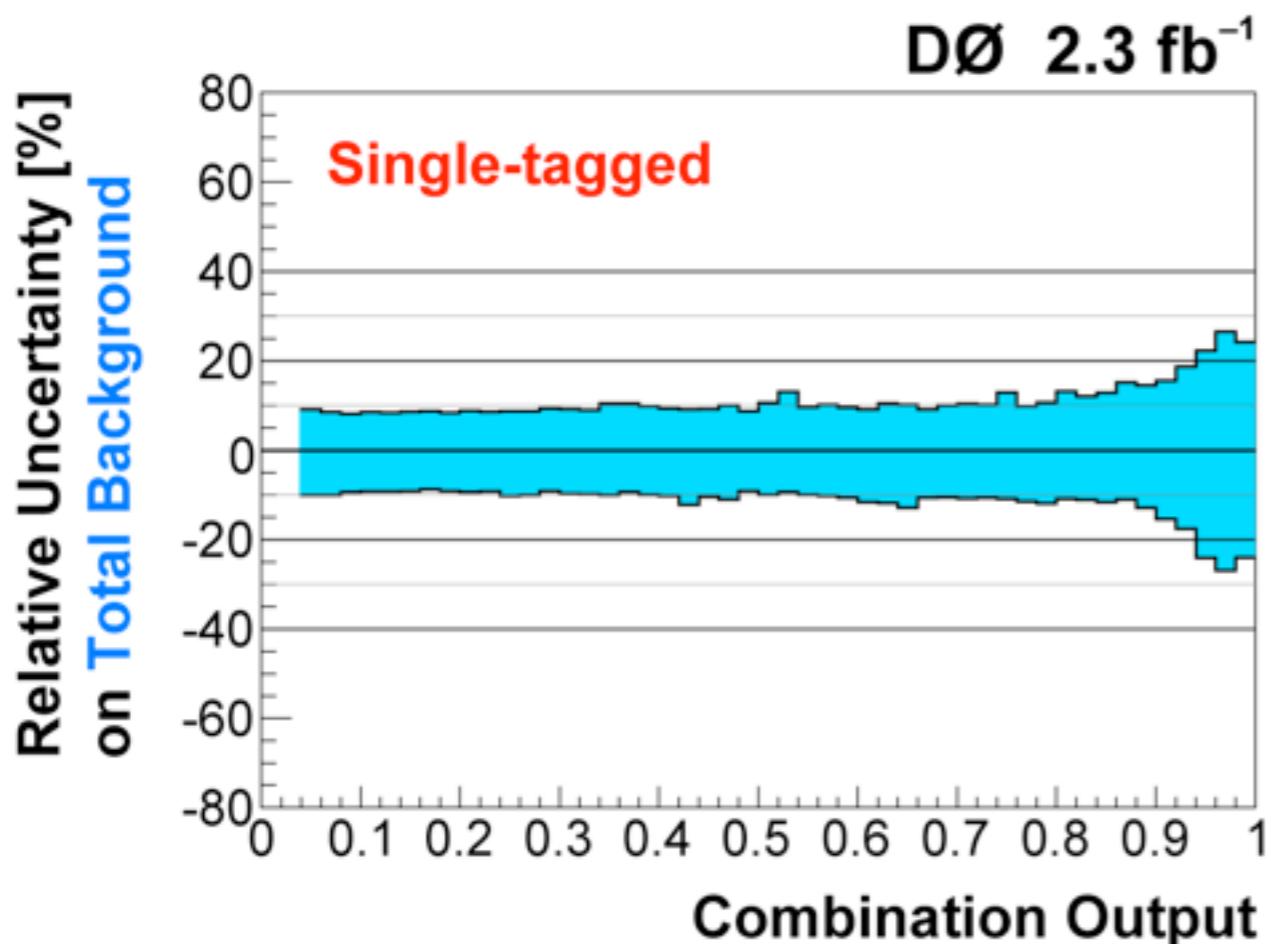
Ranked from Largest to Smallest Effect  
on Single Top Cross Section

