

Cognitive Ecology: System Complexity and Diversity of Models.

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General Interest

- ▶ Feedbacks between systems and beliefs
- ▶ Complexity and Cognition
- ▶ Sustainable Development (Collective Intelligence and Collective Action)

Motivating example: Financial Bubbles

Theories of Financial Bubbles (optimists and pessimists, e.g. Scheinkman and Xiong, 2003):

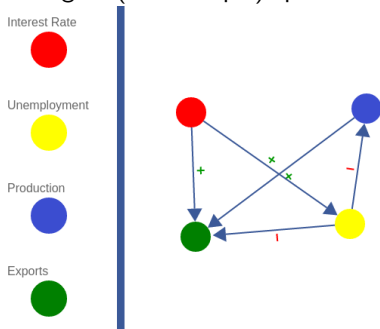
- ▶ are about institutions and beliefs: short-sale constraints in the presence of pessimists and optimists
- ▶ pessimists sell all of their shares (exit the market)
- ▶ optimists borrow and buy
- ▶ the bubble ensues
- ▶ but they do not model where beliefs come from.

My dissertation:

1) Shows that the complexity of the system and cognitive bounds jointly give rise to heterogeneity of beliefs; 2) builds an experimental platform to study belief dynamics; and 3) uses this platform to test the cognitive theory of financial bubbles.

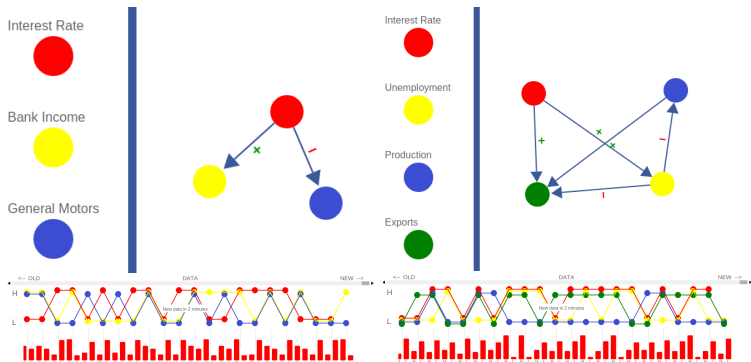
Laboratory Experiments on System Complexity and Cognitive Diversity

A participant's goal (for example): predict Interest Rates.



A belief system about a financial system: The nodes are variables and the arrows are causal relations.

Simple and Complex



Measuring Cognitive Diversity

Definition (N -Point Jensen-Shannon Divergence)

$$JSD(P_1, \dots, P_N) = H\left(\sum_{i=1}^N \pi_i P_i\right) - \sum_{i=1}^N \pi_i H(P_i), \quad (1)$$

where $H(P)$ is the Shannon entropy for joint-distribution P .

Definition (Cognitive Diversity)

Normalizing for group size I divide by $\sqrt{\log_2(N)}$ and I define Cognitive diversity as

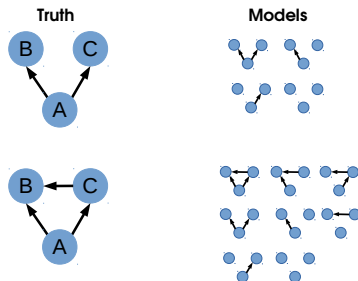
$$CD(P_1, \dots, P_N) = \sqrt{\frac{JSD(P_1, \dots, P_N)}{\log_2(N)}}. \quad (2)$$

In the 2 person case, this is a metric and I call the measure “Cognitive Distance”.

Sources of Diversity of Mental Models

1. Complexity of Causal Structure
2. Entropy
3. Attention as a limited resource (Rational Inattention)

Complexity of Causal Structure



There is a relation between the structural complexity of systems and the diversity of minds.

Entropy

If we think of causation as does Pearl (1988),

$$Pr(\text{Interest Rate} = 1 | \text{Unemployment} = a, \text{Production} = b) = 1 - (1 - \pi)^a (1 - \pi)^b, \quad (3)$$

where, $a, b \in [0, 1]$ and where 1 means high and 0 means low, then

- ▶ If $\pi = 0$ there is no causation at all.
- ▶ If $\pi = \frac{1}{2}$ entropy is maximal (the hardest case for inference).
- ▶ If $\pi = 1$ Equation 3 is the deterministic OR operator.

Human Cognition as a Noisy Channel

I use the Rational Inattention framework (Woodford, 2012) to show that

- ▶ optimizing agents pay more attention to data points that are more frequent
- ▶ diversity of predictions arises in low probability states of systems through imprecise updating

The more complex the system, the more low probability states it has and hence complexity induces diversity.



The Near Future

I will continue to triangulate

- ▶ Information and Communication Theory
- ▶ Experimental Social Science
- ▶ Social Science Theory

extending my questions to

- ▶ Conformity of Beliefs
- ▶ Political Manipulation of Beliefs
- ▶ Cultural Norms and Social Aspects of Beliefs

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- Scheinkman, J. A. and Xiong, W. (2003). Overconfidence and speculative bubbles. *Journal of Political Economy*.
- Woodford, M. (2012). Inattentive valuation and reference-dependent choice. website.