DØ 2.3 fb<sup>-1</sup>

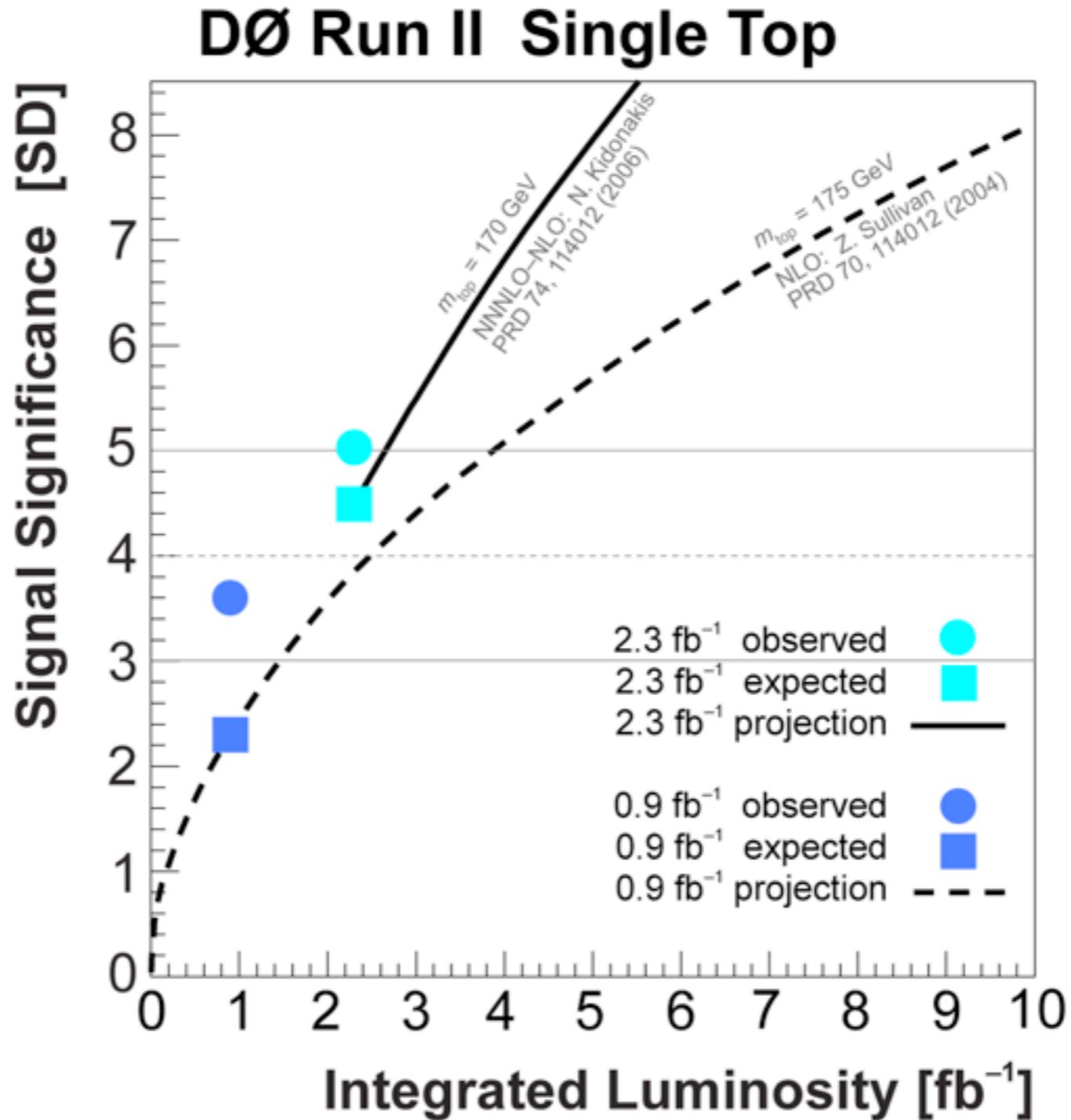
### Smaller terms

Monte Carlo statistics	(0.5–16.0)%
Jet fragmentation	(0.7–4.0)%
Branching fractions	1.5%
<i>Z+jets</i> heavy-flavor correction	13.7%
Jet reconstruction and identification	1.0%
Instantaneous luminosity correction	1.0%
Parton distribution functions (signal)	3.0%
<i>Z+jets</i> theory cross sections	5.8%
<i>W+jets</i> and multijets normalization to data	(1.8–3.9)% ( <i>W+jets</i> ) (30–54)% (multijets)
Diboson theory cross sections	5.8%
Alpgen <i>W+jets</i> shape corrections	shape only
Trigger	5%

# Relative Uncertainties



# Single Top Significance Projection



# D0 and CDF Results

Single Top Cross Section	Signal Significance Expected	Observed	CKM Matrix Element $V_{tb}$
<b>March 2009</b>	<b>DØ (2.3 fb<sup>-1</sup>)</b>	arXiv:0903.0850 ( $m_{top} = 170$ GeV)	
$3.94 \pm 0.88$ pb	$4.5 \sigma$	$5.0 \sigma$	$ V_{tb} f_1^L  = 1.07 \pm 0.12$ $ V_{tb}  > 0.78$ at 95% CL
<b>March 2009</b>	<b>CDF (3.2 fb<sup>-1</sup>)</b>	arXiv:0903.0885 ( $m_{top} = 175$ GeV)	
$2.3^{+0.6}_{-0.5}$ pb	$>5.9 \sigma$	$5.0 \sigma$	$ V_{tb} f_1^L  = 0.91 \pm 0.13$ $ V_{tb}  > 0.71$ at 95% CL

# Matrix Element

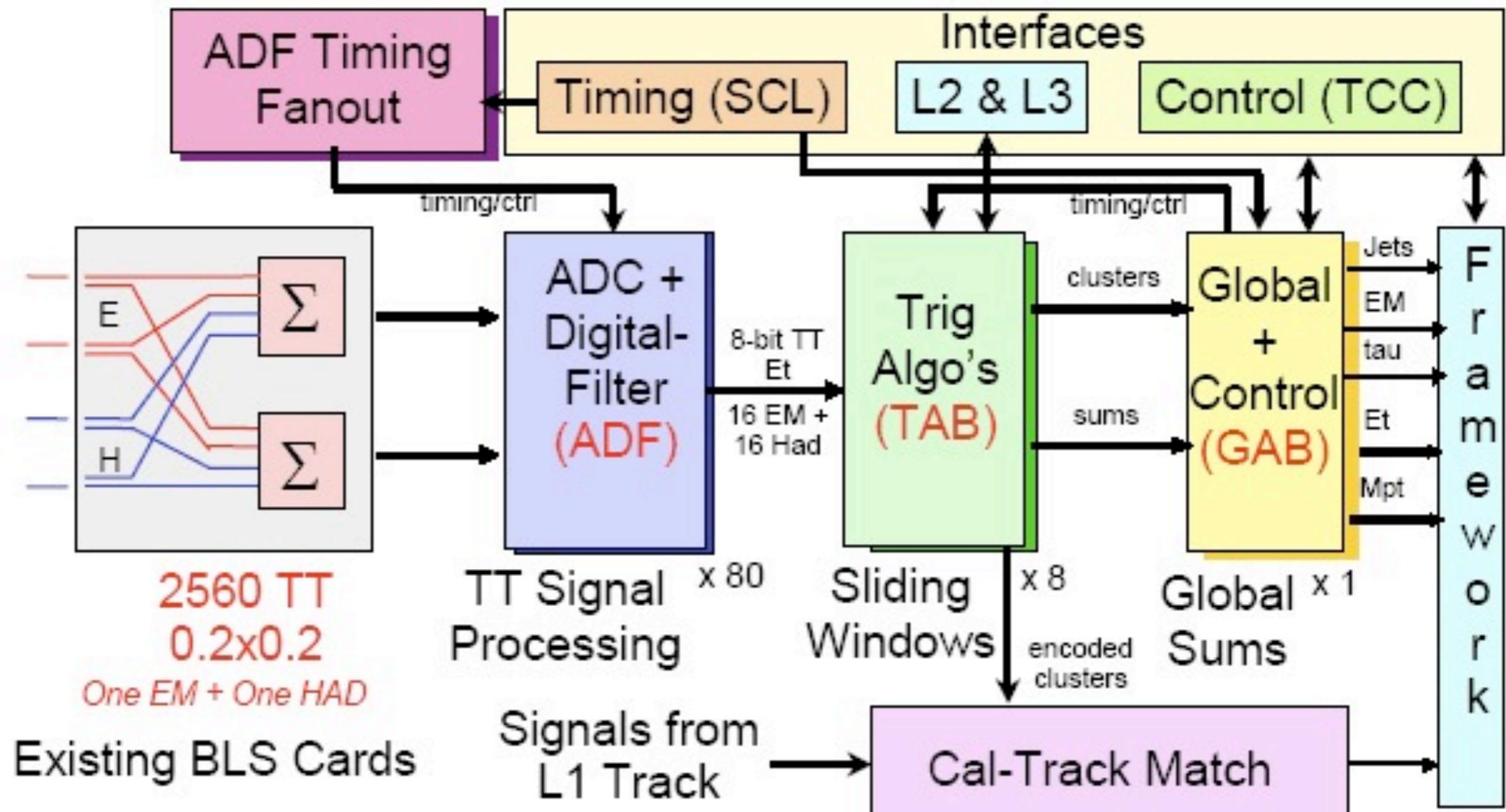
- Pioneered by DØ top mass analysis. Now used in search
- Use the 4-vectors of all reconstructed leptons and jets
- Use matrix elements of main signal and bkgd diagrams to compute event probability density for signal and bkgd hypotheses
- Goal: calculate a discriminant:

$$D_s(\vec{x}) = P(S|\vec{x}) = \frac{P_{signal}(\vec{x})}{P_{signal}(\vec{x}) + P_{bkg}(\vec{x})}$$

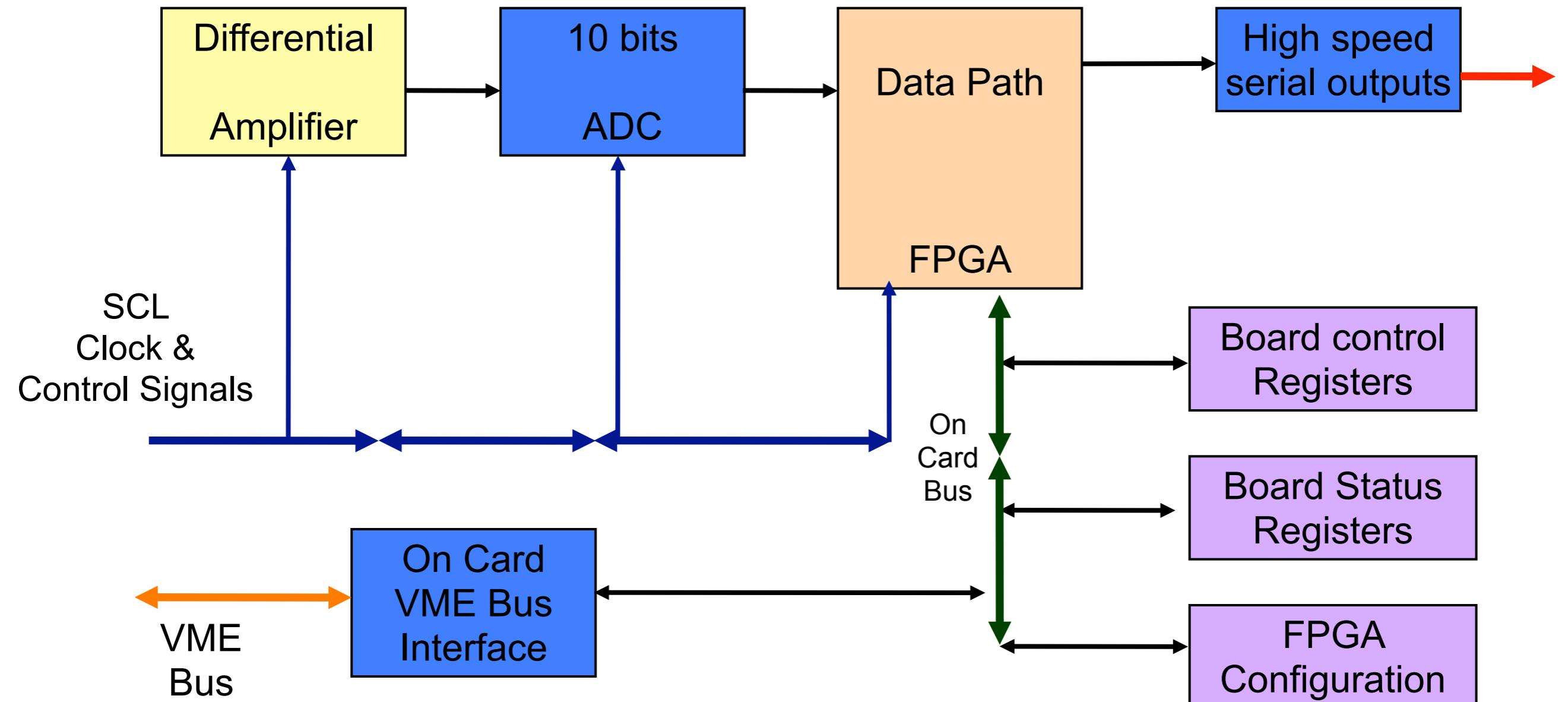
- Encoded in properly normalized differential cross section for process  $S$ :

$$P_S(\vec{x}) = \frac{1}{\sigma_S} d\sigma_S(\vec{x}), \quad \sigma_S = \int d\sigma_S(\vec{x})$$

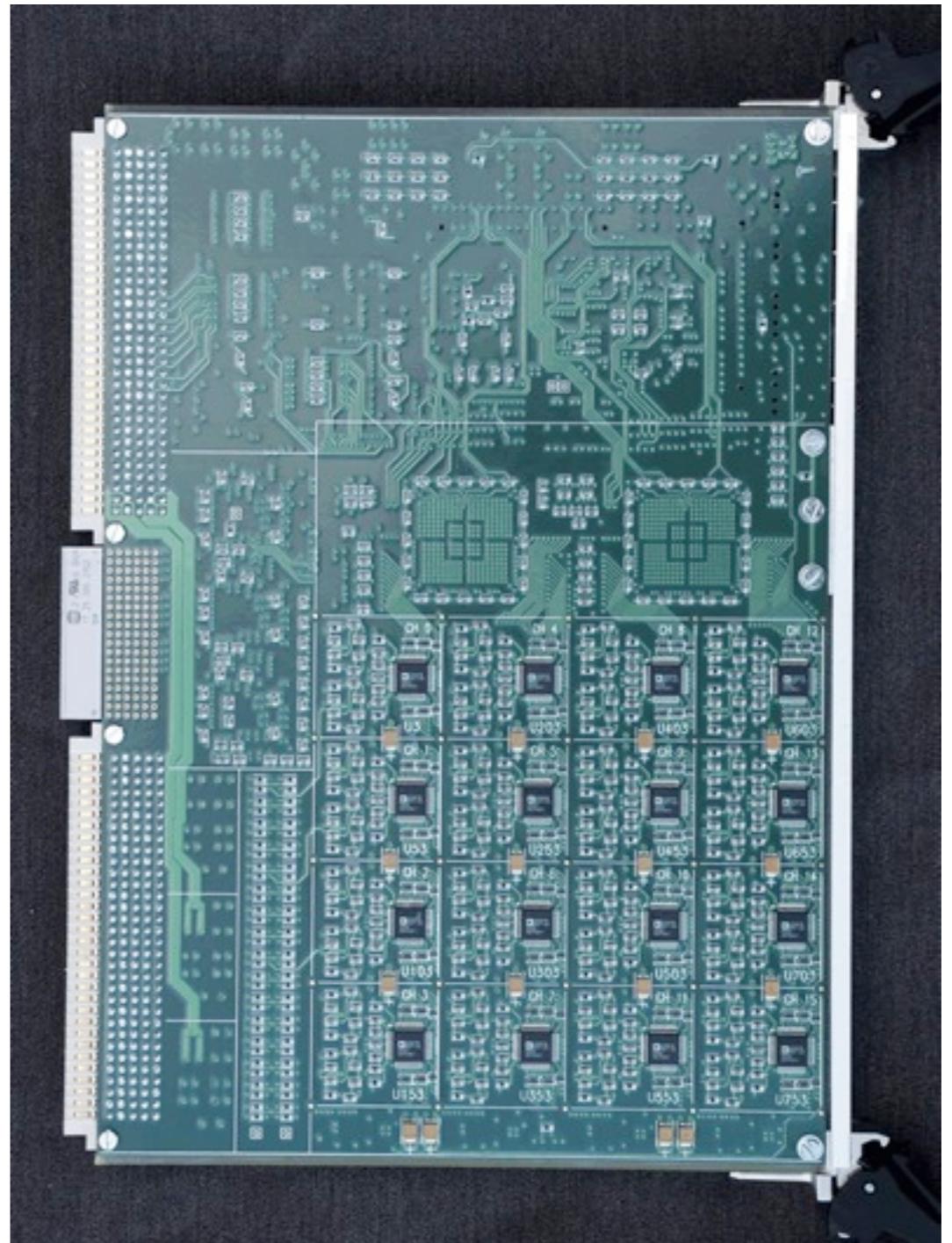
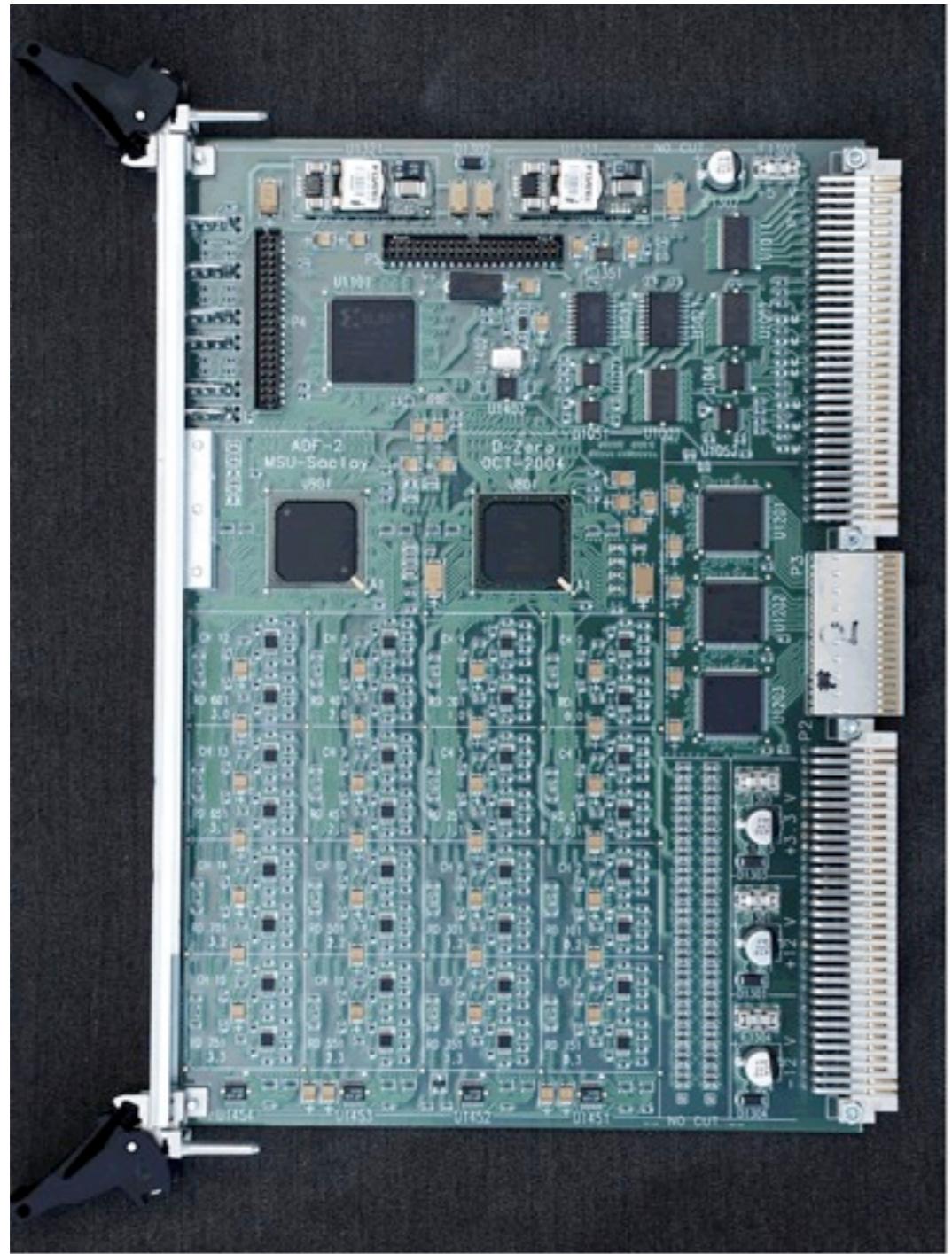
# Level 1 Cal Trigger Upgrade



# ADF Block Diagram



# ADF in Pictures...



# Test Waveform Generator System

Test Waveform Generator system

